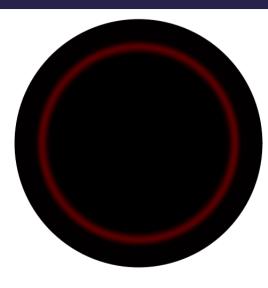
# Real time evolution of scalar fields in semiclassical gravity

Phys. Rev. D **105** (2022) no.10, 105010 [arXiv:2010.13215 [gr-qc]]

Jana N. Guenther, Christian Hölbling, Lukas Varnhorst

01. Dec. 2022





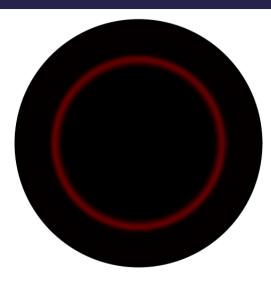
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Semiclassical gravity predicts Hawking radiation for late times.

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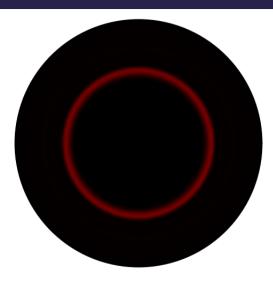
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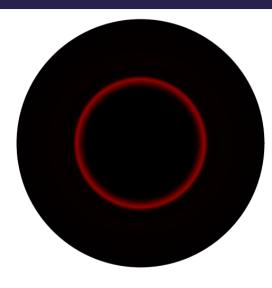
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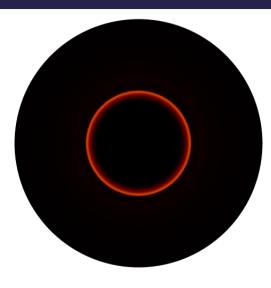
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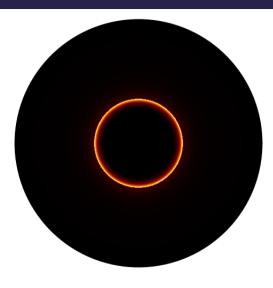
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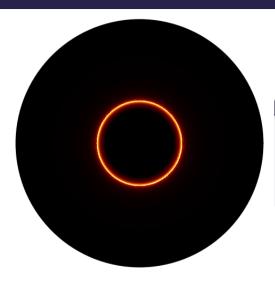
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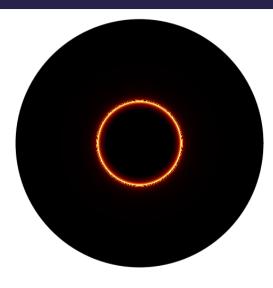
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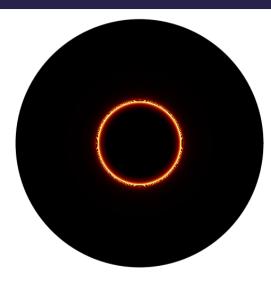
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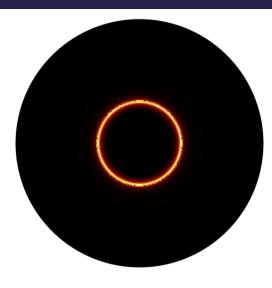
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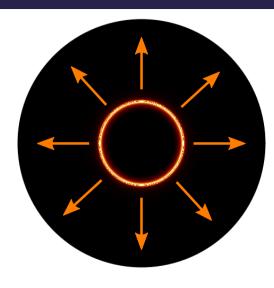
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# spherical harmonics

[1] M. W. Choptuik, "Universality and scaling in gravitational collapse of a massless scalar field," Phys. Rev. Lett.  $\bf 70~(1993), 9-12$ 

Semiclassical Einstein equation:

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = \langle \psi \mid T_{\mu\nu} \mid \psi \rangle$$

Choose state  $|\psi\rangle$  such that:

- Close to a classical state  $\rightarrow$  Coherent state.
- Expectation value is spherically symmetric.

Choose spherical symmetric coordinate system [1]

$$g_{\mu
u}=egin{pmatrix} lpha^2(t,r) & & & & & \ & -a^2(t,r) & & & & \ & & -r^2 & & \ & & & -r^2\cos^2 heta \end{pmatrix}$$

# Semiclassical approximation

Metric  $(a(t, r), \alpha(t, r))$  is classical, scalar field is fully quantum.

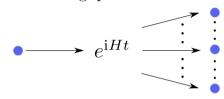
Scalar field has no self interaction  $\rightarrow$  Hamiltonian is quadratic.

Time evolution with constant metric does not change particle number.  $\rightarrow$  Full time evolution can be calculated.

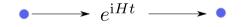
Still non-trivial effects by time dependend metric possible.

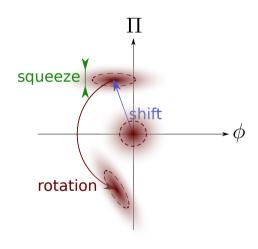
**Real time** evolution with **non-equilibrium dynamics** accessible via lattice calculations.

interacting quantum fields



semiclassical gravity





System can be understood in terms of gaussian states.

Gaussian states: State that can be written as

$$\exp(\mathrm{i}F)\mid 0\rangle$$

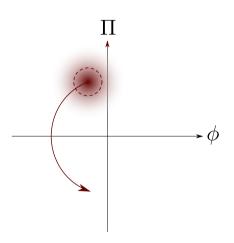
where  $| 0 \rangle$  is the ground state a harmonic Osz. and F is a quadratic function of  $a^{\dagger}$  and a.

Operation can be decomposed into

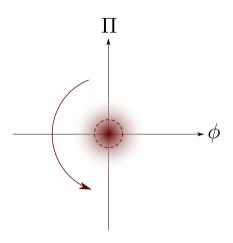
- shift
- rotation
- squeeze

State can be described by mean value  $\vec{\mu}$  and covariance matrix C.

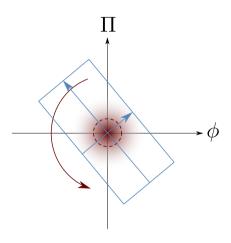
Formalism important in quatum optics.



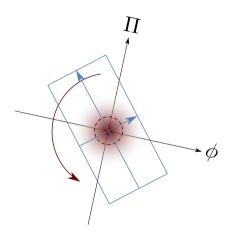
 Gaussian state parametrized by classical central value and covariance matrix



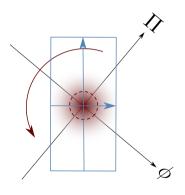
- Gaussian state parametrized by classical central value and covariance matrix
- Time evolution given by rigid rotation in phase space



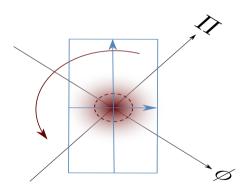
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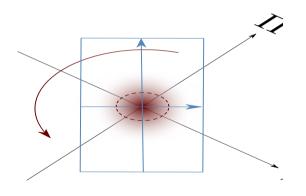
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- Evolution of metric → Change of the oscillator parameters
- Reinterpret same state in new oscillator basis



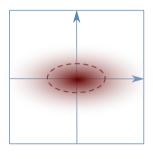
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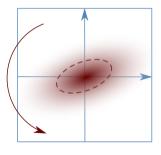
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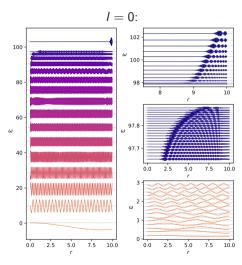


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- Gaussian state parametrized by classical central value and covariance matrix
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- Reinterpret same state in new oscillator basis
- System is in a squezed coherent state
- Field evolution not trivial

# Scalar field decomposition



Hamiltonian of the field can be written as

$$\mathcal{H} = \sum_{I=0}^{\infty} (2I+1) \left( rac{lpha a_0}{alpha_0} \Pi_I \Pi_I^\dagger + \phi_I^\dagger \sqrt{rac{alpha_0}{lpha a_0}} K \sqrt{rac{alpha_0}{lpha a_0}} \phi_I 
ight)$$

with

$$K = q^T q + \frac{I(I+1)}{r^2} \alpha^2$$

where

$$q = \sqrt{\frac{\alpha}{a}} r \partial_r \sqrt{\frac{\alpha}{a}} \frac{1}{r}$$

Eigenmodes decomposition:

$$K = V\omega^2 V^T$$

- V: Mode functions.
- $\omega$ : Mode frequency

# Phase space evolution

$$H=\Pi A\Pi^\dagger +\phi^\dagger A^{-\frac{1}{2}}KA^{-\frac{1}{2}}\phi=ec{x}^\dagger Mec{x} \quad x=\left(\Pi_1^\dagger \quad \Pi_2^\dagger \quad \dots \quad \phi_1 \quad \phi_2 \quad \dots \right)^T$$

Scalar field time evolution:  $\vec{\mu}(t+\Delta t)=S\vec{\mu}(t)$  and  $C(t+\Delta t)=SC(t)S^T$  where  $S=T^{-1}RT$ 

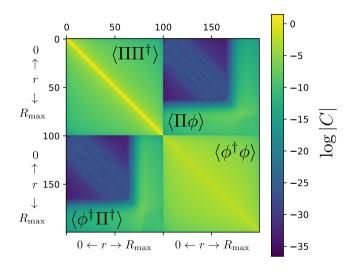
$$T = \begin{pmatrix} \frac{1}{\sqrt{\omega}} V^T \sqrt{A} & \\ & \sqrt{\omega} V^T \frac{1}{\sqrt{A}} \end{pmatrix} \quad A = \frac{\alpha a_0}{a \alpha_0}$$

$$R = \left(egin{array}{cccc} \cos(\omega_1 \Delta t) & & \sin(\omega_1 \Delta t) & & & & \\ & \cos(\omega_1 \Delta t) & & & \sin(\omega_1 \Delta t) & & & & \\ & & \ddots & & & & \ddots & & \\ -\sin(\omega_1 \Delta t) & & & \cos(\omega_1 \Delta t) & & & & \\ & & -\sin(\omega_1 \Delta t) & & & \cos(\omega_1 \Delta t) & & & & \\ & & & \ddots & & & \ddots & & \end{array}
ight)$$

- T transforms from position space to oscillator basis
- R is a rigid rotation in phase space for each oscillator

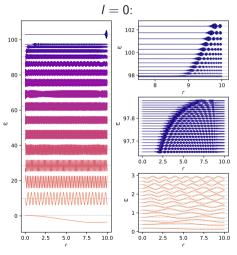
Metric change enters only through  $\,T\,$  and  $\,\omega\,$ 

#### Covariance matrix



- Covariance matrix contains full information of the state
- Blocks are the equal time correlation functions
- Entanglement is contained in that matrix

# Bogolyubov transformation



Alternative formulation: Write Hamiltonian as

$$\mathcal{H} = b_+ W_r b_+^{\dagger} + b_-^{\dagger} W_r b_- + b_+ X_r b_- + b_-^{\dagger} X_r b_+^{\dagger}.$$

 $b_{\pm}^{\dagger}/b_{\pm}$  are the creation/annihilation operators with frequencies  $\omega.$  In the Heisenberg picture:

$$b_{+}(t) = rac{1}{\sqrt{2}}(b_{u}(t) + b_{v}(t)) \quad b_{-}(t) = rac{1}{\sqrt{2}}(b_{u}^{\dagger}(t) - b_{v}^{\dagger}(t))$$

$$b_-^\dagger(t)=rac{1}{\sqrt{2}}(b_u(t)-b_v(t)) \quad b_+^\dagger(t)=rac{1}{\sqrt{2}}(b_u^\dagger(t)+b_v^\dagger(t))$$

$$b_u(t) = \frac{1}{\sqrt{2}}(b_+u(t) + b_i^{\dagger}u^*(t))V\sqrt{\omega}$$

$$b_u(t)=rac{1}{\sqrt{2}}(b_+v(t)-b_-^\dagger v^*(t))V\sqrt{\omega^{-1}}$$

 $\rightarrow$  Determine time evolution of u(t) and v(t).

# Bogolyubov transformation

Initialization:

$$u(0) = \frac{1}{\sqrt{\omega}} V^T$$
 and  $v(0) = \sqrt{\omega} V^T$ 

As long as the metric is constant, the time evolution can be solved exactly

$$egin{aligned} ig(u(t+\Delta t) & v(t+\Delta t)ig) = ig(u(t) & v(t)ig) \exp\left(-\mathrm{i}igg(egin{aligned} 0 & \sqrt{rac{\partial \alpha_0}{lpha \partial_0}} K\sqrt{rac{\partial \alpha_0}{lpha \partial_0}} \\ rac{\alpha \partial_0}{\partial lpha_0} & 0 \end{matrix}
ight) \Delta t \end{aligned}$$

Exponential can be explicitly evaluated by using SVD  $K = V\omega^2 V^T$ .

Time evolution is a Bogolyubov transformation.

1-to-1 mapping between covariance matrix C and Bogolyubov coefficients.

#### Metric evolution

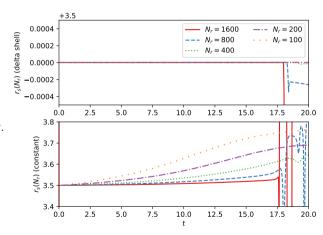
For integration of metric: Denstiy distribution of hamilton density must be defined.

Two choices:

- $lack \delta$ -distribution arround lattice points
- Constant between lattice points Both choices lead to regular behaviour.

Check validity of Birkhoff's theorem.

ightarrow Use  $\delta$  shells.



#### Metric evolution

$$g_{\mu
u} = egin{pmatrix} \hat{lpha} = lpha & \hat{lpha} = lpha a \ & -rac{r}{d} & \ & -r^2 & \ & & -r^2\cos^2 heta \end{pmatrix} \qquad egin{matrix} \hat{lpha} = lpha a \ & d = rac{r}{a^2} \ & \ln'(\hat{lpha}) = \langle\psi\mid h_r^0\mid\psi
angle \ & d'+dh_r^0 = 1-r\langle\psi\mid m_r\mid\psi
angle \end{pmatrix}$$

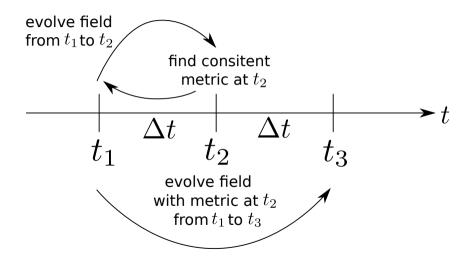
 $h_r^0$  and  $m_r$  are field operators:

$$\langle h_r^0 \rangle_{\psi} = \frac{1}{d^0 \hat{a}^0} \left( |I_{ur}|^2 + |I_{vr}|^2 + \sum_{l=0}^{\infty} (2l+1) \left( (v_l^{\dagger} v_l)_r r + (q^0 u_l^{\dagger} u_l q^{0T})_r r) \right) \right)$$

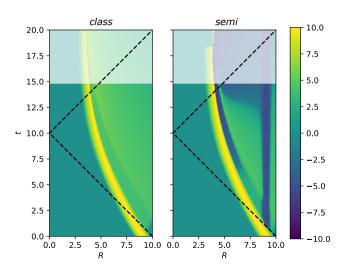
$$\langle m_r \rangle_{\psi} = \frac{d^0 \hat{\alpha}^0}{r^2} \sum_{l=0}^{\infty} (2l+1) \left( \frac{I(l+1)}{r^2} + M^2 \right) (u_l^{\dagger} u_l)_{rr}$$

- $|I_{ur}|^2 + |I_{vr}|^2$ : Classical contribution
- $u_l$ ,  $v_l$ : Coefficient of creation and anihilation operators
- $q^0 = \sqrt{\hat{\alpha} dr} \partial_r \sqrt{\hat{\alpha} dr^{-3}}$  Discretized "derivative"

#### Combined evolution



# I = 0 approximation



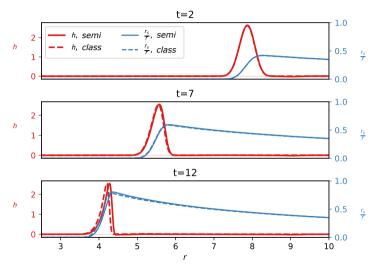
Consider only the I = 0 modes.

ightarrow Divergences of  $\langle T_{\mu\nu} \rangle_{\psi}$  can be cancelled by normal ordering

Back reaction effects can be included.

Horizon seems to form earlier due to quantum effects.

# I = 0 approximation

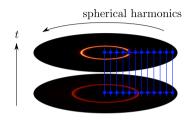


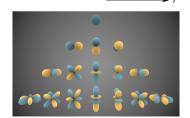
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Classically, l > 0 modes break spherical symmetry.

In the quantum case,  $\langle \psi \mid T_{\mu\nu} \mid \psi \rangle$  can be spherically symmetric even if I > 0 modes are excited.

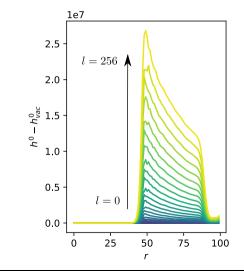
 $\rightarrow$  These modes must be included.

$$\mathcal{H} = \sum_{l=0}^{\infty} (2l+1) \left( \frac{\alpha a_0}{a \alpha_0} \Pi_l \Pi_l^{\dagger} + \phi_l^{\dagger} \sqrt{\frac{a \alpha_0}{\alpha a_0}} K \sqrt{\frac{a \alpha_0}{\alpha a_0}} \phi_l \right)$$

with

$$K = q^T q + \frac{I(I+1)}{r^2} \alpha^2$$

Additional divergence due to large / modes.



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Additional divergence due to large / modes.

## Divergence structure

Energy momentum tensor in curved space time can be calculated from the coincidence limit of the two-point function G(x, x').

For well behaved Hadamard states  $|\psi\rangle$ , the divergence structure is [1]

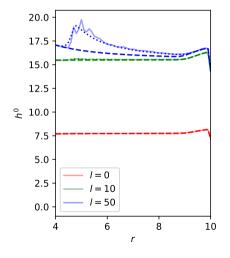
$$\lim_{x' \to x} \langle \psi \mid \textit{G}(\textbf{x}, \textbf{x}') \mid \psi \rangle = \frac{\textit{u}(\textbf{x}, \textbf{x}')}{\sigma(\textbf{x}, \textbf{x}')} + \textit{v}(\textbf{x}, \textbf{x}') \ln \sigma(\textbf{x}, \textbf{x}') + \textit{w}(\textbf{x}, \textbf{x}')$$

Here,  $\sigma(x, x')$  is the geodesic distance between x and x' and u(x, x'), v(x, x') are state-independent function that depend only on the metric and w(x, x') is regular.

How does that translate to the sum of angular / modes?

Can one use a 1/I expansion to relate them?  $\rightarrow$  Work in progress.

[1] S. A. Fulling, M. Sweeny and R. M. Wald, "Singularity Structure of the Two Point Function in Quantum Field Theory in Curved Space-Time," Commun. Math. Phys. **63** (1978), 257-264



Solid lines:  $h^0$  without subtraction.

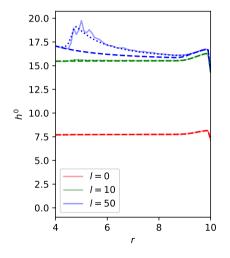
Dashed line: Normal ordering at t = 0.

Dotted line: Instantaneous normal ordering (Adiabatic approximation)

#### Approaches:

- Normal ordering at initial time
- Point splitting in  $\theta$  direction [1]
- Subtraction of adiabtic time evolution
- Subtracting the evolution with  $K = \frac{l(l+1)}{r^2}\alpha^2$

[1] A. Levi and A. Ori, "Mode-sum regularization of  $\langle \phi^2 \rangle$  in the angular-splitting method," Phys. Rev. D **94** (2016) no.4, 044054 [arXiv:1606.08451 [gr-qc]].



Solid lines:  $h^0$  without subtraction.

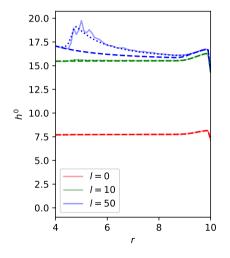
Dashed line: Normal ordering at t = 0.

Dotted line: Instantaneous normal ordering (Adiabatic approximation)

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- Point splitting in  $\theta$  direction [1]
- Subtraction of adiabtic time evolution
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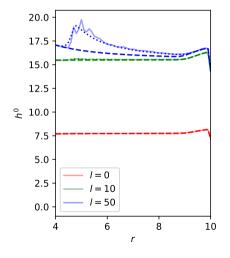
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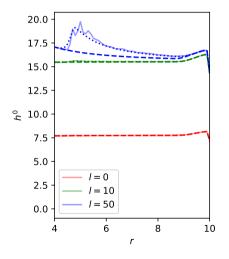
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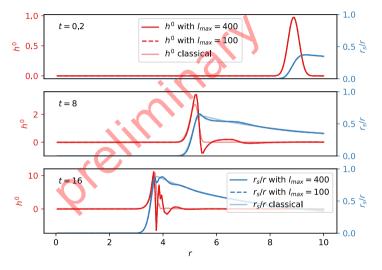
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#### Pauli-Villars fields



As suggested by [1], using Pauli-Villars fields with alternating signs and masses

$$m_2^2 + m_4^2 = m_1^2 + m_3^2 + m_5^2$$
  
 $m_2^4 + m_4^4 = m_1^4 + m_3^4 + m_5^4$ 

removes divergences for finite values of the masses.

Left side: 
$$m_1 = 1$$
.

[1] B. Berczi, P. M. Saffin and S. Y. Zhou, "Gravitational collapse of quantum fields and Choptuik scaling," JHEP **02** (2022), 183 doi:10.1007/JHEP02(2022)183 [arXiv:2111.11400 [hep-th]].

#### Conclusion

- Free scalar field evolution can be solved exactly in a static metric.
- In varying metric a leap-frog-like algorithm allows to determine the evolution.
- In the I=0 approximation, the back reaction can be calculated.
- Including higher I modes is work in progress, preliminary results with Pauli-Villars regularization.

# Thank you!