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**ENERGY**

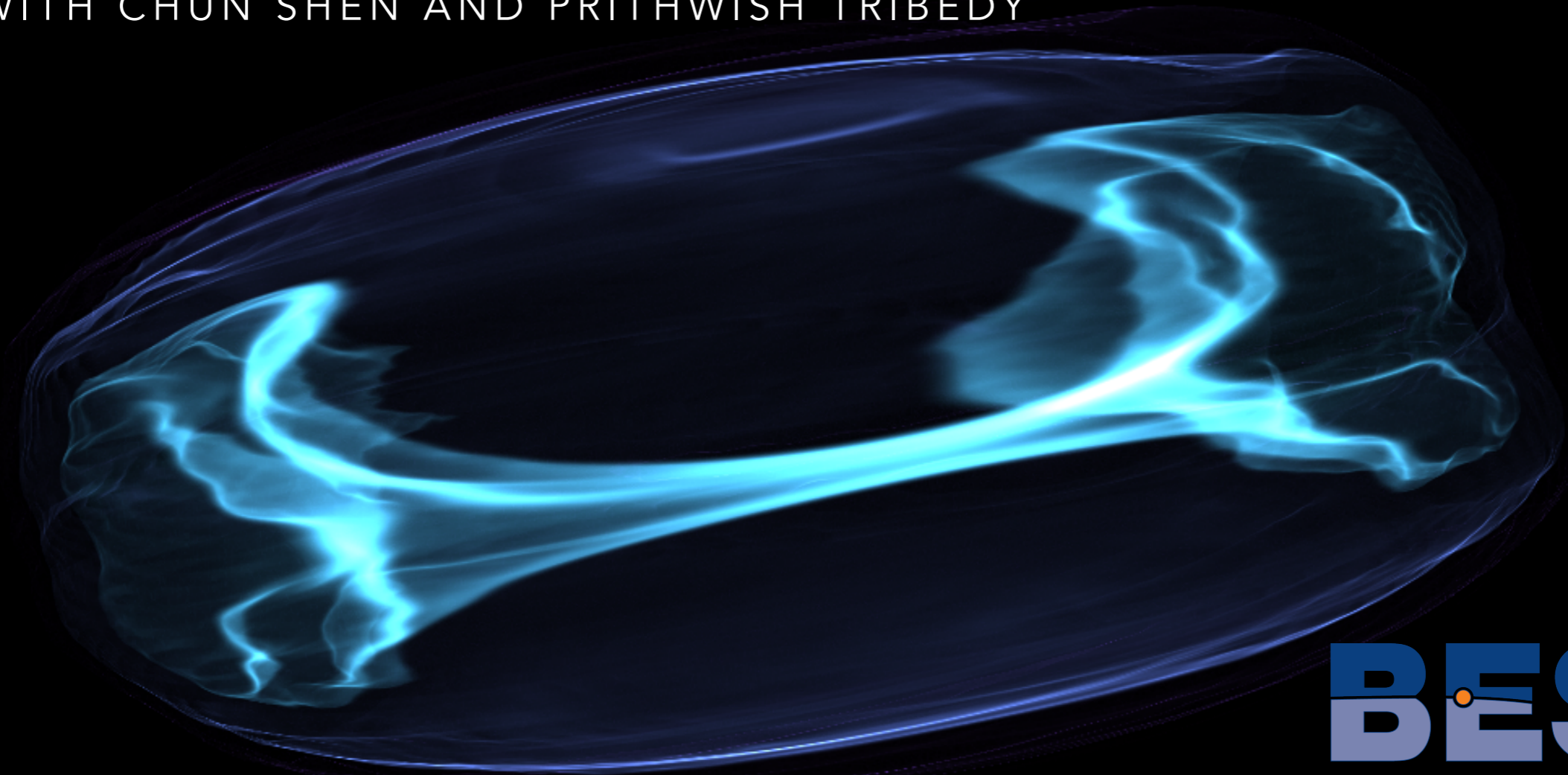
Office of  
Science

**BROOKHAVEN**  
NATIONAL LABORATORY

# MULTI-PARTICLE AZIMUTHAL CORRELATIONS AT THE RELATIVISTIC HEAVY-ION COLLIDER

BJÖRN SCHENKE - BROOKHAVEN NATIONAL LABORATORY

WORK WITH CHUN SHEN AND PRITHWISH TRIBEDY



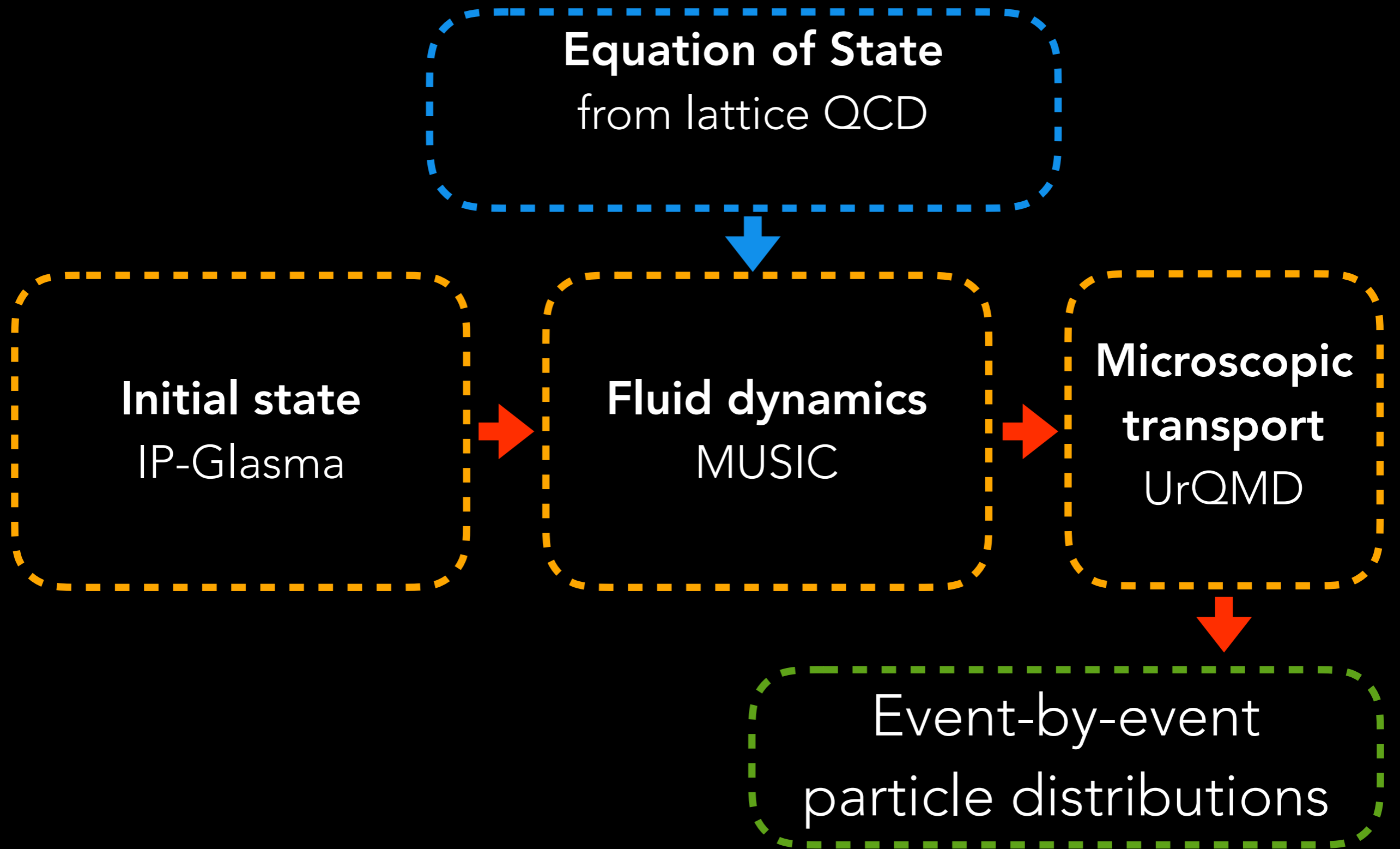
HIRSCHEGG, JANUARY 16 2019

**BEST**  
COLLABORATION

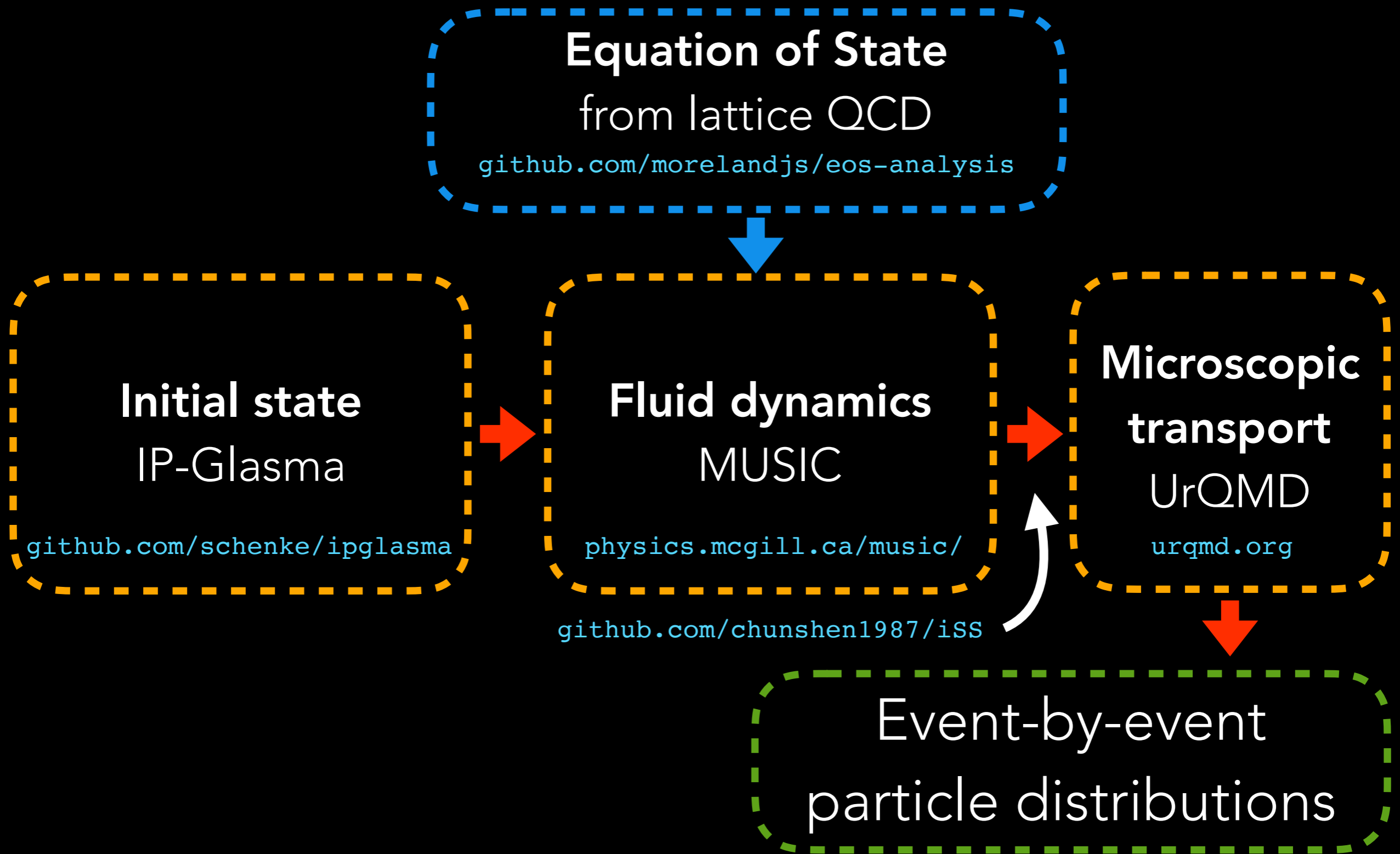
# Strategy

- Establish precise calculations of multi-particle correlators in a comprehensive framework with hydrodynamics at its core
- Constrain transport coefficients with bulk observables
- Compute more complex three and four particle correlators and compare to new data from RHIC
- Including local charge conservation during particle sampling establish baseline for chiral magnetic effect search
- Given constrained parameters from heavy ion collisions, predict observables in small systems

# Simulation Framework



# Simulation Framework



# Initial state and pre-equilibrium: IP-Glasma

B.Schenke, P.Tribedy, R.Venugopalan, PRL108, 252301 (2012), PRC86, 034908 (2012)

Solve Yang-Mills equations with incoming color currents  
constrained with IPSat model fit to HERA data

Kowalski, Teaney, Phys.Rev. D68 (2003) 114005

Kovner, McLerran, Weigert, Phys. Rev. D52, 6231 (1995)

Krasnitz, Venugopalan, Nucl.Phys. B557 (1999) 237

Color charge density constructed from nucleons (subnucleon  
structure possible, needed for p+A but also diffractive HERA data)

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301 and Phys.Rev. D94 (2016) 034042

Includes fluctuations of:

impact parameter, nucleon positions, (quark positions),  
color charge normalization, color charges

# Matching to fluid dynamics

Extract energy density and flow velocity from fields'  $T_{\text{CYM}}^{\mu\nu}$

$$\varepsilon u^\nu = u_\mu T^{\mu\nu}$$

Initial shear viscous tensor is given by (here used  $P=\varepsilon/3$ )

$$\pi^{\mu\nu} = T_{\text{CYM}}^{\mu\nu} - \underbrace{\frac{4}{3}\varepsilon u^\mu u^\nu + \frac{\varepsilon}{3}g^{\mu\nu}}_{\text{ideal part}}$$

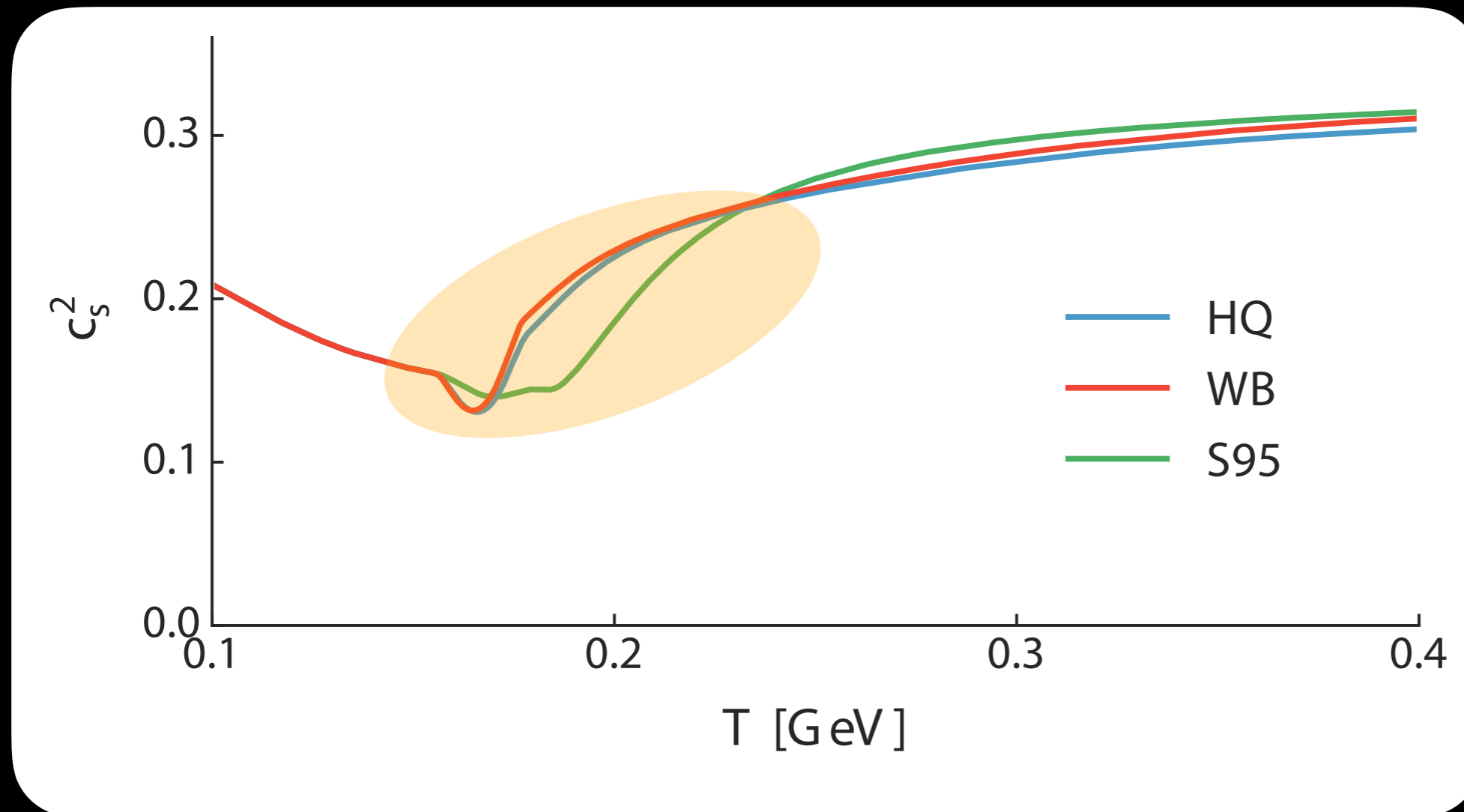
Absorb the difference to the lattice EoS in a 'bulk' stress term (here,  $P_{\text{lat}}$  from the lattice EoS)

$$\Pi = \frac{\varepsilon}{3} - P_{\text{lat}}$$

# Equation of State

Use a new EoS constructed from HotQCD LQCD data

Larger speed of sound compared to s95p leads to more flow



Affects  
extraction  
of viscosities:  
 $v_n$  change  
by 10%  
 $\eta/s$  needs to  
change by  
~50%

Figure from J.S. Moreland, R.A. Soltz, Phys.Rev. C93, 044913 (2016), also see P. Alba et al. arXiv:1711.05207

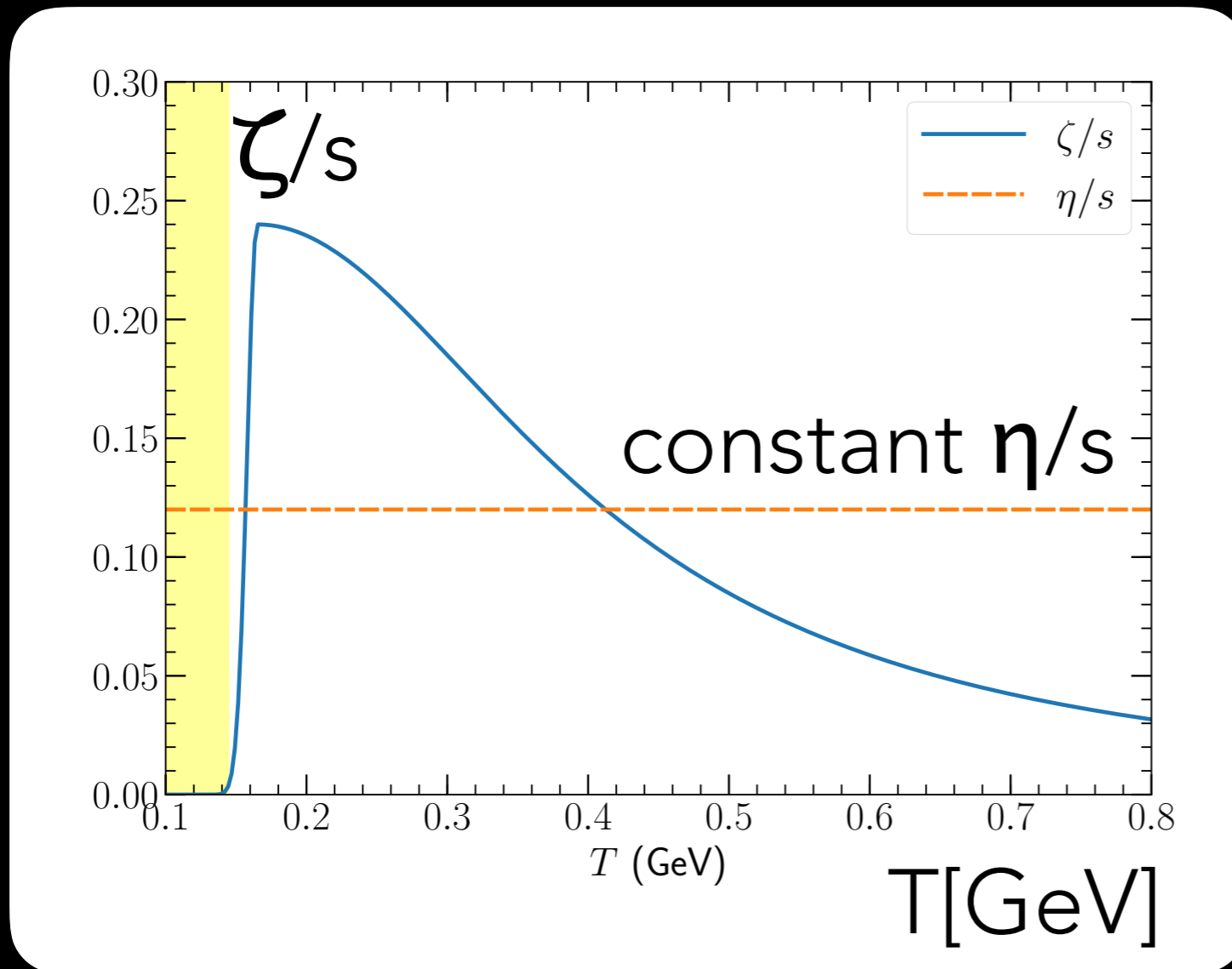
s95: P. Huovinen and P. Petreczky, Nucl. Phys. A837, 26–53 (2010)

HQ: A. Bazavov et al. (HotQCD), Phys. Rev. D90, 094503 (2014)

WB: S. Borsanyi, Z. Fodor, C. Hoelbling, S. D. Katz, S. Krieg, K. K. Szabo, Phys. Lett. B730, 99–104 (2014)

# Viscosities - all parameters fit in Au+Au

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378



Bulk viscosity  
peaks at 165 MeV

Width, height,  
and position  
are free parameters

S. Ryu, J.-F. Paquet, C. Shen, G. Denicol, B. Schenke, S. Jeon, C. Gale, Phys. Rev. C97, 034910, (2018)



# MUSIC → UrQMD

Sample particles on the freeze-out surface  
(surface of constant energy density)

according to

$$E \frac{dN_i}{d^3p} = \frac{g_i}{(2\pi)^3} \Delta^3 \sum_{\mu} p^{\mu} (f_i^{(0)} + \delta f_i)$$

then feed particles into UrQMD

S. A. Bass et al., *Prog. Part. Nucl. Phys.* 41, 255–369 (1998)

M. Bleicher et al., *J. Phys. G* 25, 1859–1896 (1999)

which performs resonance decays and scattering  
according to hadronic cross sections

Exact conservation laws should be fulfilled when  
converting to particles...

# Local charge conservation

Implement simple model that respects local charge conservation [P. Bozek, W. Broniowski, PRL 109 062301 \(2012\)](#)

- For each sampled particle sample its anti-particle in the same surface cell
- The common boost will introduce a correlation between the two opposite sign particles in momentum space



Implemented in sampler iSS available at: <https://github.com/chunshen1987/iSS>

# Global momentum conservation

- Ideally implement local momentum conservation
- But it is not trivial and left for future work
- We will concentrate on observables where the effect of local momentum conservation cancels
- For now: global momentum conservation
  - Compute net momentum of the system  $\langle \vec{p} \rangle = \sum \vec{p}_i$
  - Then we correct every particle's momentum by  $i$

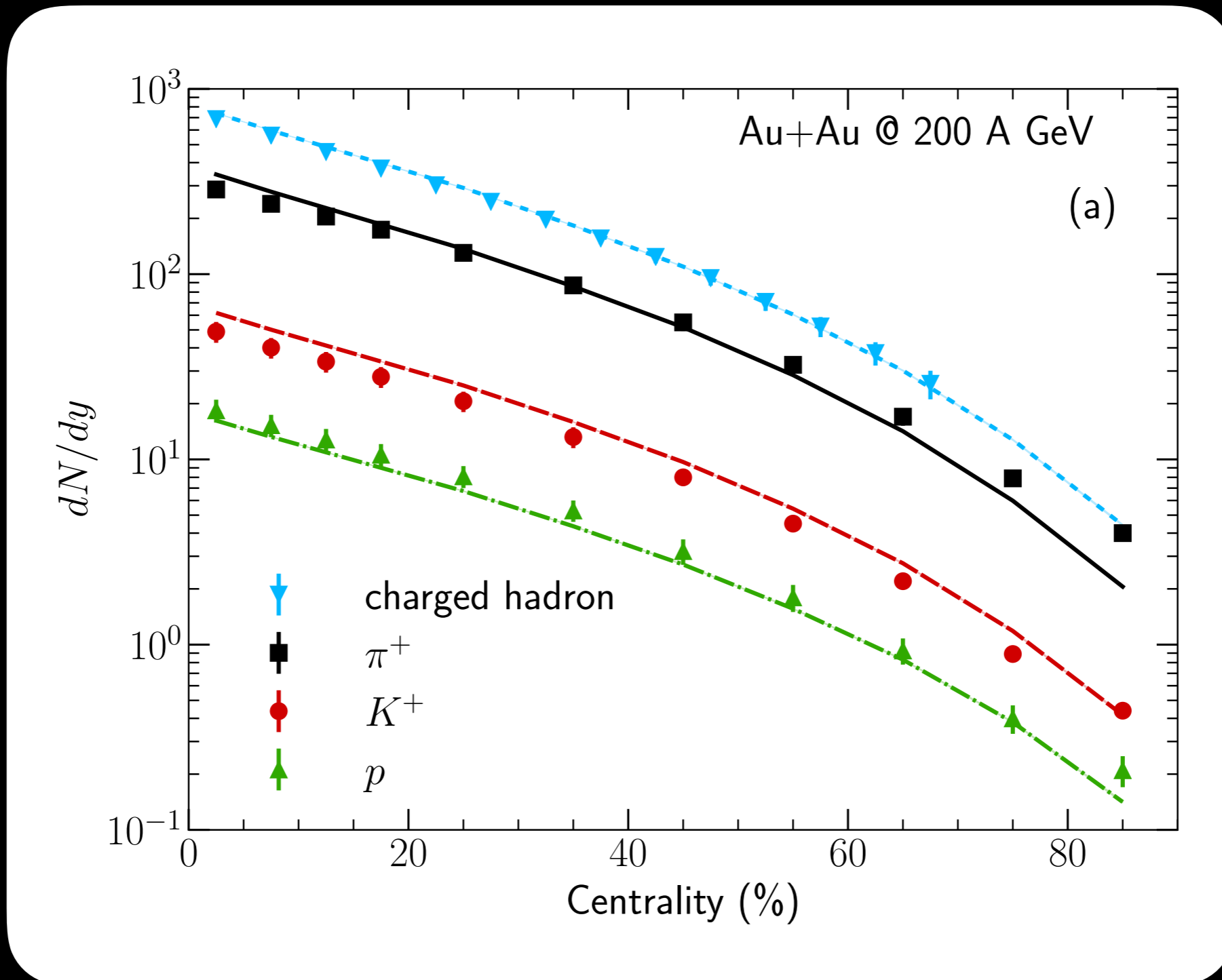
$$\vec{p}'_i = \vec{p}_i - \frac{p_{T,i}^2}{\langle p_T^2 \rangle} \langle \vec{p} \rangle$$

- Correction to each particle's momentum is order  $1/N$   
where  $N$  is the total number of particles in the sampled event

Implemented in sampler iSS available at: <https://github.com/chunshen1987/iSS>

# Identified particles

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378



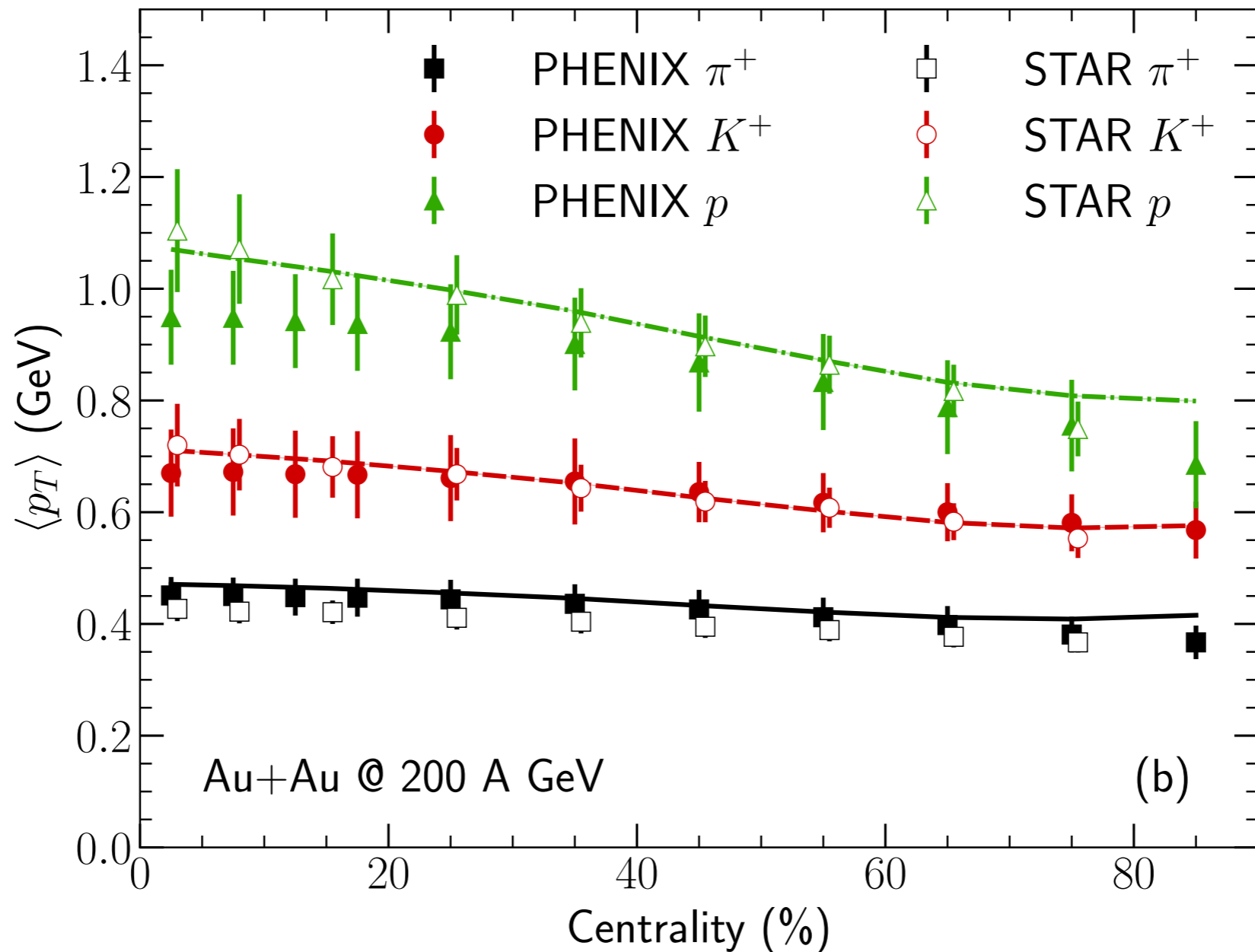
Experimental data: PHENIX Collaboration, Phys. Rev. C 69, 034909 (2004)

$\eta/s=0.12$

Björn Schenke, BNL

# Mean transverse momentum

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378



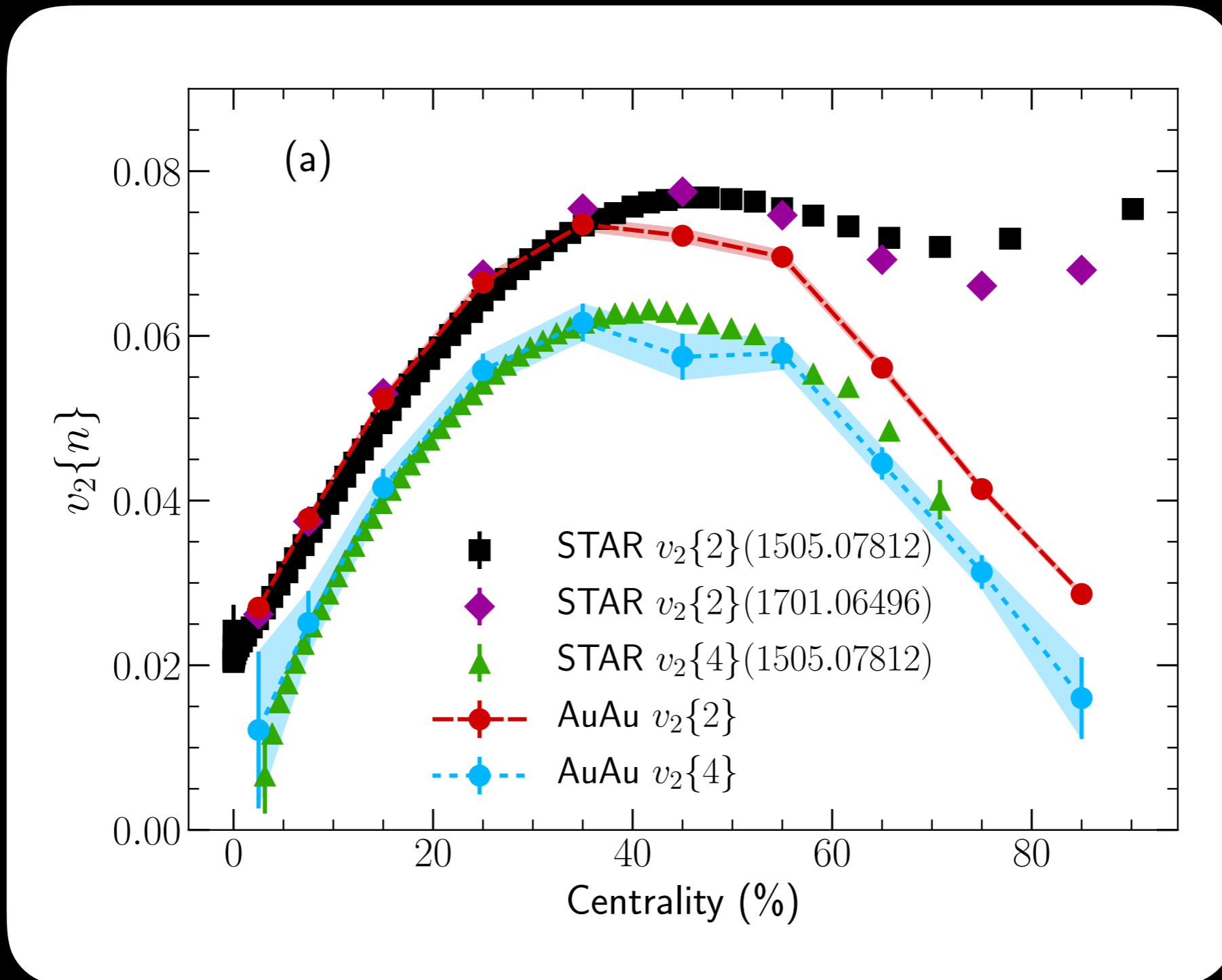
Experimental data: PHENIX Collaboration, Phys. Rev. C 69, 034909 (2004)  
STAR Collaboration, Phys. Rev. C 79, 034909 (2009)

$\eta/s=0.12$

Björn Schenke, BNL

# Elliptic anisotropy - Au+Au

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378

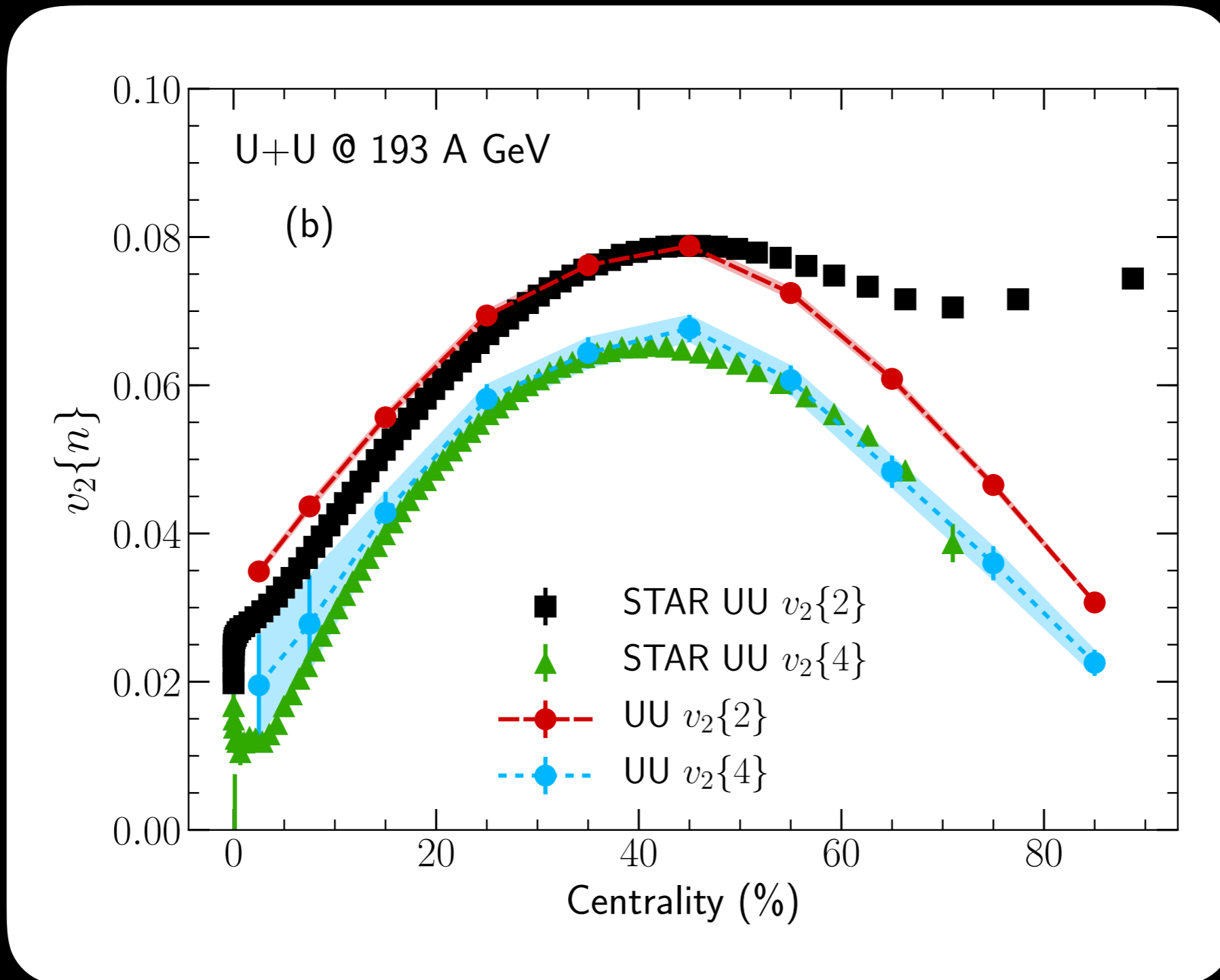


Experimental data: STAR Collaboration, Phys. Rev. Lett. 115, 222301 (2015)  
Phys. Rev. C 98, 034918 (2018)

$\eta/s=0.12$

# Elliptic anisotropy - U+U

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378

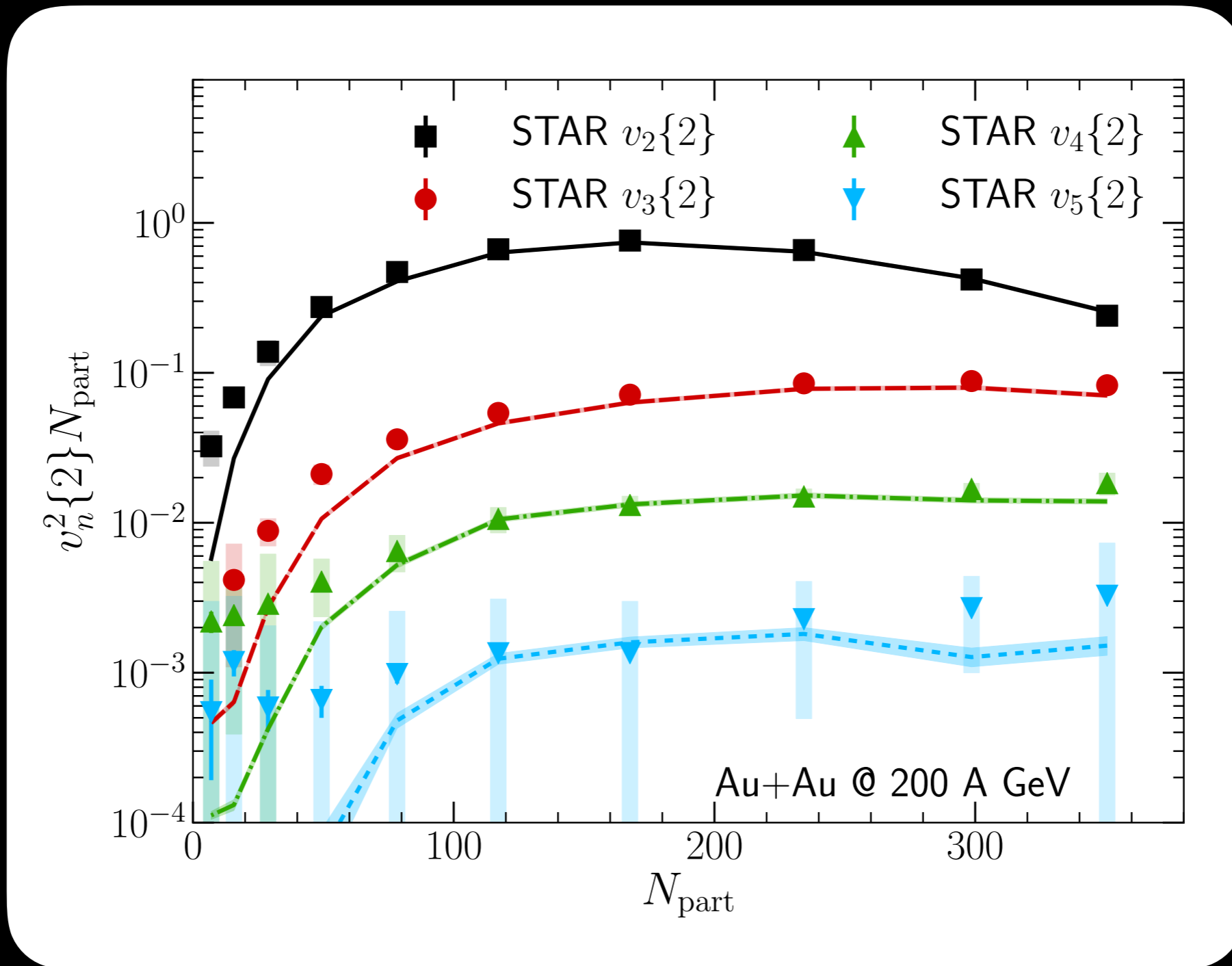


Experimental data: STAR Collaboration, Phys. Rev. Lett. 115, 222301 (2015)  
Phys. Rev. C 98, 034918 (2018)

$\eta/s=0.12$

# Higher harmonics (Au+Au)

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378



Experimental data: STAR Collaboration, Phys. Rev. Lett. 116, 112302 (2016),  
Phys. Rev. C 98, 034918 (2018)

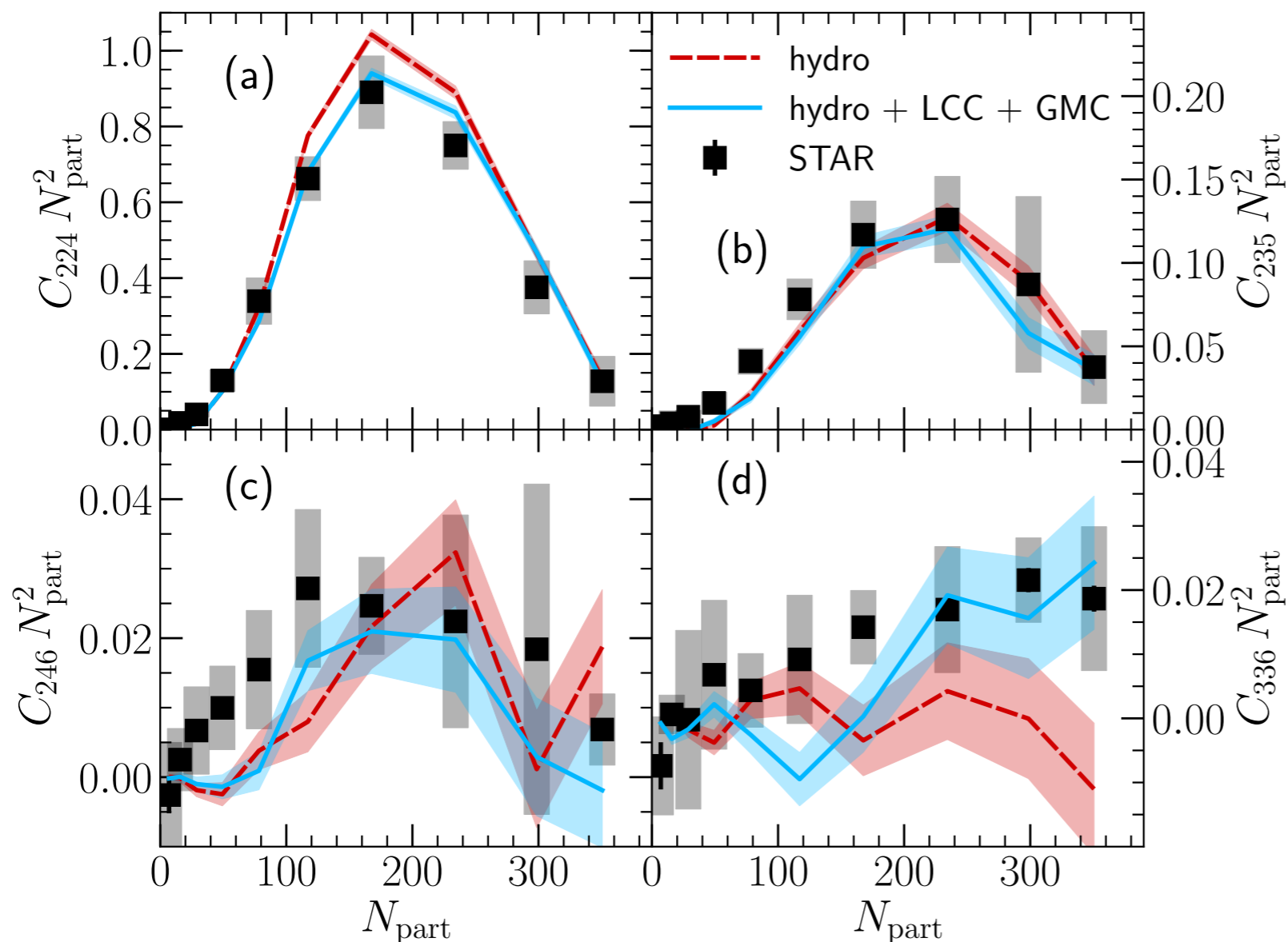
$\eta/s=0.12$



# Charge inclusive 3-particle correlations

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378

$C_{mnk} = \langle \cos(m\phi_1 + n\phi_2 - k\phi_3) \rangle$  Measures correlation between different harmonics

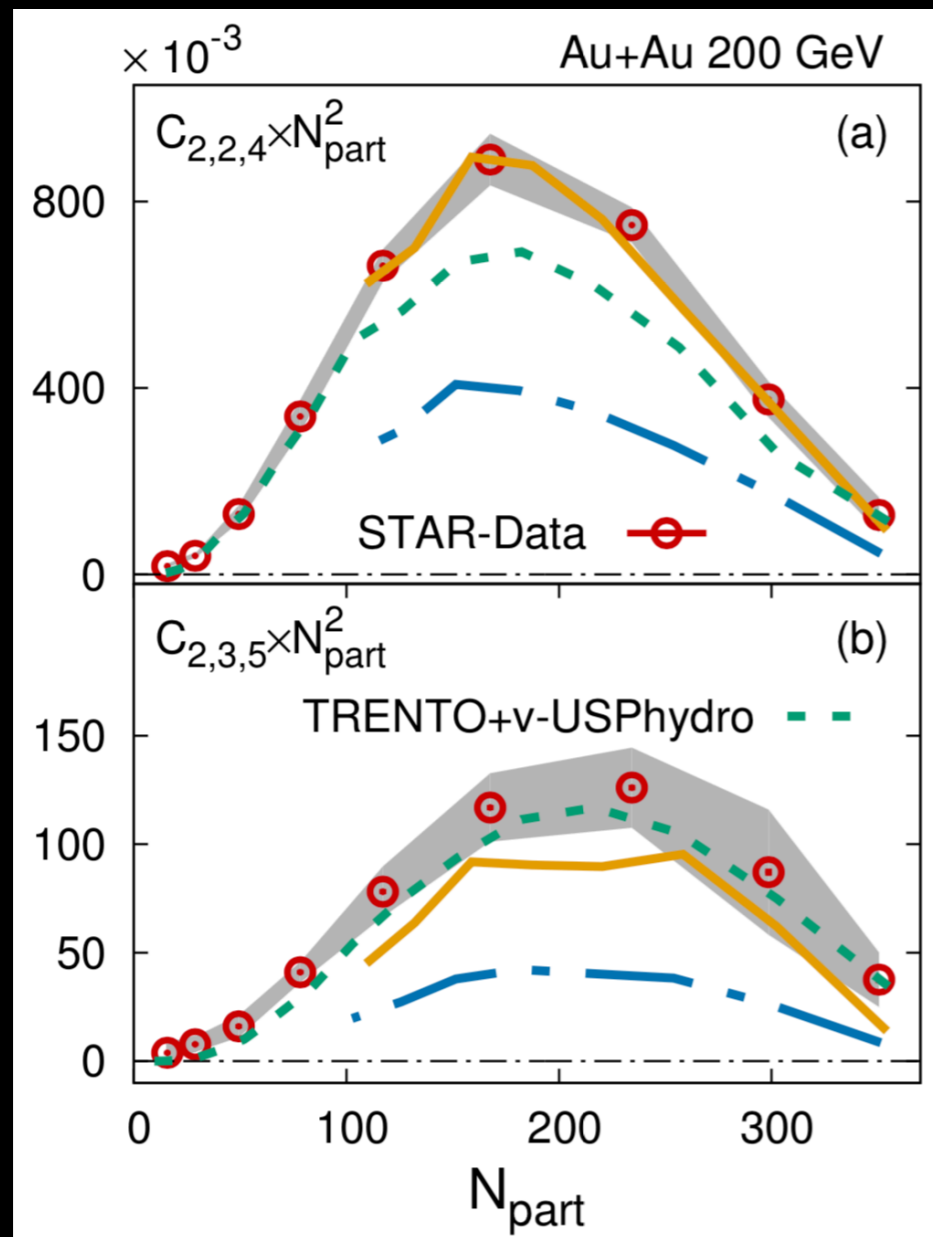


significant fraction developed in the hadronic cascade phase

Experimental data: STAR Collaboration, Phys. Rev. C 98, 034918 (2018)

# Charge inclusive 3-particle correlations

$$C_{mnk} = \langle \cos(m\phi_1 + n\phi_2 - k\phi_3) \rangle$$



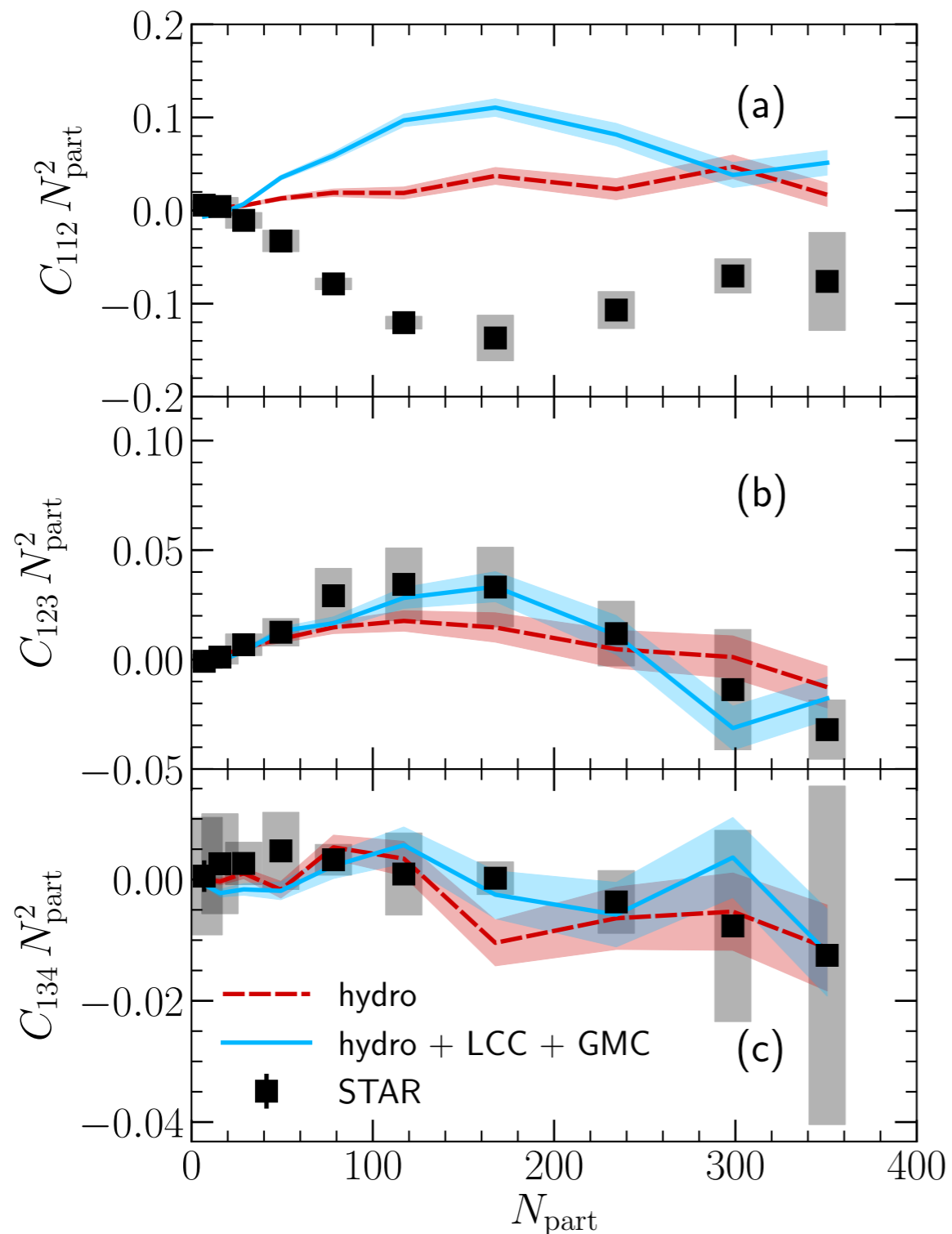
IP-Glasma+MUSIC+UrQMD —  
 IP-Glasma+MUSIC —

significant fraction developed in the hadronic cascade phase

Shown here is the older calculation with different EoS, smaller  $\eta/s$ , different  $\zeta/s$

# Charge inclusive 3-particle correlations

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378



Correlators involving  $v_1$  are sensitive to momentum conservation

Implementation of local momentum conservation in the sampling process will likely improve agreement with  $C_{112}$  from STAR

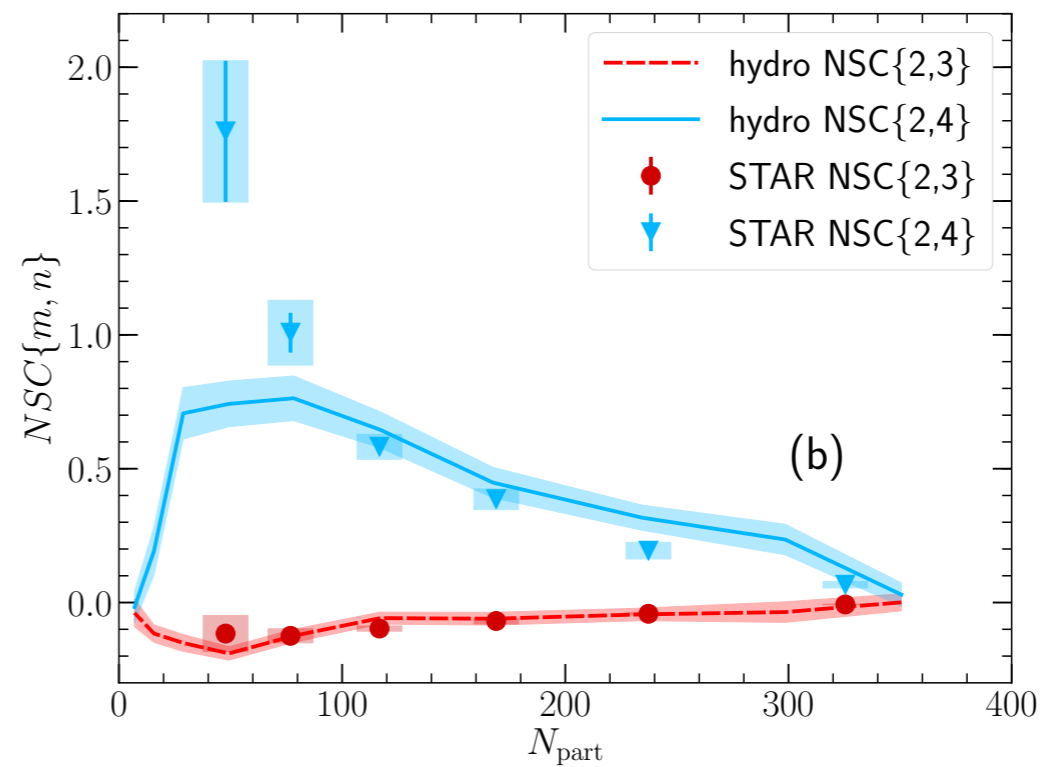
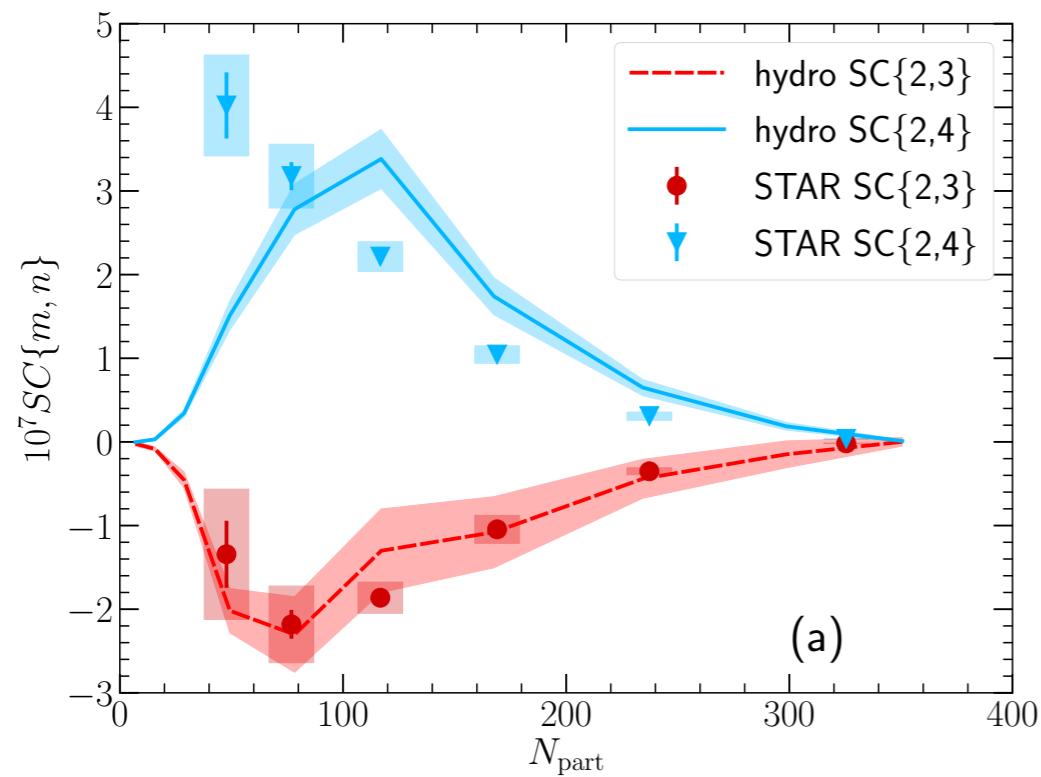
**Experimental data:**  
STAR Collaboration, Phys. Rev. C 98, 034918 (2018)

# 4-particle symmetric cumulants

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378

$$SC\{m, n\} = \frac{\langle Q_n Q_n^* Q_m Q_m^* \rangle_{ev}}{\langle M(M-1)(M-2)(M-3) \rangle_{ev}} - \frac{\langle Q_n Q_n^* \rangle}{\langle M(M-1) \rangle_{ev}} - \frac{\langle Q_m Q_m^* \rangle}{\langle M(M-1) \rangle_{ev}}$$

A. Bilandzic et al, Phys. Rev. C 89, 064904 (2014)



$$Q_n = \sum_{j=1}^M e^{in\phi_j}$$

Effect of hadronic afterburner is strong:

Experimental data:

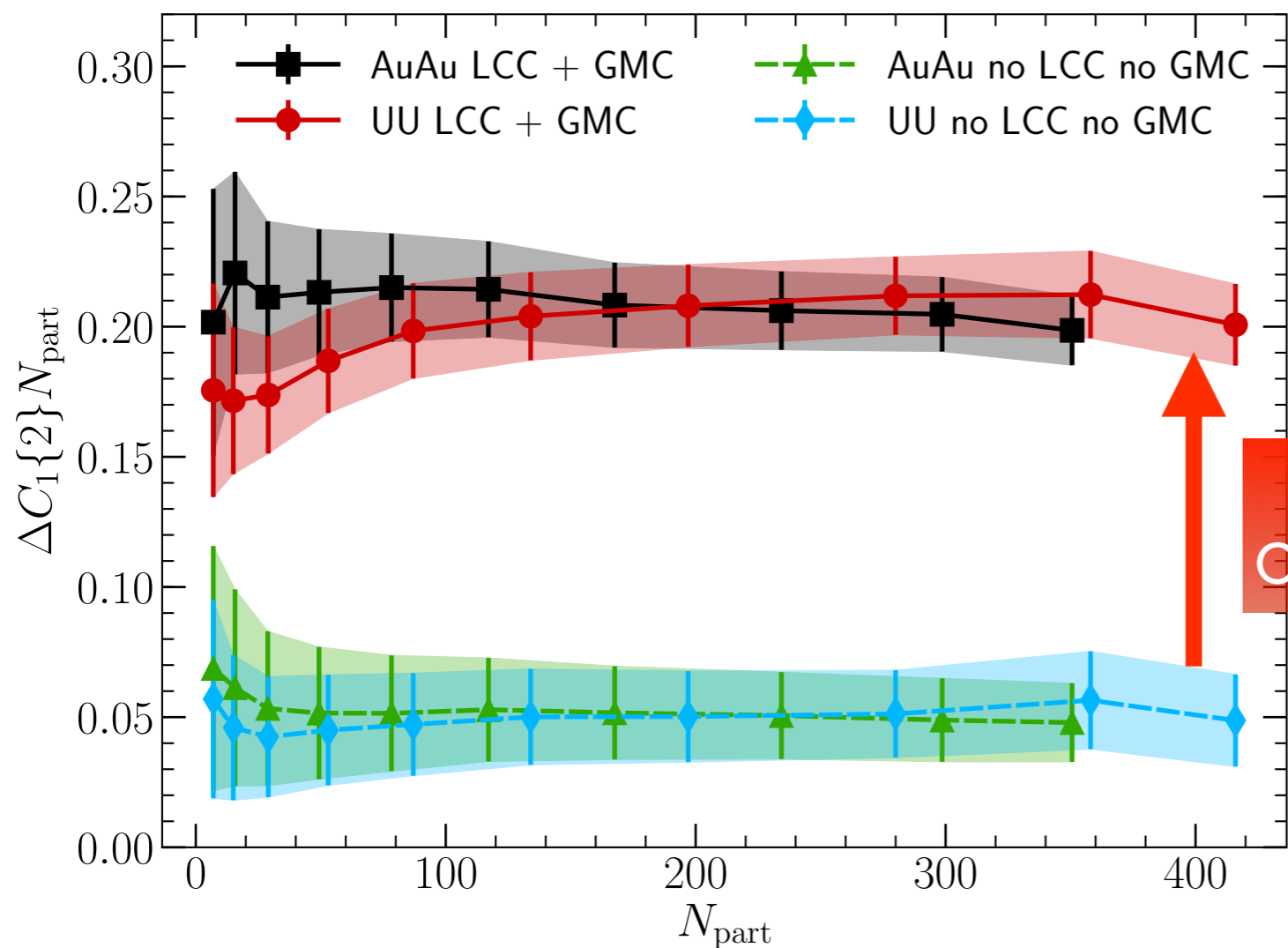
STAR Collaboration, arXiv:1803.03876

20-30%	$10^7 SC\{2,3\}$	$10^7 SC\{2,4\}$
DECAY ONLY	-0.3(4)	0.9(1)
URQMD	-1.1(4)	1.7(2)

# Charge dependent correlators

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378

$$\Delta C_n\{2\} = C_n\{2\}(\text{OS}) - C_n\{2\}(\text{SS})$$



$$C_n\{2\}(\text{OS}) = \langle \cos(n(\phi_\alpha^\pm - \phi_\beta^\mp)) \rangle$$

$$C_n\{2\}(\text{SS}) = \langle \cos(n(\phi_\alpha^\pm - \phi_\beta^\pm)) \rangle$$

EFFECT OF LOCAL CHARGE CONSERVATION

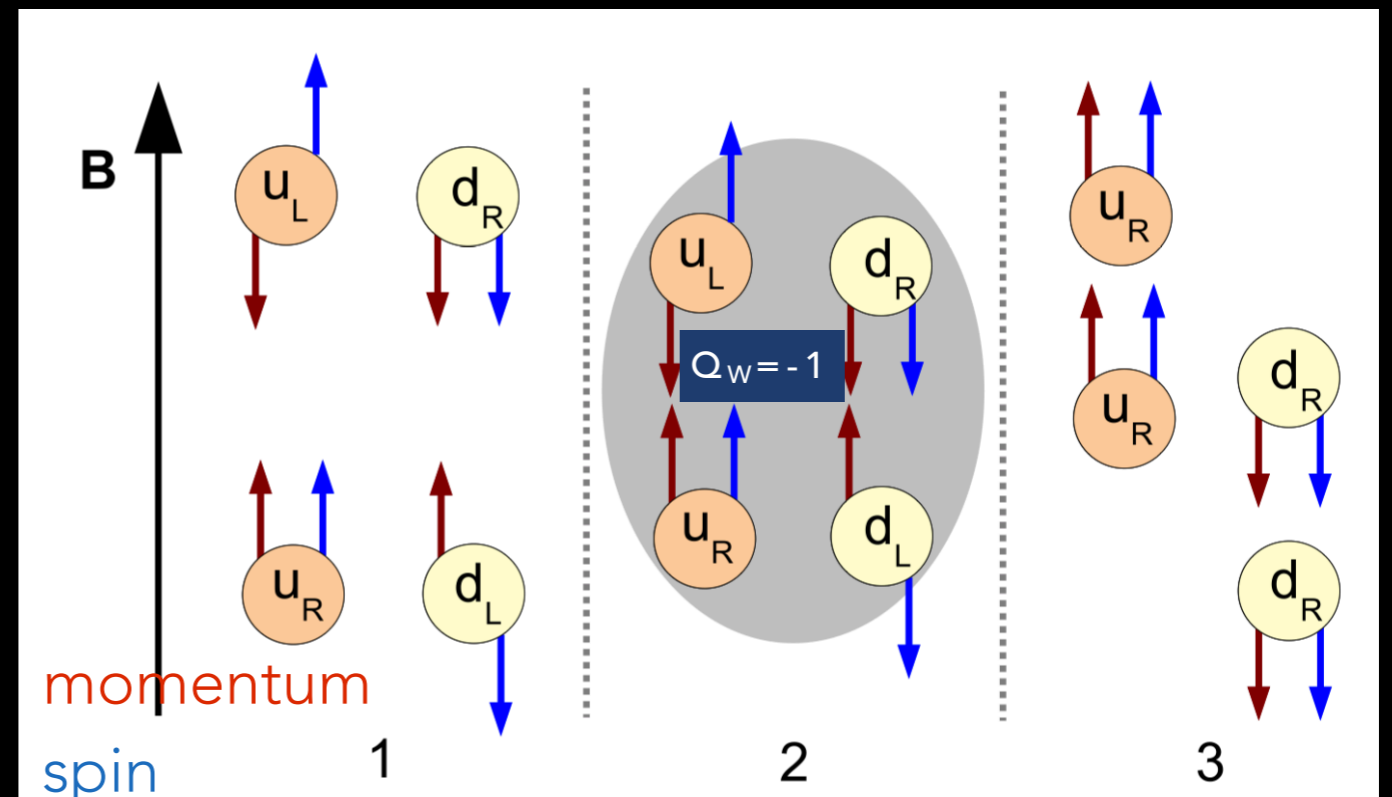
scales with  $N_{\text{part}}$

# One slide of Chiral Magnetic Effect

see [D. Kharzeev, L.D. McLerran, H.J. Warringa, Nucl.Phys.A803 : 227-253 \(2008\)](#)

- QCD has topologically non-trivial configurations of gauge fields characterized by Chern-Simons topological charge
- Sphaleron configurations dominate at high temperature
- Configurations with positive topological charge convert right-handed fermions into left-handed ones  $(N_L^f - N_R^f) = 2Q_W$
- Large magnetic field suppresses spin flip, so momenta change

- In the example a net chirality is induced by the gauge field, then a net charge separation is generated by the current along the magnetic field



# Correlators sensitive to charge separation

S. Voloshin, PRC 70, 057901 (2004)

- Measure difference in correlations along the x and y axes:

$$C_{112} = \langle \cos(\phi_\alpha + \phi_\beta - 2\phi_c) \rangle$$

Correlations that do not depend on the orientation with respect to the reaction plane cancel out

- In case of the CME:
  - $\alpha=+/-$  and  $\beta=+/-$  (same sign): negative  $C_{112}$
  - $\alpha=+/-$  and  $\beta=-/+$  (opposite sign): positive  $C_{112}$
- Generally consider the difference

$$\Delta C_{mnk} = C_{mnk}(\text{OS}) - C_{mnk}(\text{SS})$$

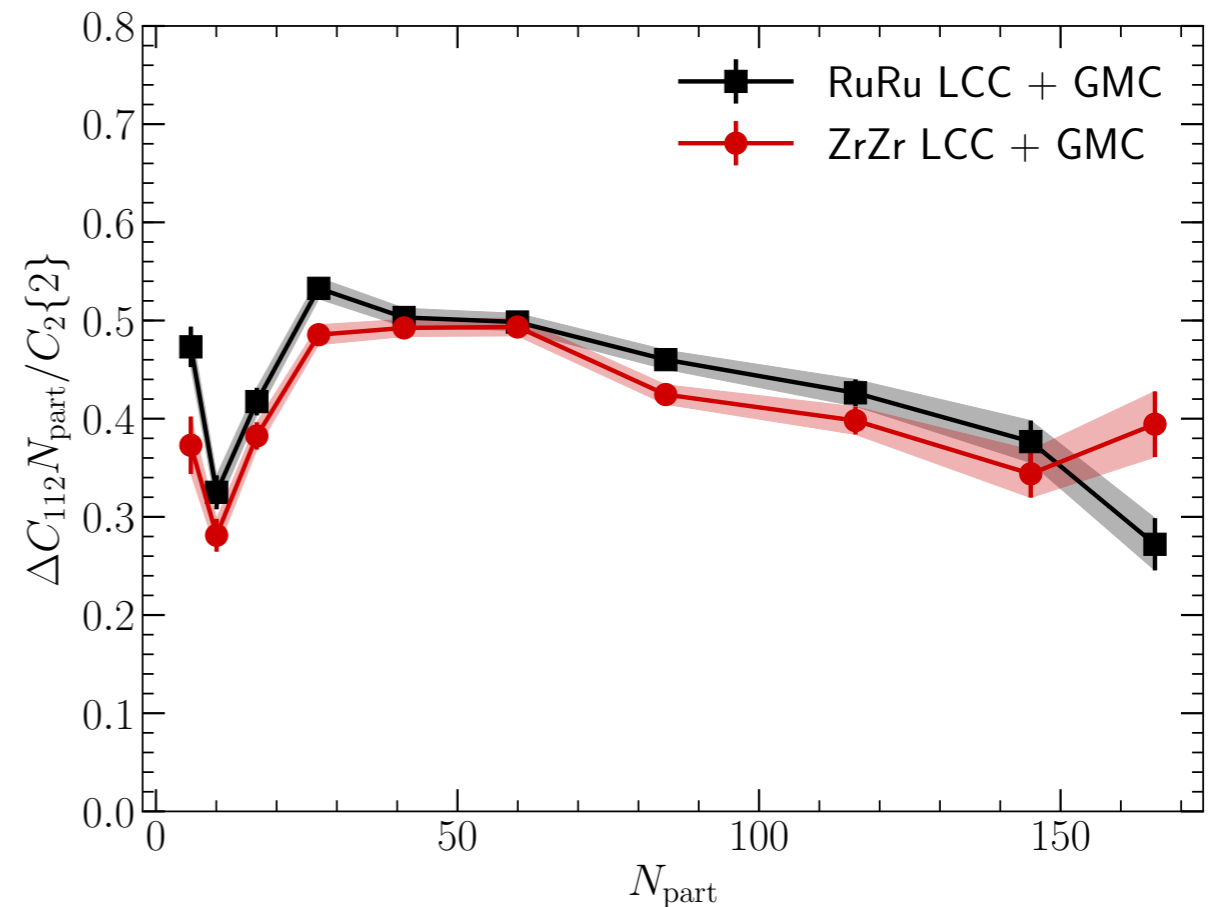
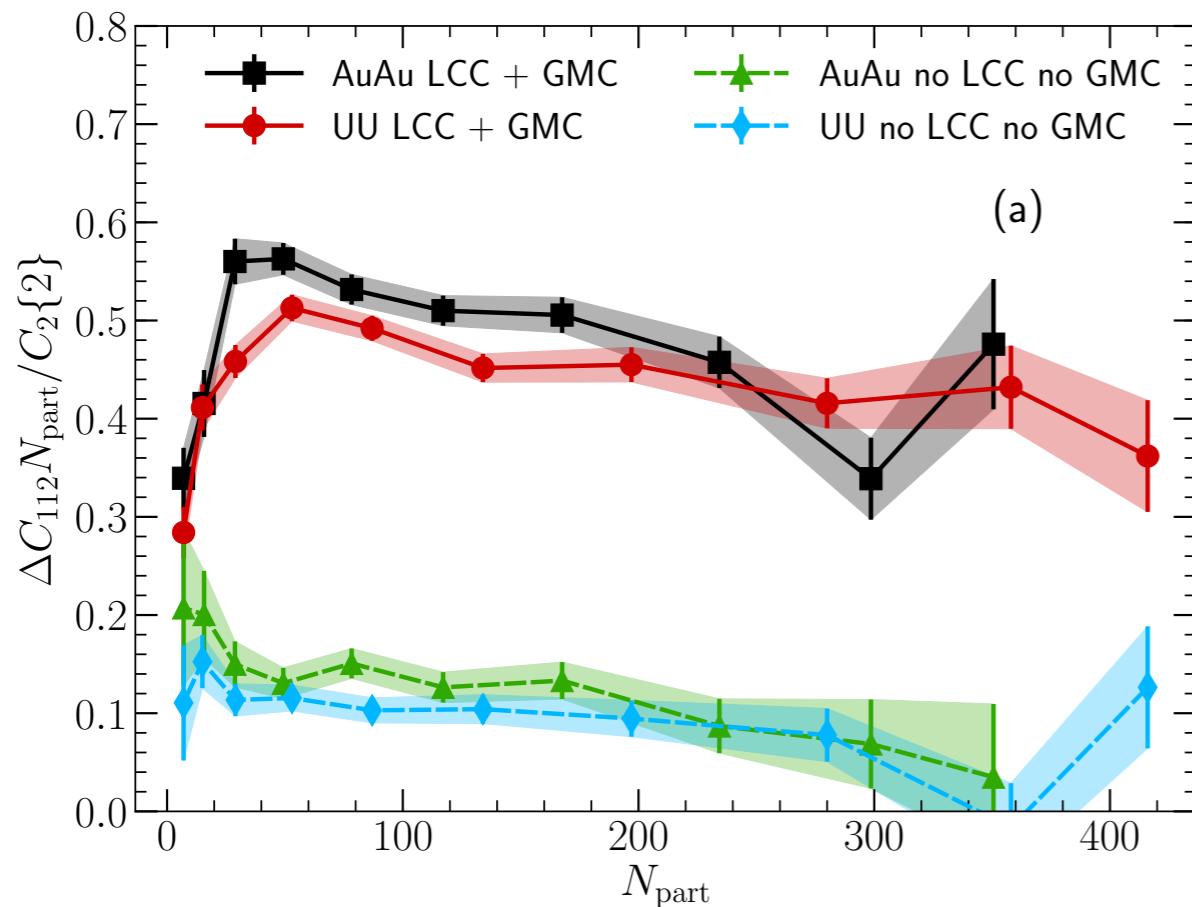
here we also cancel effects of local momentum conservation

# Baseline for the CME search

B. Schenke, C. Shen, P. Tribedy, arXiv:1901.04378

Au+Au and U+U

RHIC Isobar run



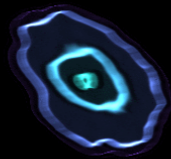
Difference in magnetic field between Ru and Zr  
expected to lead to ~10-15% larger  $\Delta C_{112}$  for Ru from CME

Deng, Huang, Ma, Wang, Phys. Rev. C 97, 044901 (2018); Shi, Jiang, Lilleskov, Liao, Annals of Physics 394 (2018) 50-72; Sun, Ko, Phys. Rev. C 98, 014911 (2018)

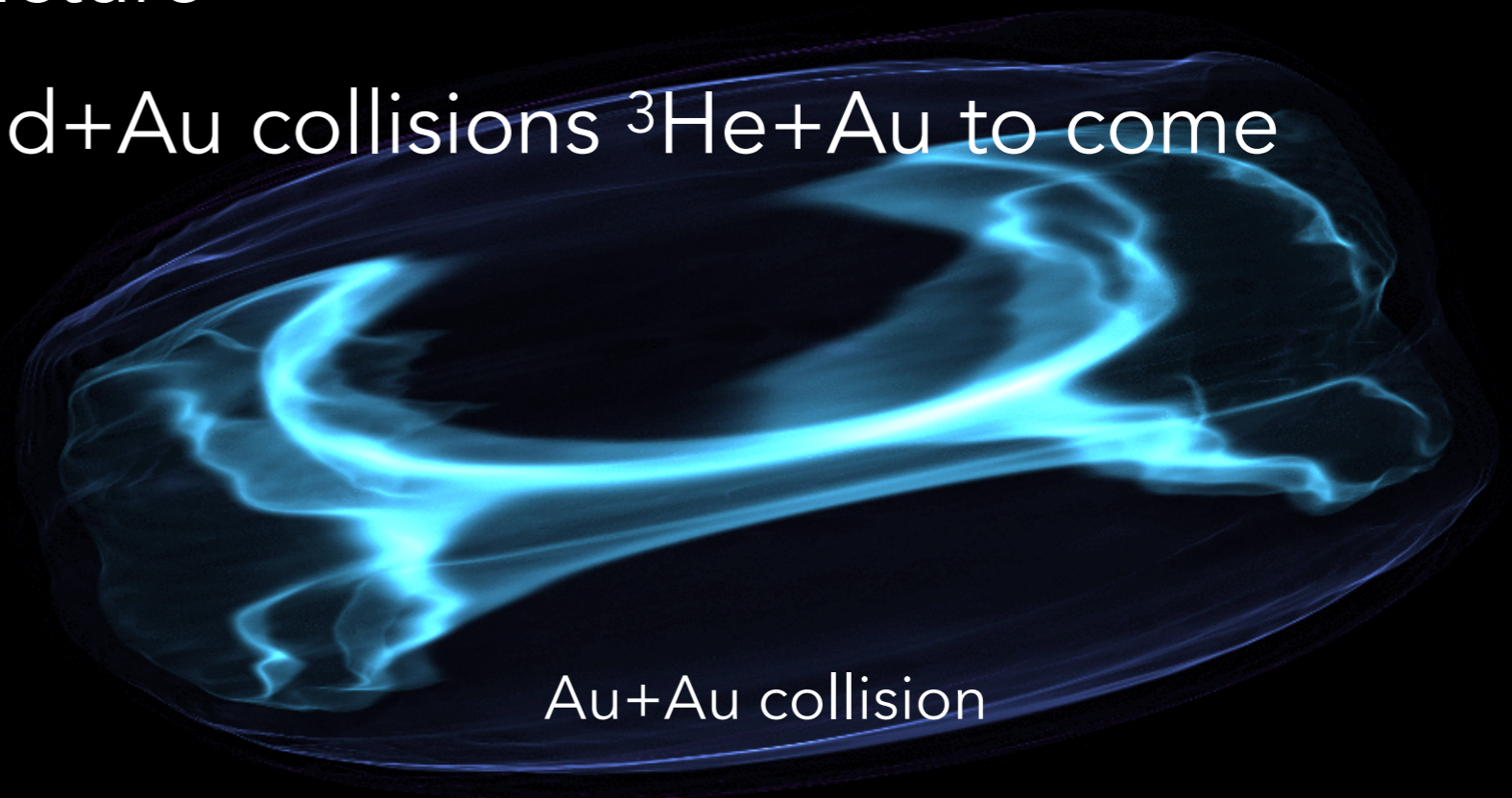


# Going smaller: What is the dominant origin of azimuthal anisotropies in small systems?

- Initial momentum anisotropy from CGC (in IP-Glasma)
- Hydrodynamics with shear and bulk viscosities
- Parameters fixed using shown AA calculations (and HERA)
  - add 3 hotspot substructure
- Predict  $v_n$  in p+Au and d+Au collisions  $^3\text{He}+\text{Au}$  to come



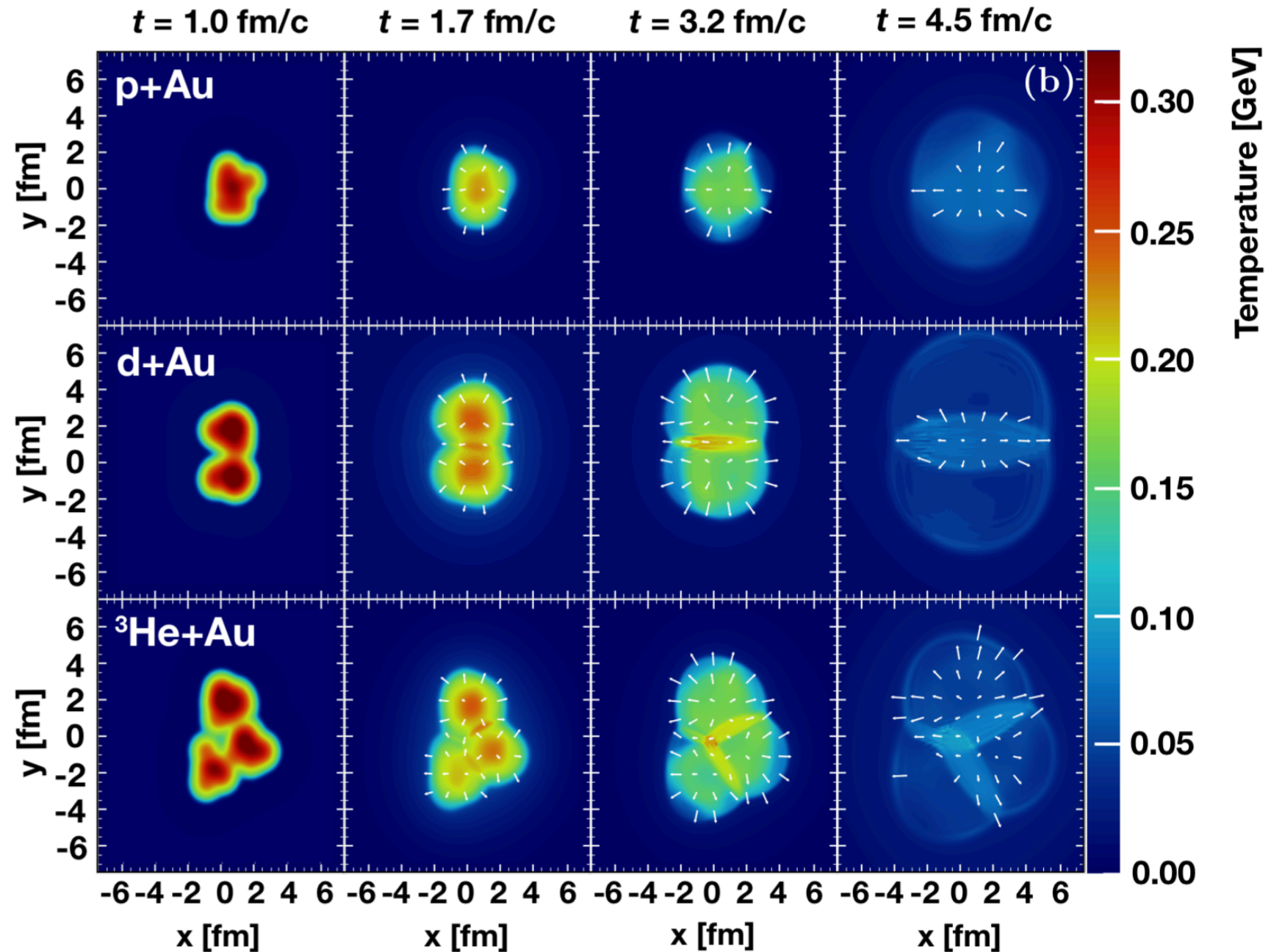
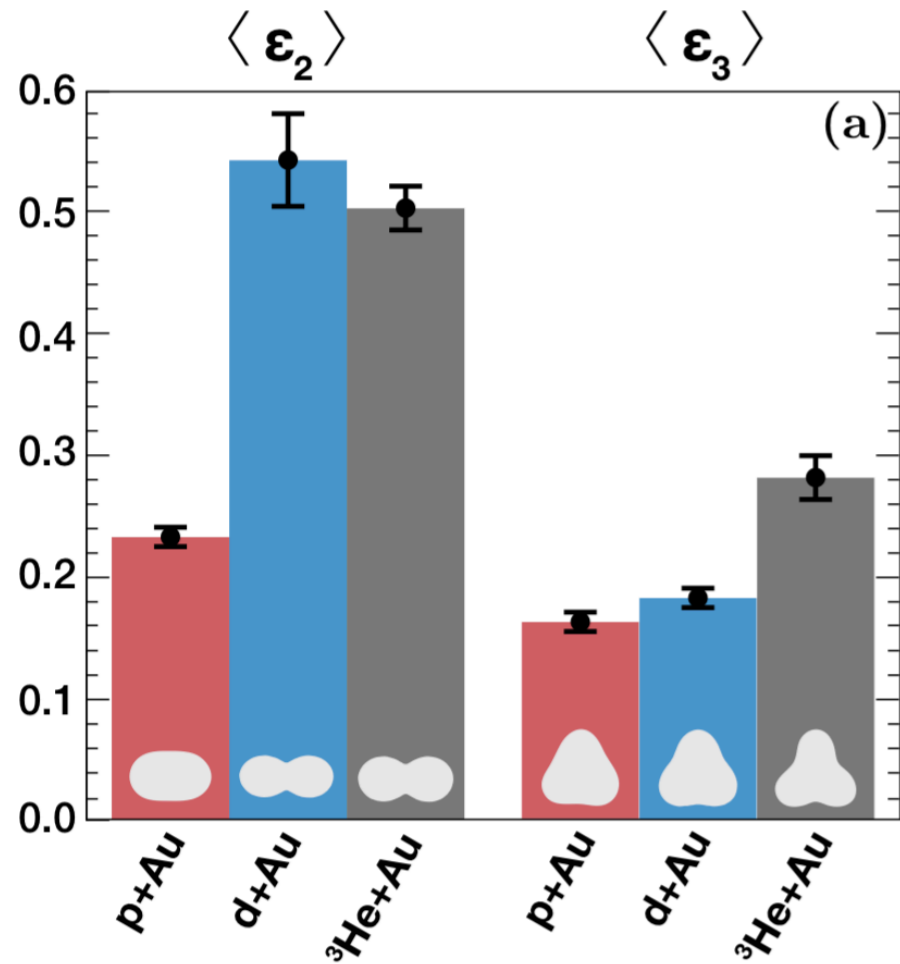
p+Au collision



Au+Au collision

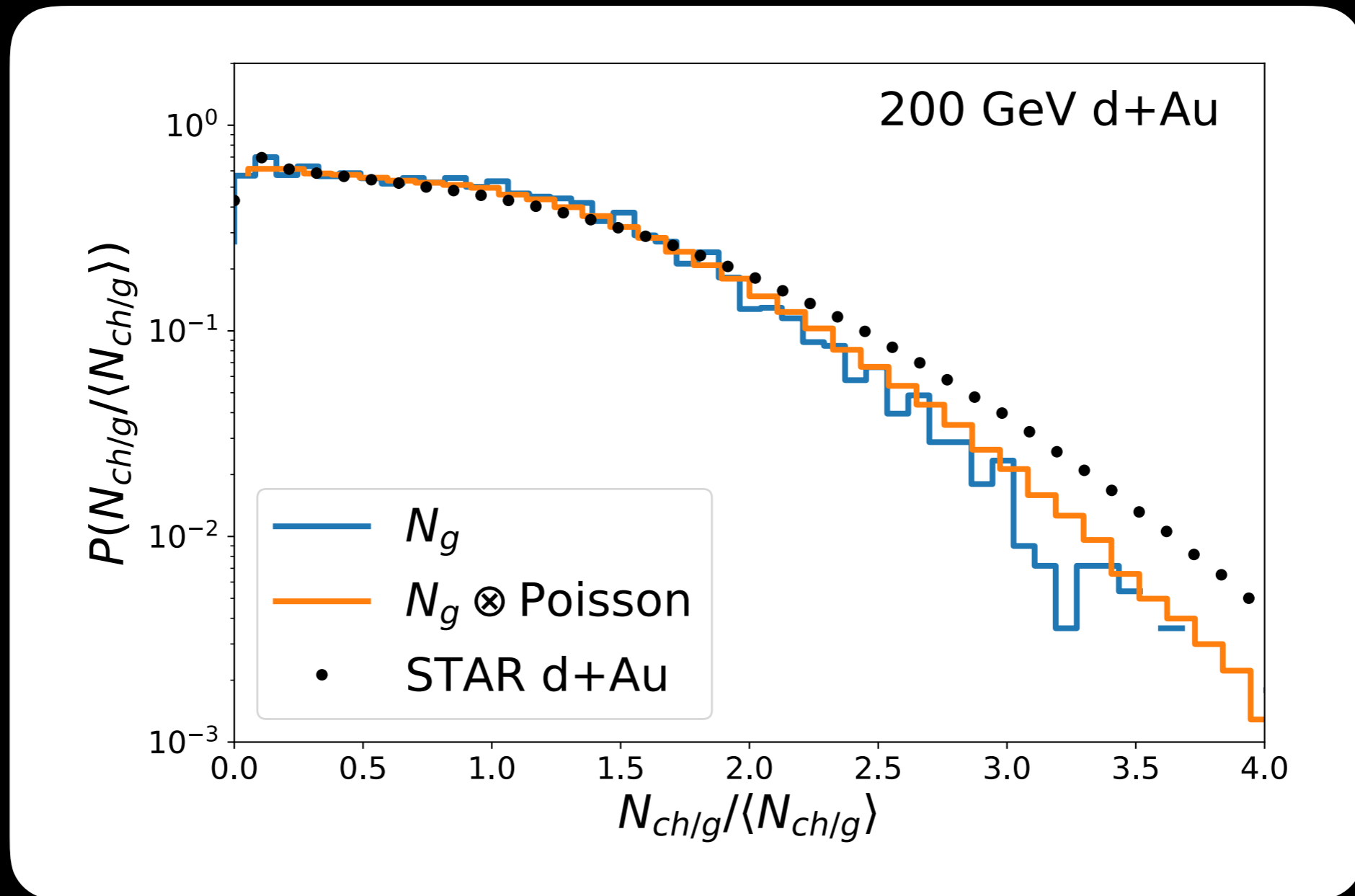
# RHIC system scan: pAu, dAu, $^3\text{HeAu}$

PHENIX Collaboration, arXiv:1805.02973v2



# RHIC system scan

B. Schenke, C. Shen, P. Tribedy, in preparation

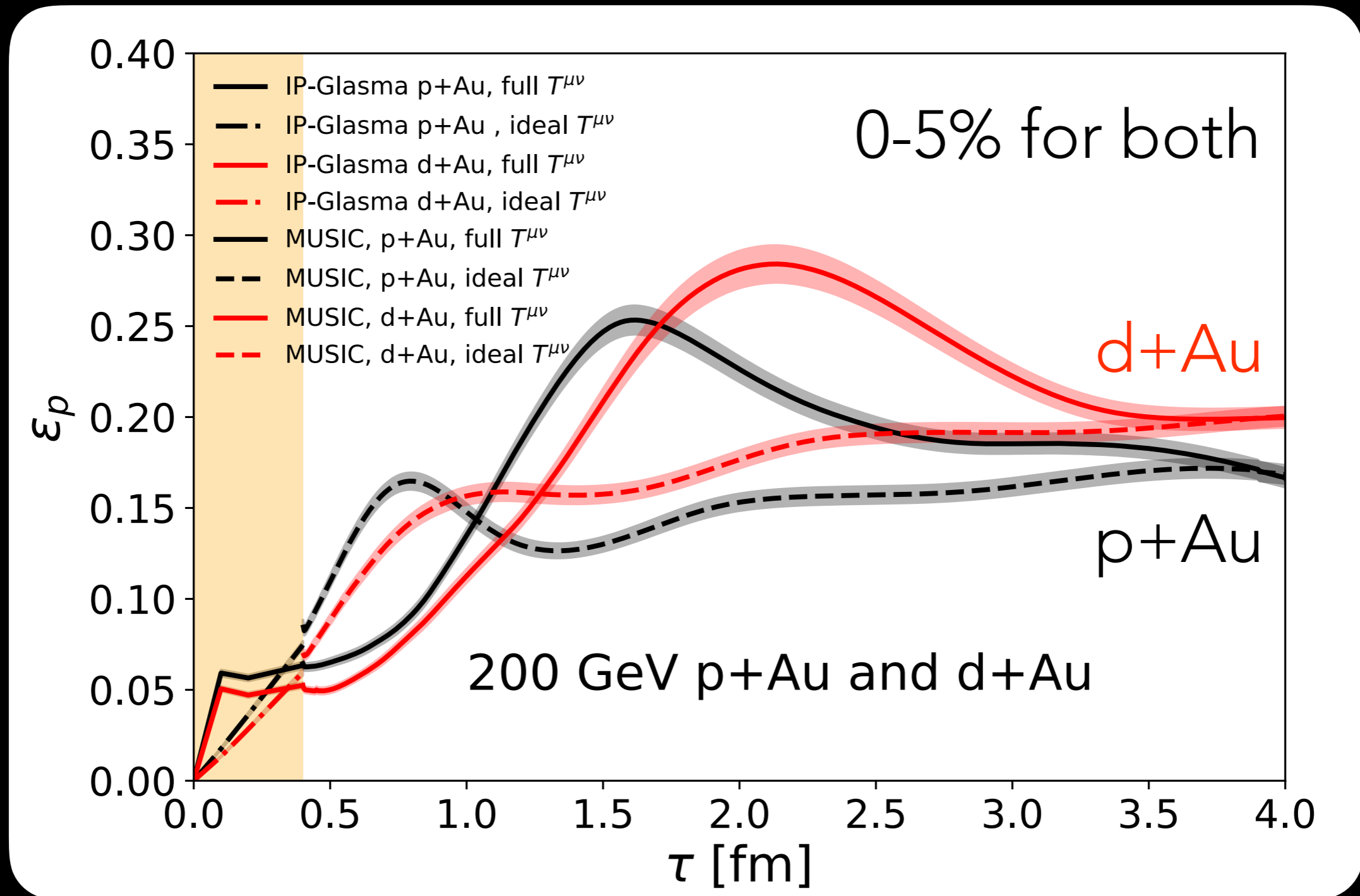


Multiplicity distribution: d+Au 200 GeV

# RHIC system scan

$$\epsilon_p = \sqrt{\frac{\langle T^{xx} - T^{yy} \rangle^2 + \langle 2T^{xy} \rangle^2}{\langle T^{xx} + T^{yy} \rangle^2}}$$

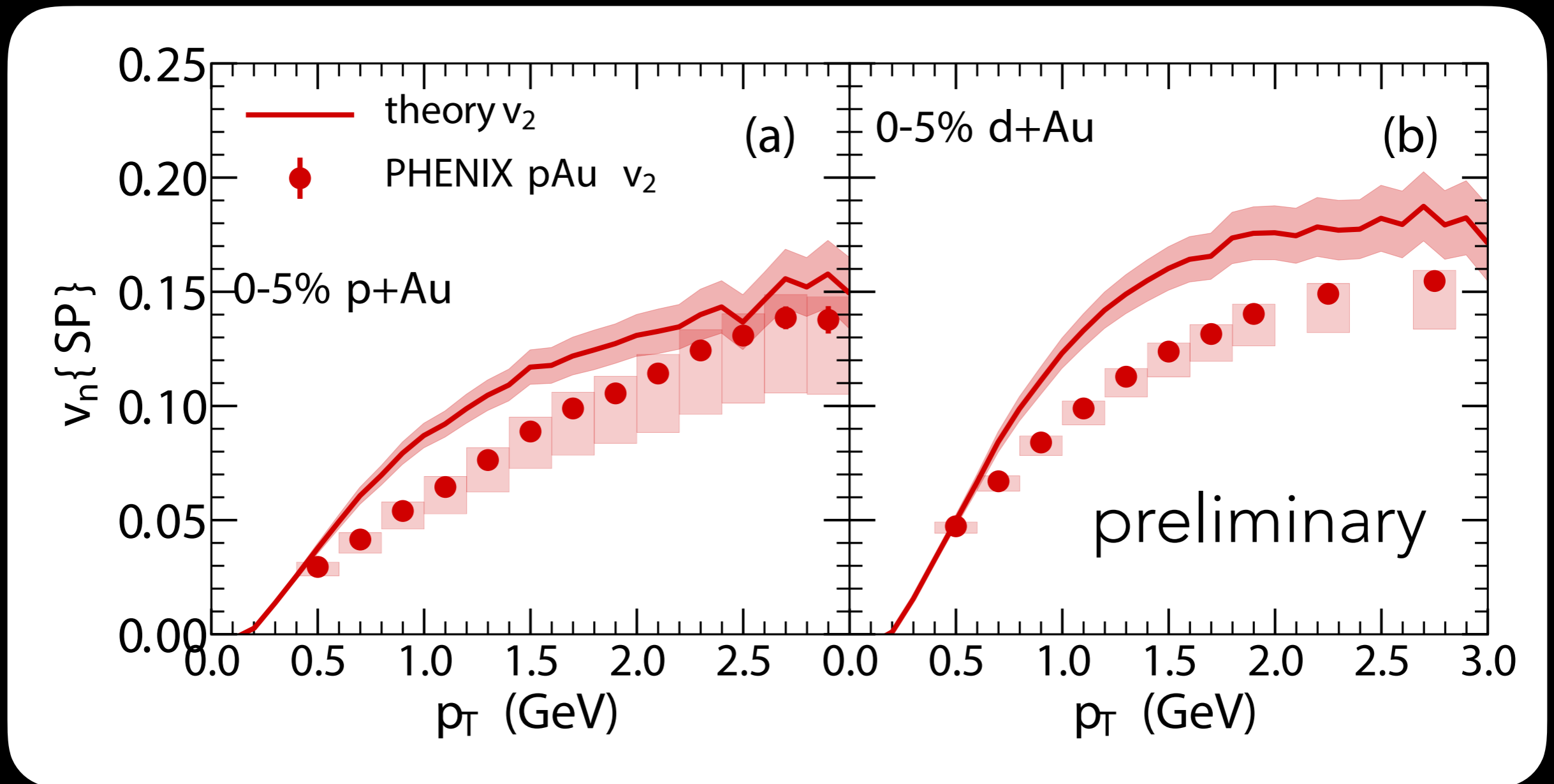
B. Schenke, C. Shen, P. Tribedy, in preparation



# $v_2$ in pAu and dAu at 0-5%

B. Schenke, C. Shen, P. Tribedy, in preparation

$\eta/s=0.12$

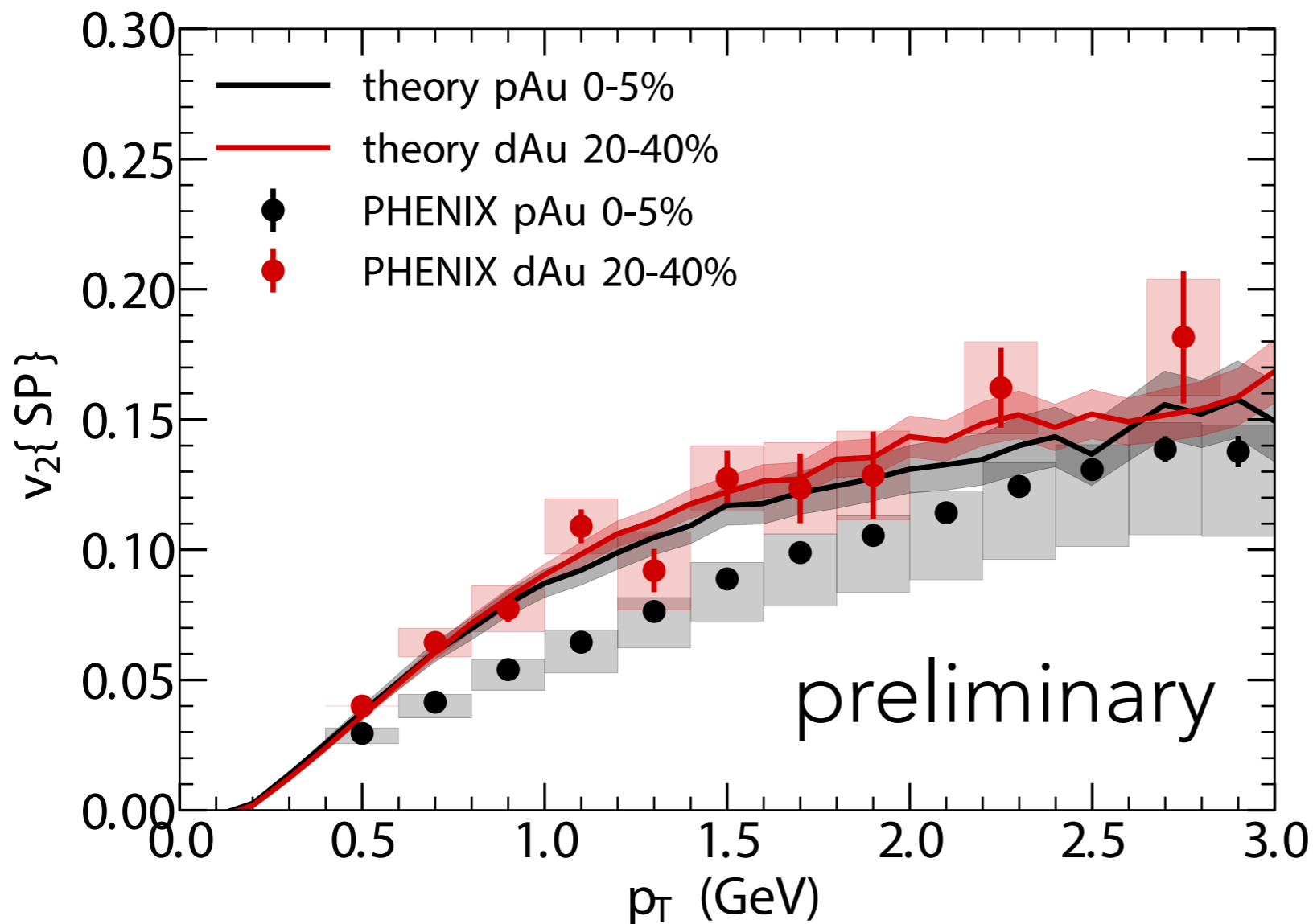


PHENIX Collaboration, e-Print: [arXiv:1805.02973](https://arxiv.org/abs/1805.02973)

Calculation:  $dN/d\eta = 19.6$  for dAu, 11.3 for pAu

# $v_2$ in pAu and dAu at $\sim$ same $N_{ch}$

B. Schenke, C. Shen, P. Tribedy, in preparation



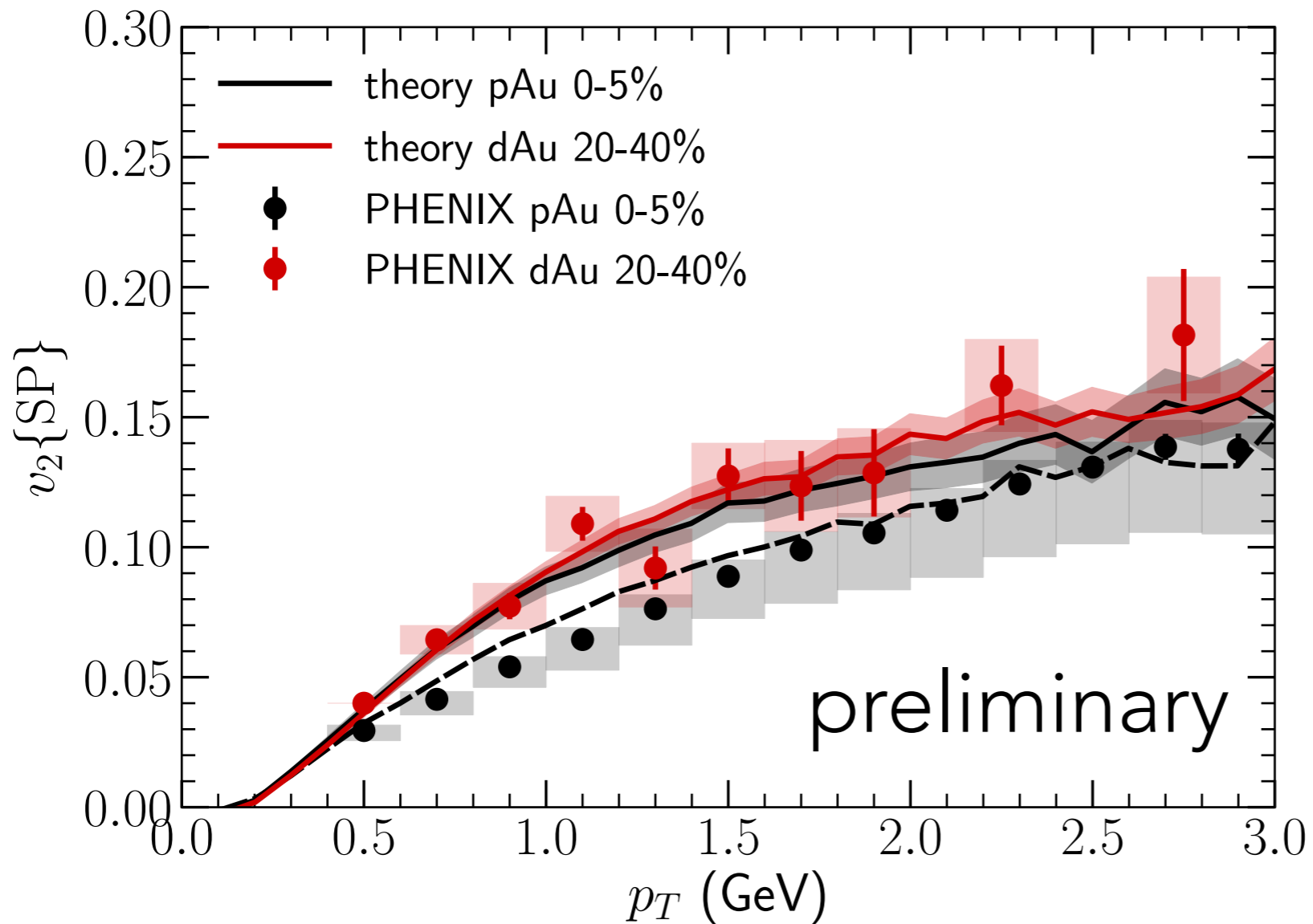
$\eta/s=0.12$

PHENIX Collaboration, e-Print: [arXiv:1805.02973](https://arxiv.org/abs/1805.02973)

Calculation:  $dN/d\eta = 9.8$  for dAu, 11.3 for pAu

# $v_2$ in pAu and dAu at $\sim$ same $N_{ch}$

B. Schenke, C. Shen, P. Tribedy, in preparation



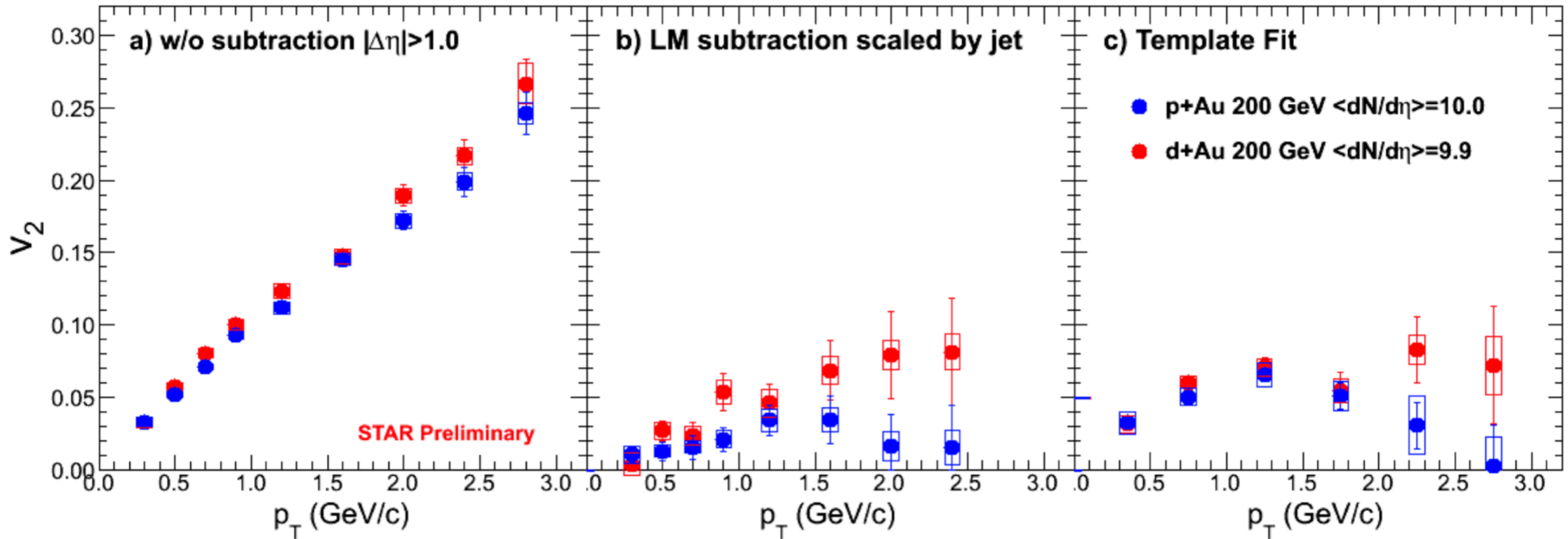
dashed line:  
different  
parameters for  
fluctuating  
proton

dAu  
little affected

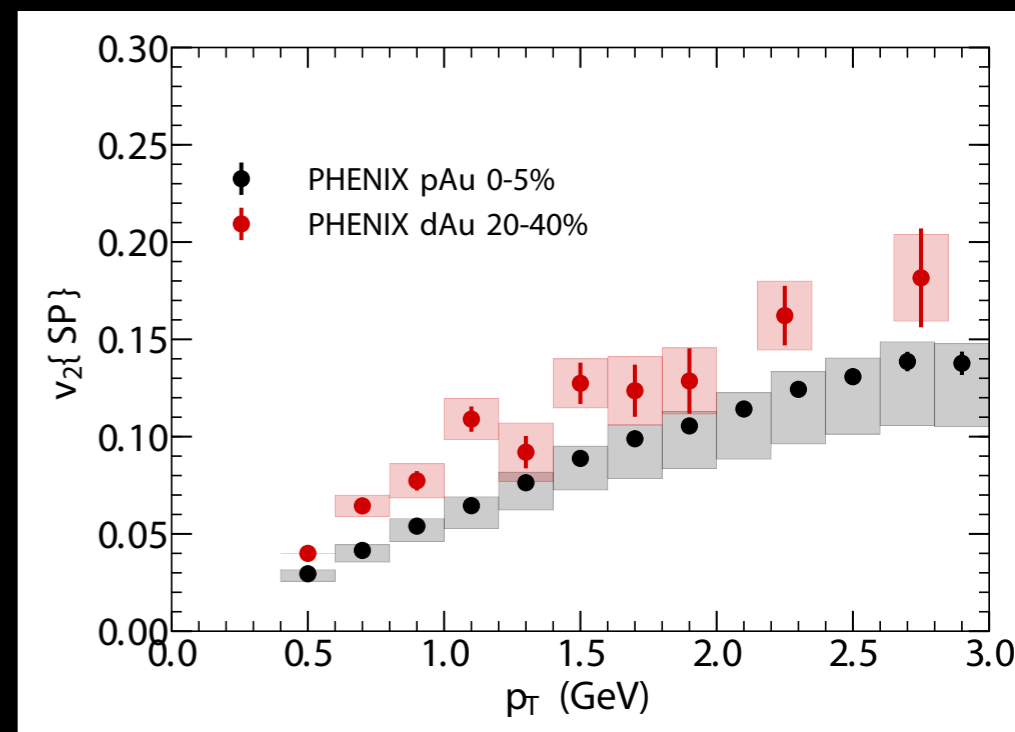
PHENIX Collaboration, e-Print: [arXiv:1805.02973](https://arxiv.org/abs/1805.02973)

Calculation:  $dN/d\eta = 9.8$  for dAu,  $11.3$  for pAu

# Data: $v_2$ in pAu and dAu at $\sim$ same $N_{ch}$



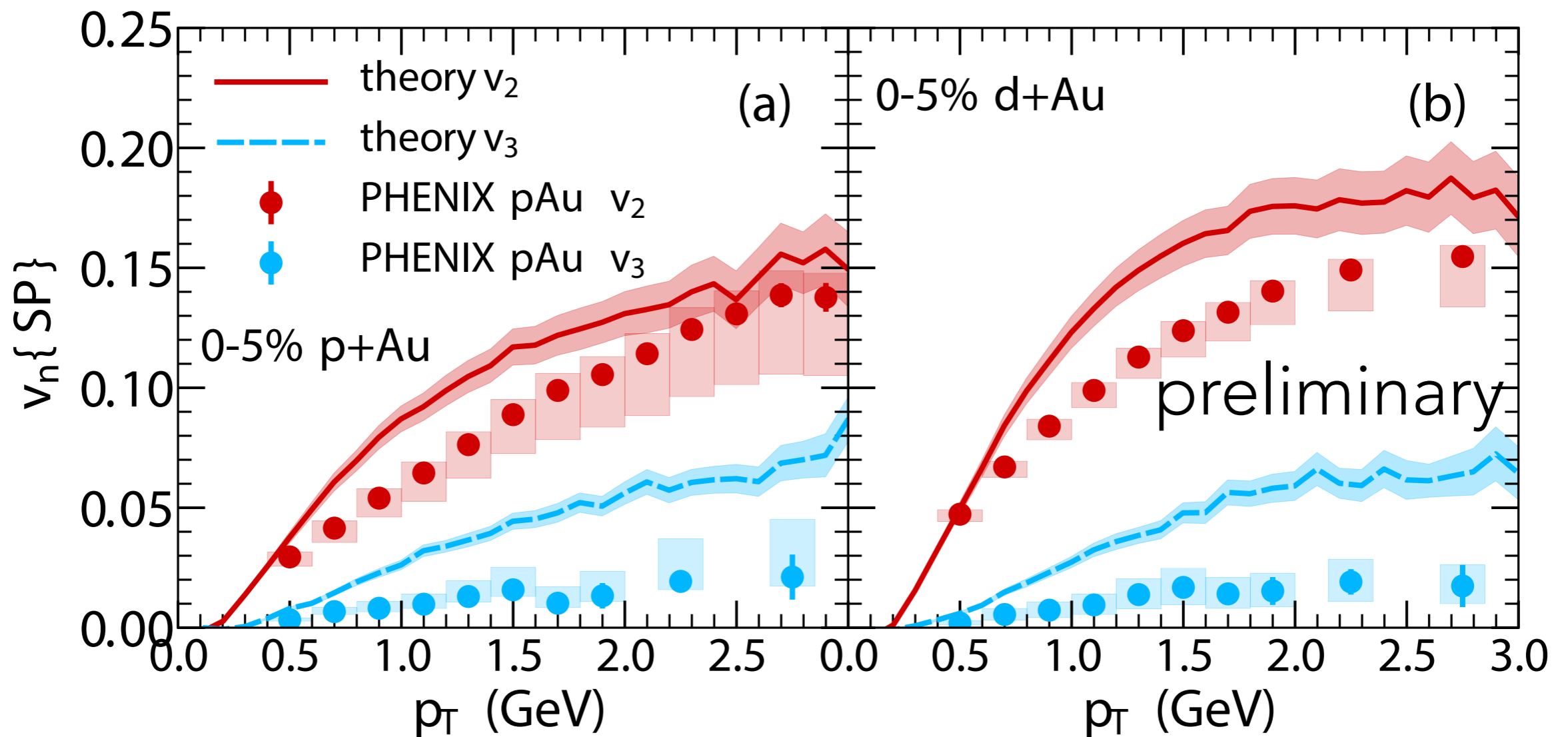
STAR Collaboration, talk by Shengli Huang, QM2018  
PHENIX Collaboration, e-Print: arXiv:1805.02973





# $v_3$ in pAu and dAu - too large...

B. Schenke, C. Shen, P. Tribedy, in preparation

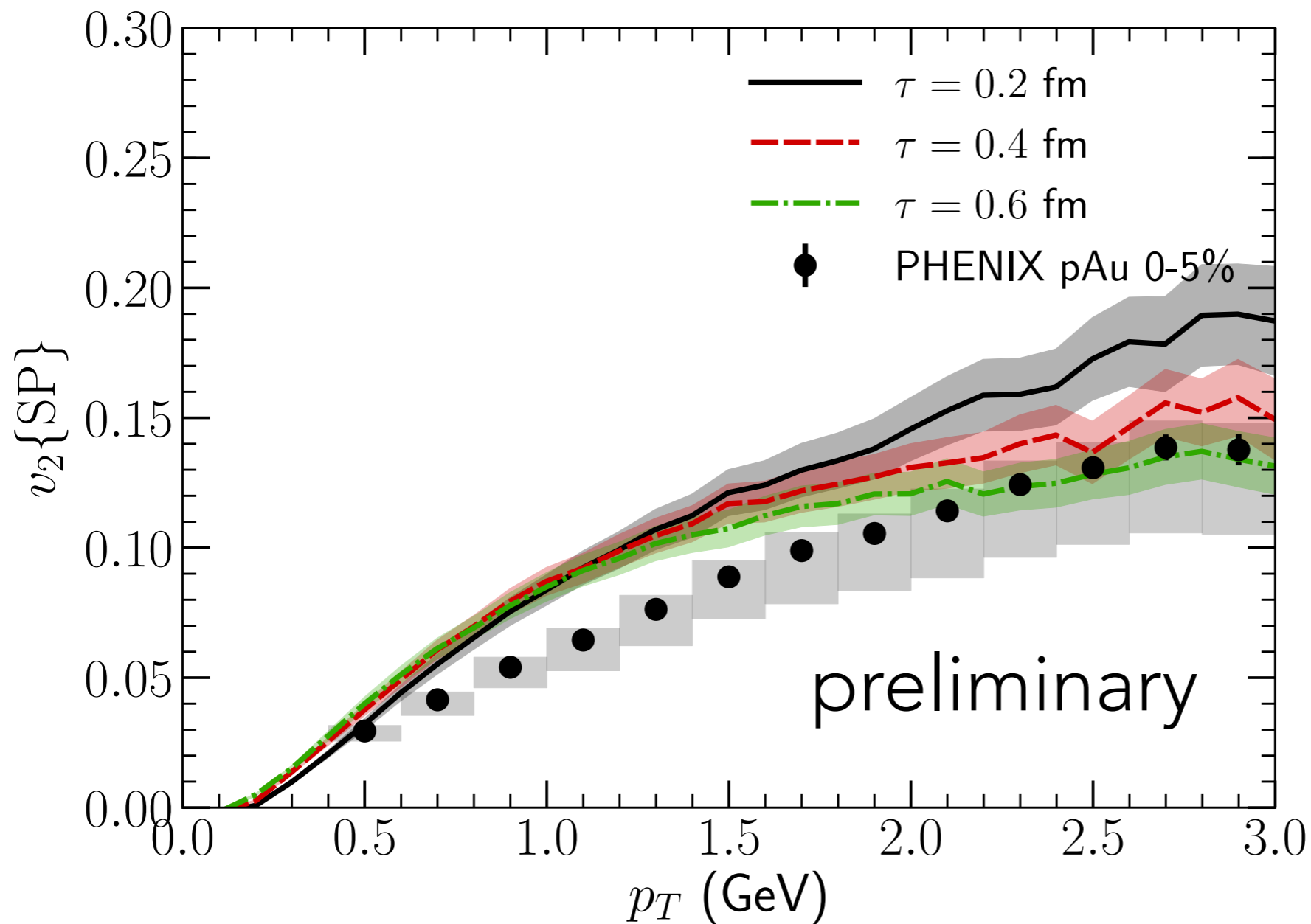


PHENIX Collaboration, e-Print: [arXiv:1805.02973](https://arxiv.org/abs/1805.02973)

Calculation:  $dN/d\eta = 19.6$  for dAu,  $11.3$  for pAu

# Effect of switching time on $v_2$

B. Schenke, C. Shen, P. Tribedy, in preparation

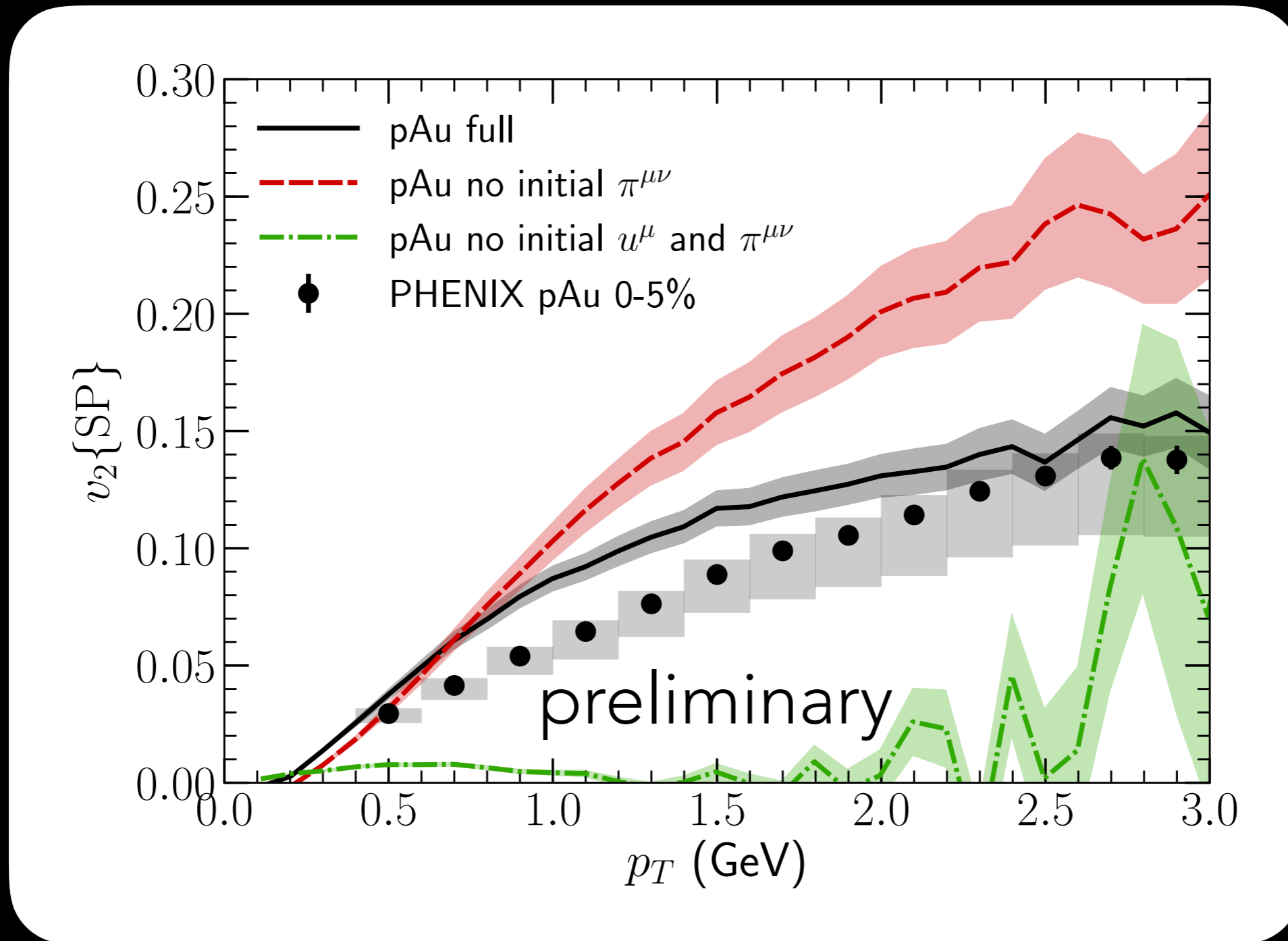


larger  
initial  $\pi^{\mu\nu}$  for  
later  
switching  
time:  
reduction of  
 $v_2$  at high  $p_T$

# Effect of initial flow and viscous tensor

B. Schenke, C. Shen, P. Tribedy, in preparation

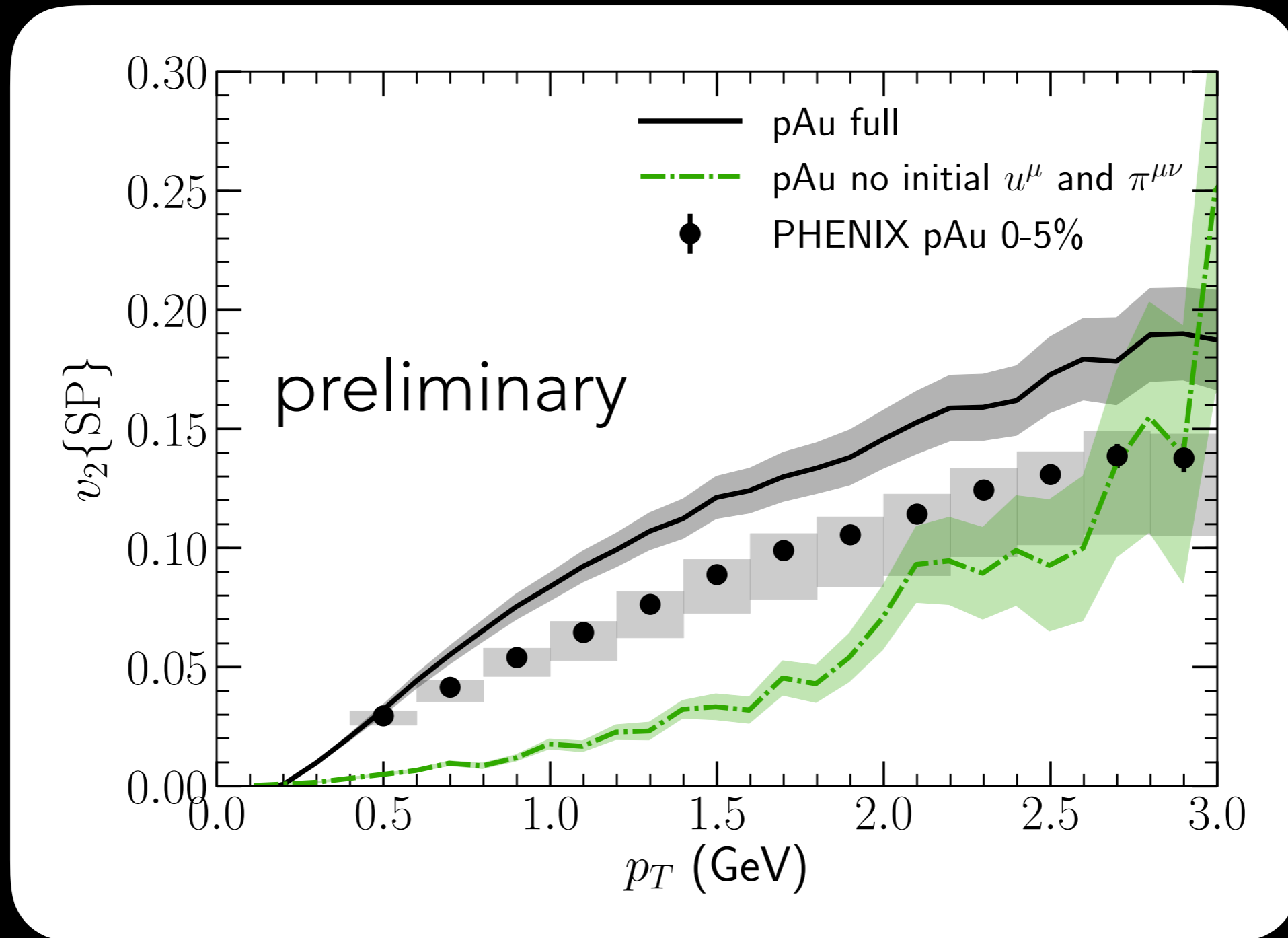
$\tau_0=0.4\text{fm}$



# Effect of initial flow

B. Schenke, C. Shen, P. Tribedy, in preparation

$\tau_0=0.2\text{fm}$



# Conclusions

- Hybrid model (IP-Glasma+MUSIC+UrQMD) provides good description of bulk observables in heavy ion collisions
- Inclusion of local charge conservation when sampling allows for predictions of CME-sensitive correlators
- We make predictions for RHIC isobar run
- Small systems not perfectly well described when all parameters are fixed to describe heavy ion collisions
- Initial flow and viscous tensor have large effect on final flow observables

# Backup