# Dynamical attractors in viscous hydrodynamics and full Boltzmann approach

#### Vincenzo Nugara

In collaboration with: S. Plumari L. Oliva V. Greco

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#### • Attractors in uRHICs

- Relativistic Boltzmann Transport Approach
- Boost-invariant systems
- Breaking boost-invariance
- Temperature-dependent  $\eta/s$
- Conclusions and outlooks



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# ultra-Relativistic Heavy-Ion Collisions (uRHICs)



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Attractor: subset of the phase space to which all trajectories converge after a certain time. Why do we look for attractors?

- Uncertainties in initial conditions affect final observables? Memory of initial conditions?
- Appearance of attractors and hydrodynamisation. The issue of small systems, as produced by p-p or p-A collisions.



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# Distribution function

Classical statistics and fugacity  $\Gamma(\tau) \neq 1$ , with an initial Romatschke-Strickland distribution:

$$f_0(\mathsf{p}) = \gamma_0 \exp\left(-rac{1}{\Lambda_0}\sqrt{p_\perp^2+p_w^2(1+\xi_0)}
ight),$$

where  $p_{\perp}^2 = p_x^2 + p_y^2$  and  $p_w = (p \cdot z)$ . Three initial parameters:

- $\Lambda_0$ , related to initial effective temperature  $T_0$ ;
- $\gamma_0$ , related to initial effective fugacity  $\Gamma_0$ ,
- $\xi_0$  fixes initial pressure anisotropy  $P_L/P_T$ .

 $\Lambda_0$  and  $\gamma_0$  computed to fix initial energy density  $\varepsilon$  and particle density n.

Cylindrical and Bjorken symmetry (boost-invariance) with Milne Coordinates  $(\eta_s, x, y, \tau)$ 

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# LRF and matching conditions

Define the Landau Local Rest Frame (LRF) via the fluid four-velocity:

$$T^{\mu
u}u_
u = arepsilon u^\mu, \ n = n^\mu u_\mu$$

 $\varepsilon$  and *n* are the energy and particles density in the LRF. Effective temperature and fugacity are defined via Landau matching conditions:

$$T = \frac{\varepsilon}{3 n}, \qquad \Gamma = \frac{n}{d T^3 / \pi^2}$$

d is the # of dofs, fixed d = 1.

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We look for attractors in the normalized moments  $\overline{M}^{nm}$  of the distribution function f(p). Moments are defined as:

$$M^{nm}[f] = \int \frac{d^3\vec{p}}{(2\pi)^3 p^0} \,(u \cdot p)^n (z \cdot p)^{2m} \,f(p)$$

They carry information about the f(p).

#### All moments $\iff$ whole f(p)

Normalized by their equilibrium values:

$$M_{eq}^{nm}[f] = \int \frac{d^3\vec{p}}{(2\pi)^3 p^0} (u \cdot p)^n (z \cdot p)^{2m} f_{eq}(p,\tau) = \frac{(n+2m+1)! \, \Gamma(\tau) \, T^{n+2m+2}(\tau)}{2\pi^2 (2m+1)}$$

For the matching conditions:

$$M^{10} = n, \ M^{20} = \varepsilon, \ M^{01} = P_L \implies \overline{M}^{10} = 1, \ \overline{M}^{20} = 1, \ \overline{M}^{01} = 3P_L/\varepsilon = P_L/P_{eq}$$

M. Strickland JHEP 12, 128, (2010)

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## Boltzmann equation

Solve the Relativistic Boltzmann Equation with the full collision integral:

$$p^{\mu}\partial_{\mu}f(x,p) = C \left[f(x,p)\right]_{p},$$
(1)

Only binary elastic  $2 \leftrightarrow 2$  collisions:

$$C[f]_{p} = \int \frac{d^{3}p_{2}}{2E_{p_{2}}(2\pi)^{3}} \int \frac{d^{3}p_{1'}}{2E_{p_{1'}}(2\pi)^{3}} \int \frac{d^{3}p_{2'}}{2E_{p_{2'}}(2\pi)^{3}} (f_{1'}f_{2'} - f_{1}f_{2}) \times |\mathcal{M}|^{2} \delta^{(4)} (p_{1} + p_{2} - p_{1'} - p_{2'})$$
(2)

 $\mathcal{M}$ : transition amplitude.  $|\mathcal{M}|^2 = 16\pi s (s - 4m^2) d\sigma/dt$ . Solve it in discretized space-time with test particles method (Wong, *PRC* 25, 1460 (1982)) :

$$f(t, x, p) = \frac{1}{N_{\text{test}}} \sum_{i=1}^{N} \delta^{(3)}(x - x_i(t)) \delta^{(3)}(p - p_i(t))$$
(3)

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# Relativistic Boltzmann Transport (RBT) Code

- It simulates the evolution of a system of partons
- Written in C language to achieve better performance (up to  $3 \cdot 10^8$  test particles)
- Stochastic Method to implement collisions between particles (Z. Xu, C. Greiner, *PRC 71* (2005), Ferini, Colonna, Di Toro, Greco, *PLB 670* (2009))
- Space is discretised in cells: only particles within the same cell can collide



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# Fixing shear viscosity $\eta/s$

- Collision probability:  $P_{22} = v_{rel}\sigma_{22}\frac{\Delta t}{\Lambda^3 x}$
- 2  $\leftrightarrow$  collisions are implemented  $\Rightarrow$  Particle conservation.

Need to take into account fugacity  $\gamma \neq 1$ .

•  $\sigma_{22}$  is the total cross section. It is fixed cell by cell via the Champan-Enskog formula (Plumari, Puglisi, Scardina, Greco, PRC 86 (2012)):

$$\eta = f(m/T) \frac{T}{\sigma_{22}} \stackrel{m=0}{=} 1.2 \frac{T}{\sigma_{22}}$$



Green-Kubo and Chapman-Enskog estimations of  $\eta$ .

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# Code setup

- Conformal system (m = 0)
- One-dimension. Periodic boundary conditions in the transverse plane.
- Boost-invariant system.  $dN/d\eta = \text{const.}$  in  $[-\eta_{s_{\text{max}}}, \eta_{s_{\text{max}}}]$ ,  $\eta_{s_{\text{max}}}$  large enough to avoid propagation of information from boundaries.
- Cell:  $\Delta x = \Delta y = 0.4$  fm,  $\Delta \eta_s = 0.08$ . Results taken in one-cell-thick slices in  $\eta_s$ .
- Test particles: from  $10^7$  up to  $3 \cdot 10^8$ .
- Time discretization: to avoid causality violation ( $\sim 10^3$  time steps).
- Performance: 30' per  $10^6$  test particles in  $10^3$  time steps.
- $\bullet$  Initial conditions:  $\mathcal{T}_0=0.5$  GeV,  $\Gamma_0=1,\,\xi_0=-0.5,\,0,\,10,\,+\infty$

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# Testing boost-invariance

Compute normalized moments at different  $\eta_s$ 's within an interval  $\Delta \eta_s = 0.04$ .



Results are clearly boost-invariant! We look for them at midrapidity:  $\eta \in [-0.02, 0.02]$ 

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# Comparison with other models

Compute normalized moments with DNMR, anisotropic hydrodynamics (aHydro) and Relaxation Time Approximation (RTA) Boltzmann Equation.



- Better agreement with RTA and aHydro for lower order moments
- Better agreement with DNMR for lower η/s (V. Ambrus *et al.*, PRD 104.9 (2021))

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# Definition of the relaxation time

RTA Boltzmann, vHydro and aHydro show attractors w.r.t scaled time  $\tau/\tau_{eq}$ .  $\tau_{eq}^{RTA} = 5(\eta/s)/T$  enters in their equations as the relaxation time (Denicol *et al.PRD* 83, 074019). In FBT no need for a  $\tau_{eq}$ ! Natural time scale average collision time per particle:

$$\tau_{coll} = \frac{1}{2} \left( \frac{1}{N_{\text{part}}} \frac{\Delta N_{\text{coll}}}{\Delta t} \right)^{-1}$$

It can be shown that

$$\tau_{eq}^{\textit{RTA}} = \tau_{tr} = \frac{3}{2} \tau_{coll} \equiv \tau_{eq}^{\textit{RBT}}$$



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#### Two kinds of attractors (Heller, Spalinski, PRL 115 (2015)) :

- Pull-back attractor
  - Fix the initial anisotropy  $\xi_0$ .
  - Change initial scaled time  $\tau_0 T_0 / (\eta/s)$ . (If ratio fixed, same curve!).

#### • Forward attractor

- Change initial anisotropy  $\xi_0$ .
- Fix initial scaled time.

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# Pull-back Attractor

Fix  $\xi_0$ , change  $\eta/s$  and  $\tau_0$ : three values for the ratio  $\tau_0/(4\pi\eta/s)$ : 0.1, 0.01, 0.05 fm.



- Curves depend only on  $au_0/(\eta/s)$  ratio
- Equilibration achieved at same  $\tau/\tau_{eq}$
- Attractor reached at different  $\tau/\tau_{eq}$
- Initial free streaming

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# Forward Attractor

Different initial anisotropies  $\xi_0 = -0.5, 0, 10, \infty$  for  $\eta/s = 1/4\pi$  and  $\eta/s = 10/4\pi$ .



- $\eta/s=1$ : attractor at  $au \sim 1.5 au_{eq}$
- $\eta/s=$  10: attractor at  $au\sim$  0.2 $au_{eq}$
- Less collisions per particle to reach the attractor?
- Strong initial expansion in  $\sim$  free streaming

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## Forward Attractor vs $\tau$

Different initial anisotropies  $\xi_0 = -0.5, 0, 10, \infty$  for  $\eta/s = 1/4\pi$  and  $\eta/s = 10/4\pi$ .



- $\eta/s=$  1: attractor at  $au\sim$  0.5 fm
- $\eta/s=$  10: attractor at  $au \sim$  1.0 fm
- Not 10 times larger!
- Less collisions to reach the attractor?
- Strong initial expansion in  $\sim$  free streaming

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• At  $\tau = \tau_0$ , three different distributions in momentum space: oblate ( $\xi_0 = 10$ ), spherical ( $\xi_0 = 0$ ) and prolate( $\xi_0 = -0.5$ ).





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- Already at  $\tau \sim 1$  fm, strong initial longitudinal expansion brings the system away from equilibrium
- Distribution functions have similar (but not identical) shape.





- At  $\tau \sim$  5 fm, clear universal behaviour also for the distribution functions.
- Two components: strongly peaked p<sub>w</sub> distribution and a more isotropic one (Strickland, JHEP 12, 128)





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 For large τ the system is almost completely thermalized and isotropized.





# Who is the attractor?

All curves scale to a universal behaviour. Which is the curve they converge to?

- vHydro and aHydro: analytical solution (M. Strickland et al.PRD, 97, 036020 (2018));
- RTA (P. Romatschke PRL 120, 012301 (2018)) :  $au_0\ll 1$  and  $\xi_0 o\infty$  (in accordance with aHydro)

In a nutshell: infinitely oblate distribution  $\xi_0 \to \infty$ , initial scaled time  $\tau_0 T_0/(\eta/s) \to 0$ . Is it the RBT attractor, too? It is. The system initially is dominated by strong longitudinal expansion.

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# Attractors in different models



- $\overline{M}^{nm}$ , m > 0: very good agreement
- Higher order moments  $\rightarrow$  stronger departure between models
- RBT thermalizes earlier
- No agreement for  $M^{n0}$

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# Finite distribution in $\eta$



- Tails of the distribution function at  $|\eta_{s}| > 1$
- Discontinuity in initial distribution  $\rightarrow$  non-analyticity points in moments' evolution

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# Forward rapidity: Forward Attractor

Fixed  $\eta/s = 1$ ; vary initial anisotropies  $\xi_0 = -0.5$ , 0. Results at different  $\eta_s : 0, 2.0, 2.5, 3.0$ .

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# Forward rapidity: Pull-Back Attractor



- Universal behaviour even at  $\eta_s = 3$ , outside the initial distribution range!
  - At large rapidities curves start earlier: more 'ordered' particles' motion ightarrowsmaller T $\rightarrow$  larger  $\tau_{eq}$

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# T-dependent $\eta/s$ . Plot with respect to rescaled time



Conclusions:

- Attractors appear in the conformal boost-invariant case in the normalized moments of the distribution function and in the distribution function itself
- RTA and aHydro attractors converge to the full Boltzmann ones: the larger the moments' order, the later the convergence
- ullet Non boost-invariant systems still show universal behaviour, also at quite large  $\eta_s$
- Even if  $\eta/s$  depends on the local temperature, attractors are still visible as functions of the scaled time  $\tau/\tau_{eq}$ , despite a temporary broken of the universal behaviour ('loops').

Outlooks:

- Non-conformal simulation in progress
- Full 3+1D simulation in progress
- Realistic initial conditions
- Attractors in collective flows

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Thank you for your attention.



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## Transport code: consistency checks

#### **Collision Rate**



Expected and computed collision rate in unit of  $n^2$ as a function of z = m/T. Theoretical value  $R = \frac{1}{2}n^2 \langle \sigma v \rangle$ .

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#### Thermalisation



value Particles initialised with momentum modulus p = 1.2 GeV. Within  $t \sim 0.6$  fm the system thermalises; equilibrium temperature T = 0.4 GeV. Dynamical attractors in 1D systems September 28<sup>th</sup>, 2023 31/30

# Boltzmann RTA Equation for number-conserving systems

Boltzmann equation in Relaxation Time Approximation (RTA) (Strickland, Tantary, JHEP10(2019) 069)

$$p^{\mu}\partial_{\mu}f_{p}=-rac{p\cdot u}{ au_{eq}}(f_{eq}-f_{p}).$$

Exactly solvable, by fixing number and energy conservation. Two coupled integral equations for  $\Gamma_{eff} \equiv \Gamma$  and  $T_{eff} \equiv T$ :  $\Gamma(\tau)T^{4}(\tau) = D(\tau,\tau_{0})\Gamma_{0}T_{0}^{4}\frac{\mathcal{H}(\alpha_{0}\tau_{0}/\tau)}{\mathcal{H}(\alpha_{0})} + \int_{\tau_{0}}^{\tau} \frac{d\tau'}{2\tau_{eq}(\tau')}D(\tau,\tau')\Gamma(\tau')T^{4}(\tau')\mathcal{H}\left(\frac{\tau'}{\tau}\right),$   $\Gamma(\tau)T^{3}(\tau) = \frac{1}{\tau}\left[D(\tau,\tau_{0})\Gamma_{0}T_{0}^{3}\tau_{0} + \int_{\tau_{0}}^{\tau} \frac{d\tau'}{\tau_{eq}(\tau')}D(\tau,\tau')\Gamma(\tau')T^{3}(\tau')\tau'\right].$ 

Here  $\alpha = (1 + \xi)^{-1/2}$ . System solvable by iteration.

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## vHydro equations

Second-order dissipative viscous hydrodynamics equations according to DNMR derivation, starting from kinetic theory (G. S. Denicol *et al.*, *PRL*105, 162501 (2010)) :

$$\partial_ auarepsilon = -rac{1}{ au}(arepsilon+P-\pi), 
onumber \ \partial_ au\pi = -rac{\pi}{ au\pi} + rac{4}{3}rac{\eta}{ au_\pi au} - eta_\pirac{\pi}{ au},$$

where  $\tau_{\pi} = 5(\eta/s)/T$  and  $\beta_{\pi} = 124/63$ . Solved with a Runge-Kutta-4 algorithm.

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# aHydro for number-conserving systems

Formulation of dissipative anisotropic hydrodynamics with number-conserving kernel (Almaalol, Alqahtani, Strickland, PRC 99, 2019). System of three coupled ODEs:

$$\partial_{ au}\log\gamma + 3\partial_{ au}\log\Lambda - rac{1}{2}rac{\partial_{ au}\xi}{1+\xi} + rac{1}{ au} = 0;$$
  
 $\partial_{ au}\log\gamma + 4\partial_{ au}\log\Lambda + rac{\mathcal{R}'(\xi)}{\mathcal{R}(\xi)}\partial_{ au}\xi = rac{1}{ au}\left[rac{1}{\xi(1+\xi)\mathcal{R}(\xi)} - rac{1}{\xi} - 1
ight];$   
 $\partial_{ au}\xi - rac{2(1+\xi)}{ au} + rac{\xi(1+\xi)^2\mathcal{R}^2(\xi)}{ au_{eq}} = 0.$ 

Solved with a Runge-Kutta-4 algorithm.

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# Auxiliary functions

$$D(\tau_2, \tau_1) = \exp\left[-\int_{\tau_1}^{\tau_2} \frac{d\tau}{\tau_{eq}\tau}\right];$$
$$\mathcal{H}^{nm}(y) = \frac{2y^{2m+1}}{2m+1} F_1\left(\frac{1}{2} + m, \frac{1-n}{2}; \frac{3}{2} + m; 1-y^2\right).$$

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# Computation of moments in other models

• RTA:

$$\begin{split} \mathcal{M}^{nm}(\tau) &= \frac{(n+2m+1)!}{(2\pi)^2} \Big[ D(\tau,\tau_0) \alpha_0^{n+2m-2} T_0^{n+2m+2} \Gamma_0 \frac{\mathcal{H}^{nm}(\alpha\tau_0/\tau)}{[\mathcal{H}^{20}(\alpha_0)/2]^{n+2m-1}} + \\ &+ \int_{\tau_0}^{\tau} \frac{d\tau'}{\tau_{eq}(\tau')} D(\tau',\tau') \Gamma(\tau') T^{n+2m+2}(\tau') \mathcal{H}^{nm}\left(\frac{\tau'}{\tau}\right) \Big]; \end{split}$$

• DNMR:

$$\overline{M}_{\mathsf{DNMR}}^{nm} = 1 - rac{3m(n+2m+2)(n+2m+3)}{4(2m+3)} rac{\pi}{arepsilon};$$

• a Hydro:

$$\overline{M}_{\mathsf{aHydro}}^{nm}(\tau) = (2m+1)(2\alpha)^{n+2m-2} \frac{\mathcal{H}^{nm}(\alpha)}{[\mathcal{H}^{20}(\alpha)]^{n+2m-1}};$$

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# Pressure anisotropy in different frameworks

For  $\eta/s = 1/4\pi$  and  $\eta/s = 10/4\pi$ , compute  $P_L/P_T$  from three different initial anisotropies:  $\xi_0 = -0.5, 0, 10.$ 



- RTA (not showed) really similar to aHydro
- $\bullet\,$  aHydro attractor reached  $\sim\,$  time than RBT
- vHydro attractor reached at later time, especially for larger  $\eta/s$

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# Midrapidity



At midrapidity no difference w.r.t. the boost invariant case.

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# Non-monotonic $\tau/\tau_{eq}$ for Case 1



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T-dependent  $\eta/s$ : Plot with respect to proper time

