

Enhanced pion-to-proton ratio at a dynamical QCD phase transition

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Phys. Lett. B **835**, 2022 [arXiv:2209.04096]

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NeD workshop 2022, Krabi

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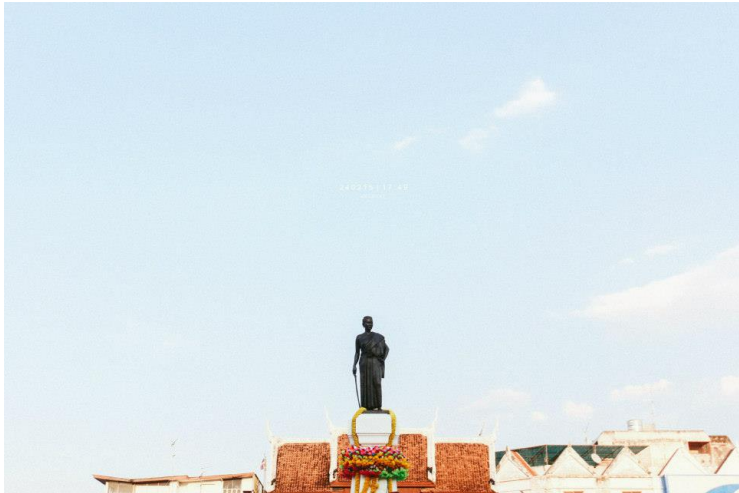
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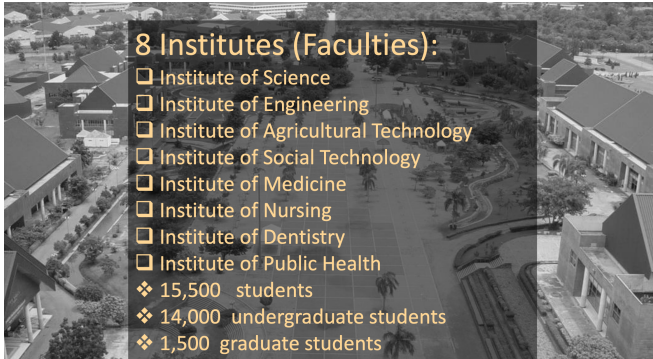
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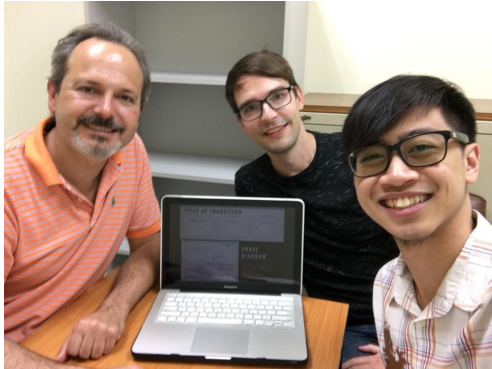
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Outline

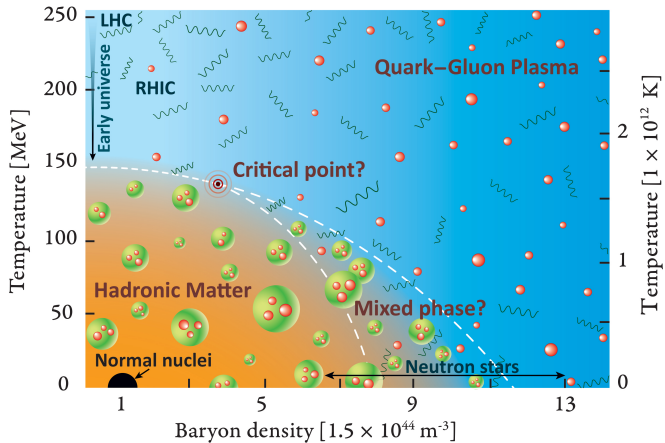
The QCD Phase Diagram

Chiral Fluid Dynamics

Multiplicity Ratios

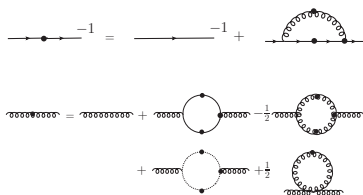
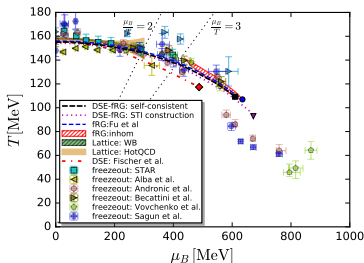
Summary

The QCD Phase Diagram



First principle calculations

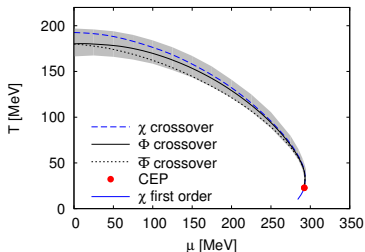
- Partition function \mathcal{Z} on a lattice (sign problem for finite μ)
- Solve Dyson-Schwinger equations



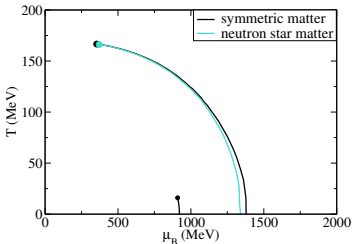
(Gao, Pawłowski, Phys. Lett. B **820**, 2021)

Effective Models

- Start with (chiral) symmetry, sigma, NJL model
- Extension with Polyakov loop, baryonic degrees of freedom
- Existence/location of CP not universal



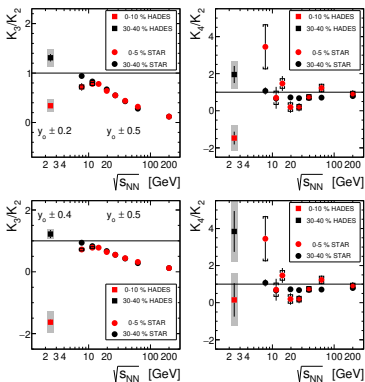
(Herbst, Pawlowski, Schaefer, Phys. Lett. B **696**, 2011)



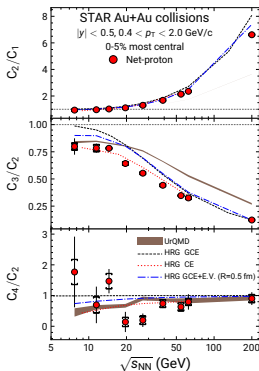
(Dexheimer, Schramm, Phys. Rev. C **81**, 2010)

Critical Point - Signals and Observables

1. Higher order cumulants: HADES and STAR data



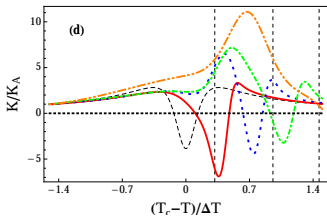
(HADES coll., Phys. Rev. C **102**, 2020)



(STAR coll., Phys. Rev. C **104**, 2021)

Critical Point - Signals and Observables

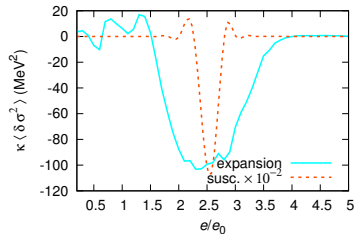
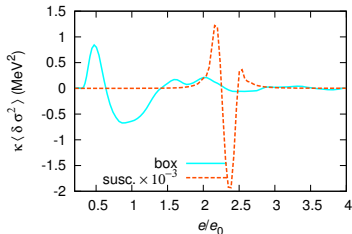
2. Nonequilibrium effects



(Mukherjee, Venugopalan, Yin, Phys. Rev. C **92**, 2015)

Cumulants are influenced by:

- Dependence on ξ
- Relaxation time
- Inhomogeneities



(CH, Nahrgang, Bleicher et al., EPJ A**54**, 2018)

Critical Point - Signals and Observables

- Determine cumulants of the 0-mode of the sigma field at freeze-out

$$\sigma_V = \int_V d^3x \sigma(x) = \sigma V$$

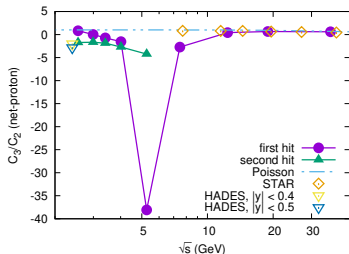
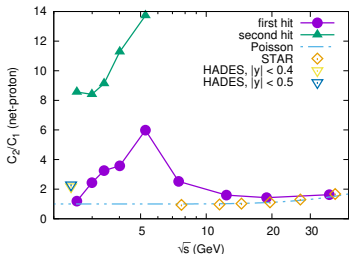
- Net-proton number fluctuations from Poisson plus critical fluct.

$$\delta N = \delta N^0 + V g \delta \sigma d \int \frac{d^3p}{(2\pi)^3} \frac{\partial n_p}{\partial m}$$

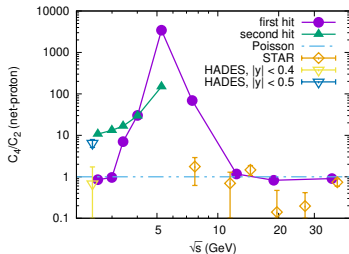
- Relate net-proton to sigma cumulants

$$\langle (\delta N)^4 \rangle_c = \langle N \rangle + \langle \sigma_V^4 \rangle_c \left(\frac{g d}{T} \int \frac{d^3p}{(2\pi)^3} \frac{n_p}{\gamma} \right)^4 + \dots,$$

Critical Point - Signals and Observables

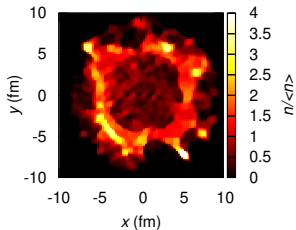
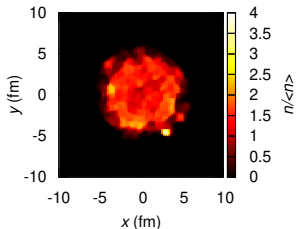


- Poisson baseline approached for large \sqrt{s}
- Strongly enhanced cumulants near spinodal line
- FOPT allows for wider range of cumulants

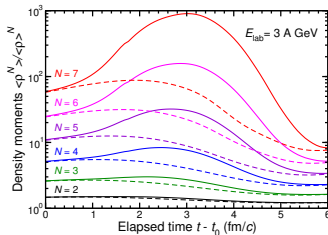


First-order Phase Transition - Signals and Observables

1. Nonequilibrium effects: Spinodal instabilities



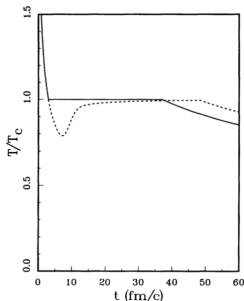
- Formation of Metastable phase
- Dynamical fragmentation
- Non-statistical multiplicity fluctuations
- Signal in momentum space?



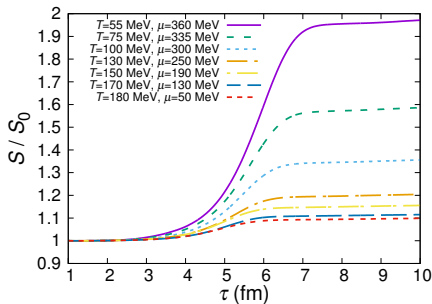
First-order Phase Transition - Signals and Observables

2. Delayed Expansion

- Thermal radiation, dileptons
- Hanbury-Brown-Twiss Interferferometry
- Generation of **Extra entropy** from nonequilibrium phase transition



(Csernai, Kapusta, Phys. Rev. Lett. **69**, 1992)

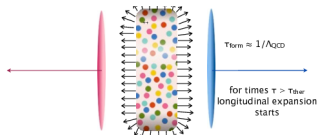


(CH, Kittiratpattana et al., Phys. Lett. B **790**, 2019)

N χ FD

Nonequilibrium Chiral Fluid Dynamics (N χ FD)

- Nonequilibrium dynamics of σ
- Fluid dynamic expansion
- **damping** and **stochastic noise**



(G. Martinez, arXiv:1304.1452)

$$\ddot{\sigma} + \eta \dot{\sigma} + \frac{\delta\Omega}{\delta\sigma} = \xi$$

$$\dot{e} = -\frac{e + P}{\tau} + \left(\frac{\delta\Omega}{\delta\sigma} + \eta \dot{\sigma} \right) \dot{\sigma}, \quad \dot{n} = -\frac{n}{\tau}$$

(CH, Kittiratpattana, Kobdaj, Limphirat, Yan, Nahrgang, Steinheimer, Bleicher, Phys. Lett. B **790**, 2019)

$$\mathcal{L} = \bar{q} (i\gamma^\mu \partial_\mu - g\sigma) q + \frac{1}{2} \partial_\mu \sigma \partial^\mu \sigma - U(\sigma)$$

Lagrangian of the quark-meson model

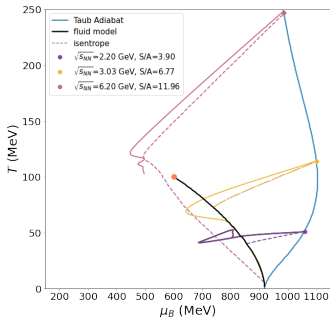
Initial Conditions

- Realistic initial conditions
- 1D shock wave solution (Rankine-Hugoniot-Taub adiabat)

$$(P_0 + \varepsilon_0) (P + \varepsilon_0) n^2 = (P_0 + \varepsilon) (P + \varepsilon) n_0^2$$

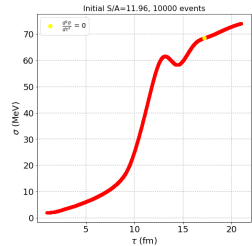
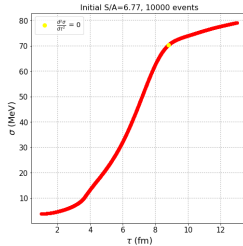
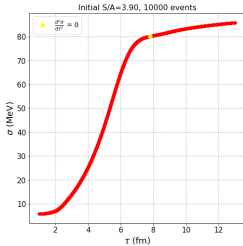
- Relate collision energy from compression:

$$\gamma^{\text{CM}} = \frac{\varepsilon n_0}{\varepsilon_0 n}, \quad \gamma^{\text{CM}} = \sqrt{\frac{1}{2} \left(1 + \frac{E_{\text{lab}}}{m_N} \right)}$$



(Bummedpan, CH, JS, MB, Phys. Lett. B **835**, 2022)

"Freeze-out" condition



Test different freeze-out criteria depending on the evolution of σ

- Freeze-out at constant value of $\sigma = 70$ MeV
- Freeze-out at "end" of the rapid transition, i.e. $d^2\sigma/d\tau^2 = 0$

Fit to chemical freeze-out curves

- Use two parametrized freeze-out curve obtained from hadron multiplicity ratios

$$T_{\text{freeze}}(\mu_B) = a - b\mu_B^2 - c\mu_B^4$$

- Parameter set A:

$$a = 0.157 \text{ GeV}, b = 0.087 \text{ GeV}^{-1} \text{ and } c = 0.092 \text{ GeV}^{-3}$$

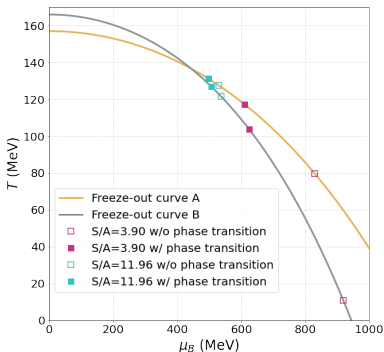
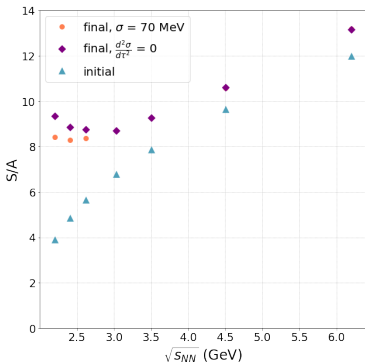
(Vovchenko, Begun, Gorenstein, Phys. Rev. C **93**, 2016)

- Parameter set B:

$$a = 0.166 \text{ GeV}, b = 0.139 \text{ GeV}^{-1} \text{ and } c = 0.053 \text{ GeV}^{-3}$$

(Cleymans, Oeschler, Redlich, Wheaton, Phys. Rev. C **73**, 2006)

Entropy per baryon number

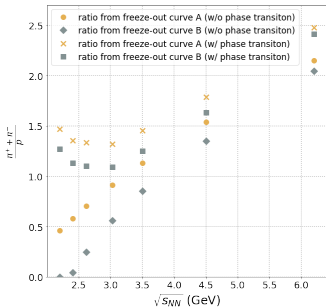


(Bummedpan, CH, JS, MB, Phys. Lett. B **835**, 2022)

- Qualitatively similar results for S/A , slight deviations at low \sqrt{s}
- Fit to freeze-out curves using Thermal-FIST HRG toolkit

(Vovchenko, Stoecker, Comput. Phys. Commun. **244**, 2019)

Pion-to-proton ratio

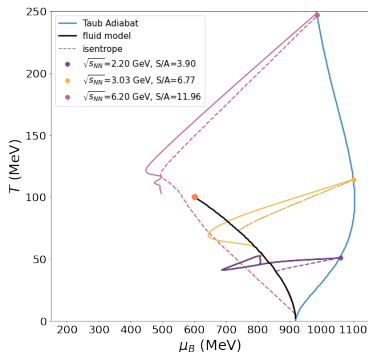


- Pion-to-proton ratio as observable for S/A
- FOPT scenario leads to increase at low \sqrt{s}
- In the model: Initial state always in restored phase
- Realistically: Jump in π/p at onset of chiral PT, around ~ 3 GeV

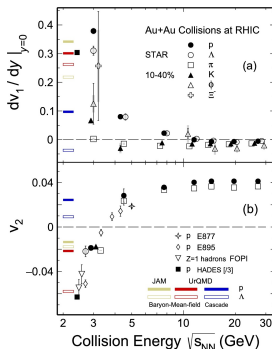
(STAR, Phys. Lett. B **827**, 2022)

(Bummedpan, CH, JS, MB, Phys. Lett. B **835**, 2022)

Caveats and what to look for



(Bummedpan, CH, JS, MB, Phys. Lett. B **835**, 2022)

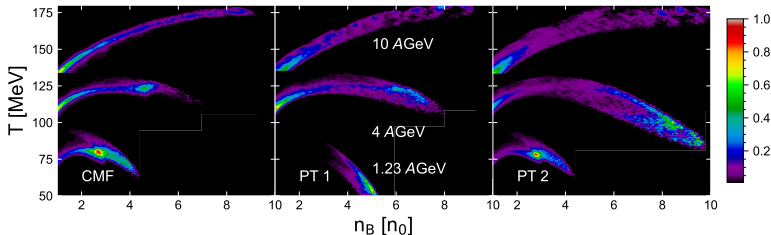


(STAR coll., Phys. Lett. B **827**, 2022)

- Model caveat: Initial state always in the restored phase
- Measurements of v_1 , v_2 at STAR suggest dominance of baryons for $\sqrt{s_{NN}} \lesssim 3$ GeV
- Expect jump in π/p at onset of chiral PT around ~ 3 GeV

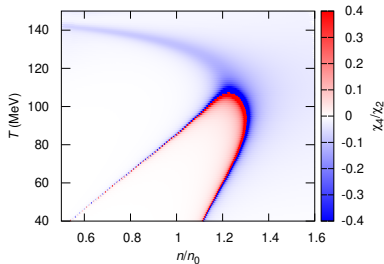
Summary and outlook

- Nonequilibrium chiral dynamics describes entropy production
- FOPT dynamics leads to significant increase in S/A
- Strong enhancement of π/p at onset of QCD phase transition
- Next: Dilepton production



(Savchuk, Motornenko, Steinheimer et al., arXiv:2209.05267)

Susceptibilities near the critical point



- Phase diagram in $T-n_q$ plane
- Spinodal instabilities at $T < T_{cp}$
- Diverging susceptibilities

