

Towards a Stability Analysis of Inhomogeneous Phases in QCD

Theo F. Motta (JLU Gießen & TU Darmstadt)

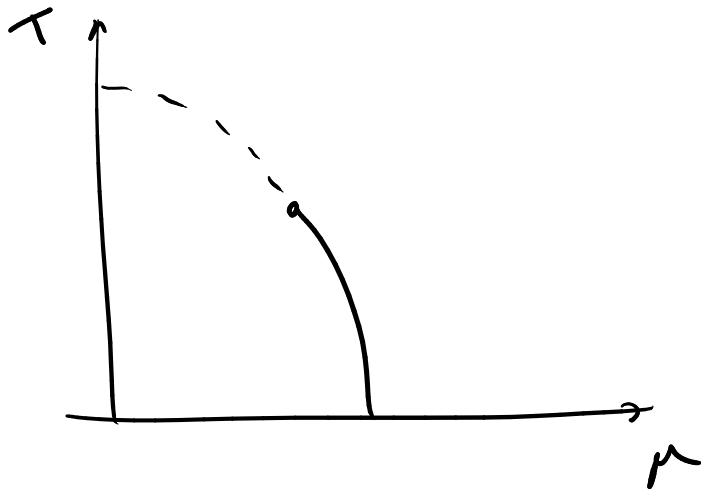
October 3, 2023

in collaboration with C.S. Fischer, M. Buballa & J. Bernhardt
STRONG2020 HFHF Retreat 2023 Giardini-Naxos

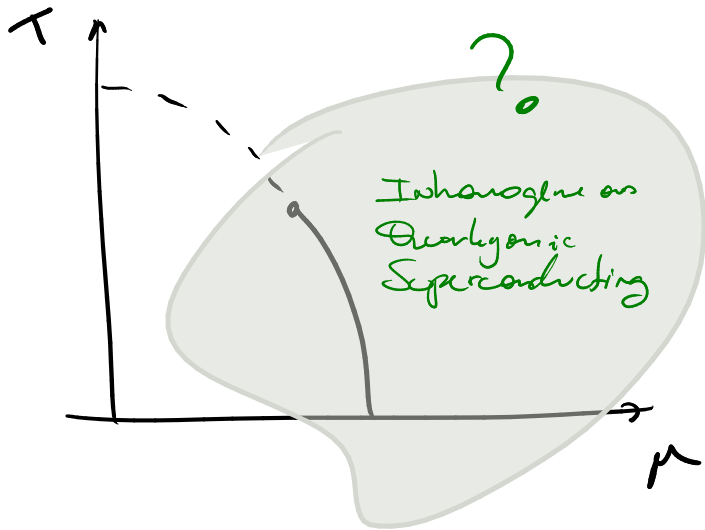
Based on [arXiv:2306.09749]

Overview of Inhomogeneous Phases

Inhomogeneous Phases



Inhomogeneous Phases



How to Study *Inhomogeneous* Phases?

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- Usually, with Models of QCD:
 - Gross-Neveu
 - NJL
 - QM
 - ...

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- By Direct Ansatz
- By Stability Analysis

$$\mathcal{L} = \bar{\psi}(i\cancel{\partial} - m)\psi + G \left\{ (\bar{\psi}\psi)^2 + (\bar{\psi}i\gamma_5\vec{\tau}\psi)^2 \right\}$$

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↓ Mean Field Free Energy ↓

$$\Omega_{\text{MF}}[\phi] = -\frac{T}{V} \text{Tr} \log \left(\frac{S_0^{-1} + G(\phi_S(\mathbf{x}) + \phi_P(\mathbf{x}))}{T} \right) \\ + G \frac{1}{V} \int d^3x (\phi_S^2(\mathbf{x}) + \phi_P^2(\mathbf{x}))$$

- Chiral Density Wave:

$$\phi_S(\vec{X}) = -\frac{\Delta}{2G_S} \cos(\vec{q} \cdot \vec{X}), \quad \phi_P(\vec{X}) = -\frac{\Delta}{2G_P} \sin(\vec{q} \cdot \vec{X})$$

Ansatz

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- Real-Kink-Crystal:

$$M(x) = \Delta \sqrt{\nu} \operatorname{sn}(\Delta x | \nu)$$

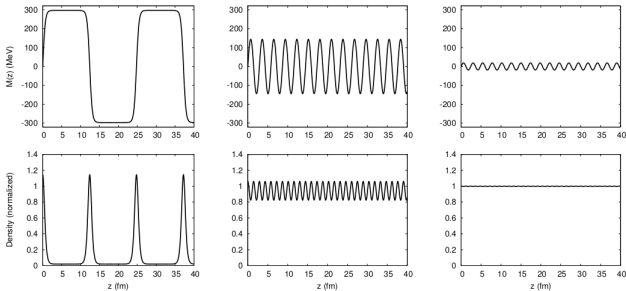
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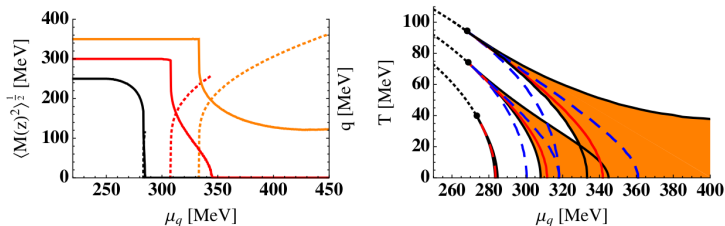
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PHYSICAL REVIEW D **80**, 074025 (2009)

Inhomogeneous phases in the Nambu–Jona-Lasinio and quark-meson model

Dominik Nickel

Center for Theoretical Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA
(Received 10 July 2009; published 22 October 2009)



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Stability Analysis

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↓ Leading Order ↓

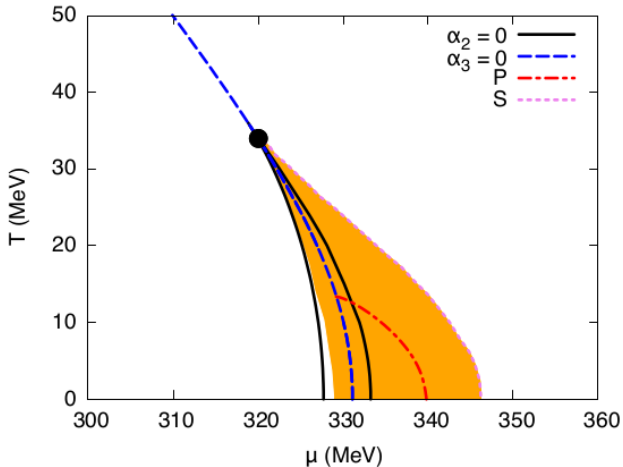
$$\Omega^{(2)} = \frac{2G^2}{V} \int_{\vec{q}} |\delta\phi_S(\vec{q})|^2 D_S^{-1}(q)$$

Inhomogeneous chiral phases away from the chiral limit

Michael Buballa¹ and Stefano Carignano²

¹Theoriezentrum, Institut für Kernphysik, Technische Universität Darmstadt,
Schlossgartenstr. 2, D-64289 Darmstadt, Germany

²Departament de Física Quàntica i Astrofísica and Institut de Ciències del Cosmos,
Universitat de Barcelona, Martí i Franquès 1, 08028 Barcelona, Catalonia, Spain.



Quantum Chromodynamics

- We start from a 2PI effective action

$$\Gamma[S] = \text{Tr} \log [S^{-1}] - \text{Tr} [\mathbf{1} - S_0^{-1}S] + \Phi_{2\text{PI}}[S]$$

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$$S(x, y) = \bar{S}(x, y) + \delta S(x, y)$$

- Same principle

$$\Gamma[S + \delta S] = \Gamma^{(0)}[\delta S^0] + \Gamma^{(1)}[\delta S] + \Gamma^{(2)}[\delta S^2] + \dots$$

- So zero-th order is

$$\Gamma^{(0)} = -\text{Tr} \log[\bar{S}] - \text{Tr} [\mathbf{1} - S_0^{-1} \bar{S}] + \Phi_{2\text{PI}}[\bar{S}] = \Gamma[\bar{S}]$$

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$$\Gamma^{(1)} = \text{Tr} \left[\frac{\delta \bar{\Gamma}}{\delta S} \delta S \right] = \text{Tr} \left[\left(\bar{S}^{-1} - S_0^{-1} - \frac{\delta \Phi_{2\text{PI}}}{\delta S} \right) \delta S \right]$$

Stability Analysis

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$$\Gamma^{(1)} = \text{Tr} \left[\frac{\delta \bar{\Gamma}}{\delta S} \delta S \right] = \text{Tr} \left[\left(\bar{S}^{-1} - S_0^{-1} - \frac{\delta \Phi_{2\text{PI}}}{\delta S} \right) \delta S \right]$$

- Second order is the leading order

$$\Gamma^{(2)} = \frac{1}{2!} \text{Tr} \left[\frac{\delta^2 \bar{\Gamma}}{\delta S \delta S} \delta S \delta S \right]$$

- Can this formalism reproduce the NJL stability analysis?

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Yes.

- Can this formalism reproduce the *homogeneous* chiral phase transition?

A Test Case: The Chiral Phase Transition

$$\text{---} \bullet \text{---}^{-1} = \text{---}^{-1} + \text{---} \bullet \text{---} \bullet \text{---} \bullet \text{---}$$

A Test Case: The Chiral Phase Transition



The diagram shows an equation between two terms. The left term is a horizontal line with a single black dot in the middle, followed by a superscript -1 . The right term is a horizontal line with a superscript -1 plus a diagram of a horizontal line with three black dots. The middle dot is larger than the two side dots. A semi-circular chain of small circles (representing gluons) connects the two side dots, with the larger middle dot positioned at the top center of the arc.

- Rainbow-Ladder

$$\Gamma_\nu(k, q; l) = Z_{1F} \gamma_\nu.$$

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- Not dynamical symmetric gluon

$$D_{\mu\nu}^{ab}(l) = \delta^{ab} \left(\delta_{\mu\nu} - \frac{l_\mu l_\nu}{l^2} \right) D(l)$$

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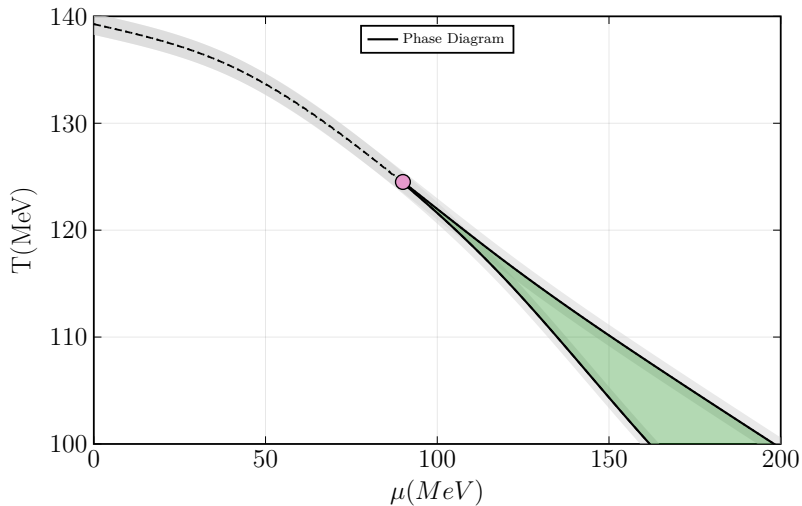
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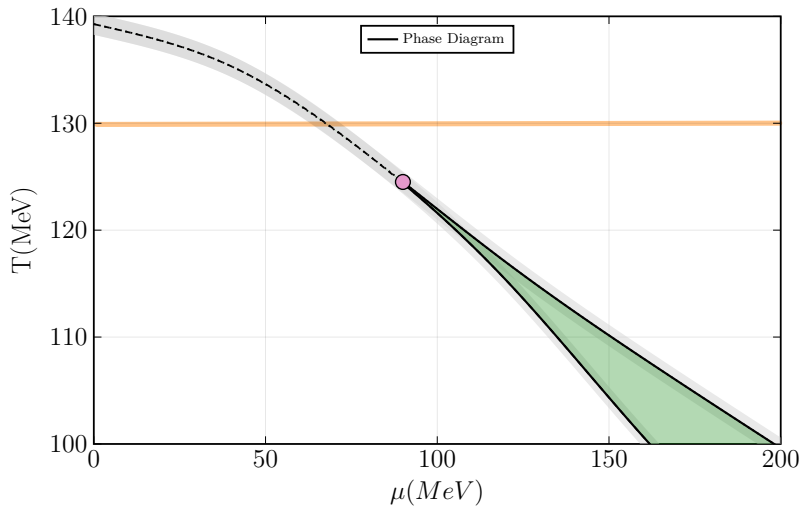
- Watson Model

$$D(l) = \frac{(Z_2)^2}{g^2 (Z_{1F})^2} \frac{8\pi^2}{\omega^4} D e^{-l^2/\omega^2}$$

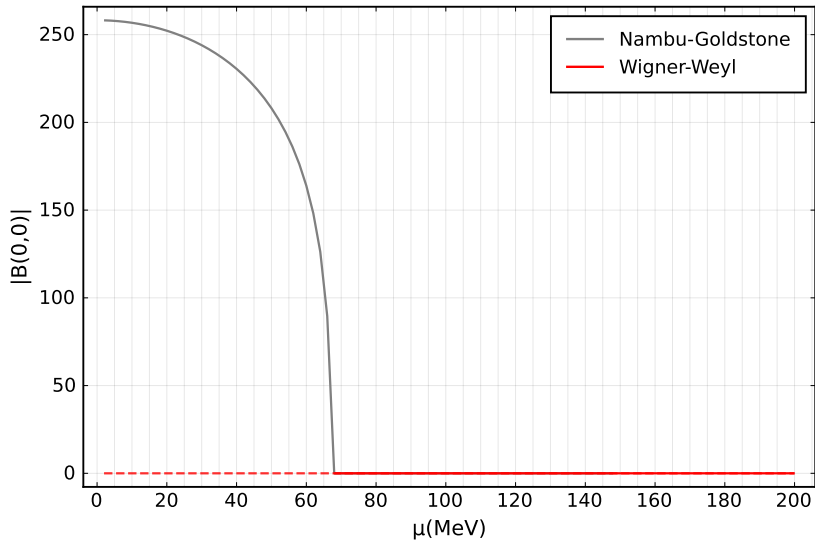
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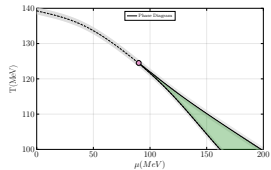
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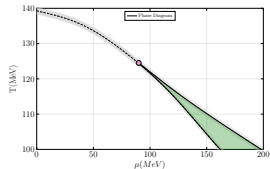
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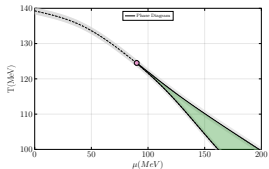
A Test Case: The Chiral Phase Transition



- Chiral

$$S(k) = \frac{-i\vec{k}A_R - i(\omega + i\mu)\gamma_4 C_R}{\vec{k}^2 A_R^2 + (\omega + i\mu)^2 C_R^2}$$

A Test Case: The Chiral Phase Transition



- Chiral

$$S(k) = \frac{-i\vec{k}A_k - i(\omega + i\mu)\gamma_4 C_k}{\vec{k}^2 A_k^2 + (\omega + i\mu)^2 C_k^2}$$

- Chiral Broken

$$S = S_{\text{chiral}} + \delta S_{\text{breaks}}$$

$$\delta S_{\text{breaks}} = \frac{\delta m(k)}{\vec{k}^2 A_k^2 + (\omega + i\mu)^2 C_k^2}$$

Conditions on the test-function

- Let's look at my stability condition ($\Omega \propto -\Gamma$)

$$\Omega_{\mu}^{(2)}[\delta m] = \int_k \left(4 \frac{\delta m(k)^2}{d(k)} - 12 C_F Z_2^2 \int_q \frac{\delta m(k)}{d(k)} \frac{\delta m(k-q)}{d(k-q)} \mathcal{G}(q) \right)$$

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- Also the imaginary part of the test-function has to be fixed

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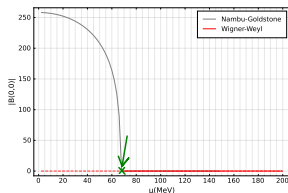
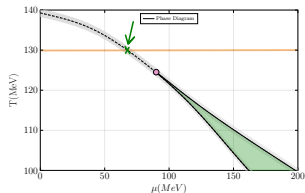
- What about L and whatever other parameters you put in your test-function? Let's see!

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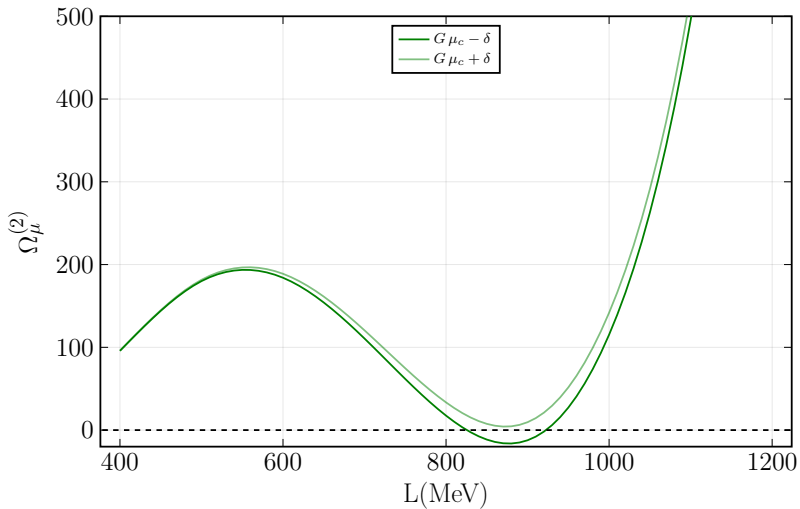
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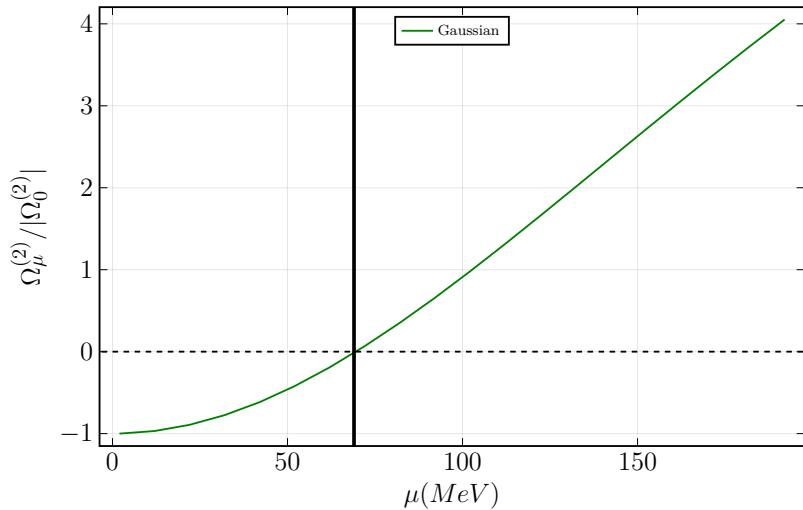
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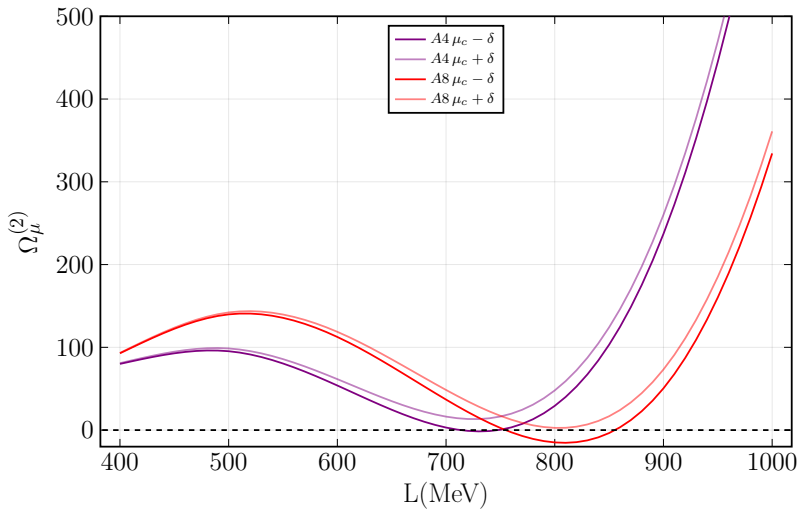
- What if we didn't know what the "real answer" was?

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- Take an "Algebraic decaying function"

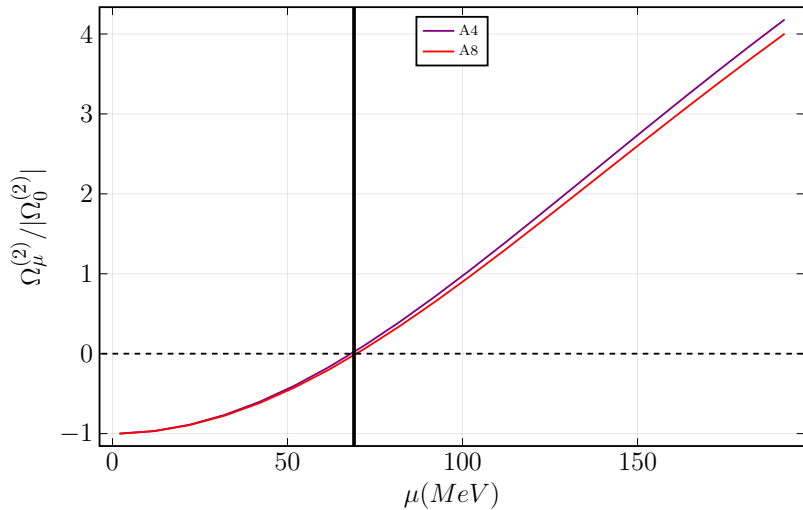
$$\delta m(k) = \lambda \left(1 + \frac{k^2}{L^2}\right)^{-N}$$

with $N = 2, 3, 4, \dots$

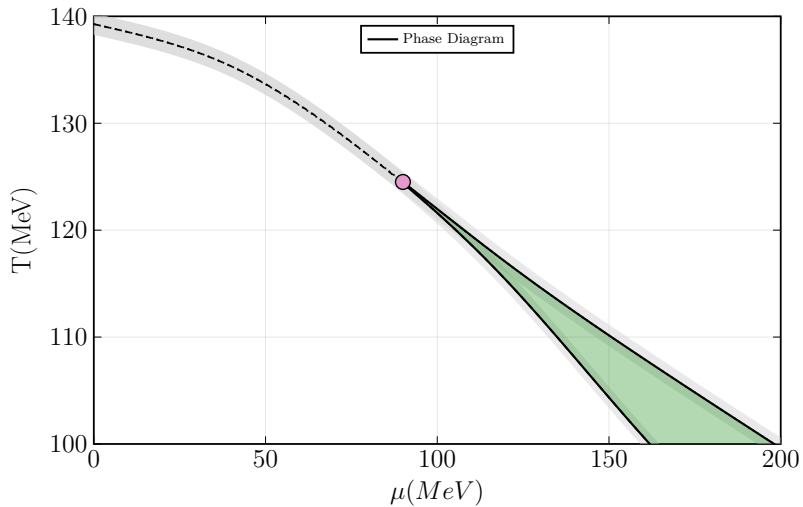
The Test



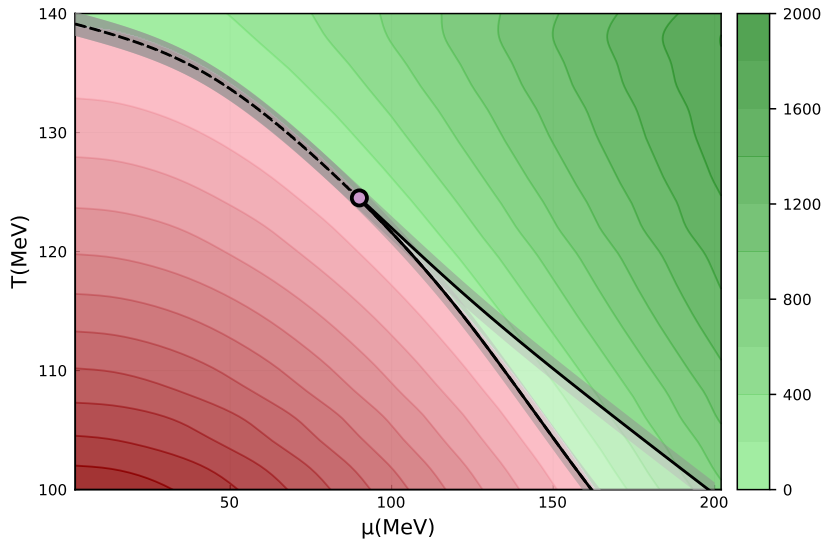
The Test



The Test



The Test



Inhomogeneous Tests

The
~~PRELIMINARY~~
~~TWILIGHT~~
ZONE

Inhomogeneous Tests

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Inhomogeneous Tests

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- It's best to think of an inhom. perturbation to the self energy $\delta\Sigma(k_1, k_2)$ which we relate to the propagator as

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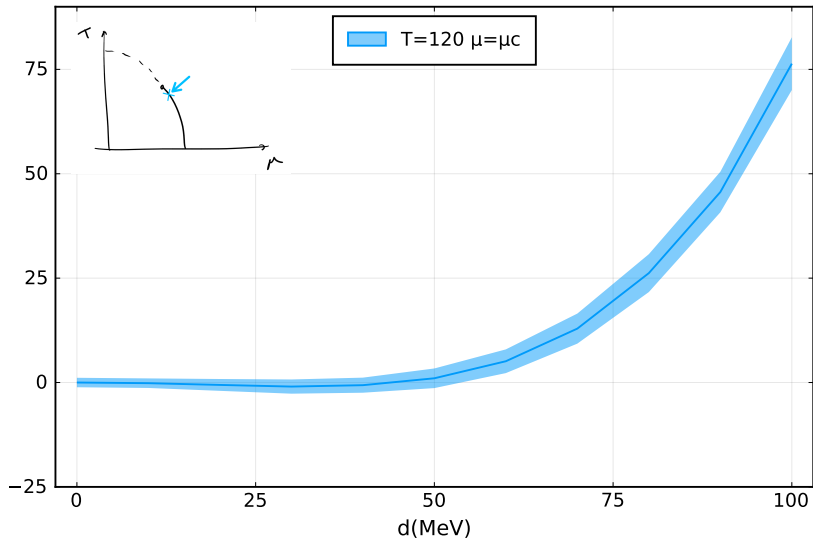
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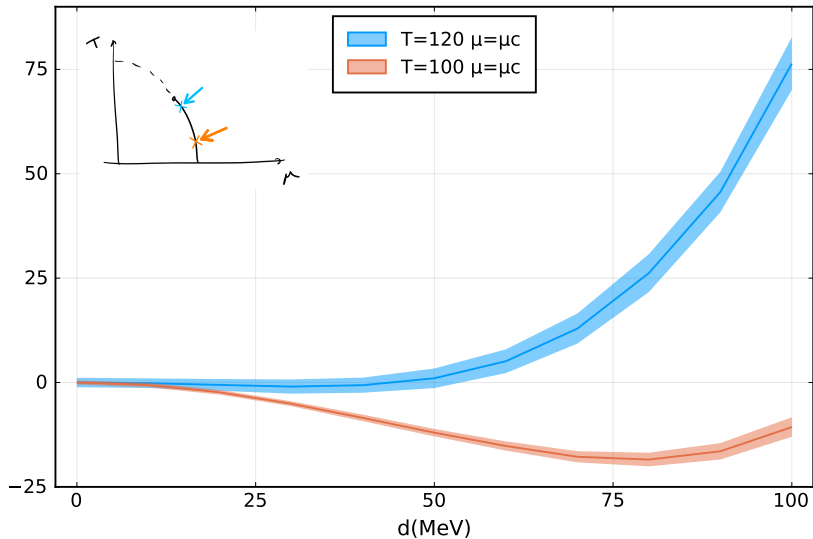
- It's nice if when $d = k_1 - k_2 = 0$, I recover my previous test-function...

$$\delta S(k, k) = \frac{\delta m(k)}{\vec{k}^2 A_k^2 + (\omega + i\mu)^2 C_k^2}$$

Inhomogeneous Tests $T=120\text{MeV}$



Inhomogeneous Tests $T=100\text{MeV}$



Summary & Outlook

- Some preliminar results:
 - No local fluctuations
 - Beyond local, Watson model is too simplistic
 - Gluons should be split. Preferably dynamic.
- Outlook:
 - Go to lower temperatures
 - Improve truncation

Thanks!

Backups

Inhomogeneous Tests

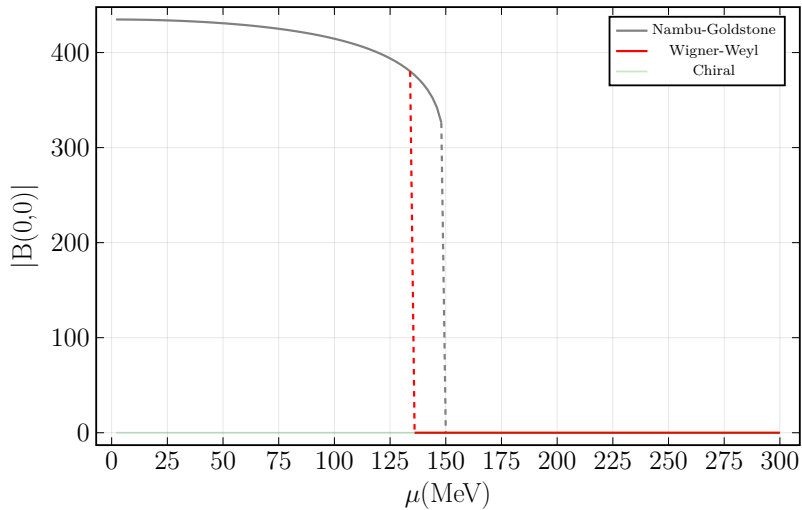
- Test Functions?

$$\delta S(\omega_1, \vec{k}_1, \omega_2, \vec{k}_2)^\dagger = \gamma_4 \delta S(-\omega_2, \vec{k}_2, -\omega_1, \vec{k}_1) \gamma_4$$

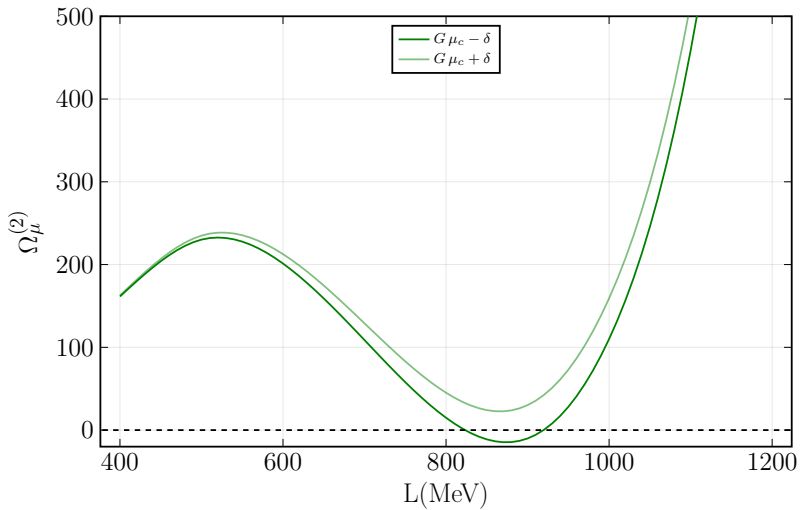
test function 1:
$$\delta \Sigma(k_1, k_2) = \left(\frac{\delta m(k_1)}{d(k_1)} + \frac{\delta m(k_2)}{d(k_2)} \right) F(k_1 - k_2)$$

test function 2:
$$\delta \Sigma(k_1, k_2) = \left(\frac{\delta m(k_1 + k_2)}{d(k_1 + k_2)} \right) F(k_1 - k_2)$$

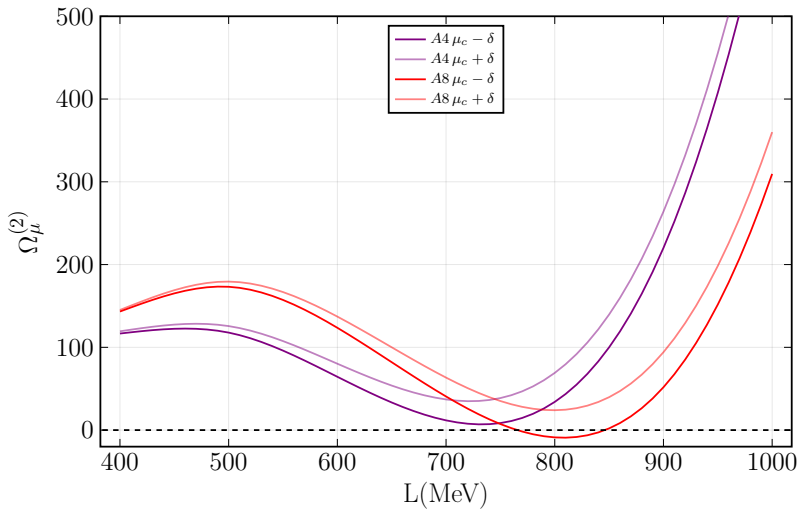
Lower T



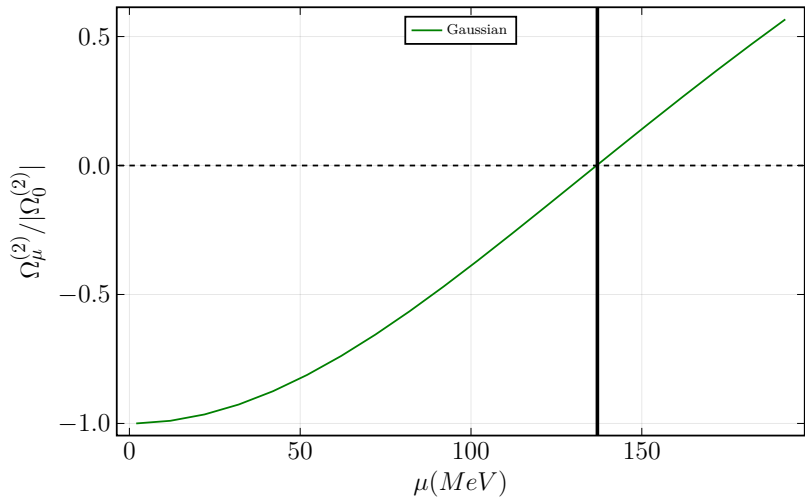
Lower T



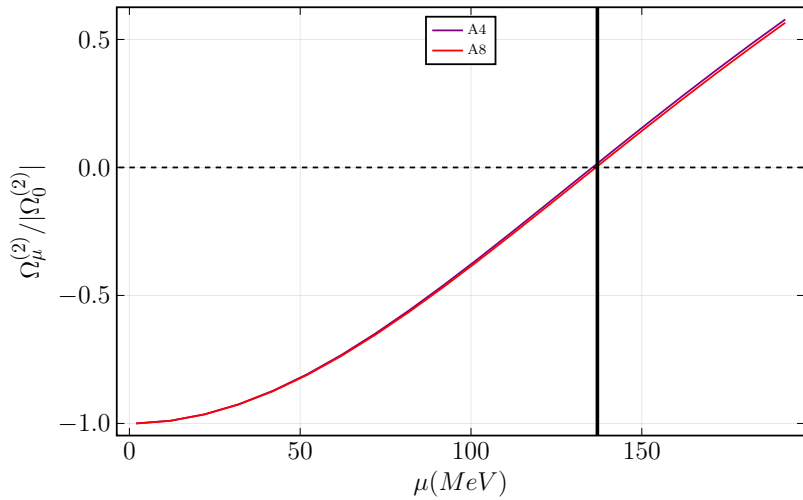
Lower T



Lower T



Lower T



Fluctuations and m_σ in QM

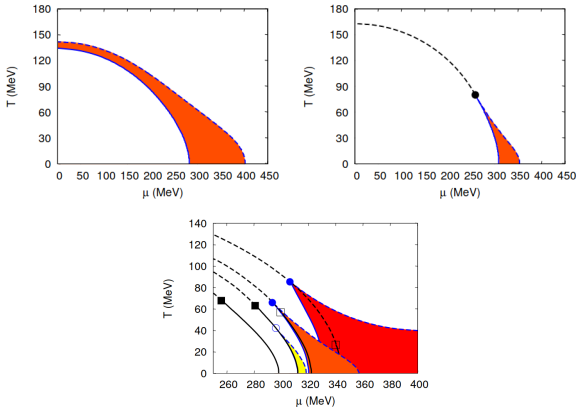
Inhomogeneous phases in the quark-meson model with vacuum fluctuations

Stefano Carignano,¹ Michael Buballa,² and Bernd-Jochen Schaefer³

¹Department of Physics, The University of Texas at El Paso, USA

²Theoriezentrum, Institut für Kernphysik, Technische Universität Darmstadt, Germany

³Institut für Theoretische Physik, Justus-Liebig-Universität Gießen, Germany



How about QCD?

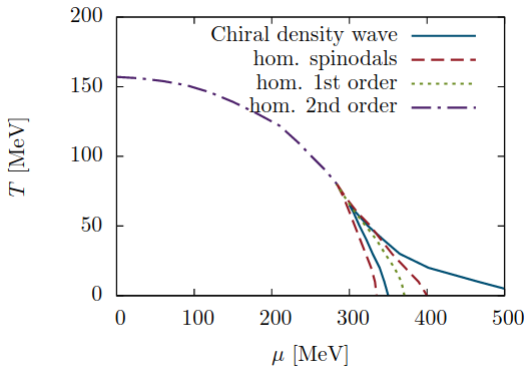
How about QCD?

Dyson-Schwinger study of chiral density waves in QCD

D. Müller^a, M. Buballa^a, J. Wambach^{a,b}

^aInstitut für Kernphysik (Theoriezentrum), Technische Universität Darmstadt, Germany

^bGSI Helmholtzzentrum für Schwerionenforschung, Darmstadt, Germany



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- You need an ansatz for the propagator that supports a self-consistent solution of the Dyson-Schwinger Equations

$$\begin{aligned} S^{-1}(p, p') = & \left[-i(\omega_n + i\mu) \gamma_4 C(p) - ip_3 \gamma_3 E(p) - i\vec{p}_\perp A(p) \right. \\ & \left. - i(\omega_n + i\mu) \gamma_5 \gamma_4 C_5(p) - ip_3 \gamma_5 \gamma_3 E_5(p) - i\gamma_5 \vec{p}_\perp A_5(p) \right] \delta(p - p') \\ & + \left(B(p, p') - i\gamma_4 \gamma_3 F(p, p') - i\gamma_4 \frac{\vec{p}_\perp}{|\vec{p}_\perp|} G(p, p') - i\gamma_3 \frac{\vec{p}_\perp}{|\vec{p}_\perp|} H(p, p') \right) \frac{(1 - \gamma_5)}{2} \delta(p - p' + Q) \\ & + \left(B(p, p') + i\gamma_4 \gamma_3 F(p, p') + i\gamma_4 \frac{\vec{p}_\perp}{|\vec{p}_\perp|} G(p, p') + i\gamma_3 \frac{\vec{p}_\perp}{|\vec{p}_\perp|} H(p, p') \right) \frac{(1 + \gamma_5)}{2} \delta(p - p' - Q). \end{aligned}$$

How about QCD?

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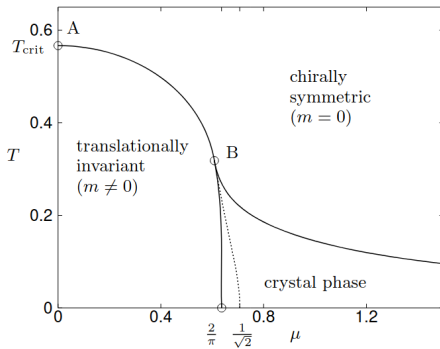
$$\begin{aligned} S^{-1}(p, p') = & \left[-i(\omega_n + i\mu) \gamma_4 C(p) - ip_3 \gamma_3 E(p) - i\vec{p}_\perp A(p) \right. \\ & \left. - i(\omega_n + i\mu) \gamma_5 \gamma_4 C_5(p) - ip_3 \gamma_5 \gamma_3 E_5(p) - i\gamma_5 \vec{p}_\perp A_5(p) \right] \delta(p - p') \\ & + \left(B(p, p') - i\gamma_4 \gamma_3 F(p, p') - i\gamma_4 \frac{\vec{p}_\perp}{|\vec{p}_\perp|} G(p, p') - i\gamma_3 \frac{\vec{p}_\perp}{|\vec{p}_\perp|} H(p, p') \right) \frac{(1 - \gamma_5)}{2} \delta(p - p' + Q) \\ & + \left(B(p, p') + i\gamma_4 \gamma_3 F(p, p') + i\gamma_4 \frac{\vec{p}_\perp}{|\vec{p}_\perp|} G(p, p') + i\gamma_3 \frac{\vec{p}_\perp}{|\vec{p}_\perp|} H(p, p') \right) \frac{(1 + \gamma_5)}{2} \delta(p - p' - Q). \end{aligned}$$

- Then you solve the DSE **and**, in theory, you must calculate whether or not this solution is favoured!

A plot twist? Gross-Neveu Model!

Revised Phase Diagram of the Gross-Neveu Model

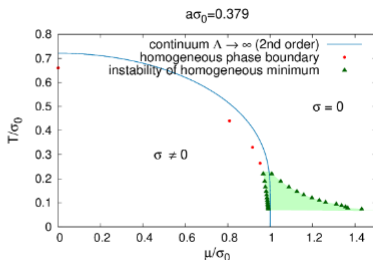
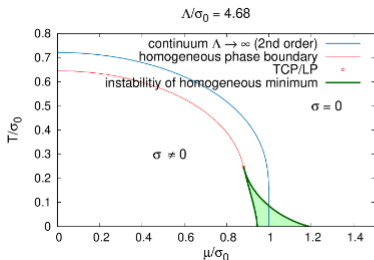
Michael Thies and Konrad Urlichs
Institut für Theoretische Physik III
Universität Erlangen-Nürnberg
Staudtstraße 7
D-91058 Erlangen
Germany
(Dated: October 25, 2018)



A plot twist? Gross-Neveu Model!

Regulator dependence of inhomogeneous phases in the 2+1-dimensional Gross-Neveu model

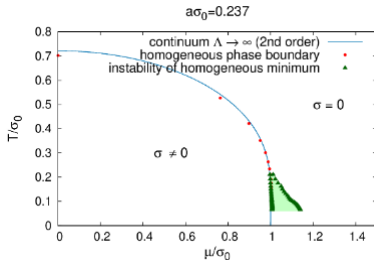
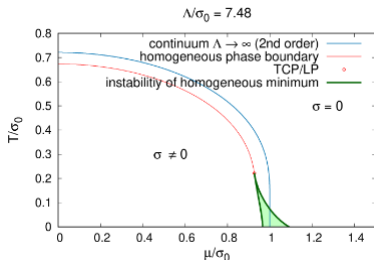
Michael Buballa^{a,c}, Lennart Kurth^a, Marc Wagner^{b,c}, Marc Winstel^b



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