



Transport coefficients and evolution of QGP phase at finite baryon density

Olga Soloveva



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In collaboration with D. Fuseau, J. Aichelin







ubatech

Properties of QGP: transport coefficients

"Numerical simulations are now essential to make contact between theory and experiment" - J. Kapusta SQM 22

! One has to specify transport and microscopic properties as well as EoS for theoretical simulations of HICs (hydro / transport approaches)



```
EoS(\epsilon,n) \sigma(\sqrt{s}, m_q, m_q, T, \mu_B) m(T, \mu_B)
```

On practice: effective models for QGP

Transport simulations with QGP phase:

Catania transport — QuasiParticle Model F. Scardina, S. K. Das, V. Minissale, S. Plumari, and V. Greco, PRC 96, 044905 (2017).

Dynamical QPM for partonic phase

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919P. Moreau, O. S , L. Oliva, T. Song, W. Cassing, E. Bratkovskaya, PRC 100 (2019) , 014911;

O. S, P. Moreau, L. Oliva, V. Voronyuk, V. Kireyeu, T. Song, E. Bratkovskaya, Particles 3 (2020), 178-192

AMPT – PNJL EoS (Mean field potentials)

K.J. Sun, C. M. Ko, and Z.-W. Lin, PRC 103(2021)

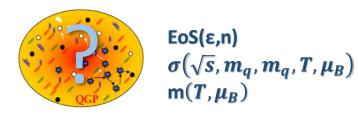
Hybrid simulations with QGP:

vHLLE/Music+UrQMD/SMASH

lu.A. Karpenko, P. Huovinen, H. Petersen and M. Bleicher PRC 91 (2015), 064901.

S. Ryu, J.F.Paquet, C. Shen, G.S. Denicol, B. Schenke PRL 115 (2015), 132301

Properties of QGP: transport coefficients



On practice: effective models for QGP

Today:

Transport coefficients at finite ${f T}$ and ${f \mu}_B$

- 1.) crossover, CEP and 1st order phase transition ($N_f = 3 PNJL model$)
- 2.) crossover + CEP (Nf = 3 DQPM)



Dynamical QPM for partonic phase

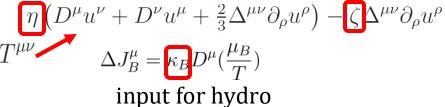
W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919
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Properties of QGP: transport coefficients

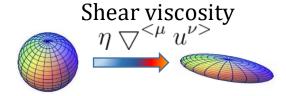
Hydrodynamics

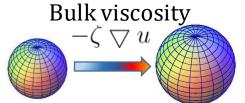
$$\partial_{\mu} T^{\mu\nu} = 0 \quad T^{\mu\nu} = -Pg^{\mu\nu} + wu^{\mu}u^{\nu} + \Delta T^{\mu\nu}$$

$$\partial_{\mu} J_{B}^{\mu} = 0 \quad J_{B}^{\mu} = n_{B}u^{\mu} + \Delta J_{B}^{\mu}$$



Transport coefficients:

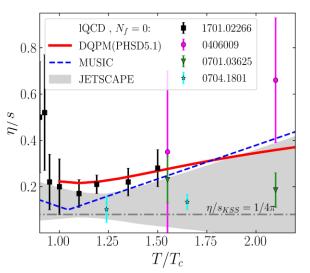


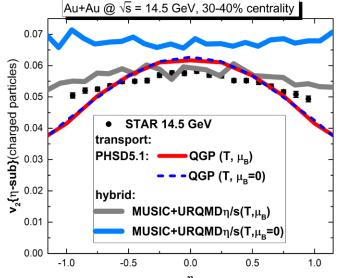


(B, Q, S) diffusion coefficients

Model predictions for QGP: ! same EoS but different transport coefficients

Transport coefficients can serve a bridge for comparison transport and hydro



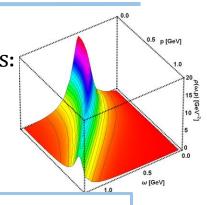


MUSIC: C. Shen, S.Alzhrani, PRC 102 (2020) 1, 014909

Dynamical Quasi-Particle Model

The QGP phase is described in terms of strongly-interacting quasiparticles - quarks and gluons with Lorentzian spectral functions:

$$\rho_j(\omega, \mathbf{p}) = \frac{\gamma_j}{\tilde{E}_j} \left(\frac{1}{(\omega - \tilde{E}_j)^2 + \gamma_j^2} - \frac{1}{(\omega + \tilde{E}_j)^2 + \gamma_j^2} \right)$$
$$\equiv \frac{4\omega\gamma_j}{\left(\omega^2 - \mathbf{p}^2 - M_j^2\right)^2 + 4\gamma_j^2\omega^2}$$



resummed propagators: $\Delta_i(\omega, \mathbf{p}) = \frac{1}{\omega^2 - \mathbf{p}^2 - \Pi_i}$ & self-energies: $\Pi_i = m_i^2 - 2i\gamma_i\omega$

Re Π_i : thermal mass (M_q, M_q)

$$m_{q(\bar{q})}^2(T,\mu_{\rm B}) = C_q \frac{g^2(T,\mu_{\rm B})}{4} T^2 \left[1 + \left(\frac{\mu_B}{3\pi T}\right)^2\right]$$
 quark mass

Im Π_i : interaction width (γ_g, γ_q)

$$\gamma_j(T,\mu_{\rm B}) = \frac{1}{3}C_j\frac{g^2(T,\mu_{\rm B})T}{8\pi}\ln\left(\frac{2c_m}{g^2(T,\mu_{\rm B})}+1\right)$$

0.70

Peshier, Cassing, PRL 94 (2005) 172301; Cassing, NPA 791 (2007) 365; H. Berrehrah, E. Bratkovskaya, T. Steinert, W. Cassing, Int. J. Mod. Phys. E 25 (2016), 164200; P. Moreau, O. Soloveva, L. Oliva, T. Song, W. Cassing, E. Bratkovskaya, PRC 100 (2019), 014911;

PM: EoS

 $\bar{q} = \bar{u}, \bar{d}, \bar{s}$

Entropy and baryon density in the quasiparticle limit (G. Baym 1998, Blaizot et al. 2001):

$$s^{dqp} = n^{dqp} = -\int \frac{d\omega}{2\pi} \frac{d^3p}{(2\pi)^3} \left[d_g \frac{\partial n_B}{\partial T} \left(\operatorname{Im} (\ln -\underline{\Delta}^{-1}) + \operatorname{Im} \underline{\Pi} \operatorname{Re} \underline{\Delta} \right) \right]$$

$$+ \sum_{q=u,d,s} d_q \frac{\partial n_F(\omega - \mu_q)}{\partial T} \left(\operatorname{Im} (\ln -\underline{S}_q^{-1}) + \operatorname{Im} \underline{\Sigma}_q \operatorname{Re} \underline{S}_q \right)$$

$$+ \sum_{q=u,d,s} d_{\bar{q}} \frac{\partial n_F(\omega + \mu_q)}{\partial T} \left(\operatorname{Im} (\ln -\underline{S}_q^{-1}) + \operatorname{Im} \underline{\Sigma}_q \operatorname{Re} \underline{S}_q \right)$$

$$+ \sum_{q=u,d,s} d_{\bar{q}} \frac{\partial n_F(\omega + \mu_q)}{\partial \mu_q} \left(\operatorname{Im} (\ln -\underline{S}_q^{-1}) + \operatorname{Im} \underline{\Sigma}_q \operatorname{Re} \underline{S}_{\bar{q}} \right)$$

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$$+ \sum_{\bar{q}=\bar{u},\bar{d},\bar{s}} d_{\bar{q}} \frac{\partial n_{F}(\omega + \mu_{q})}{\partial T} \left(\operatorname{Im}(\ln -\underline{S_{q}^{-1}}) + \operatorname{Im} \underline{\Sigma}_{\underline{q}} \operatorname{Re} \underline{S_{q}} \right)$$

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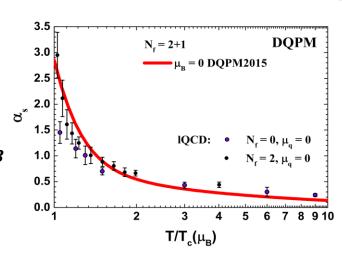
$$+ \sum_{\bar{q}=\bar{u},\bar{d},\bar{s}} d_{\bar{q}} \frac{\partial n_{F}(\omega + \mu_{q})}{\partial \mu_{q}} \left(\operatorname{Im}(\ln -\underline{S_{q}^{-1}}) + \operatorname{Im} \underline{\Sigma}_{\bar{q}} \operatorname{Re} \underline{S_{q}} \right)$$

Input: entropy density as a f(T, $\mu_B = 0$)

$$g^2(s/s_{SB})=d\left((s/s_{SB})^e-1
ight)^f$$
 fix the parameters $s^{DQPM}(\Pi,\Delta,S_q,\Sigma)=s^{lattice}$

Scaling hypothesis for the crossover region at finite μ_R

$$g^2(T/T_c, \mu_B) = g^2\left(\frac{T^*}{T_c(\mu_B)}, \mu_B = 0\right)$$
 with $T^* = \sqrt{T^2 + \mu_q^2/\pi^2}$



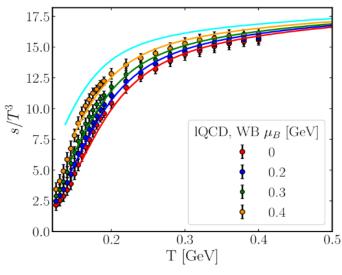
DQPM: EoS

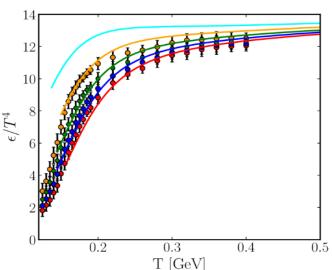


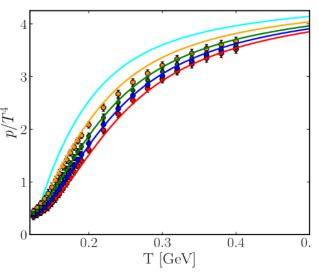
lattice EoS $\mu_B = 0$ (red dots)

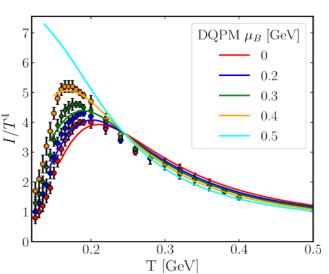
Output:

DQPM EoS $\mu_B \geq 0$ (lines)

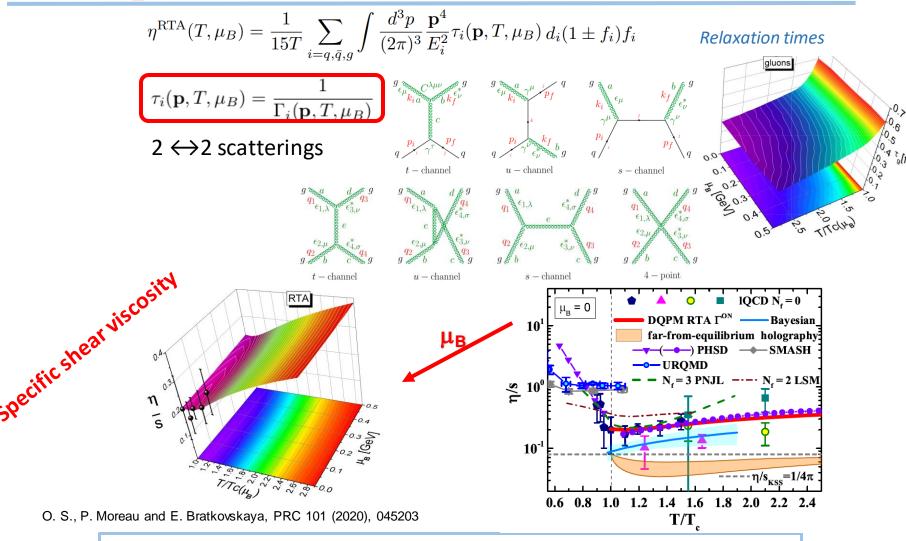






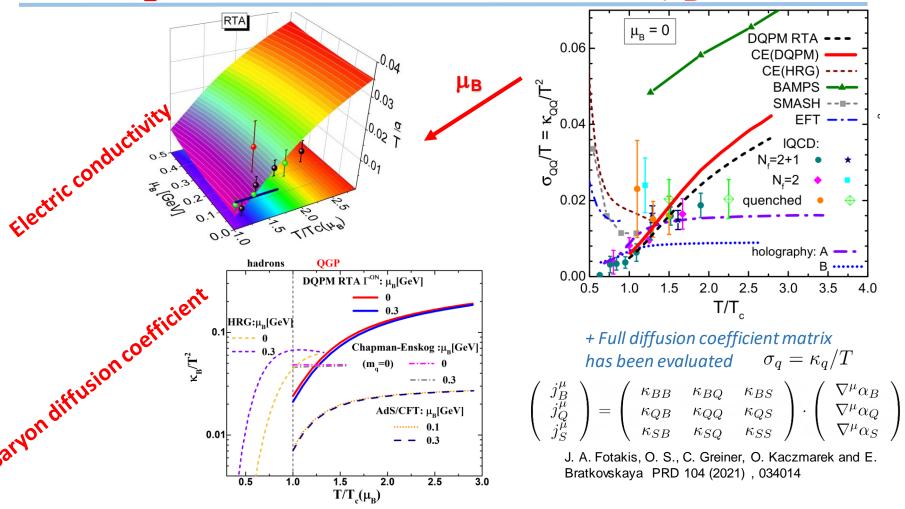


Transport coefficients at finite μ_B



- Good agreement with IQCD predictions and Bayesian estimates
- Light increase with μ_B in the crossover region for viscosities and electric conductivity

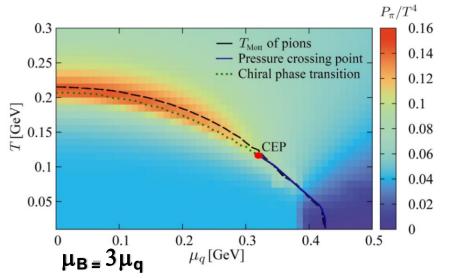
Transport coefficients at finite μ_B

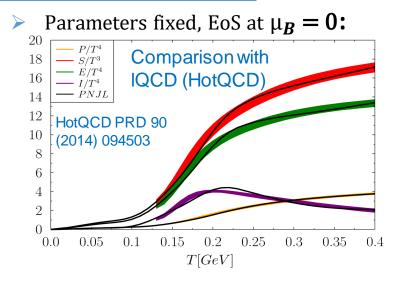


- Light increase with μ_B in the crossover region for shear and bulk viscosities and electric conductivity
- Baryon diffusion coefficients decrease with μ_B

QGP in the Polyakov extended NJL model

- PNJL allows for prediction of macroscopic properties of QGP at finite ${f T}$ and ${f \mu}_{{m B}}$
- & QGP transport coefficients for $0 \le \mu_B \le 1.2$ GeV

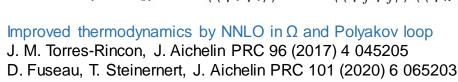


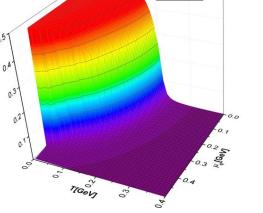


- ightharpoonup CEP: (T, μ_B) = (110,960) MeV, $\mu_B/T = 8.73$
- \triangleright 1st order PT at high μ_B
- same symmetries for the quarks as QCD

Chiral masses (M_l, M_s)

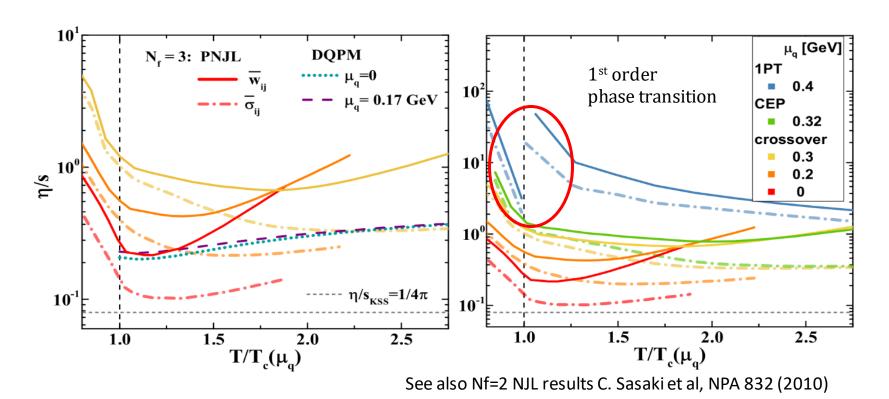
$$m_i = m_{0i} - 4G\langle\langle\bar{\psi}_i\psi_i\rangle\rangle + 2K\langle\langle\bar{\psi}_i\psi_i\rangle\rangle\langle\langle\bar{\psi}_k\psi_k\rangle\rangle$$





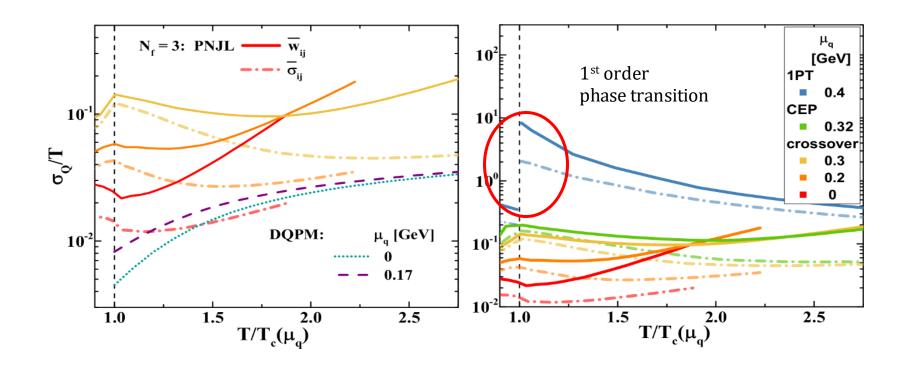
M.[GeV]

Specific shear viscosity at high μ_B



- Two different models have similar increase with μ_B –dependence in the crossover region
- Drastic change of T-dependence for all transport coefficients after
 1st order phase transition

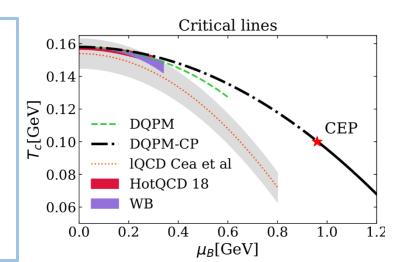
Electric conductivity at high µB



- Two different models have similar increase with μ_B –dependence in the crossover region
- Drastic change of T-dependence for all transport coefficients after
 1st order phase transition

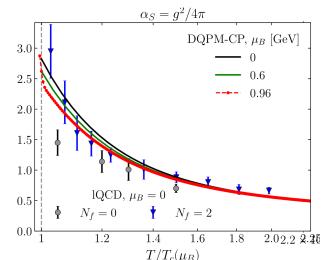
Quasiparticle model with CEP at high μ_B

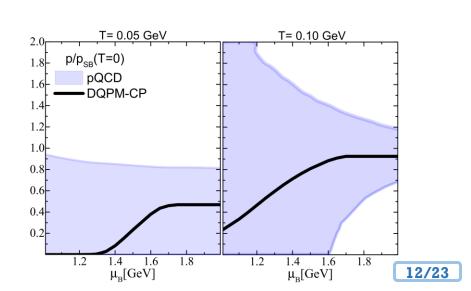
- DQPM-CP for high μ_B , including the CEP region based on the scaling properties of the entropy density from the PNJL model
- DQPM-CP interpolates EoS and microscopic properties between two asymptotics high
 T > Tc, μ_B = 0 and T > Tc, μ_B >> T
- EoS and transport coefficients of the QGP phase for the wide range of T > Tc, μ_B



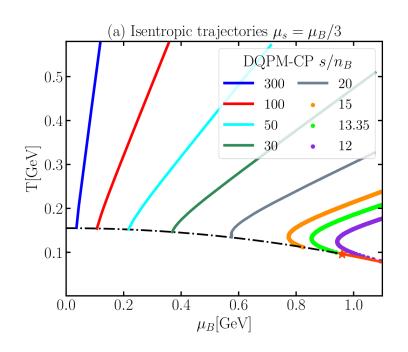
- ightharpoonup CEP: (T, μ_B) = (100,960) MeV, μ_B /T = 9.6
- \triangleright EoS: for μ_B/T <2 agreement with lQCD for μ_B/T >6 agreement with pQCD

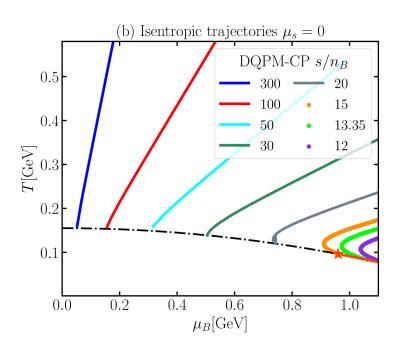
Near CEP:
$$g^2 = f(s^{PNJL}(T/T_c)) \rightarrow g^2(T/T_c)$$





Isentropic trajectories

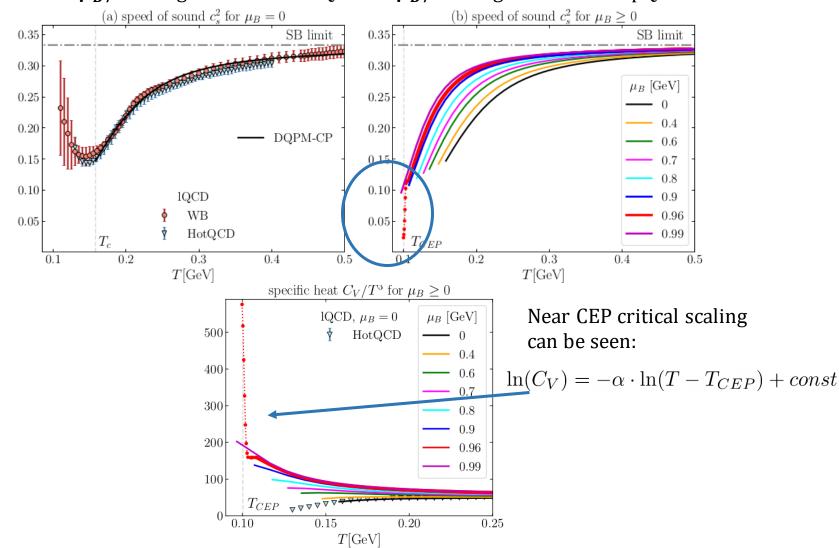




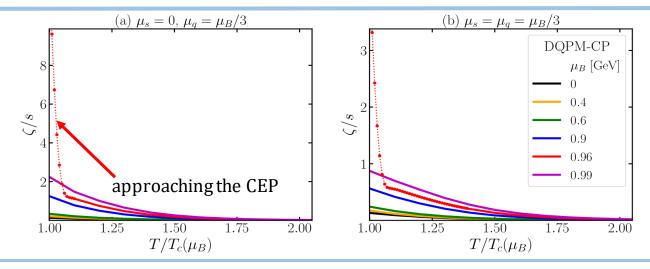
- CEP acts as an attractor of isentropic trajectories (Chiho Nonaka and Masayuki Asakawa PRC 71 (2005), 044904)
- Trajectories of $s/n_B = const$ for $< n_S > = 0$ are shifted towards higher μ_B

Speed of sound

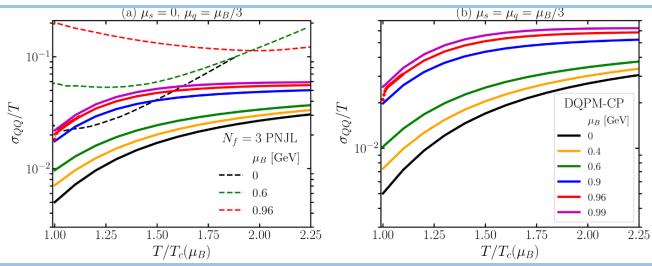
EoS: for μ_B/T < 2 agreement with IQCD for μ_B/T > 6 agreement with pQCD



Shear and bulk viscosities near the CEP

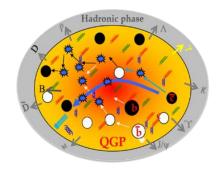


Sudden rise of specific bulk viscosity approaching the CEP



- B,Q,S diffusion coefficients have pronounced μ_B , μ_S -dependence
- Only small increase approaching the CEP

Modelling HICs: PHSD



QGP out-of equilibrium ←→ HIC

Parton-Hadron-String-Dynamics (PHSD)

Non-equilibrium microscopic transport approach for the description of strongly-interacting hadronic and partonic matter created in heavy-ion collisions

Dynamics: based on the solution of generalized off-shell transport equations derived from Kadanoff-Baym many-body theory



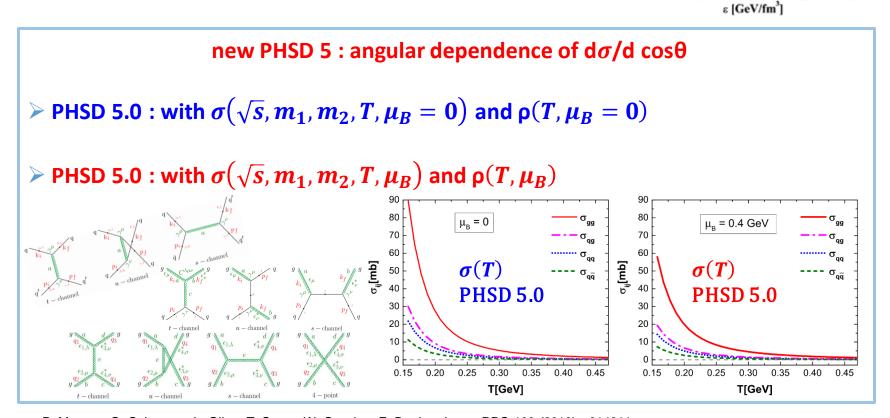
- W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919; NPA831 (2009) 215; W. Cassing, EPJ ST 168 (2009) 3;;
- P. Moreau, O. Soloveva, L. Oliva, T. Song, W. Cassing, E. Bratkovskaya, PRC 100 (2019), 014911;
- O. Soloveva, P. Moreau, L. Oliva, V. Voronyuk, V. Kireyeu, T. Song, E. Bratkovskaya, Particles 3 (2020), 178-192;....

PHSD

PHSD 4.0 : only isotropic $\sigma(T)$ and $\rho(T)$ parton cross parton

sections spectral function

(masses and widths)



P. Moreau, O. Soloveva, L. Oliva, T. Song, W. Cassing, E. Bratkovskaya, PRC 100 (2019), 014911; O. Soloveva, P. Moreau, L. Oliva, V. Voronyuk, V. Kireyeu, T. Song, E. Bratkovskaya, Particles 3 (2020), 178-192

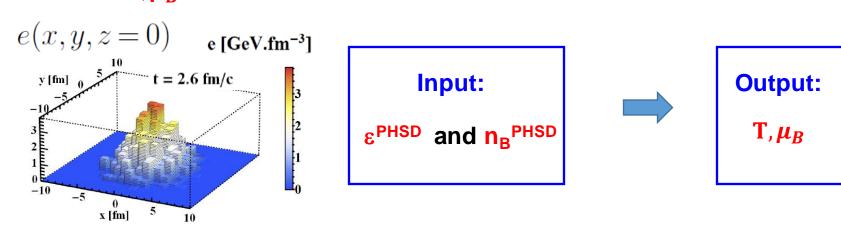
PHSD: extraction of T and µB

For each space-time cell of the PHSD: $T^{\mu\nu} = \sum_{i} \frac{p_{i}^{\mu} p_{i}^{\nu}}{E_{i}}$ \longrightarrow Diagonalize in LRF $\longrightarrow \epsilon^{\text{PHSD}}$

- 1. Calculate the local energy density ϵ^{PHSD} and baryon density n_B^{PHSD}
- 2. use IQCD relations (up to 6th order):

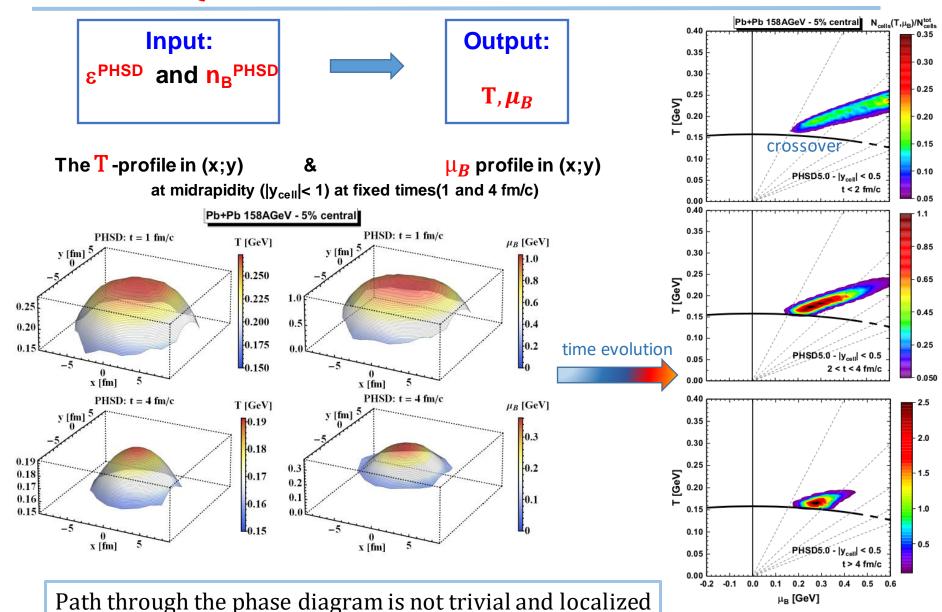
$$\begin{cases} \frac{n_B}{T^3} \approx \chi_2^B(T) \left(\frac{\mu_B}{T}\right) + \dots \\ \Delta \epsilon / T^4 \approx \frac{1}{2} \left(T \frac{\partial \chi_2^B(T)}{\partial T} + 3\chi_2^B(T)\right) \left(\frac{\mu_B}{T}\right)^2 + \dots \end{cases}$$

Use baryon number susceptibilities χ_n from IQCD Obtain T, μ_R by solving sistem of coupled eqs using ϵ , n_B



for details see P. Moreau, O. S., L. Oliva, T. Song, W. Cassing, E. Bratkovskaya arXiv:1903.10157, PRC 100 (2019) no. 1, 014911

PHSD: QGP evolution in HICs

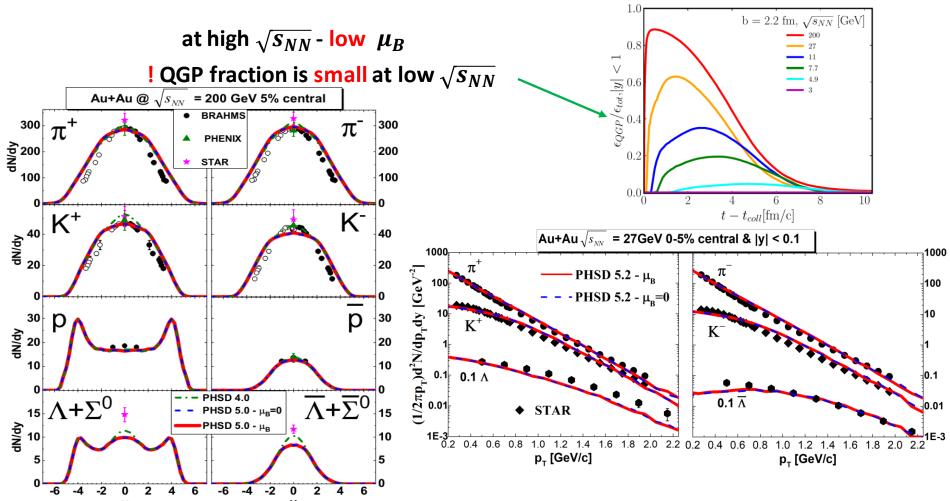


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Results for $(\sqrt{s_{NN}} = 200 \text{ GeV} - 7 \text{ GeV})$



- No visible effects on p_T -spectra, dN/dy of μ_B -dependence
- Small effect of the angular dependence of $d\sigma/d\cos\theta$

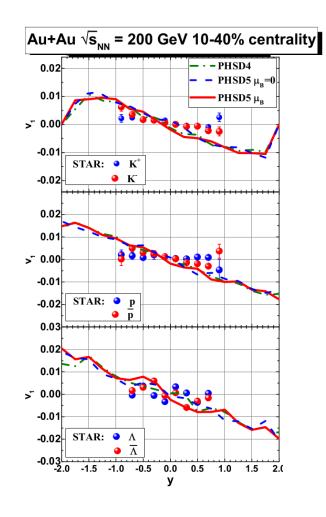


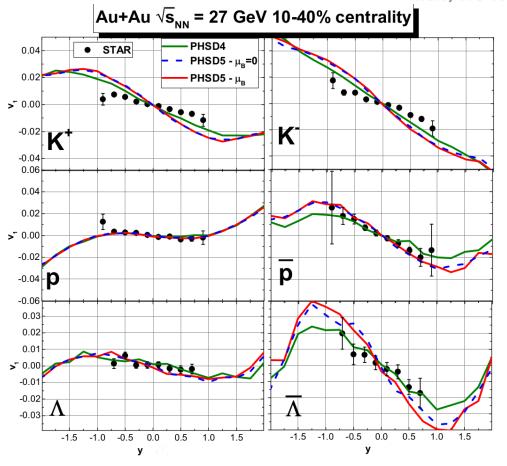
Directed flow $(\sqrt{s_{NN}} = 200 \text{ GeV } vs 27 \text{ GeV})$

$$v_1 = \left\langle \frac{p_x}{p_T} \right\rangle$$

- Influence of the QGP dynamics on final particles observables
- Weak μ_B -dependence small fraction of QGP or low μ_B

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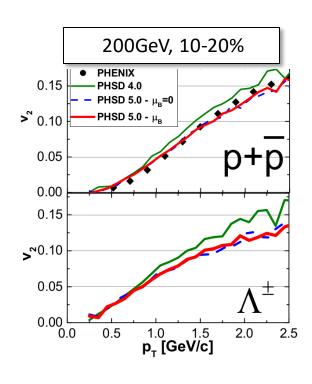


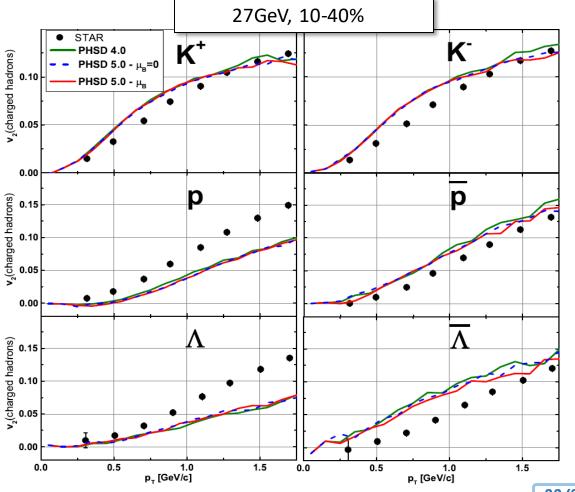
Elliptic flow $(\sqrt{s_{NN}} = 200 \text{ GeV } vs 27 \text{GeV})$

$$v_2 = \left\langle \frac{p_x^2 - p_y^2}{p_T^2} \right\rangle$$

- Weak μ_B -dependence
- Small effect of the angular dependence of $d\sigma/d\cos\theta$
- Strong flavor dependence

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Summary

Transport properties of the strongly-interacting QGP matter at finite **T** and μ_B have been investigated.

Influence of an order of a phase transition on thermodynamic and transport properties has been studied.

• Transport coefficients can differ among the models, which have similar phase structures and EoS

Evolution of the QGP matter created in HICs and the sensitivity of the bulk and flow observables on the QGP interactions and transport properties have been explored by the simulations within the PHSD transport approach

- High- μ_B regions are probed at low $\sqrt{s_{NN}}$ or high rapidity regions Moreover, QGP fraction is small at low $\sqrt{s_{NN}}$: small effect seen in observables
- μ_B -dependence of QGP interactions is more pronounced in observables for strange hadrons and antiprotons

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Outlook:

- 1st/2nd order phase transition in the PHSD
- Possible effects of phase transitions on flow observables

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Thank you for your attention!

Back up slides

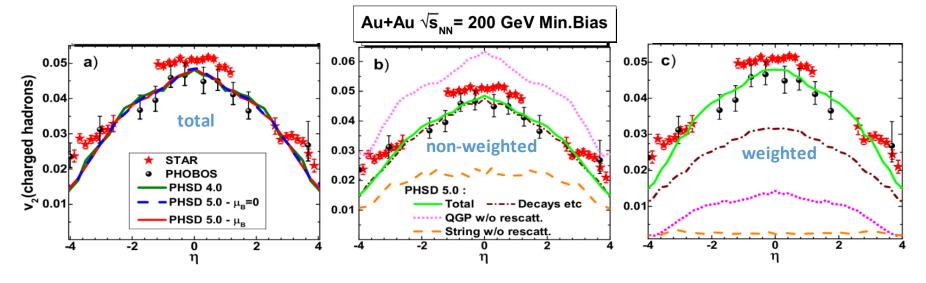
Elliptic flow $(\sqrt{s_{NN}} = 200 \text{ GeV } vs 27 \text{GeV})$

$$v_2 = \left\langle \frac{p_x^2 - p_y^2}{p_T^2} \right\rangle$$

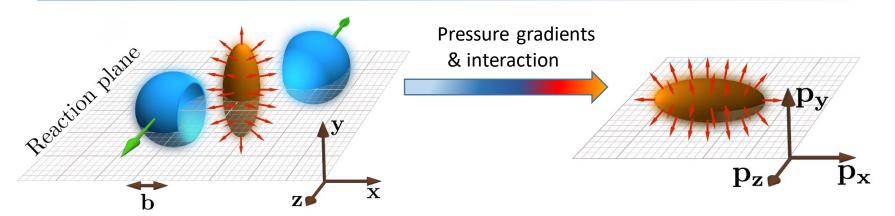
- Weak µ_B -dependence
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Channel decomposition:

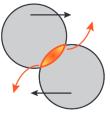


Anisotropic flow coefficients

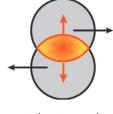


Quantify the anisotropic flow using Fourier expansion

$$\frac{dN}{d\varphi} \propto \left(1 + 2\sum_{n=1}^{+\infty} v_n \cos\left[n(\varphi - \psi_n)\right]\right)$$
$$v_n = \left\langle\cos n(\varphi - \psi_n)\right\rangle, \quad n = 1, 2, 3...,$$



$$v_1 = \left\langle \frac{p_x}{p_T} \right\rangle$$



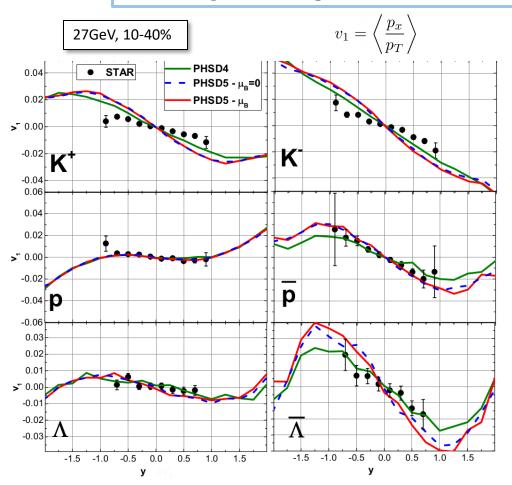
$$v_1 = \left\langle \frac{p_x}{p_T} \right\rangle \qquad v_2 = \left\langle \frac{p_x^2 - p_y^2}{p_T^2} \right\rangle$$

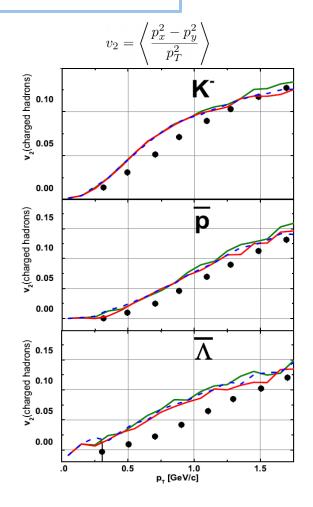
Anisotropic flow

- Assess the transport properties of the QGP
- Sensitive to the QGP EoS and initial state
- Validate models of bulk evolution that are used in the computation of other observables

Elliptic flow $(\sqrt{s_{NN}} = 200 \ GeV - 27 GeV)$

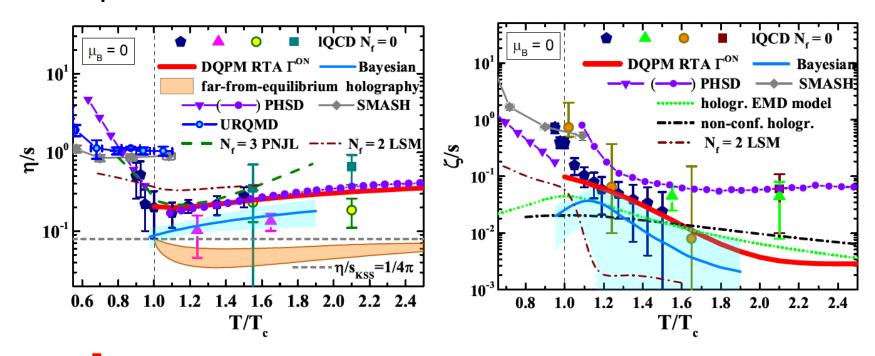
- Weak μ_B –dependence small fraction of QGP or low μ_B
- Small effect of the angular dependence of $d\sigma/d\cos\theta$
- Strong flavor dependence





Specific shear viscosity compilation

Model predictions:



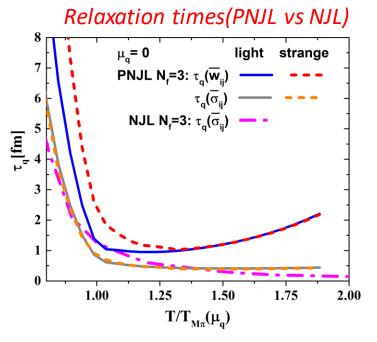
Different models using the same EoS can have completely different transport coefficients!

PNJL relaxation times

$$\tau_i(\mathbf{p}, T, \mu_B) = \frac{1}{\Gamma_i(\mathbf{p}, T, \mu_B)}$$

$$\Gamma_{i}^{\text{on}}(\mathbf{p}_{i}, T, \mu_{q}) = \frac{1}{2E_{i}} \sum_{j=q,\bar{q},g} \int \frac{d^{3}p_{j}}{(2\pi)^{3}2E_{j}} d_{j} f_{j}(E_{j}, T, \mu_{q}) \underbrace{\mathbf{E}}_{\mathbf{p}}^{5} \underbrace{\mathbf{A}}_{\mathbf{q}}^{5} \underbrace{\mathbf{A}}_{\mathbf{q}}^{5}$$

qq - interactions:



4 point interaction -> meson exchange(π , σ , η , η , κ ,... for s,t,u channels)

$$d' = = = = = = = = = d$$

$$= = = = = = = = (i\gamma_5)\tau^{(-)} \frac{-ig_{\pi qq}^2}{k^2 - m_{\pi}^2} (i\gamma_5)\tau^{(+)}$$

meson propagator $\mathscr{D} = \frac{2ig_m}{1-2g_m\Pi_{ff'}^{\pm}(k_0,\vec{k})}$

Effective interaction in RPA

PNJL relaxation times

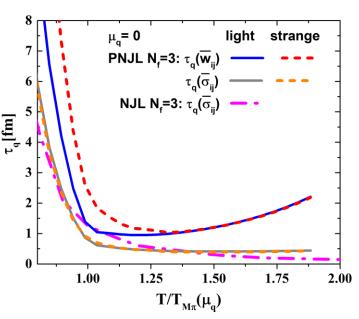
$$au_i(\mathbf{p}, T, \mu_B) = \frac{1}{\Gamma_i(\mathbf{p}, T, \mu_B)}$$

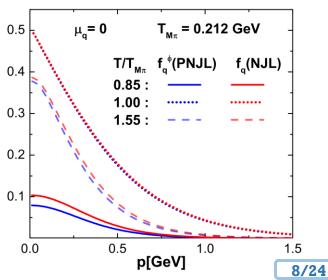
$$\Gamma_{i}^{\text{on}}(\mathbf{p}_{i}, T, \mu_{q}) = \frac{1}{2E_{i}} \sum_{j=q,\bar{q},g} \int \frac{d^{3}p_{j}}{(2\pi)^{3}2E_{j}} d_{j} \mathbf{f}_{j}(E_{j}, T, \mu_{q}) \mathbf{E}_{\mathbf{p}}^{5} \mathbf{f}_{4}$$

$$\int \frac{d^{3}p_{3}}{(2\pi)^{3}2E_{3}} \int \frac{d^{3}p_{4}}{(2\pi)^{3}2E_{4}} (1 \pm f_{3})(1 \pm f_{4}) \mathbf{f}_{4}^{5} \mathbf{f}_{4}^{5} \mathbf{f}_{4}^{5} \mathbf{f}_{5}^{6} \mathbf{f}_{5}$$

Modified distribution functions: Polyakov loop contributions

$$f_{q} \rightarrow f_{q}^{\Phi}(\mathbf{p}, T, \mu) = \frac{(\bar{\Phi} + 2\Phi e^{-(E_{\mathbf{p}} - \mu)/T})e^{-(E_{\mathbf{p}} - \mu)/T} + e^{-3(E_{\mathbf{p}} - \mu)/T}}{1 + 3(\bar{\Phi} + \Phi e^{-(E_{\mathbf{p}} - \mu)/T})e^{-(E_{\mathbf{p}} - \mu)/T} + e^{-3(E_{\mathbf{p}} - \mu)/T}},$$





QGP in the Polyakov extended NJL model

 PNJL model based on effective Lagrangian with the same symmetries for the quark dof as QCD

$$\begin{split} \mathscr{L}_{PNJL} &= \sum_{i} \bar{\psi}_{i} (iD - m_{0i} + \mu_{i} \gamma_{0}) \psi_{i} \\ &+ G \sum_{a} \sum_{ijkl} \left[(\bar{\psi}_{i} \ i \gamma_{5} \tau_{ij}^{a} \psi_{j}) \ (\bar{\psi}_{k} \ i \gamma_{5} \tau_{kl}^{a} \psi_{l}) + (\bar{\psi}_{i} \tau_{ij}^{a} \psi_{j}) \ (\bar{\psi}_{k} \tau_{kl}^{a} \psi_{l}) \right] \\ &- K \det_{ij} \left[\bar{\psi}_{i} \ (-\gamma_{5}) \psi_{j} \right] - K \det_{ij} \left[\bar{\psi}_{i} \ (+\gamma_{5}) \psi_{j} \right] \\ &- \mathcal{U}(T; \Phi, \bar{\Phi}) \end{split} \qquad \begin{array}{c} \text{Polyakov-loop effective potential fitted} \\ \text{to the YM} \end{split}$$

5 parameters fixed by vacuum values K,π masses, η-η'mass splitting, π decay constant, Chiral condensate

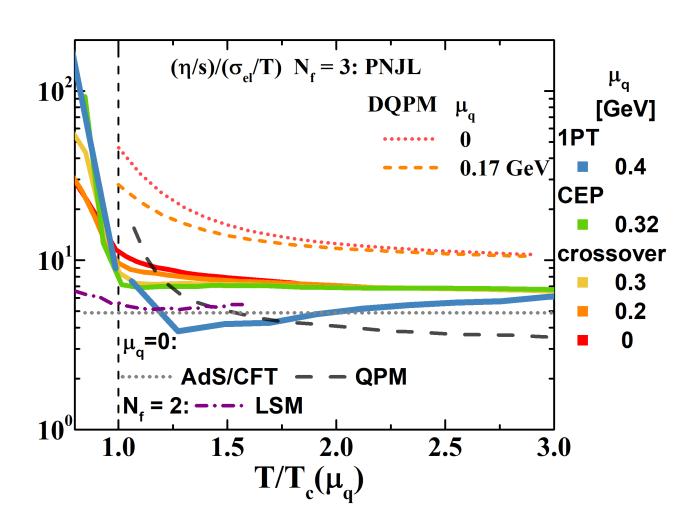
Improvements:

Next to leading order in $Nc(O(1/Nc)^{0})$ of the grand-canonical potential: presence of the mesons below Tc

$$\Omega_{\mathrm{PNJL}}(T,\mu_i) = \Omega_q^{(-1)}(T,\mu_i) + \sum_{M \in J^\pi = \{0^+,0^-\}} \Omega_M^{(0)}(T,\mu_M(\mu_i)) + \mathcal{U}_{glue}(T) \; ,$$
 J. M. Torres-Rincon, J. Aichelin PRC 96 (2017) 4 045205 D. Fuseau, T. Steinernert, J. Aichelin PRC 101 (2020) 6 065203

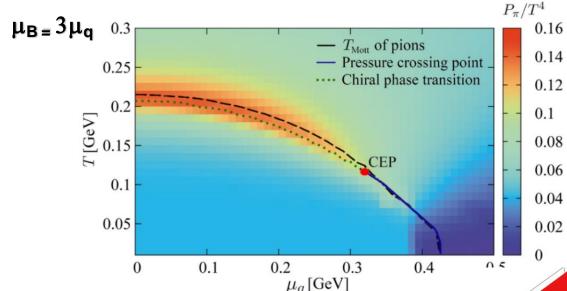
Modification of the gluon potential due to the presence of the quark

Specific shear viscosity to conductivity



QGP in the Polyakov extended NJL model

- PNJL allows for prediction of macroscopic properties of QGP at finite ${f T}$ and $\mu_{{m B}}$
- & QGP transport coefficients for $0 \le \mu_B \le 1.2$ GeV

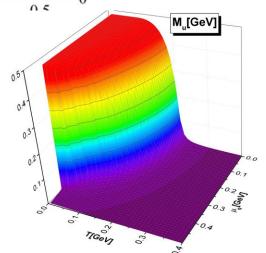


D. Fuseau, T. Steinert, J. Aichelin PRC 101 (2020) 6 065203

- ightharpoonup CEP: (T, μ_B) = (110,960) MeV, μ_B /T = 8.73
- \geq 1st order PT at high μ_B
- same symmetries for the quarks as QCD

Chiral masses (M_l, M_s)

$$m_i = m_{0i} - 4G\langle\langle\bar{\psi}_i\psi_i\rangle\rangle + 2K\langle\langle\bar{\psi}_j\psi_j\rangle\rangle\langle\langle\bar{\psi}_k\psi_k\rangle\rangle$$



Specific shear viscosity compilation

Kubo formalism: transport coefficients are expressed through correlation functions of stress-energy tensor

used in lattice QCD, transport approaches(hadrons), effective models

$$\eta = \frac{1}{20} \lim_{\omega \to 0} \frac{1}{\omega} \int d^4x \, e^{i\omega t} \left\langle \left[\mathcal{S}^{ij}(t, \mathbf{x}), \, \mathcal{S}^{ij}(0, \mathbf{0}) \right] \right\rangle \theta(t) \qquad \qquad \mathcal{S}^{ij} = T^{ij} - \delta^{ij} \mathcal{P}$$

$$\zeta = \frac{1}{2} \lim_{\omega \to 0} \frac{1}{\omega} \int d^4x \, e^{i\omega t} \left\langle \left[\mathcal{P}(t, \mathbf{x}), \, \mathcal{P}(0, \mathbf{0}) \right] \right\rangle \theta(t) \qquad \qquad \mathcal{P} = -\frac{1}{3} T^i_{i}$$

R. Lang and W. Weise, EPJ. A 50, 63 (2014) (NJL model) A. Harutyunyan et al, PRD 95, 114021, (2017)

Kinetic theory:

Relaxation time approximation(RTA): consider relaxation time $\frac{df_a^{\rm eq}}{dt}=\mathcal{C}_a=-\frac{f_a^{\rm eq}\phi_a}{ au_a}$

P. Chakraborty and J. I. Kapusta, PRC 83,014906 (2011)

Chapman-Enskog: expand the distribution in terms of the Knudsen number J. A. Fotakis et al, PRD 101 (2020) 7, 076007 (HRG)

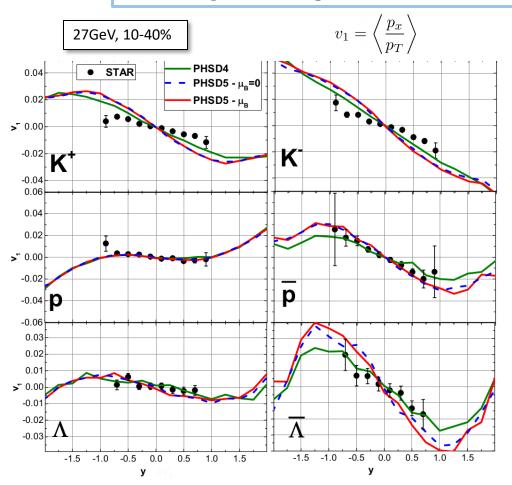
And more!

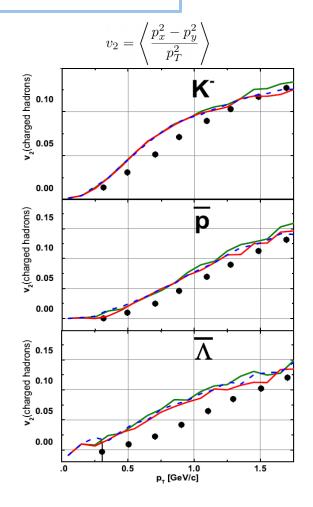
Holographic models: AdS/CFT correspondence

D. T. Son and A. O. Starinets, JHEP 0603, 052 (2006)M. Attems et al , JHEP 10 (2016), 155.

Elliptic flow $(\sqrt{s_{NN}} = 200 \ GeV - 27 GeV)$

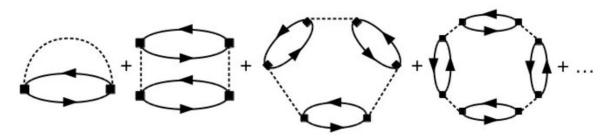
- Weak μ_B –dependence small fraction of QGP or low μ_B
- Small effect of the angular dependence of $d\sigma/d\cos\theta$
- Strong flavor dependence





PNJL improvements

Next to leading order in Nc $(O(1/Nc)^0)$ of the grand-canonical potential: presence of the mesons below Tc



J. M. Torres-Rincon, J. Aichelin PRC 96 (2017) 4 045205

Modification of the gluon potential due to the presence of the quark

$$\begin{split} \frac{U(\phi,\bar{\phi},T)}{T^4} &= -\frac{b_2(T)}{2}\bar{\phi}\phi - \frac{b_3}{6}(\bar{\phi}^3 + \phi^3) + \frac{b_4}{4}(\bar{\phi}\phi)^2 \\ b_2(T) &= a_0 + \frac{a_1}{1+\tau} + \frac{a_2}{(1+\tau)^2} + \frac{a_3}{(1+\tau)^3} \quad \text{where} \quad \tau_{\text{phen}} = 0.57 \\ \frac{T - T_{\text{phen}}^{\text{cr}}(T)}{T_{\text{phen}}^{\text{cr}}(T)} \end{split}$$

$$T_{phen}(T) = a + bT + cT^2 + dT^3 + e\frac{1}{T}$$

D. Fuseau, T. Steinernert, J. Aichelin PRC 101 (2020) 6 065203

Stages of collisions in PHSD

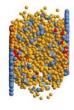
Initial A+A collision



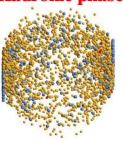
Partonic phase



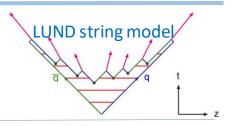
Hadronization



Hadronic phase



- > String formation in primary NN collisions
 - → decays to pre-hadrons (baryons and mesons)



- Formation of a QGP state if $\mathcal{E} > \mathcal{E}_{critical}$:
 Dissolution of pre-hadrons \rightarrow DQPM
 - → massive quarks/gluons and mean-field energy (quasi-)elastic collisions : inelastic collisions:

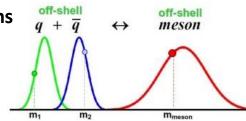
$$q+q \rightarrow q+q \quad g+q \rightarrow g+q$$
 $q+\overline{q} \rightarrow q+\overline{q} \quad g+\overline{q} \rightarrow g+\overline{q}$
 $\overline{q}+\overline{q} \rightarrow \overline{q}+\overline{q} \quad g+g \rightarrow g+g$

$$q + \overline{q} \to g$$
$$g \to q + \overline{q}$$

Hadronization to colorless off-shell mesons and baryons

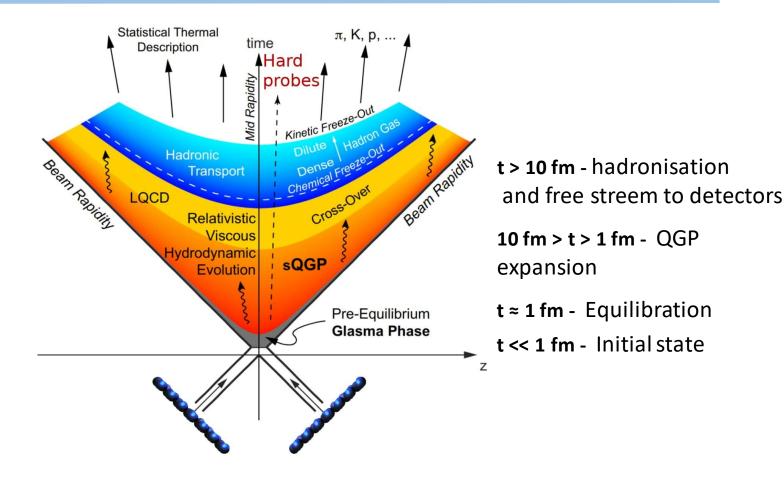
$$g \rightarrow q + \overline{q}$$
, $q + \overline{q} \leftrightarrow meson ('string')$
 $q + q + q \leftrightarrow baryon ('string')$

Strict 4-momentum and quantum number conservation



- Hadron-string interactions off-shell HSD
 - W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919; NPA831 (2009) 215; W. Cassing, EPJ ST 168 (2009) 3

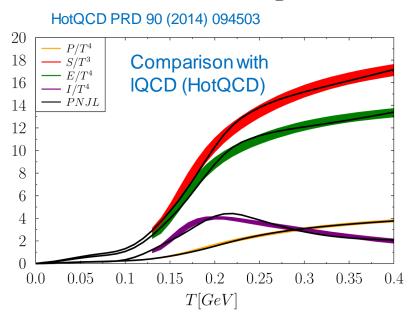
Stages of HIC



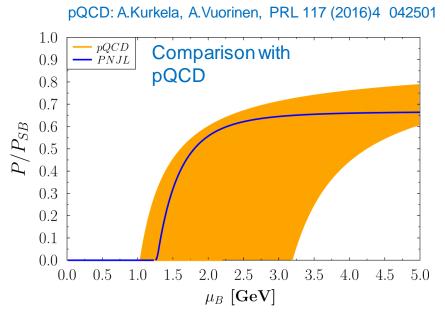
QGP out-of equilibrium ←→ HIC

QGP in the Polyakov extended NJL model

- PNJL allows for prediction of macroscopic properties of QGP at finite ${\bf T}$ and $\mu_{\it B}$
- & QGP transport coefficients for $0 \le \mu_B \le 1.2$ GeV
- Parameters fixed, EoS at $μ_B = 0$:



\triangleright EoS at high μ_B :

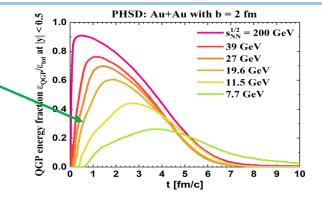


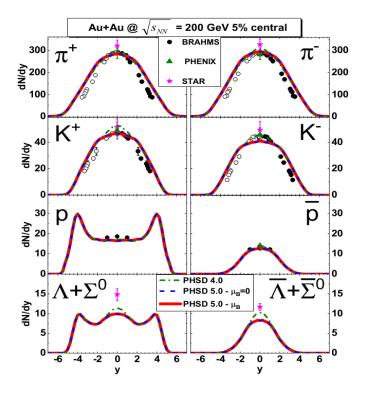
Results for $(\sqrt{s_{NN}} = 200 \text{ GeV} - 7 \text{ GeV})$

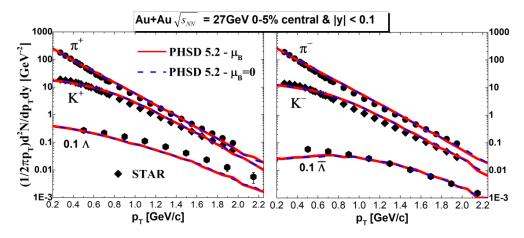


- No visible effects on p_T -spectra, dN/dy of μ_B -dependence
- Small effect of the angular dependence of $d\sigma/d\cos\theta$

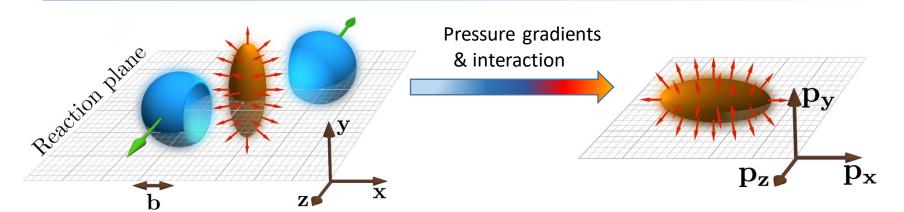
at high $\sqrt{s_{NN}}$ - low $\,\mu_B$! QGP fraction is small at low $\sqrt{s_{NN}}$







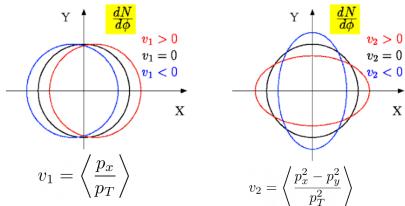
Anisotropic flow coefficients



Quantify the anisotropic flow using Fourier expansion

$$\frac{dN}{d\varphi} \propto \left(1 + 2\sum_{n=1}^{+\infty} v_n \cos\left[n(\varphi - \psi_n)\right]\right)$$

$$v_n = \left\langle\cos n(\varphi - \psi_n)\right\rangle, \quad n = 1, 2, 3...,$$

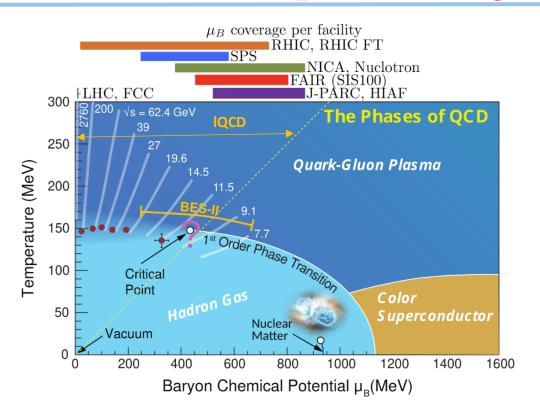


 $v_n = \langle \cos(n(\phi - \Psi_r)) \rangle$

Anisotropic flow

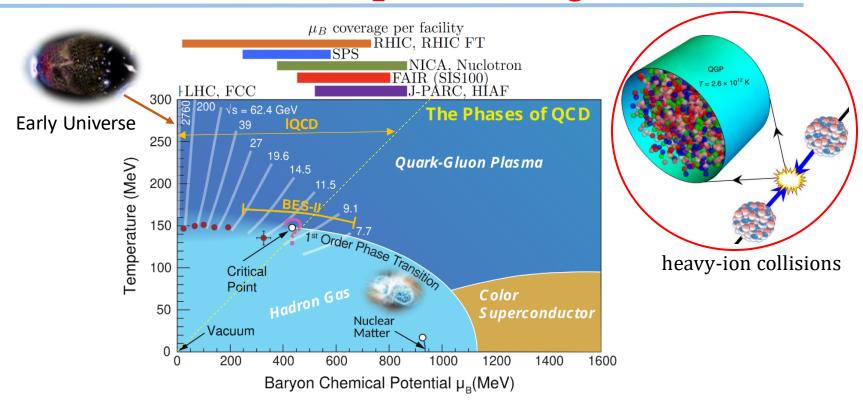
- Assess the transport properties of the QGP
- Sensitive to the QGP EoS and initial state
- Validate models of bulk evolution that are used in the computation of other observables

Motivation: the QCD phase diagram



- \triangleright Explore the QCD phase diagram at finite T and μ_B through heavy-ion collisions
- > Search for a possible Critical End Point (CEP) and 1st order phase transition
- \triangleright Quantify macroscopic properties of the QCD matter at finite T and μ_B and relate them to its microscopic structures

Motivation: the QCD phase diagram



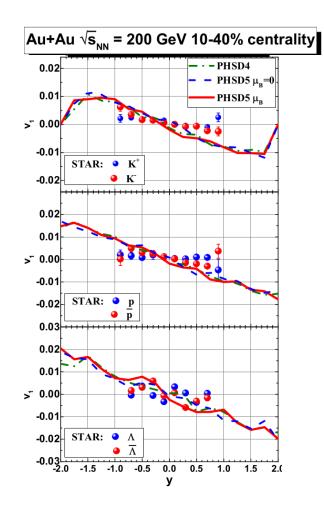
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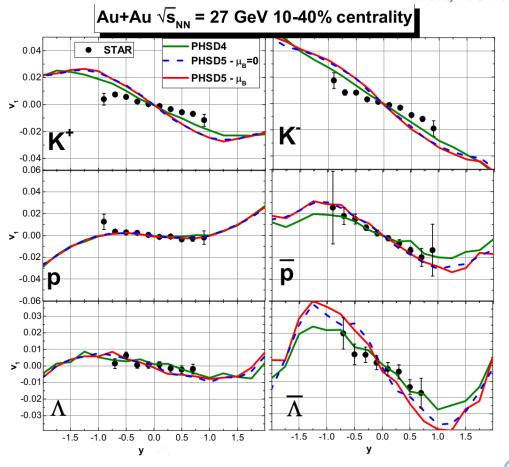
Directed flow $(\sqrt{s_{NN}} = 200 \text{ GeV } vs 27 \text{ GeV})$

$$v_1 = \left\langle \frac{p_x}{p_T} \right\rangle$$

- Influence of the QGP dynamics on final particles observables
- Weak μ_B -dependence small fraction of QGP or low μ_B

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Elliptic flow $(\sqrt{s_{NN}} = 200 \, GeV \, vs \, 27 GeV)$

$$v_2 = \left\langle \frac{p_x^2 - p_y^2}{p_T^2} \right\rangle$$

- Weak µ_B -dependence
- Small effect of the angular dependence of $d\sigma/d\cos\theta$
- Strong flavor dependence

Particles 3 (2020) no.1, 178-192

