

# The high density QCD EoS from heavy ion observables

**Jan Steinheimer-Froschauer**

many thanks to

A. Motornenko, M. Omana Kuttan, O. Savchuk, E. Most, M Bleicher, H. Stöcker  
and many more.

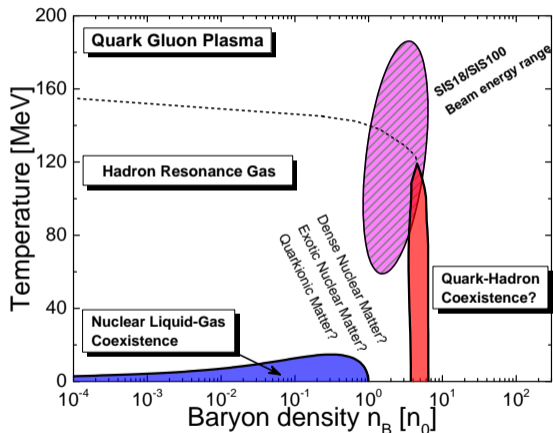
Frankfurt Institute for Advanced Studies

28.11.2022



**FIAS** Frankfurt Institute  
for Advanced Studies 

# The interesting part of the phase diagram



- This is just a sketch.
- QCD based methods break down for  $\mu_B/T \gtrsim 3 - 4$ .
- $T_{cep} \lesssim 120$  MeV.
- Results at low density: Crossover is now confirmed.
- High density: room for speculations.

# The Strategy

## Relying on experimental observations?

We want to understand QCD matter, not neutron star matter or heavy ion collision matter. The latter are mere inputs for simulations.

- 1 Calculate/construct an EoS that can be used for finite temperature and density QCD matter. Check consistency with known properties at small  $\mu_B/T$  and nuclear matter.

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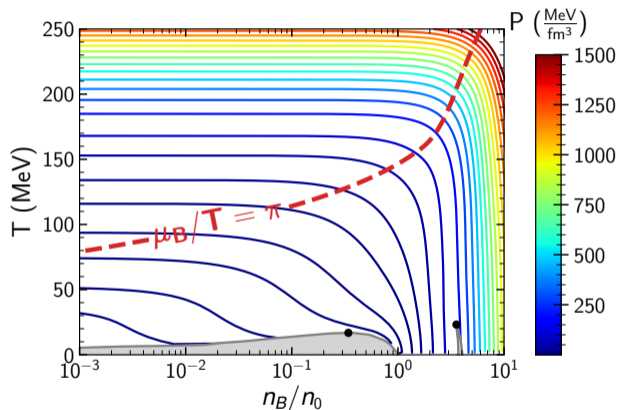
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- 4 Cross check with astrophysical observations.
- 5 Reject unlikely EoS.

# 1. The baryonic problem



## Why do the methods break down?

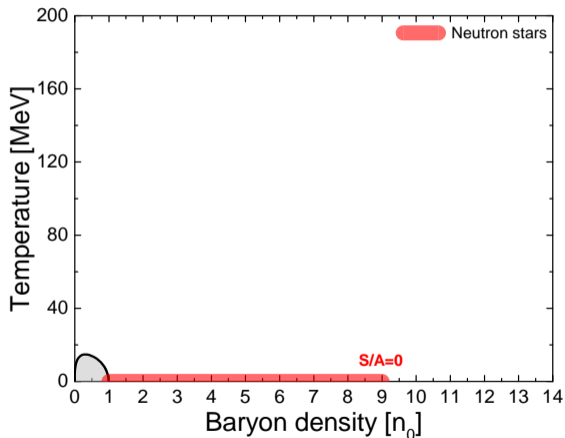
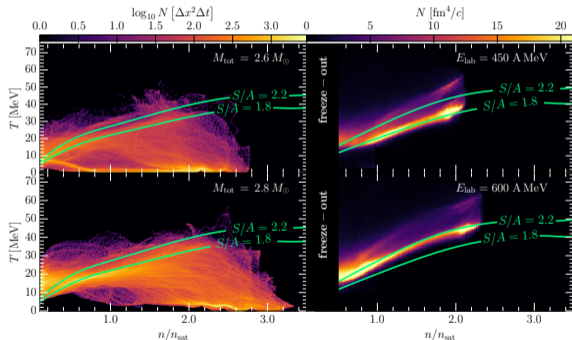
- Sudden change of isobaric lines at this point.
- From Boson (mesons/gluons) dominated matter to fermionic matter (nucleons/quarks).
- Calculations seem to fail for matter where (multi-) baryonic interactions become important.
- Positive: for the region of interest a density dependent EoS may be enough.

A. Motornenko, JS, V. Vovchenko, S. Schramm and H. Stoecker, Nucl. Phys. A 1005 (2021), 121836



# Regions of access to the PD - BNSM

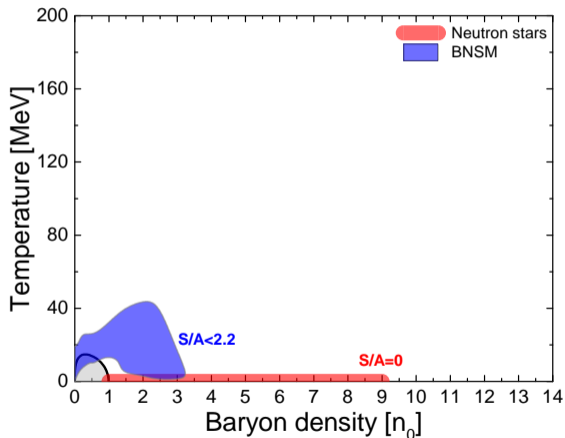
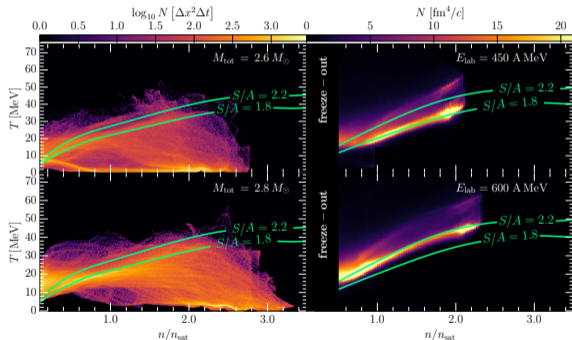
- Using BNSM we can also turn on the heat.
- During the post-merger  $T < 40$  MeV is reached
- Observables?



E. R. Most, A. Motornenko, JS, V. Dexheimer, M. Hanauske, L. Rezzolla and H. Stoecker, [arXiv:2201.13150 [nucl-th]].

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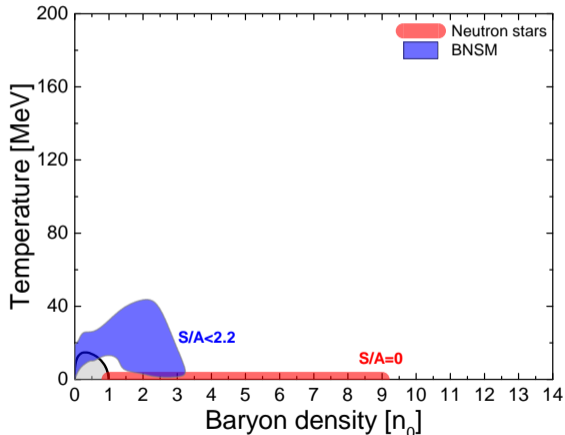
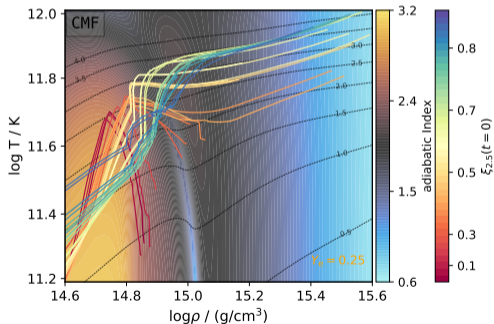
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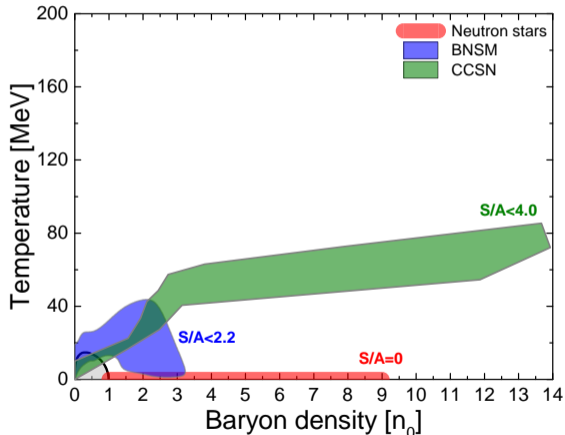
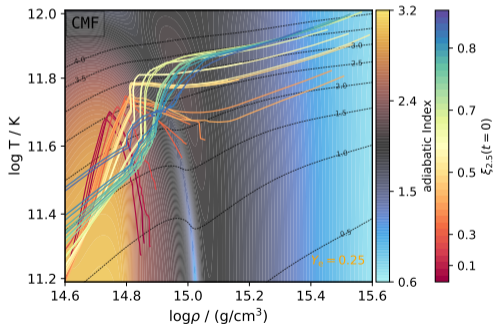
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- Core Collapse Supernovae (CCSN) can reach even higher  $S/A$
- GR Hydro simulation with same EoS (CMF model):



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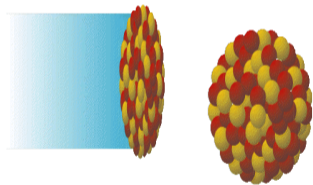
- Core Collapse Supernovae (CCSN) can reach even higher  $S/A$
- GR Hydro simulation with same EoS (CMF model):
- Observables: Neutrinos, GW?



# How to study the equation of state using heavy ion collisions

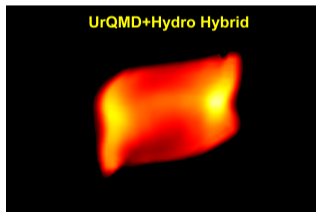
Much of what we today think about heavy ion dynamics is motivated by the fluid dynamic picture of HIC:

Pre-equilibrium phase



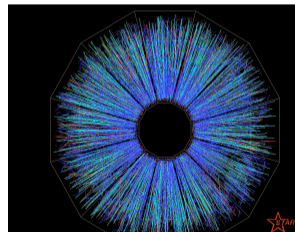
Non-equilibrium initial state

Equilibrated? phase



Fluid dynamic evolution

Final stage and particle freeze-out

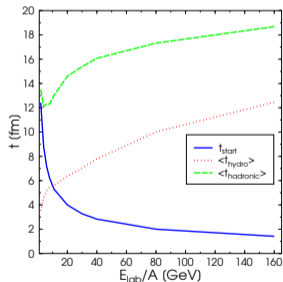


Freeze-out: chemical and thermal

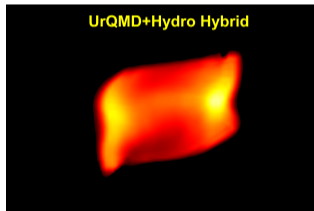
# How to study the equation of state using heavy ion collisions

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At low beam energies the initial compression is most relevant.

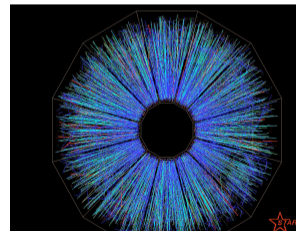
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Equilibrated? phase



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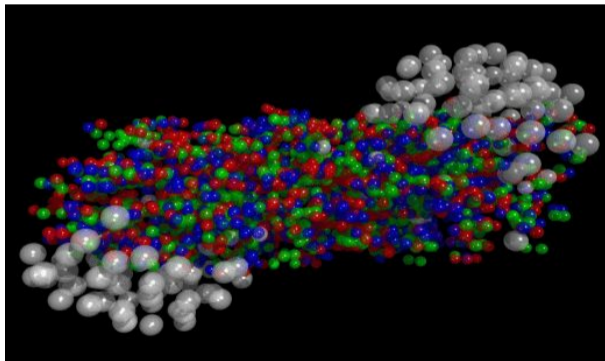
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## UrQMD for the description

UrQMD is a microscopic transport model

- In cascade mode: Particles follow a straight line until they scatter.
- EoS resembles a hadron resonance gas.



## UrQMD is a microscopic transport model

- Only  $2 \leftrightarrow 2$ ,  $2 \leftrightarrow 1$ ,  $2 \rightarrow N$  and  $1 \rightarrow N$  interactions allowed.
- Resonance decays according to PDG values + guesstimates.
- Detailed balance. (Violated in string excitations, annihilations and some decays)



# The Skyrme EoS in UrQMD

To implement any density dependent EoS in UrQMD:

In UrQMD the real part of the interaction is implemented by a density dependent potential energy  $V(n_B)$ .

Once the potential energy is known, the change of momentum of each baryon is calculated as:

$$\dot{\mathbf{p}}_i = -\frac{\partial H}{\partial \mathbf{r}_i} = -\left(\frac{\partial V_i}{\partial n_i} \cdot \frac{\partial n_i}{\partial \mathbf{r}_i}\right) - \left(\sum_{j \neq i} \frac{\partial V_j}{\partial n_j} \cdot \frac{\partial n_j}{\partial \mathbf{r}_i}\right), \quad (1)$$

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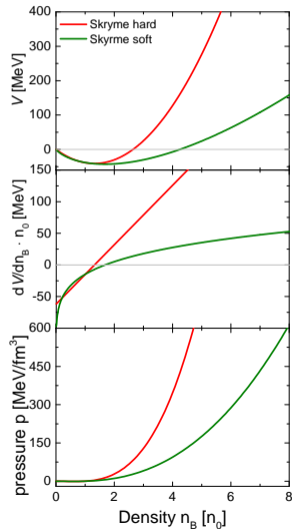
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For the potential energy  $V$  often a Skyrme model was used that is based on a 2-term expansion in density:

$$U(n_B) = \alpha \cdot n_B + \beta \cdot n_B^\gamma \quad \text{with} \quad U(n_B) = \frac{\partial(n_B \cdot V(n_B))}{\partial n_B} \quad (2)$$

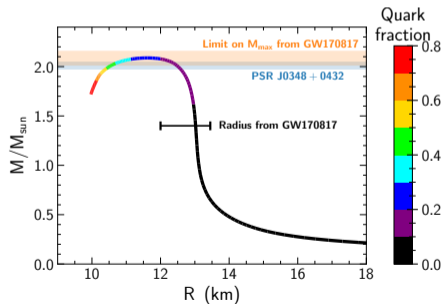
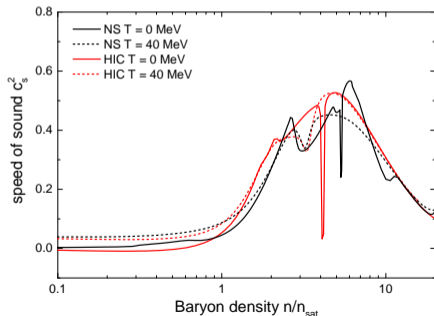
Problem: Once saturation density and binding energy is fixed, only 1 d.o.f. left and EoS likely becomes unphysical. No phase transition possible.



# A different effective model: the CMF

## Application for cold compact stars

- Compressibility of the CMF EoS is  $\kappa_0 = 267$  MeV and the symmetry energy is  $S_0 = 31.9$  MeV.
- Speed of sound for neutron star matter.
- Mass radius diagram consistent with astrophysical constraints.



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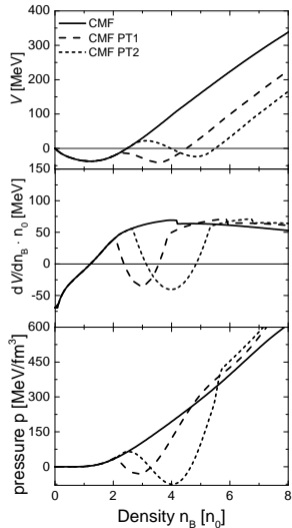
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In CMF we can simply use the effective field energy per baryon  $E_{\text{field}}/A$  calculated from the CMF model:

$$V_{CMF} = E_{\text{field}}/A = E_{CMF}/A - E_{FFG}/A, \quad (4)$$

A phase transition can be simply included by adding another minimum in the potential energy: leading to (meta-)stable solutions at high density.



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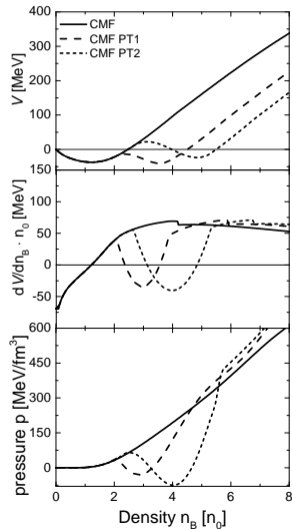
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**Disadvantage:** Only density dependence + no change in d.o.f.

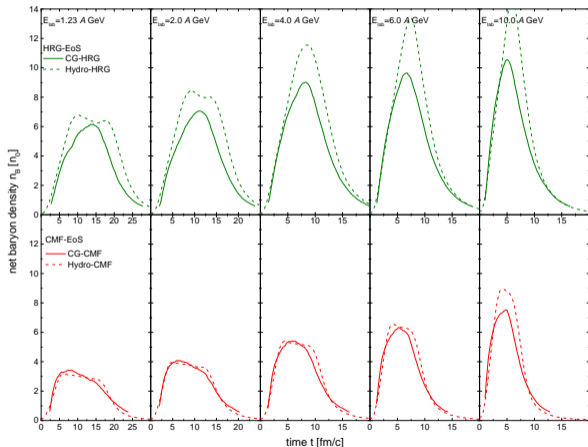
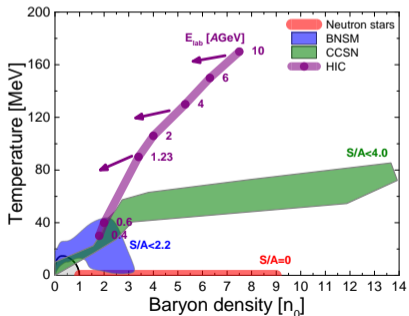
**Advantage:** Consistent description throughout, i.e. no change of model or d.o.f. required.

→ Focus on the effects of the equation of state and dynamic phase separation.



# 1. HIC UrQMD vs. hydro, regions of access

- Including the CMF EoS in UrQMD vs. a hadron resonance gas baseline.
- Bulk evolution consistent with 3+1D hydro + CMF
- Initial compression from CMF model in UrQMD

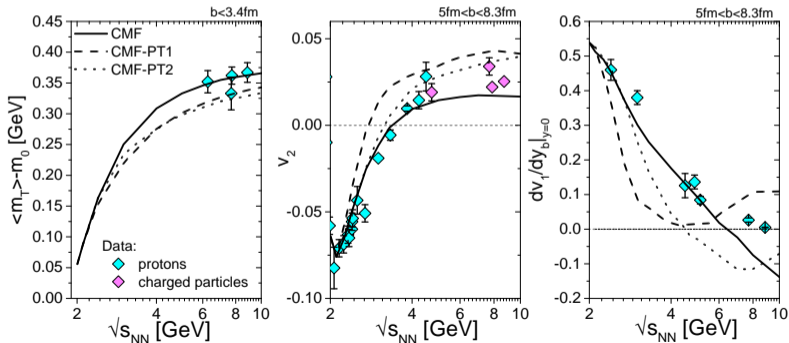


M. Omana Kuttan, A. Motornenko, JS, H. Stoecker, Y. Nara and M. Bleicher, Eur. Phys. J. C 82 (2022) no.5, 427

## 2. Results on flow

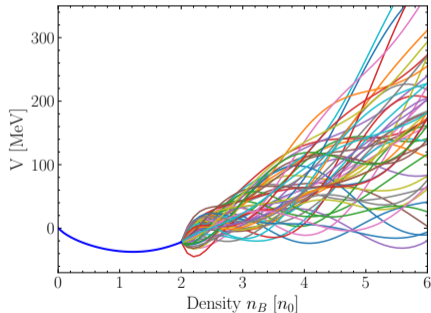
- The CMF EoS gives good results on all flow coefficients.
- Significant effects of a phase transition on all flow observables.
- Minimum in the slope of the directed flow confirmed.
- Sensitivity only up to  $\approx 4n_0$ .

- $m_T = p_T^2 + m^2$
- $v_1 = p_x/p_T$
- $v_2 = (p_x^2 - p_y^2)/p_T^2$



## 2. Statistical analysis of available flow data

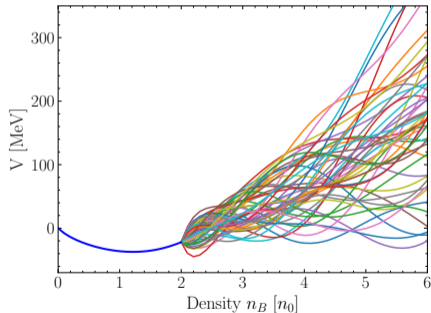
- Using Bayesian inference methods we can try to constrain the EoS from flow data
- Use UrQMD as described but parameterize  $V(n_B)$  with a seventh order polynomial.



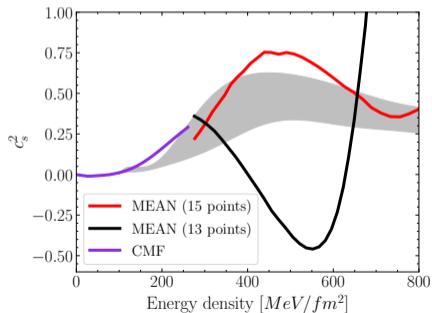


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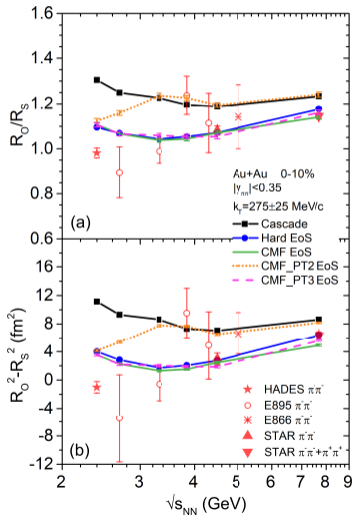
- Results depend strongly on the data used.
- If all data on the mean  $m_T$  and  $v_2$  are used, constraints are similar to those from astrophysics (NS and BNSM).



### 3. HBT

- Hanbury-Brown-Twiss (HBT) correlations for charged pions are a tool to measure the freezeout volume and time.
- Pions that are emitted close in coordinate space are correlated in momentum space.
- Simulation with a PT show a clear maximum.
- 'Old' data seem inconclusive, newest STAR data have much smaller error and favor the no-PT scenario.
- Sensitivity only up to  $\approx 4n_0$ .

P. Li, T. Reichert, A. Kittiratpattana, JS, M. Bleicher, Q. Li



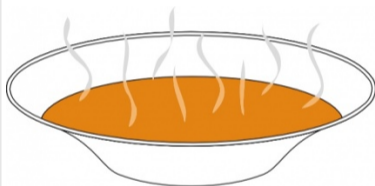
## 4. Dileptons

Electromagnetic probes offer a chance to probe the whole time evolution of the fireball.

In particular di-lepton pairs created by the decay of hadrons or quark annihilation.

- $\rho \rightarrow e^+ + e^-$
- $q + \bar{q} \rightarrow e^+ + e^-$

Process sensitive to the medium in which it takes place ( $T$  and  $\rho_B$ ).



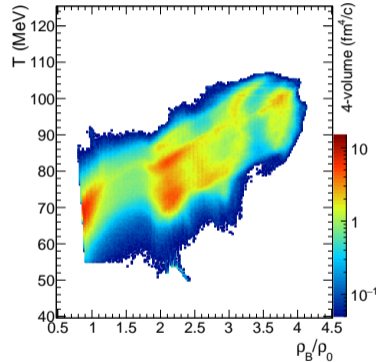
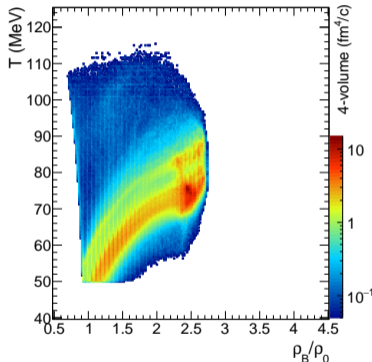
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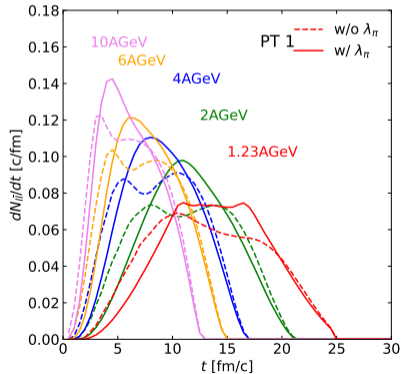
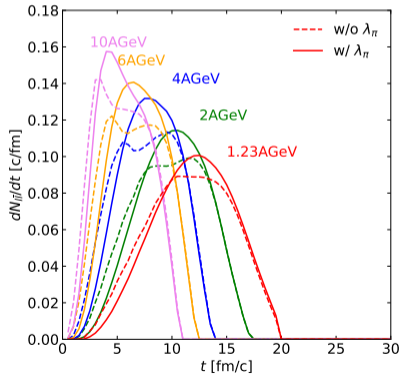


Distinct differences CMF with or without a phase transition

F. Seck, T. Galatyuk, A. Mukherjee, R. Rapp, JS and J. Stroth, [arXiv:2010.04614 [nucl-th]].

## 4. Dileptons

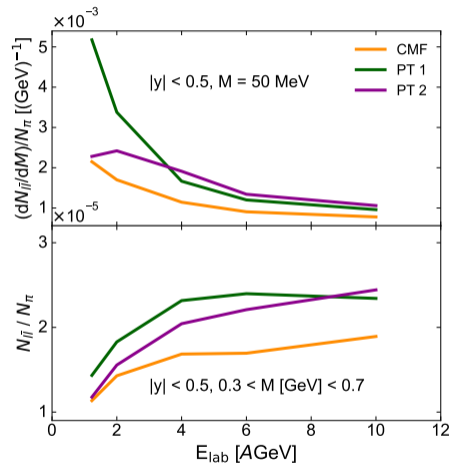
- Dilepton emission is sensitive to the time-integrated bulk evolution properties.
- Results from the UrQMD+CMF(+PT) transport model.
- Effect due to extended lifetime.



## 4. Dileptons

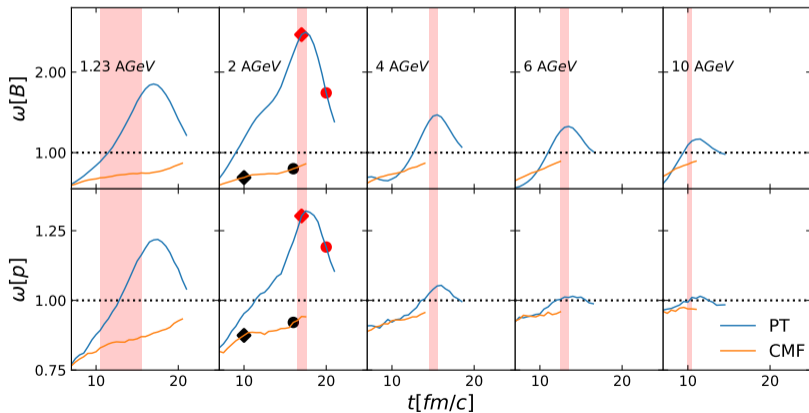
- Hydro simulations have suggested a strong increase (of factor 2) of the dilepton yield for a phase transition:  
F. Seck, T. Galatyuk, A. Mukherjee, R. Rapp, JS and J. Stroth, [arXiv:2010.04614 [nucl-th]].
- A significant increase of the low mass dilepton yield is observed when a phase transition is included in the UrQMD-CMF model.

O. Savchuk, A. Motornenko, JS, V. Vovchenko, M. Bleicher, M. Gorenstein, T. Galatyuk, [arXiv:2209.05267 [nucl-th]].



## 5. Fluctuations

- As we employ a QMD approach local clumping in the unstable phase can occur.
- This leads to enhanced fluctuations of the baryon number in coordinate space, already observed in the scaled variance.

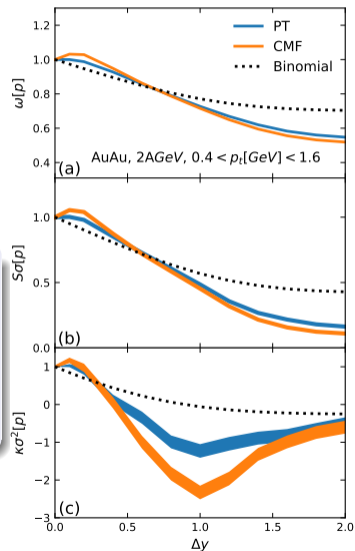


O. Savchuk, et.al., in preparation

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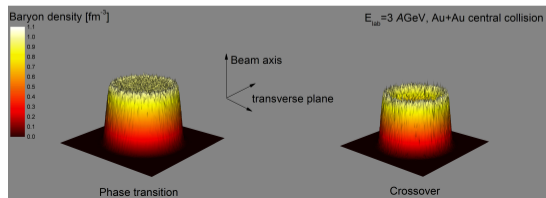
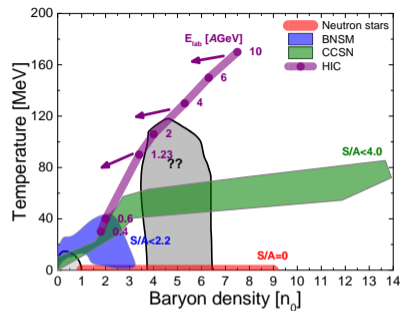
- While in coordinate space the fluctuations/correlations are enhanced due to the phase transition.
- In momentum space no enhancement is observed.
- The crossover scenario even shows an increased scaled variance. This is due to the larger radial flow pushing into the spectators leading to larger volume fluctuations.





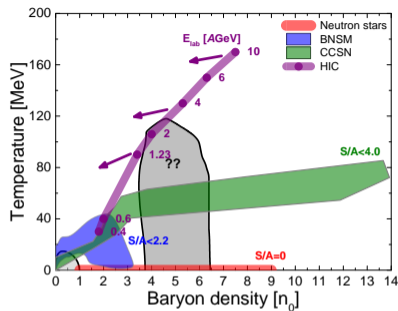
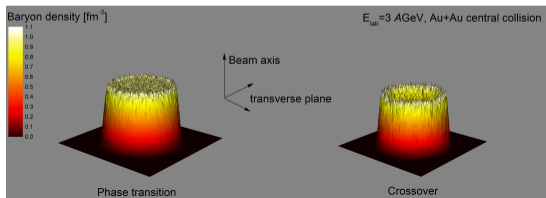
## Summary and conclusions

- Can use HIC and BNSM to scan the high density QCD PD.
- Especially for HIC in the FAIR-regime new ideas/methods for old and new models are necessary.
- This work: Phase transitions in transport shown to influence observables.
- Best results obtained for model w/o phase transition, consistent with astrophysical observations (sensitivity only up to  $\approx 4n_0$ ).
- Only consistent models can be used for statistical analyses of large datasets available now and in the future.
- Still room for development of critical phenomena, relativistic treatment of transport models...



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- The minimum of  $v_1$  coincides with the maximum of the dilepton emission.
- The effect on HBT and maximum of the fluctuation enhancement seems to occur at even lower beam energies.
- Effects don't occur at the same beam energy: **Need consistent modeling!!**

## 4. Light nuclei production

- The double ratio  $t \cdot p / (d^2)$  is thought to be sensitive to spatial baryon fluctuations at freeze-out.  
K. J. Sun, L. W. Chen, C. M. Ko, J. Pu and Z. Xu, Phys. Lett. B **781** (2018), 499-504
- Can be studied by coalescence in UrQMD.  
P. Hillmann, K. Käfer, JS, V. Vovchenko and M. Bleicher, J. Phys. G **49**, no.5, 055107 (2022)
- We see a very small enhancement in the scenario with a phase transition.
- Important to use realistic EoS with proper hadronic/nuclear matter.

