

Review on Hadron Spectroscopy

Frank Nerling

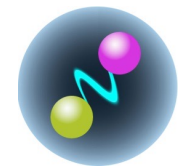
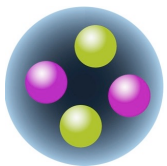
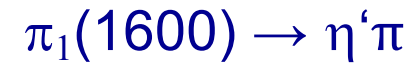
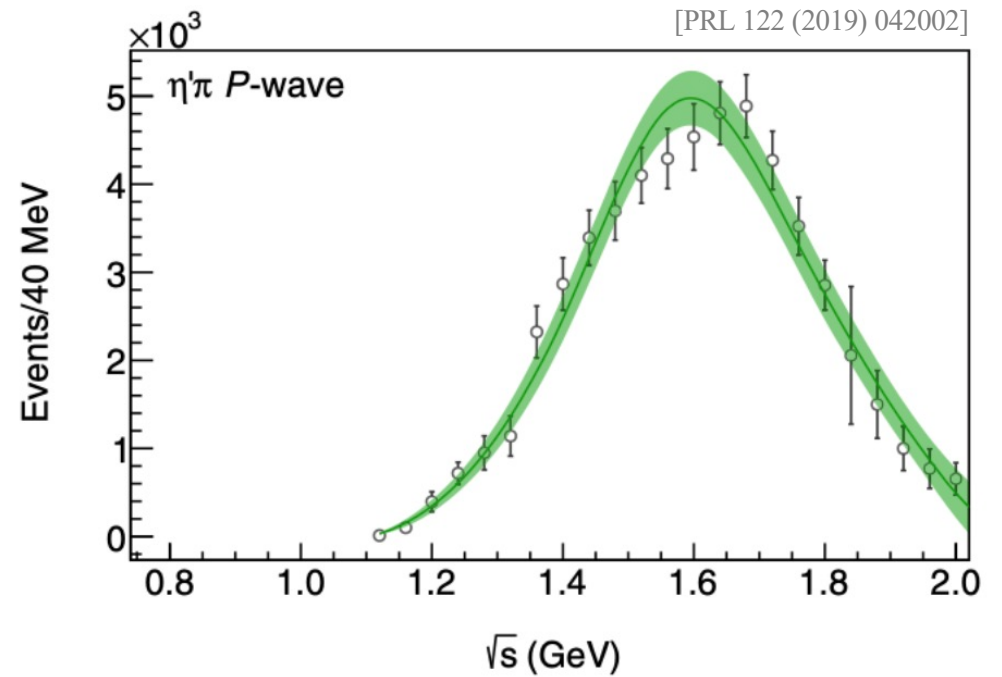
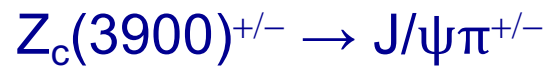
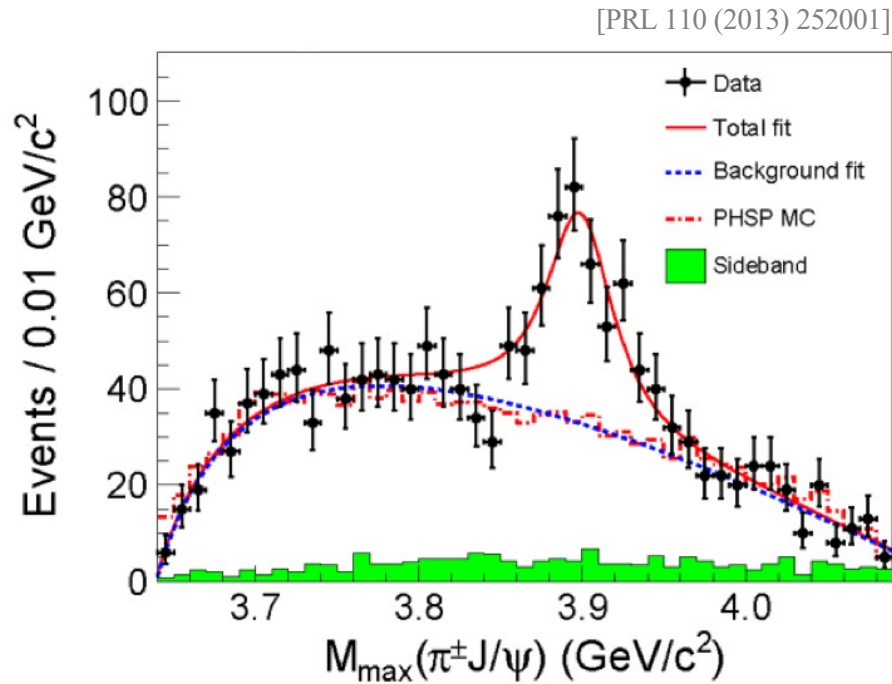
HFHF, GU Frankfurt & GSI Darmstadt

10th International Symposium on Non-equilibrium Dynamics –
NED2024, Krabi, Thailand, Nov 25th - 29th 2024

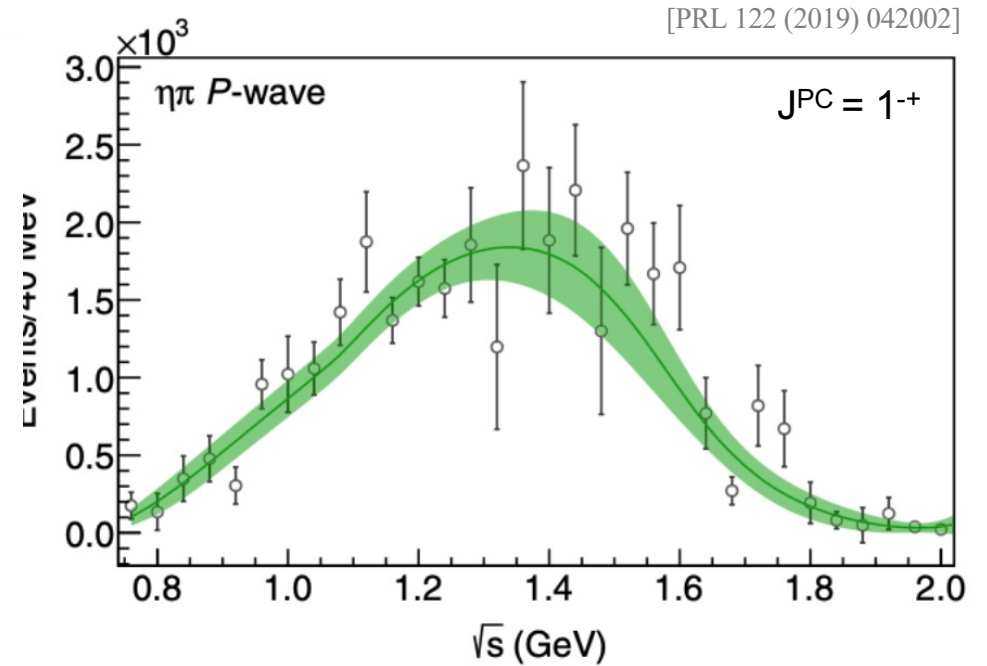
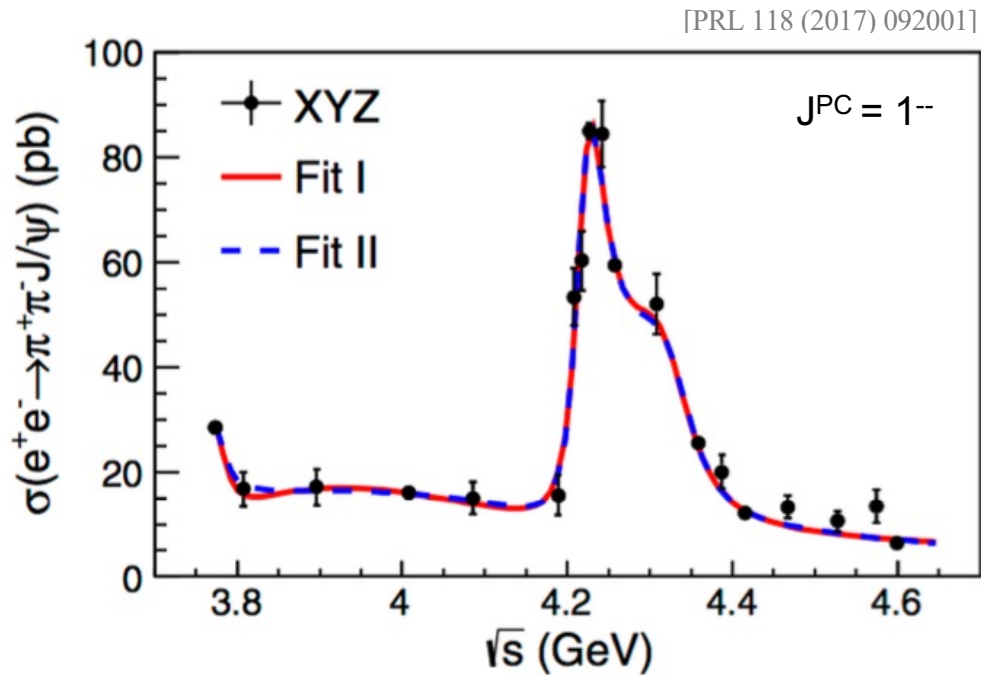
Outline

- **Introduction: From cosmic rays to hadrons**
- **The powerful Quark Model and QCD**
- **A selection of recent results at BESIII**
 - Supernumerary vector Y states
 - Manifestly exotic Z_c states)
 - The X(3872) and other X states
- **Ongoing analysis at GlueX:**
 - Search for the Y(2175) in photoproduction
- **Summary & prospectives**

Recent hot topics



Recent hot topics

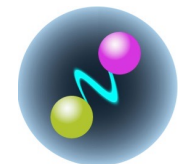
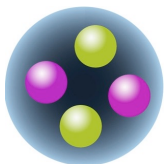


$$Z_c(3900)^{+/-} \rightarrow J/\psi \pi^{+/-}$$

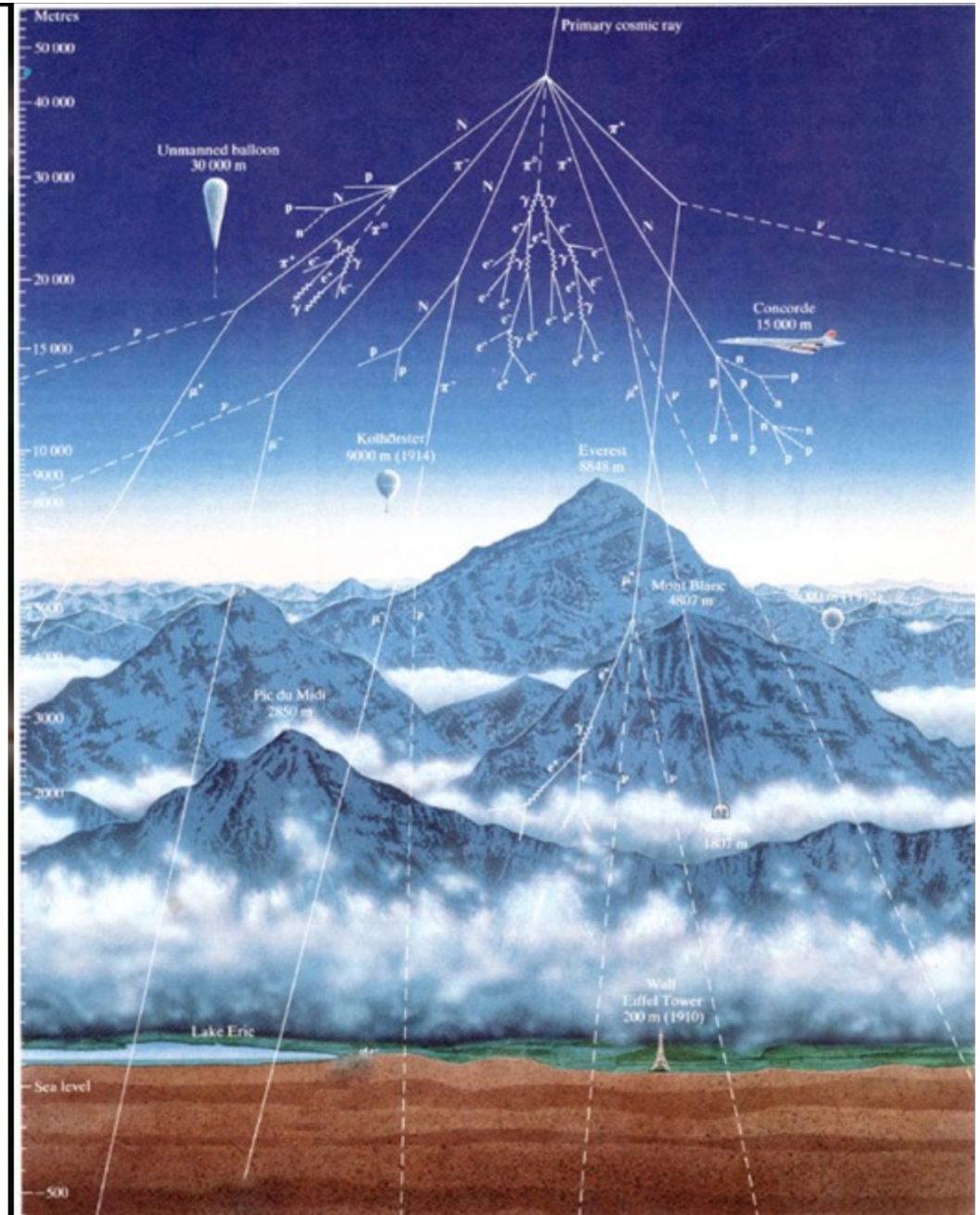
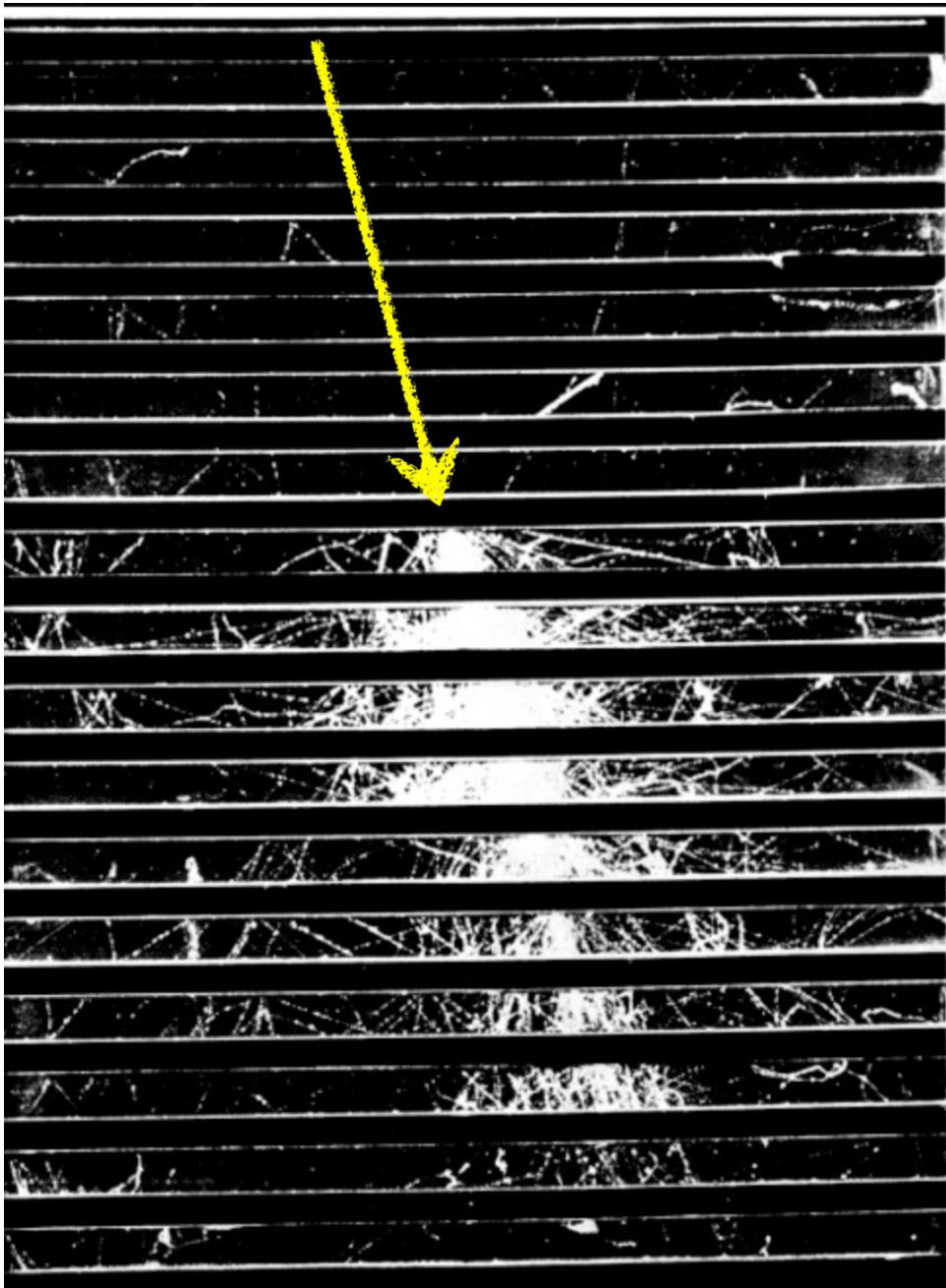
$$Y(4230) \rightarrow J/\psi \pi^+ \pi^-$$

$$\pi_1(1600) \rightarrow \eta' \pi$$

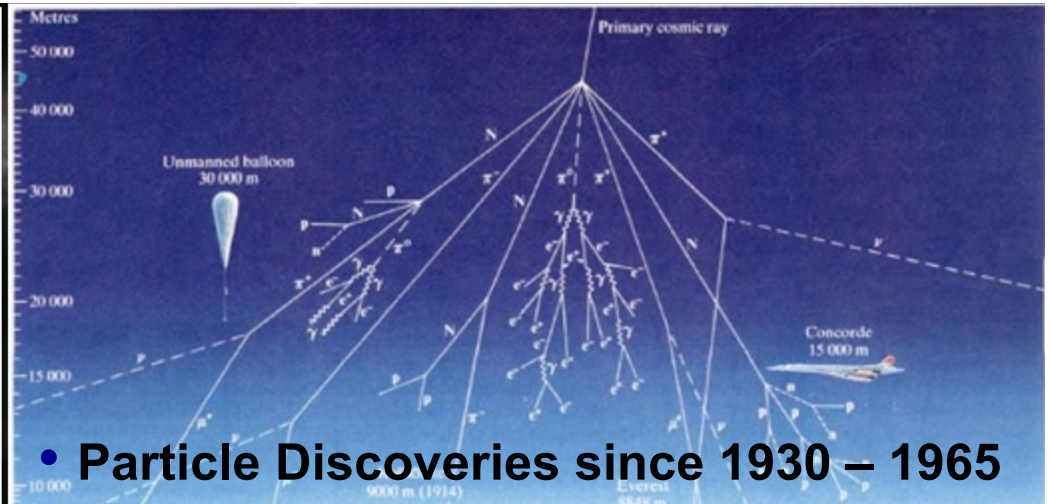
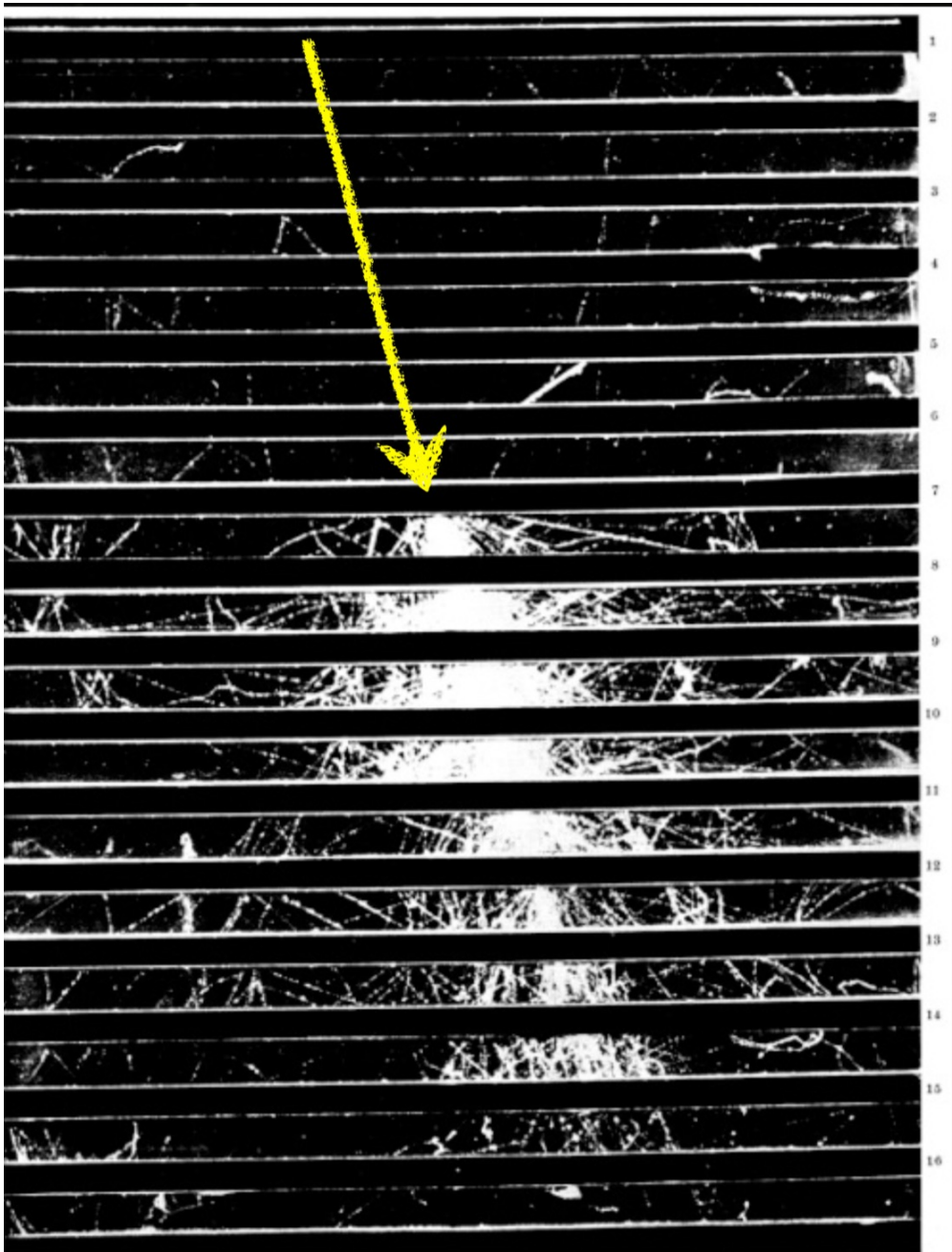
$$\pi_1(1400) = \pi_1(1600) \rightarrow \eta \pi$$



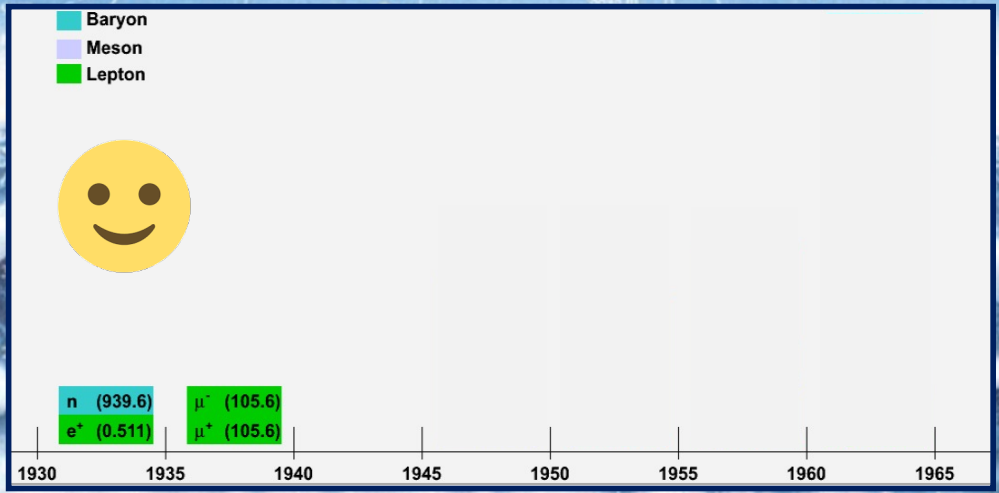
Extensive air showers (1938)



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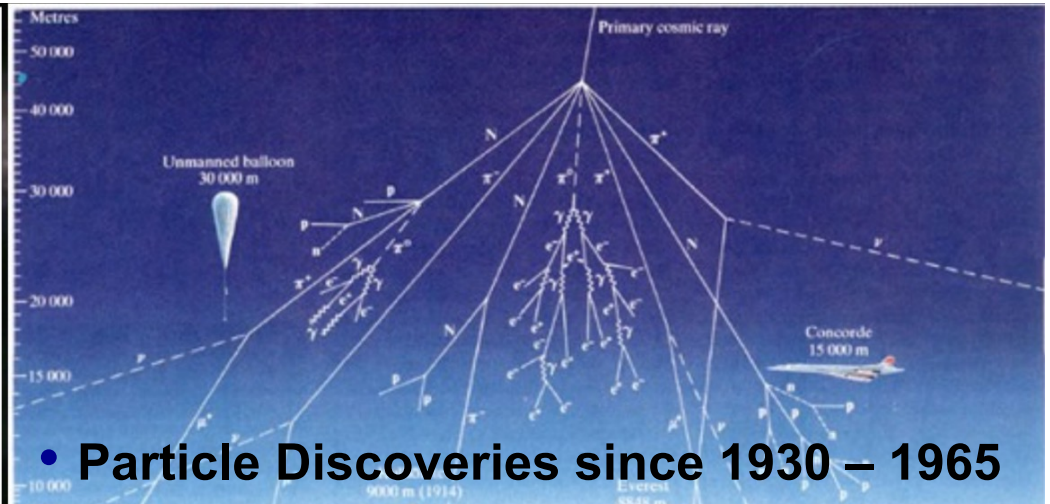
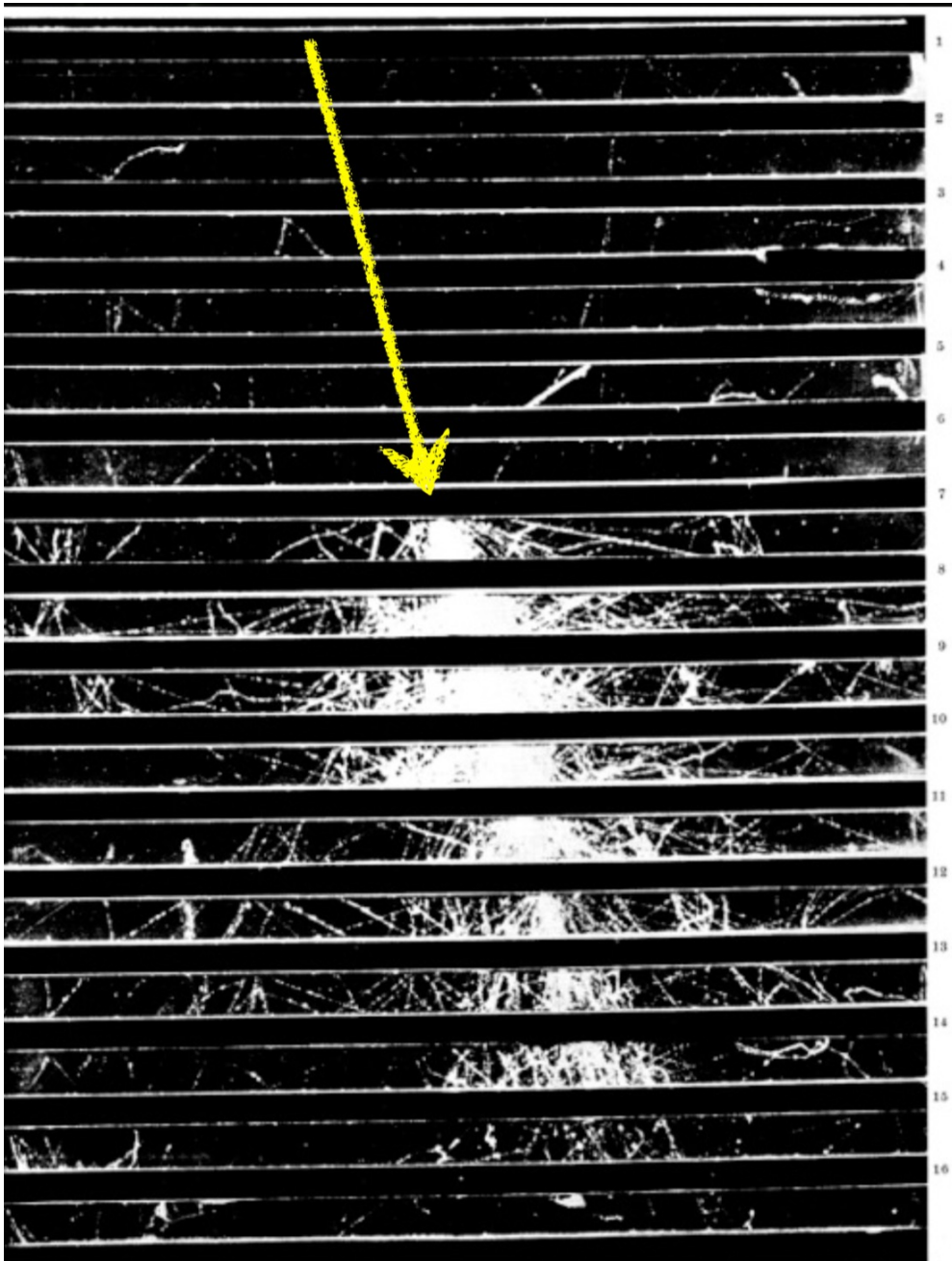
• Particle Discoveries since 1930 – 1965



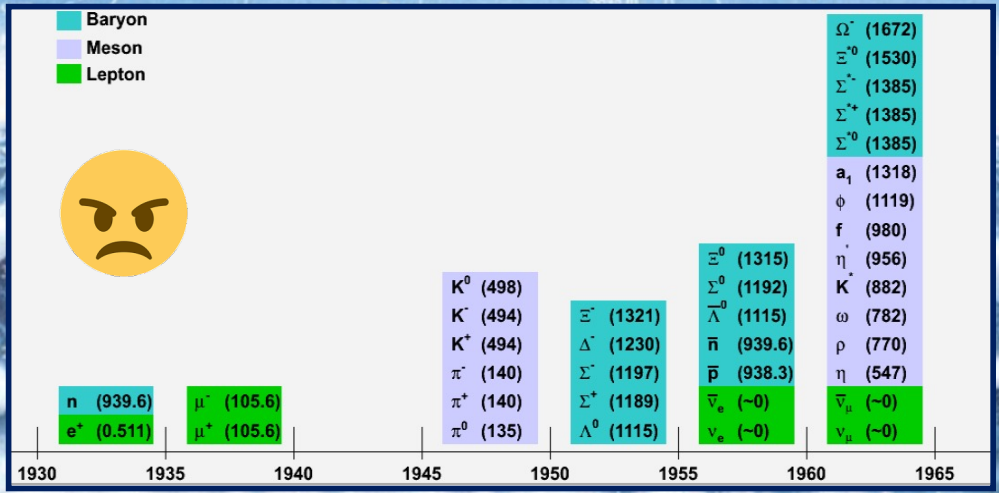
• Since then it got more and more ...



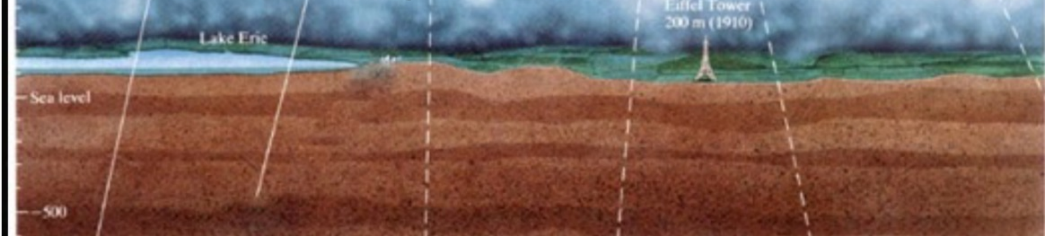
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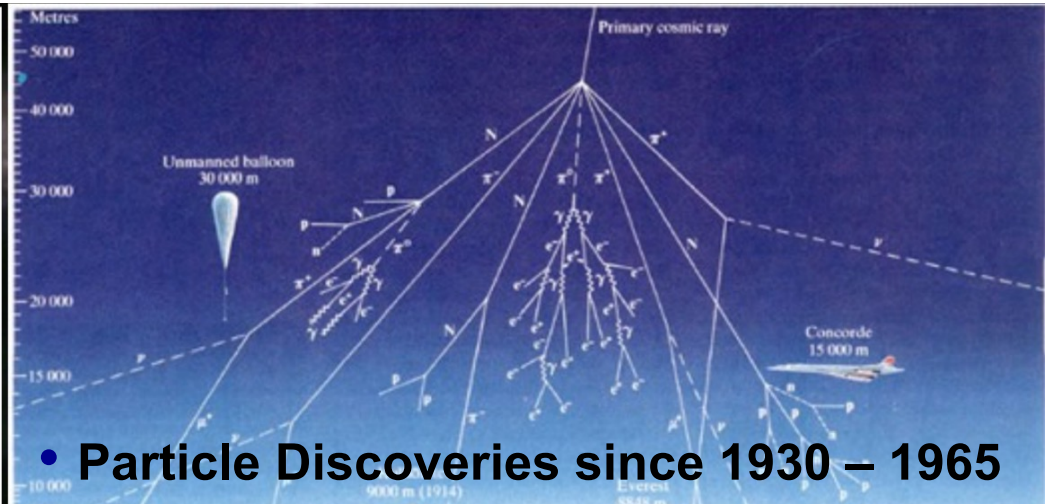
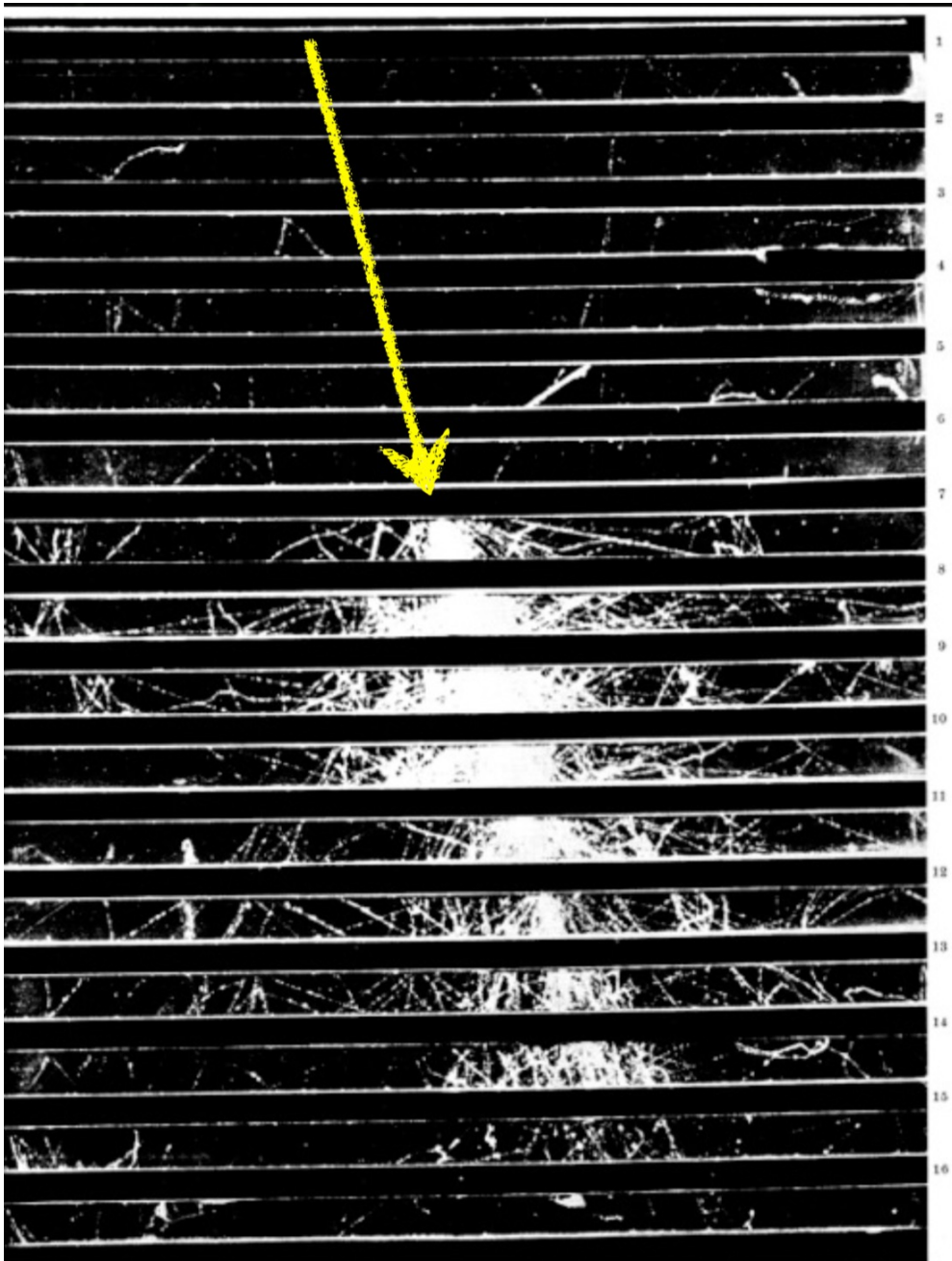
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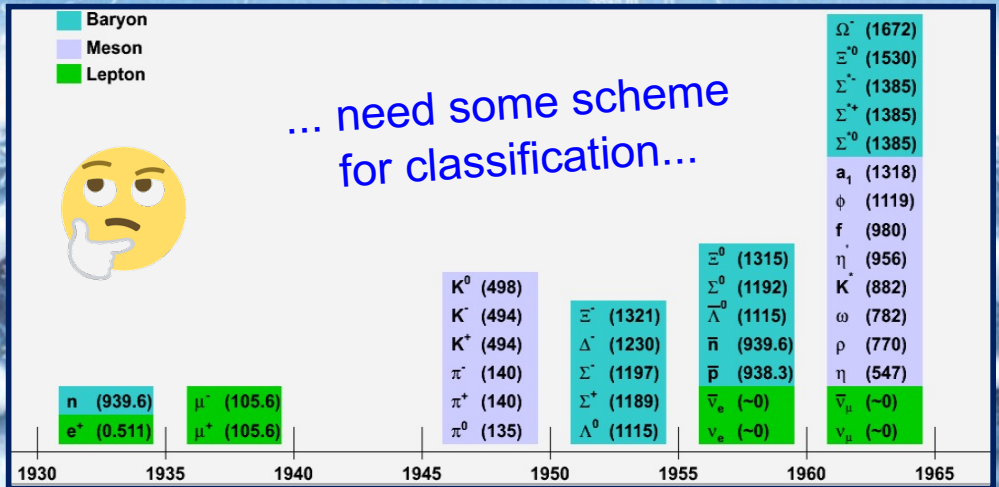
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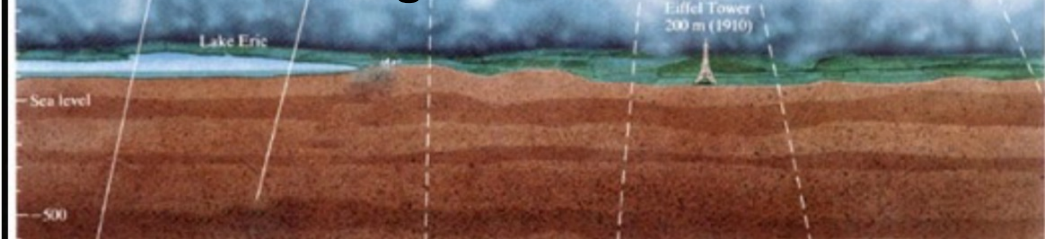
Extensive air showers (1938)



• Particle Discoveries since 1930 – 1965



• Since then it got more and more ...





1964



Volume 8, number 3

PHYSICS LETTERS

1 February 1964

A SCHEMATIC MODEL OF BARYONS AND MESONS *

M. GELL-MANN

California Institute of Technology, Pasadena, California

Received 4 January 1964

...

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon b if we assign to the triplet t the following properties: spin $\frac{1}{2}$, $z = -\frac{1}{3}$, and baryon number $\frac{1}{3}$. We then refer to the members $u^{\frac{2}{3}}$, $d^{-\frac{1}{3}}$, and $s^{-\frac{1}{3}}$ of the triplet as "quarks" q and the members of the anti-triplet as anti-quarks \bar{q} . Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqq\bar{q}\bar{q})$ etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc. It is assumed that the lowest baryon configuration (qqq) gives just the representations 1, 8, and 10 that have been observed, while

8419/TH.412

21 February 1964

AN SU_3 MODEL FOR STRONG INTERACTION SYMMETRY AND ITS BREAKING

II *)

G. ZWEIF

CERN---Geneva

*) Version I is CERN preprint 8182/TH.401, Jan. 17, 1964.

...

6) In general, we would expect that baryons are built not only from the product of three aces, AAA , but also from $\bar{A}AAAA$, $\bar{A}AAAAA$, etc., where \bar{A} denotes an anti-ace. Similarly, mesons could be formed from $\bar{A}A$, $\bar{A}AAA$ etc. For the low mass mesons and baryons we will assume the simplest possibilities, $\bar{A}A$ and AAA , that is, "deuces and treys".

PHYSICAL REVIEW D

VOLUME 15, NUMBER 1

1 JANUARY 1977

Multiquark hadrons. I. Phenomenology of $Q^2\bar{Q}^2$ mesons*

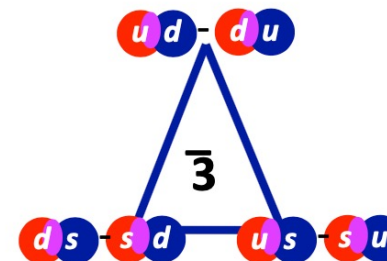
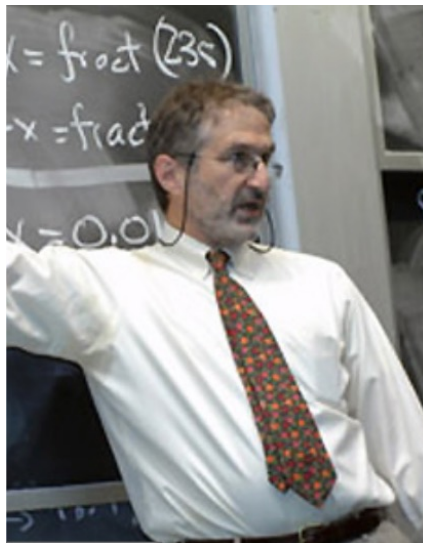
R. J. Jaffe[†]

Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305

and Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139

(Received 15 July 1976)

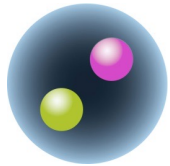
The spectra and dominant decay couplings of $Q^2\bar{Q}^2$ mesons are presented as calculated in the quark-bag model. Certain known 0^+ mesons [$\epsilon(700), S^*, \delta, \kappa$] are assigned to the lightest cryptoexotic $Q^2\bar{Q}^2$ nonet. The usual quark-model 0^+ nonet ($Q\bar{Q} L=1$) must lie higher in mass. All other $Q^2\bar{Q}^2$ mesons are predicted to be broad, heavy, and usually inelastic in formation processes. Other $Q^2\bar{Q}^2$ states which may be experimentally prominent are discussed.



Antisymmetric in:
color
flavor
spin ($S=0$)

Simple Quark model

- Mesons: Color neutral $q\bar{q}$ systems



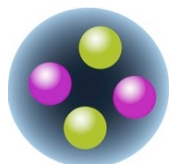
Conventional ($q\bar{q}$)

QCD

- Meson states beyond $q\bar{q}$



Hybrid ($q\bar{q}$)g

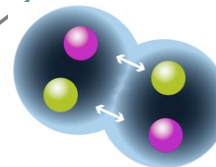


Tetraquark ($q\bar{q}q\bar{q}$)

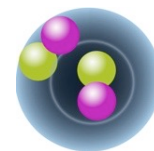


Glue-ball (gg) or (ggg)

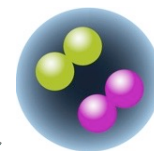
Alternative 4-quark configurations:



Molecule ($q\bar{q}$)($q\bar{q}$)



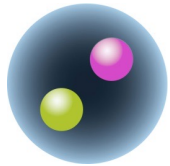
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Di-quarkonium (qq)($q\bar{q}$)

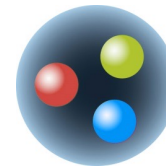
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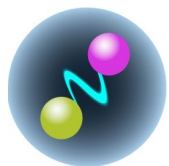
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- Baryons: $(qqq) / (\bar{q}\bar{q}\bar{q})$

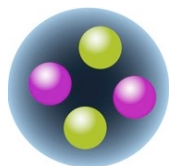


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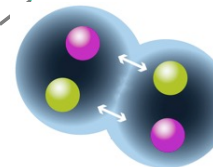


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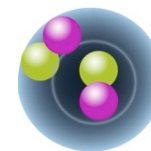


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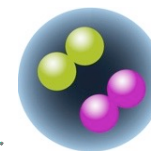
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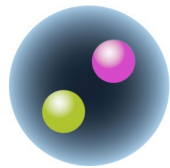
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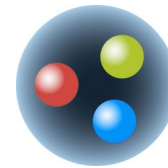
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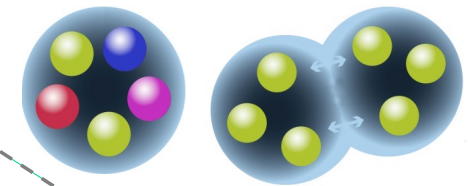


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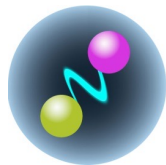


Lead to further alternative multi-quark configurations:

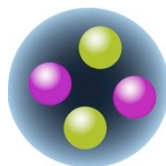


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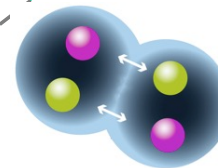


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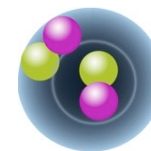


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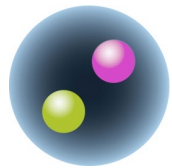
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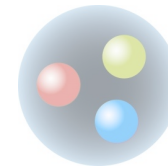
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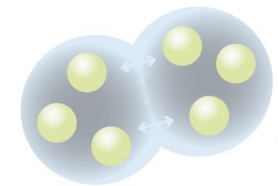
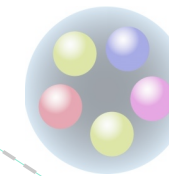


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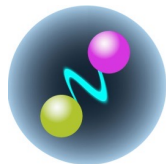


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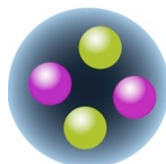


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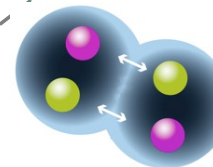
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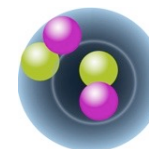
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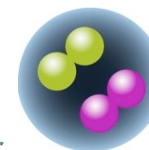
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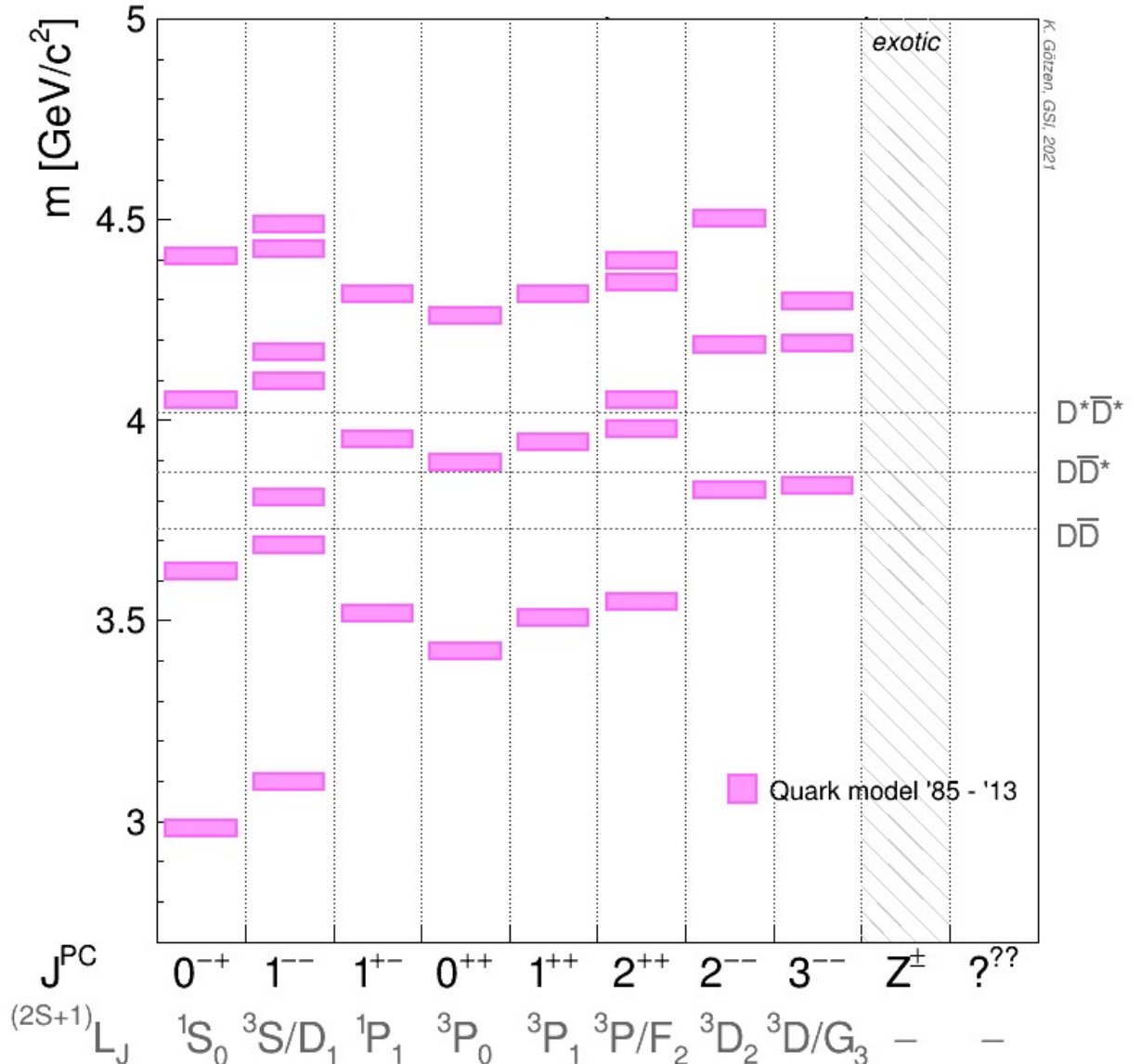
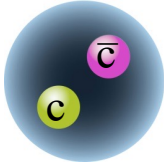
Hadro-quarkonium ($Q\bar{Q}$)($q\bar{q}$)



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Alternative 4-quark configurations:

Charmonium spectrum ($c\bar{c}$)



Potential model:

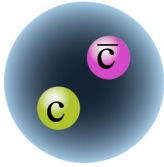
$$V_0^{c\bar{c}} = -\frac{4}{3} \frac{\alpha_s}{r} + br + \frac{32\pi\alpha_s}{9m_c^2} \delta(r) \vec{S}_c \vec{S}_{\bar{c}}$$

$$V_{\text{spin-dep.}} = \frac{1}{m_c^2} \left[\left(\frac{2\alpha_s}{r^3} - \frac{b}{2r} \right) \vec{L} \cdot \vec{S} + \frac{4\alpha_s}{r^3} T \right]$$

+ relativistic corrections!

[Godfrey & Isgur, PRD 32 (1985) 189]

[Barnes, Godfrey & Swanson, PRD 72 (2005) 054026]



- Before 2003:
 - Good agreement between theory and experiment, particularly beneath open charm thresholds

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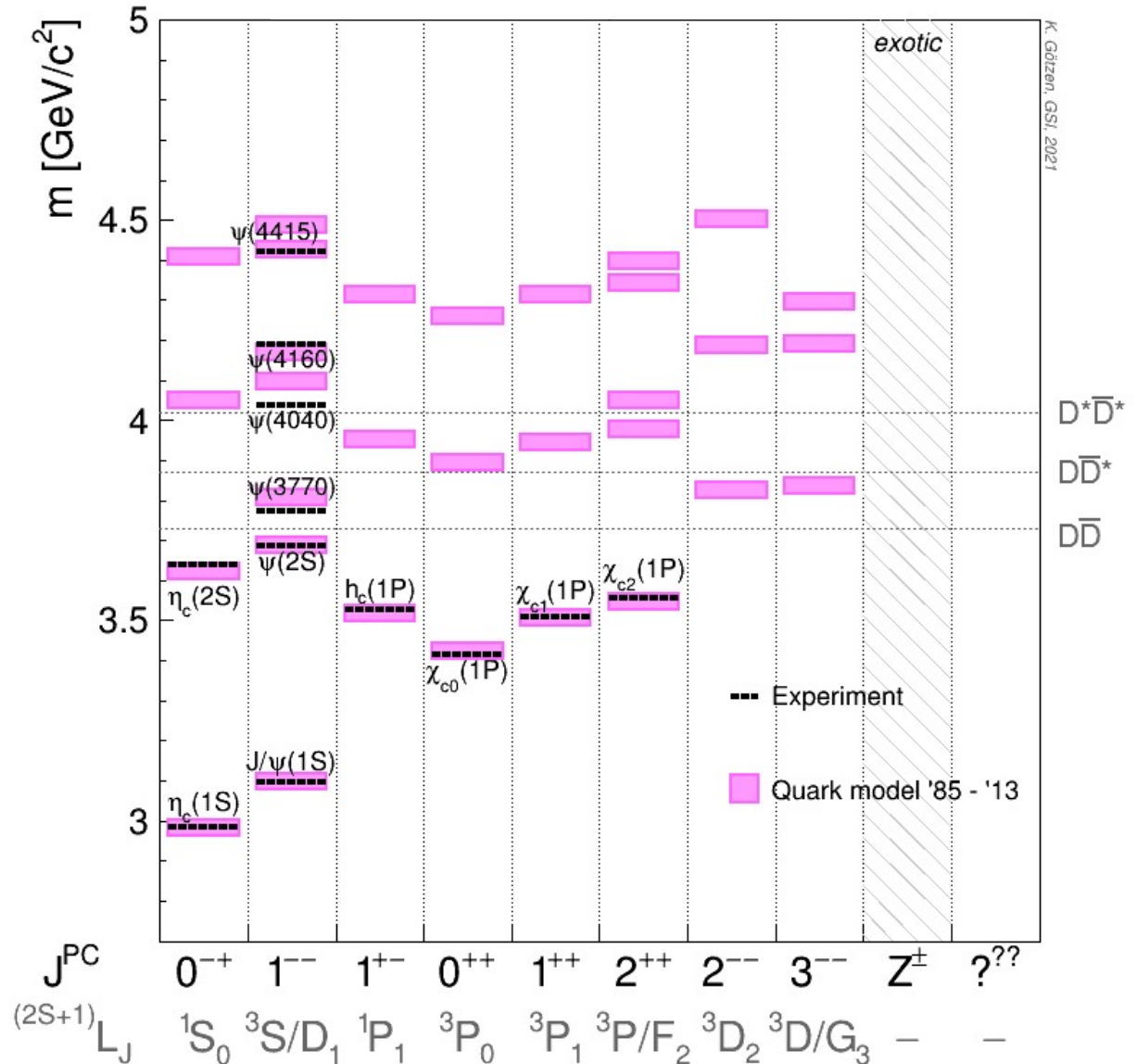
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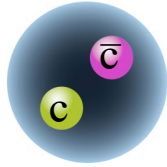
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Charmonium spectrum ($c\bar{c}$)



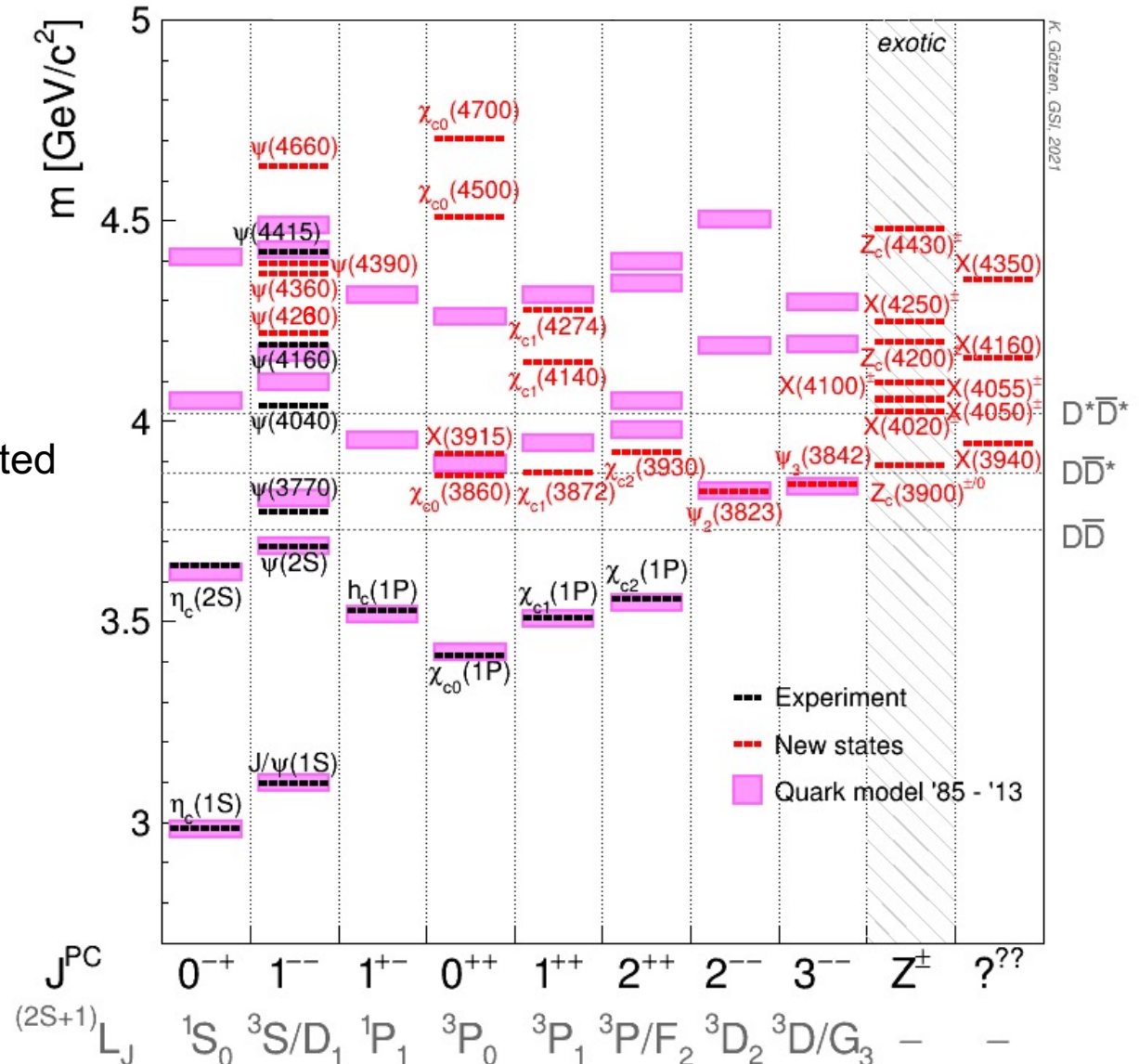
- Before 2003:
 - Good agreement between theory and experiment, particularly beneath open charm thresholds
- After 2003:
 - Severe mismatch between predicted and observed spectrum

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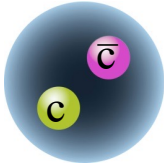
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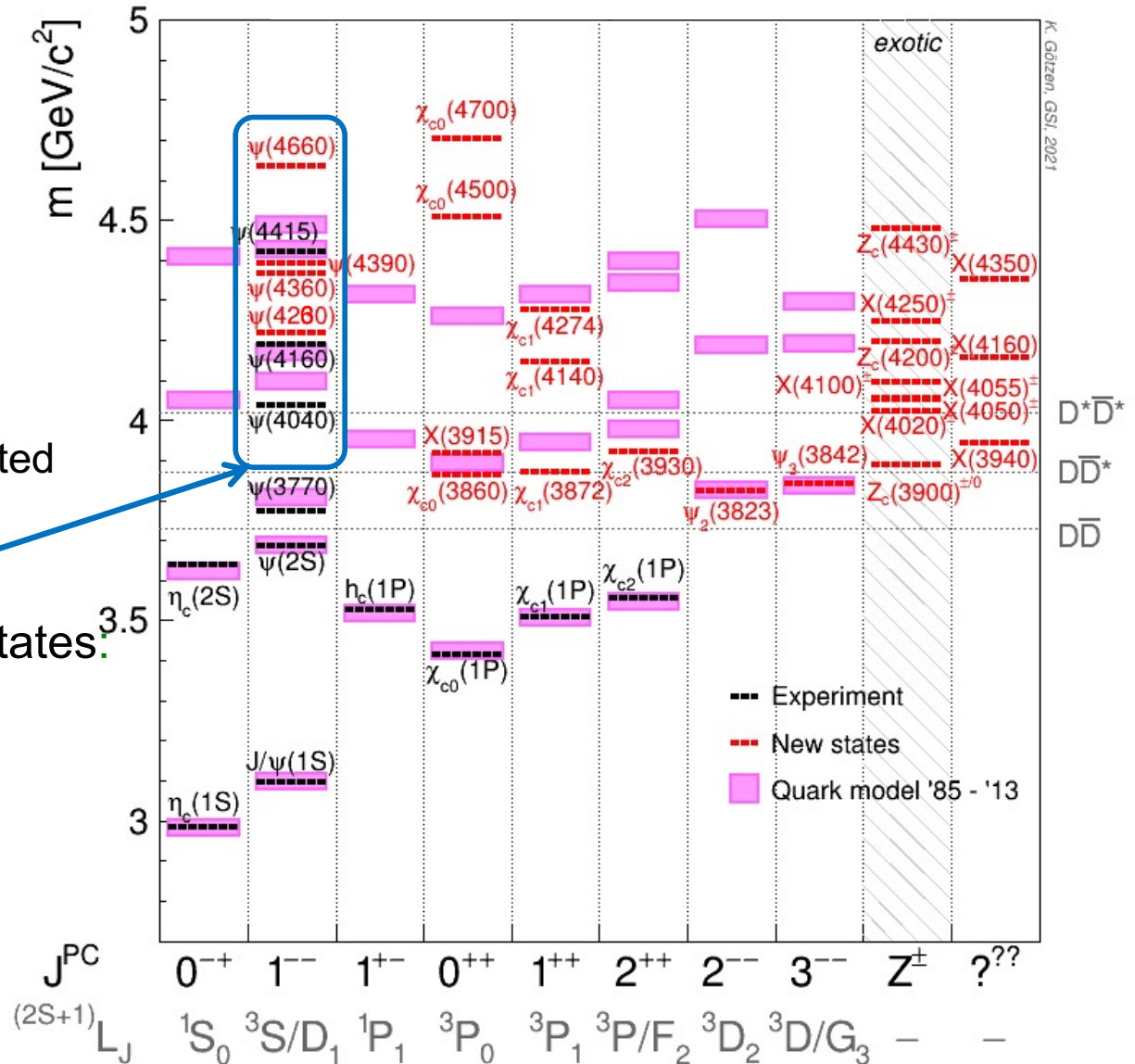
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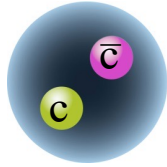
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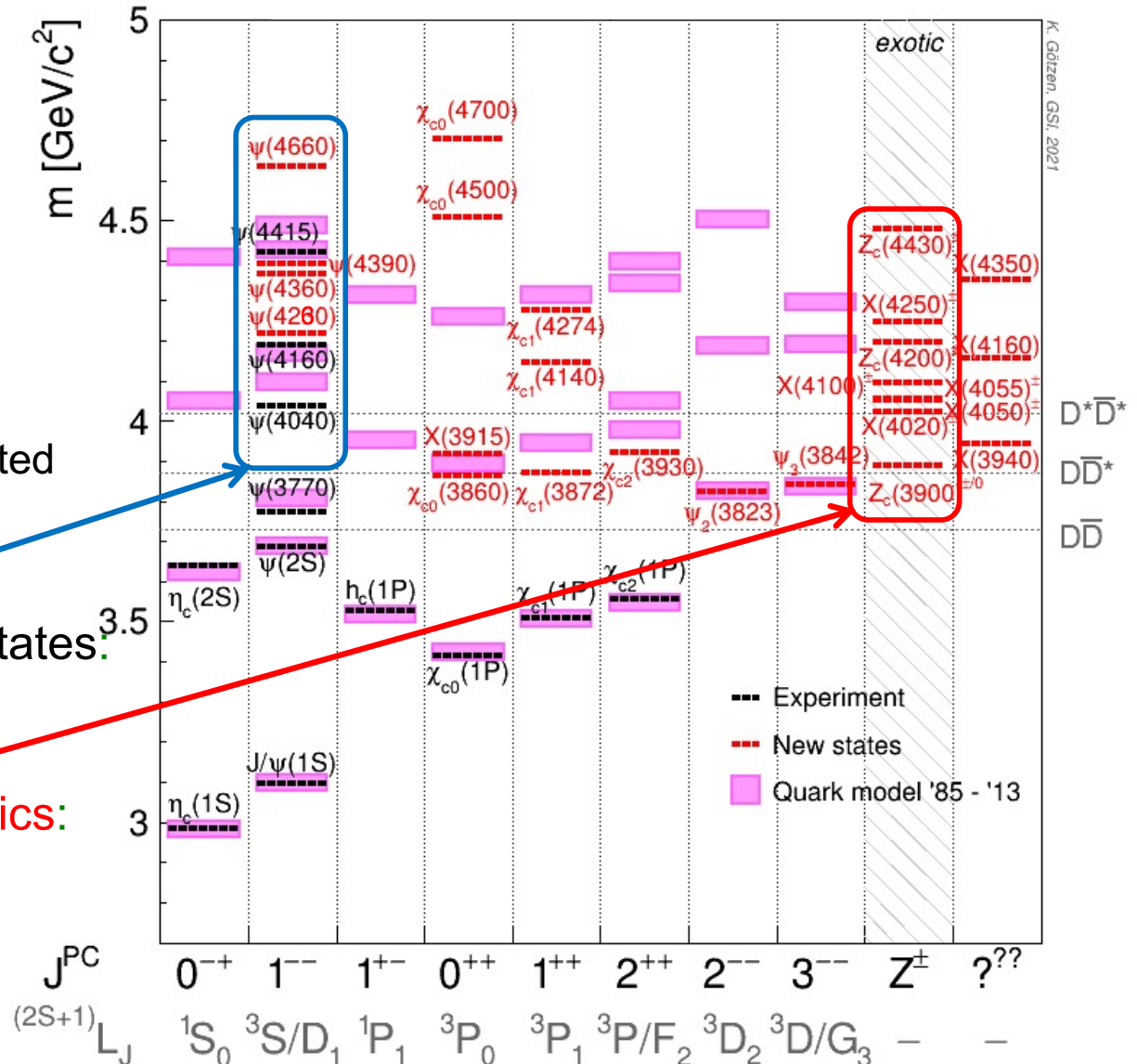
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- Several supernumerary vector states:
Y(4260), ..., Y(4660)

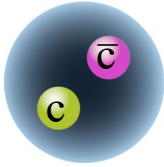


Charmonium spectrum ($c\bar{c}$)

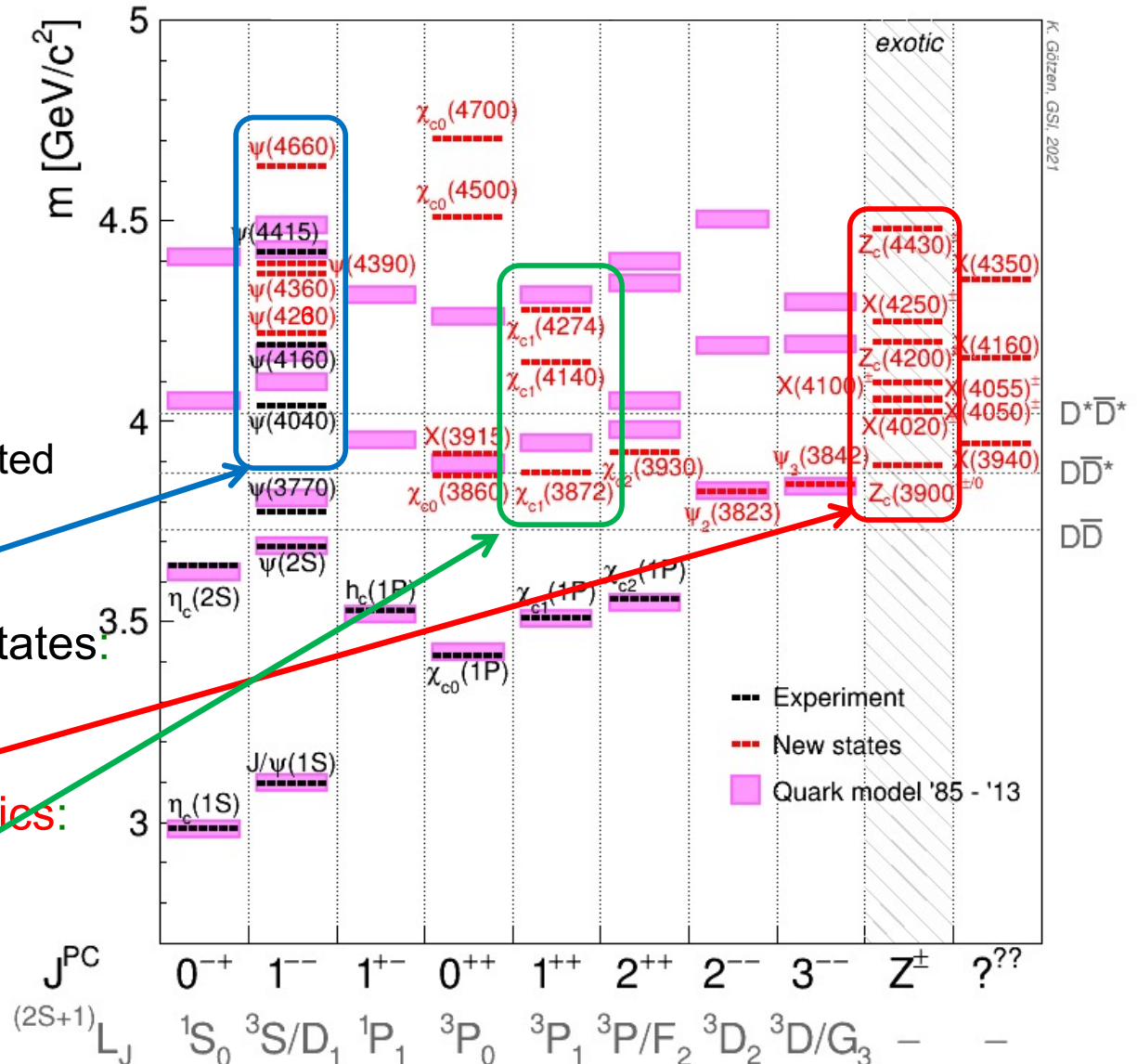


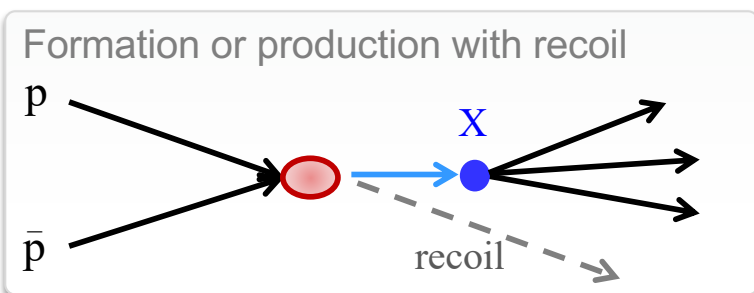
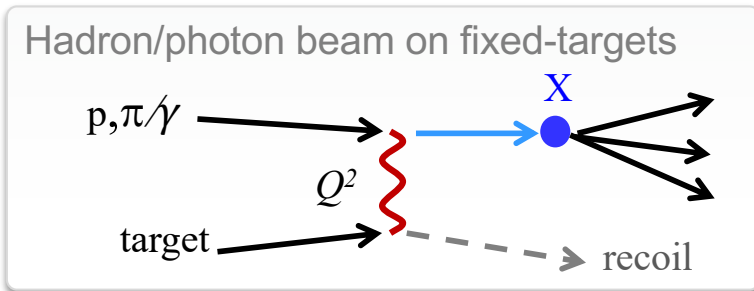
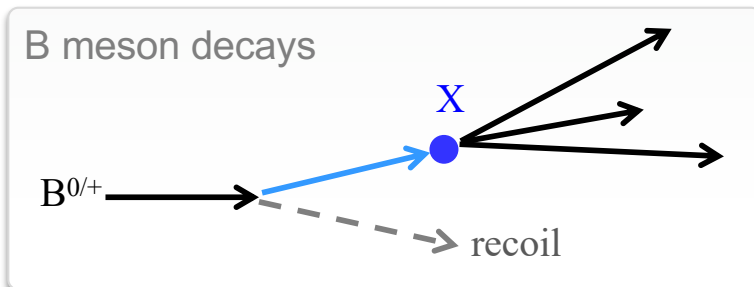
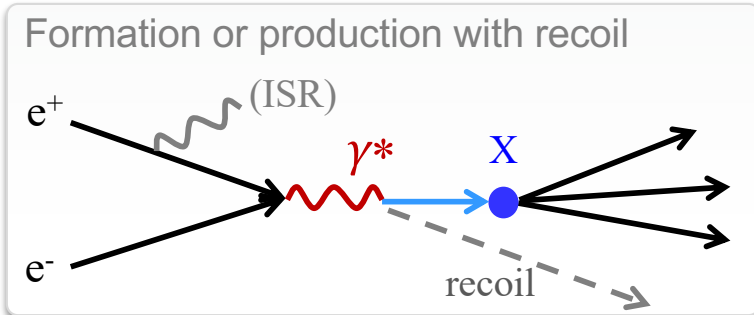
- Before 2003:
 - Good agreement between theory and experiment, particularly beneath open charm thresholds
- After 2003:
 - Severe mismatch between predicted and observed spectrum
- Several supernumerary vector states: $Y(4260), \dots, Y(4660)$
- Several charged manifestly exotics: $Z_c(3900)^{+/-}, \dots, Z_c(4430)^{+/-}$





- Before 2003:
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- Several supernumerary vector states: $Y(4260)$, ..., $Y(4660)$
- Several charged manifestly exotics: $Z_c(3900)^{+/-}$, ..., $Z_c(4430)^{+/-}$
- The X states – the $X_{c1}(3872)$ was the first observed in 2003



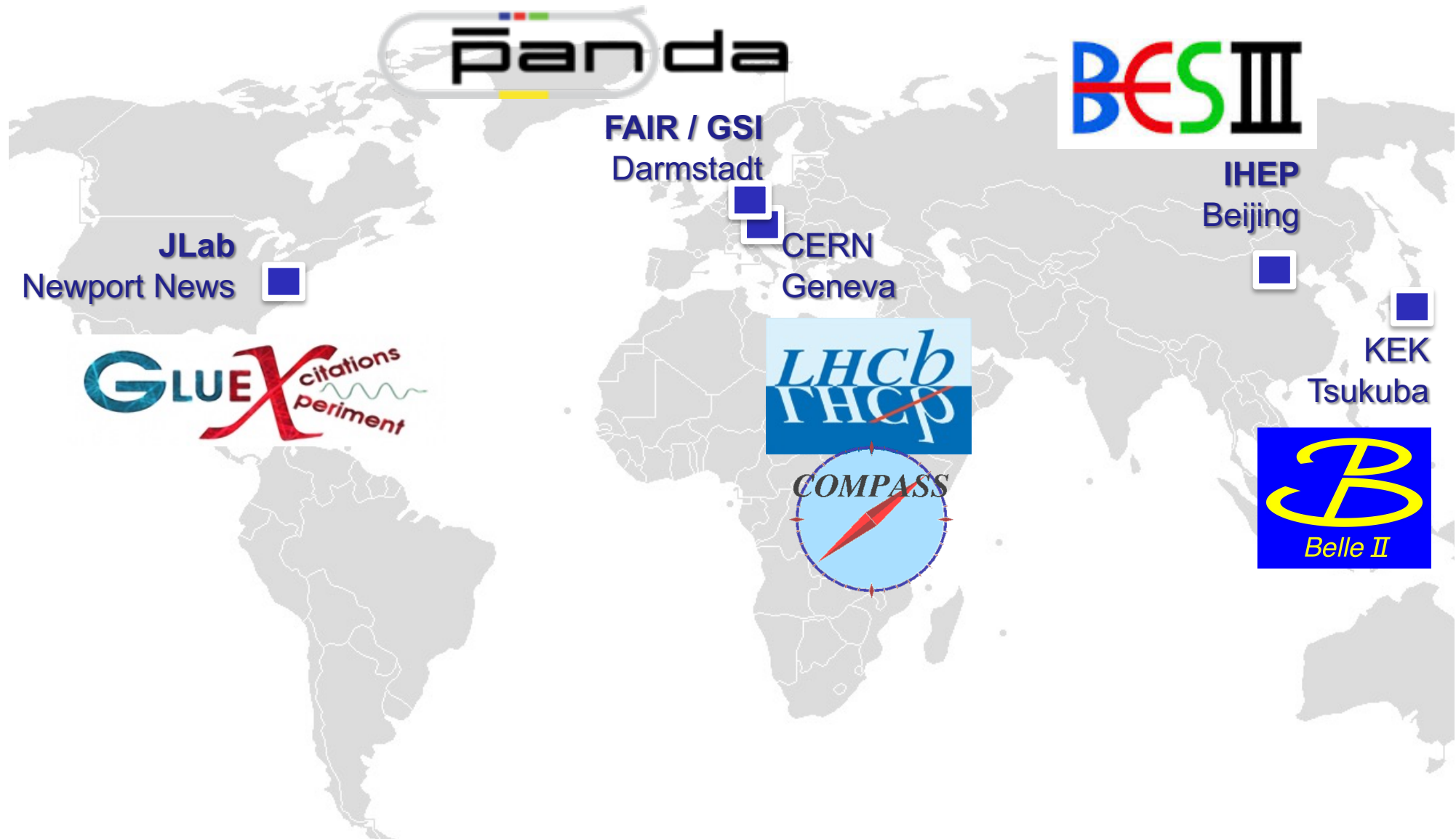


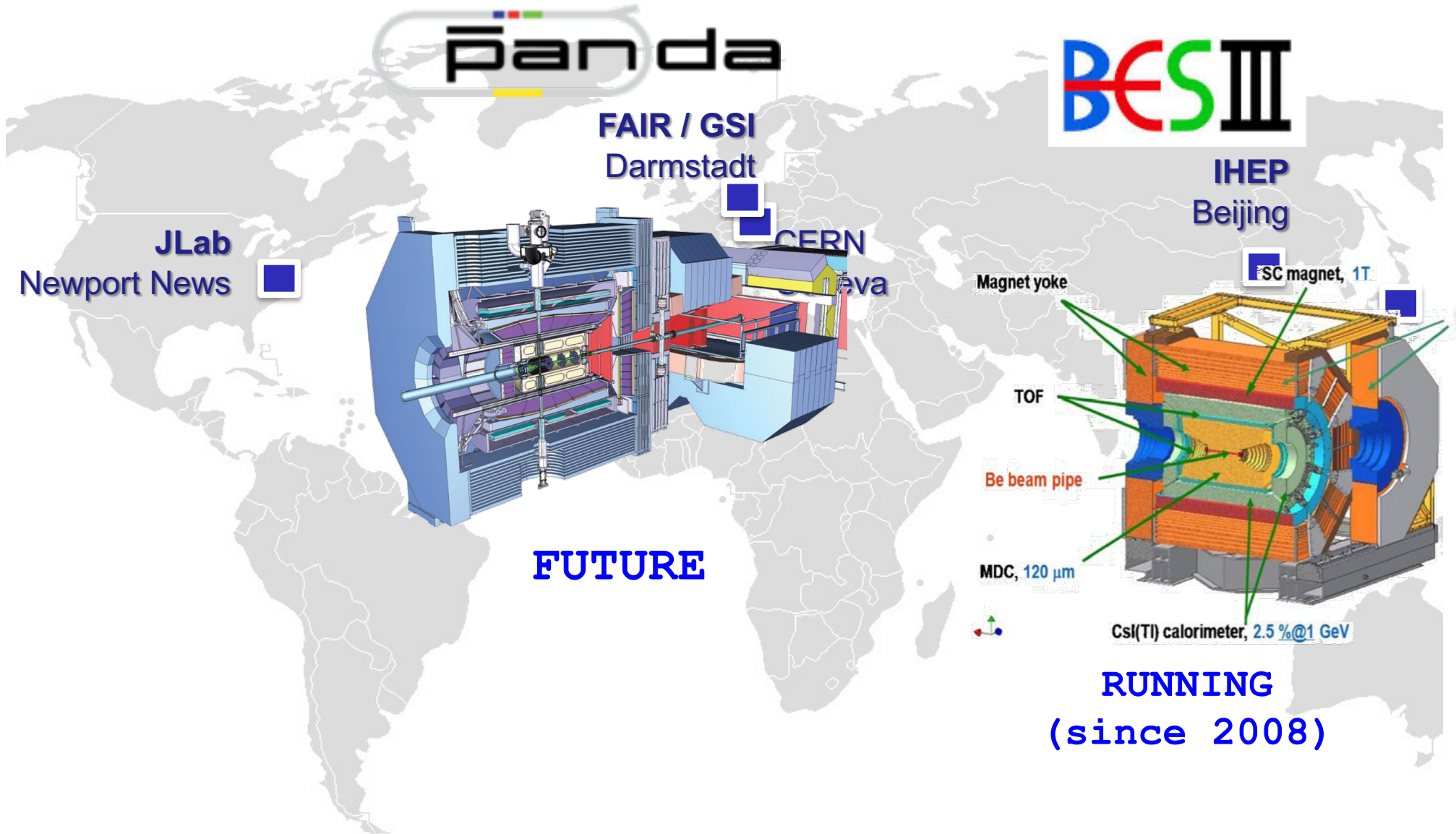
- Formation & Production with recoil particle(s)
 - CLEO(-c), BaBar, Belle(II) ($E_{\text{cms}} \leq 12$ GeV)
 - BESIII ($E_{\text{cms}} \leq 4.9$ GeV)

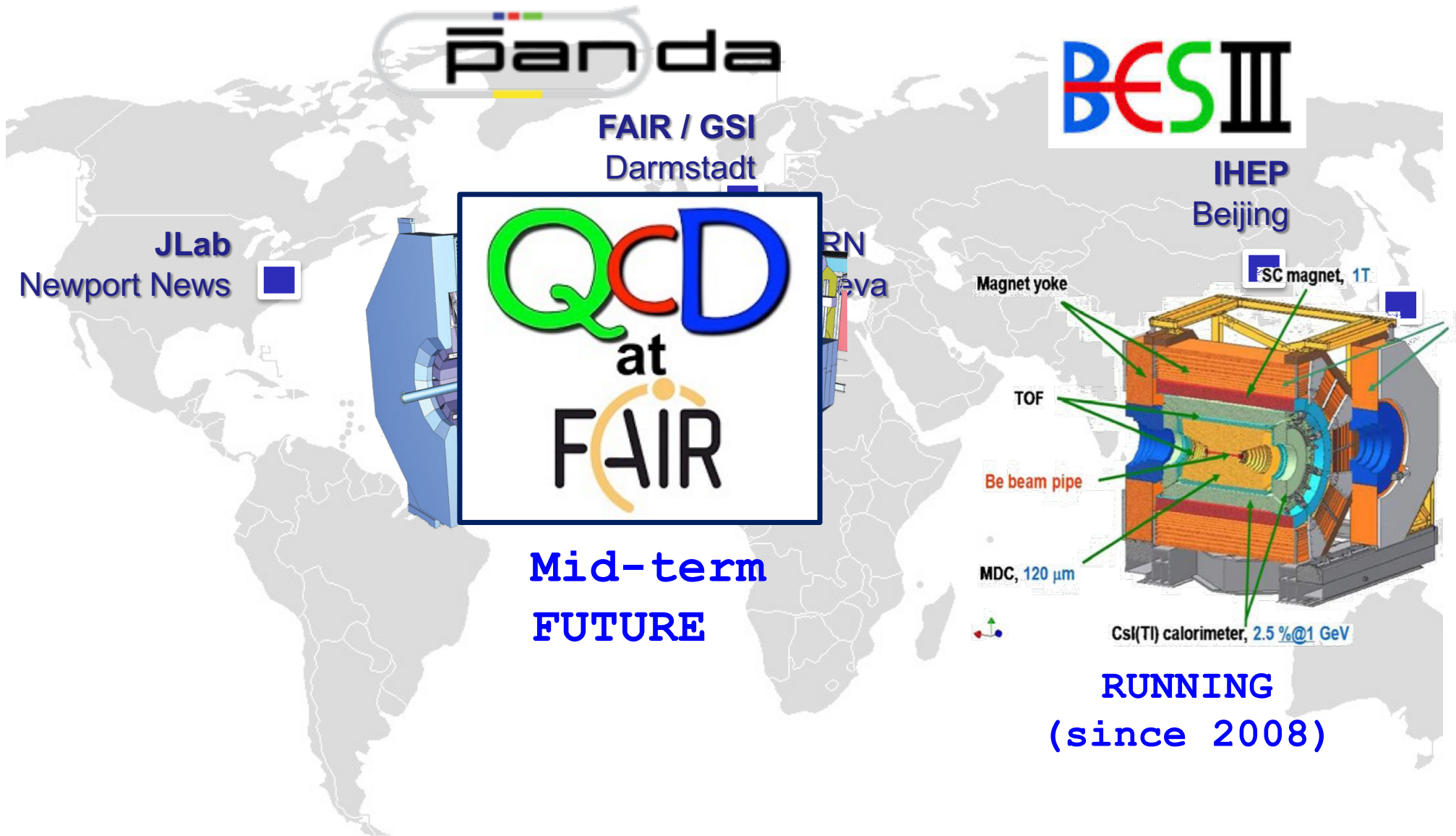
- B meson decays
 - CLEO, BaBar, Belle(II) ($E_{\text{cms}} \leq 12$ GeV)
 - LHCb: pp (7 TeV/c)

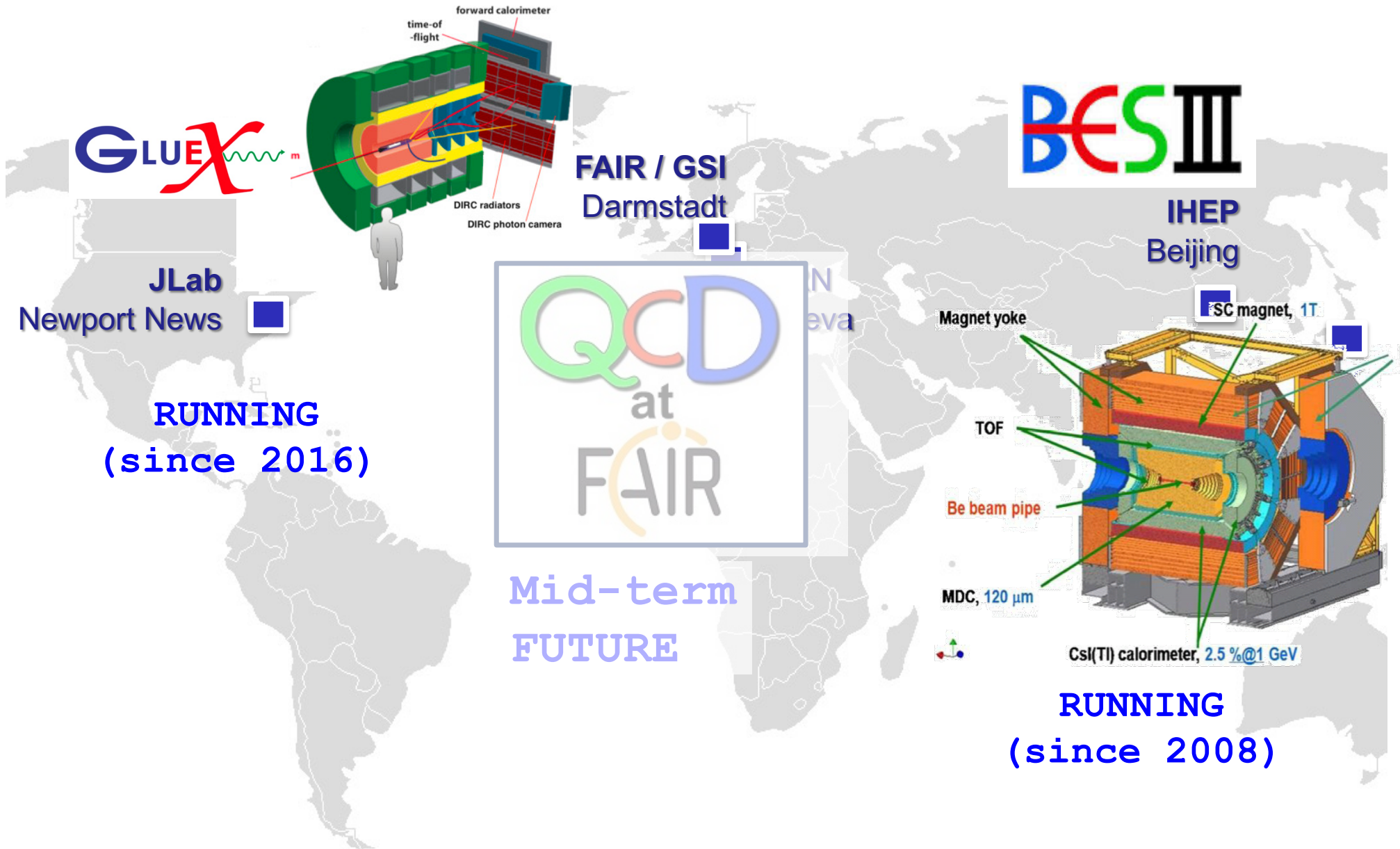
- Diffractive, photoproduction
 - GlueX: γ p (9 GeV/c),
 - COMPASS: π /K/p p (190-270 GeV/c)

- Formation & Production with recoil particle(s)
 - E760/E835, PANDA ($E_{\text{cms}} \leq 5.5$ GeV)
 - No running experiment presently











- Symmetric e^+e^- collider:
 - $\sqrt{s} = 2.0 - 4.6 \text{ GeV}$
- Design luminosity:
 - $1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ (at $\psi(3770)$, achieved in 04/2016)

- Multi-purpose 4π detector with
 - good tracking
 - calorimetry
 - PID and muon detection
- Operating since March 2008

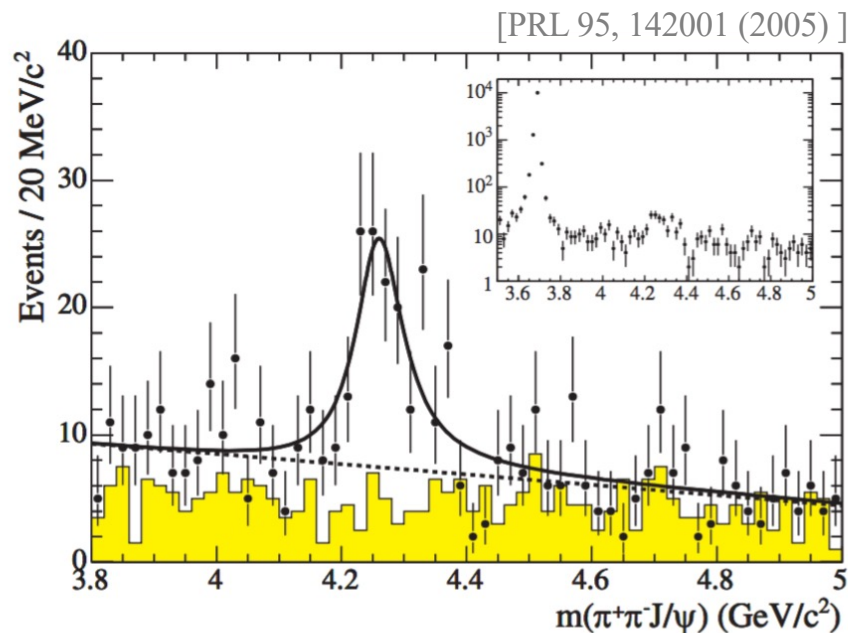


The $Y(4260)$ and further supernumerary vector states

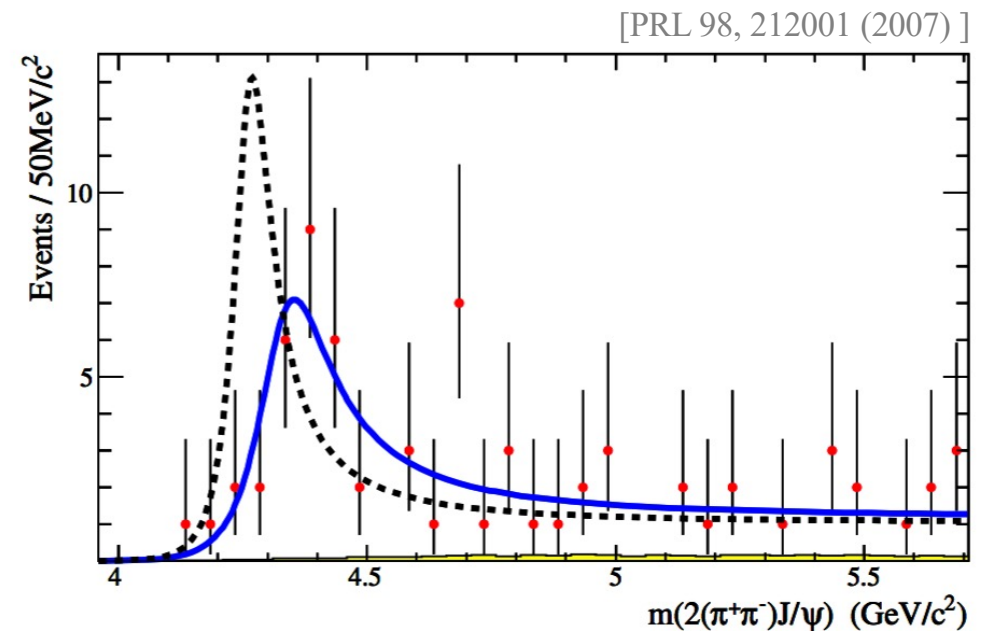
The Y states, e^+e^- production of $J/\psi\pi\pi$, $h_c\pi\pi$ and $\psi(2S)\pi\pi$

Some history:

$$e^+e^- \rightarrow J/\psi\pi^+\pi^-$$



$$e^+e^- \rightarrow \psi(2S)\pi^+\pi^-$$



- Discovery of the $Y(4260)$ using ISR by BaBar in $J/\psi\pi^+\pi^-$

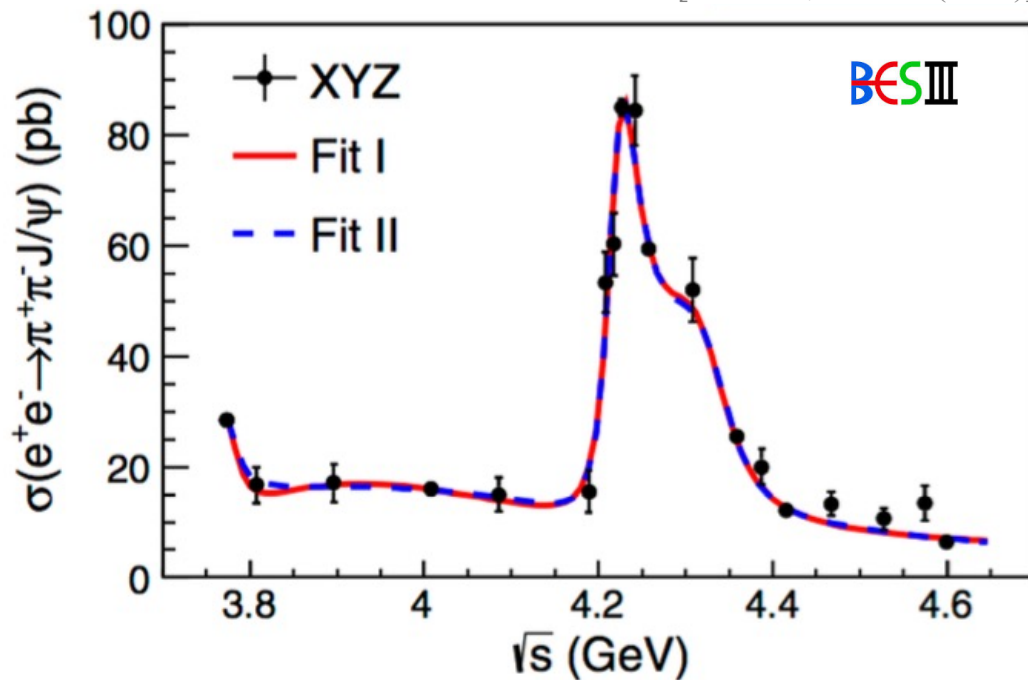
- Discovery of the $Y(4360)$ using ISR by BaBar in $\psi(2S)\pi^+\pi^-$

The Y states, e^+e^- production of $J/\psi\pi\pi$, $h_c\pi\pi$ and $\psi(2S)\pi\pi$

BESIII result, published

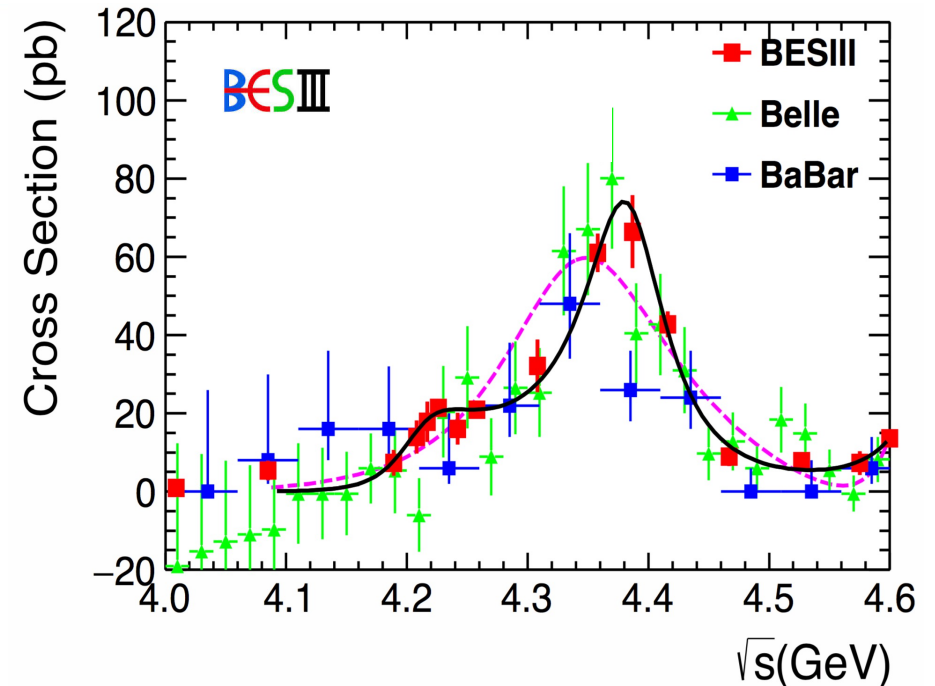
$$e^+e^- \rightarrow J/\psi\pi^+\pi^-$$

[PRL 118, 092001 (2017)]



$$e^+e^- \rightarrow \psi(2S)\pi^+\pi^-$$

[Phys. Rev. D 96, 032004 (2017)]



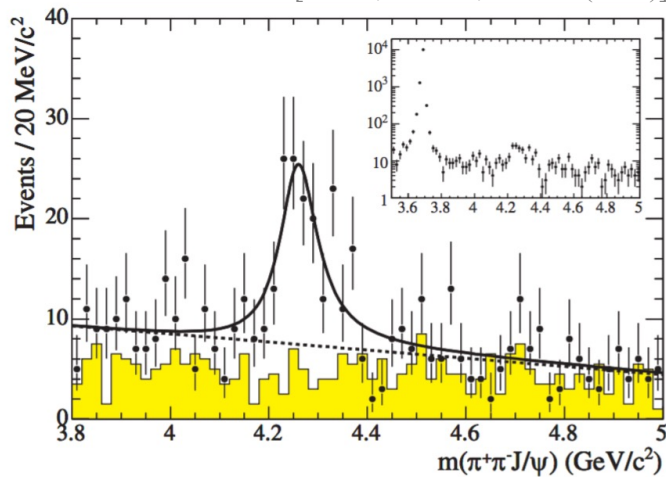
- Cross-section inconsistent with the single resonance $Y(4260)$!
- Two favoured over one by $>7\sigma$

- BESIII: Much higher precision (5.8σ)
- Coherent BW fit: $Y(4230)$ and $Y(4390)$

What happened to the Y states?

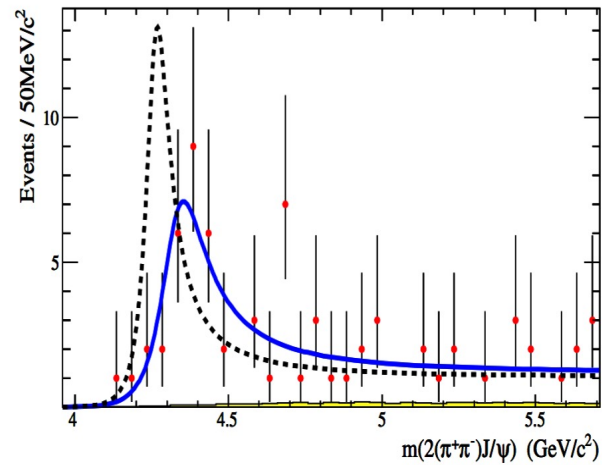
$$e^+e^- \rightarrow J/\psi\pi^+\pi^-$$

[BaBar, PRL 95, 142001 (2005)]

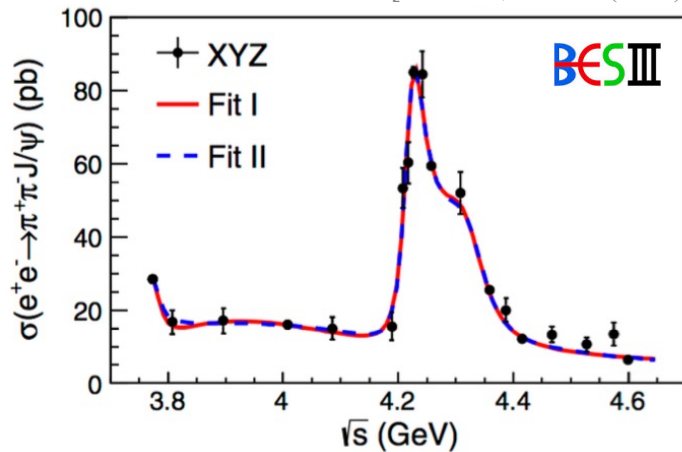


$$e^+e^- \rightarrow \psi(2S)\pi^+\pi^-$$

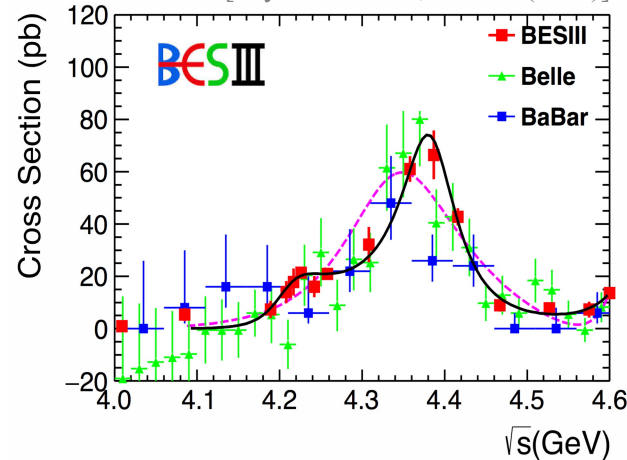
[BaBar, PRL 98, 212001 (2007)]



[PRL 118, 092001 (2017)]



[Phys. Rev. D 96, 032004 (2017)]

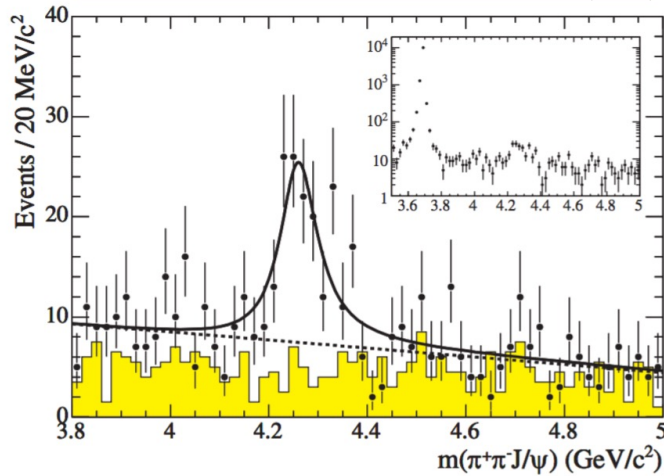


Two structures now resolved: $Y(4260) \rightarrow Y(4230)$, $Y(4360) \rightarrow Y(4390)$

What happened to the Y states?

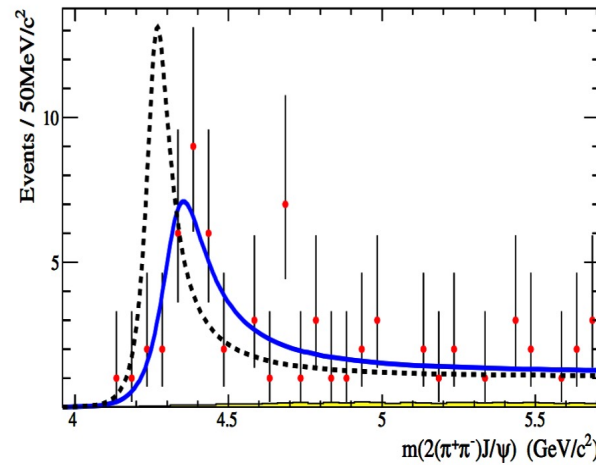
$$e^+e^- \rightarrow J/\psi\pi^+\pi^-$$

[BaBar, PRL 95, 142001 (2005)]

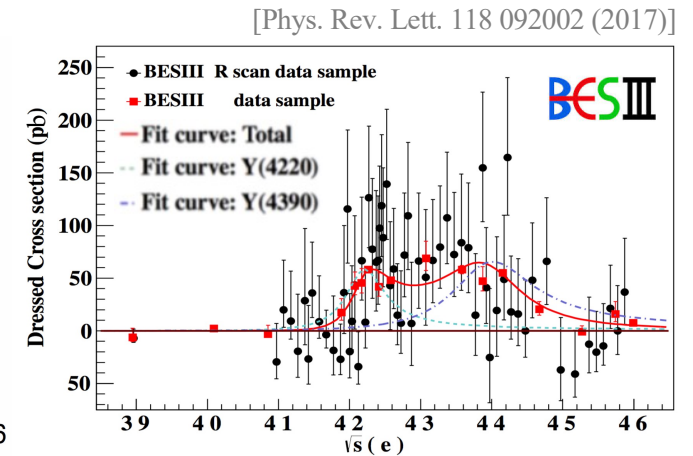
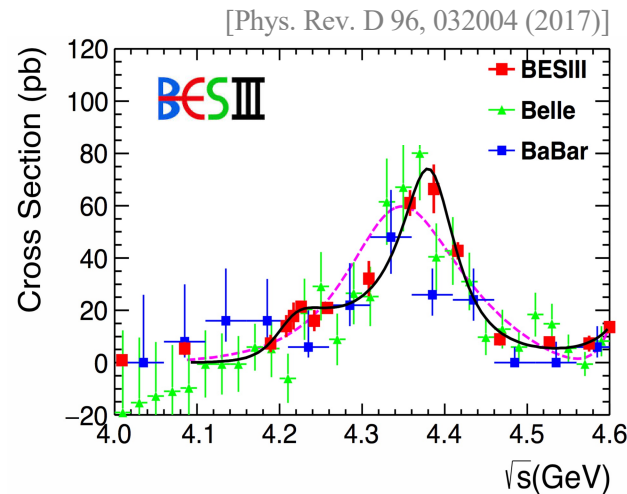
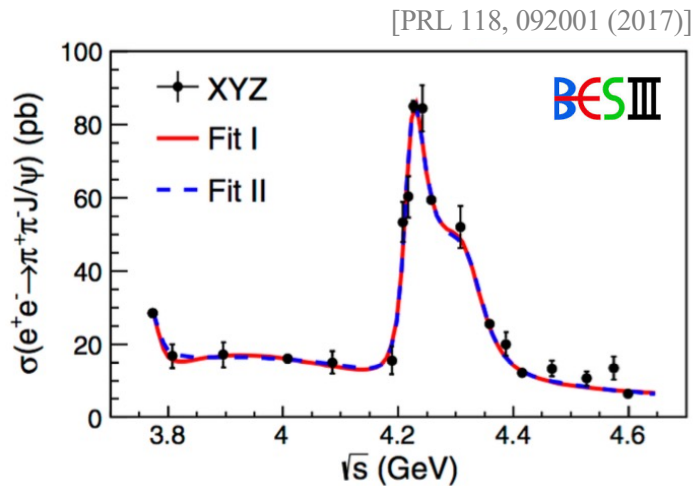
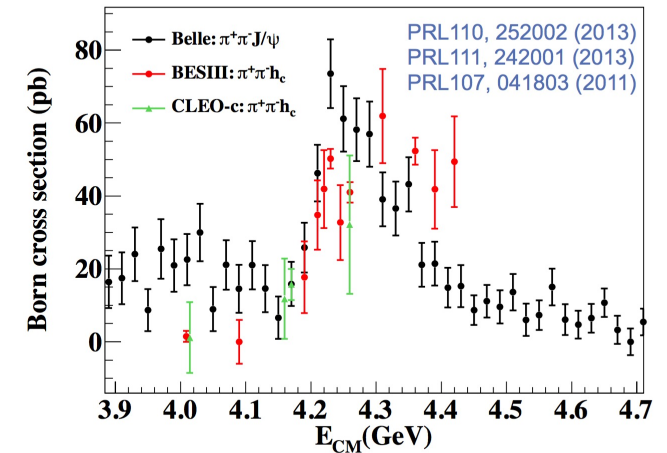


$$e^+e^- \rightarrow \psi(2S)\pi^+\pi^-$$

[BaBar, PRL 98, 212001 (2007)]



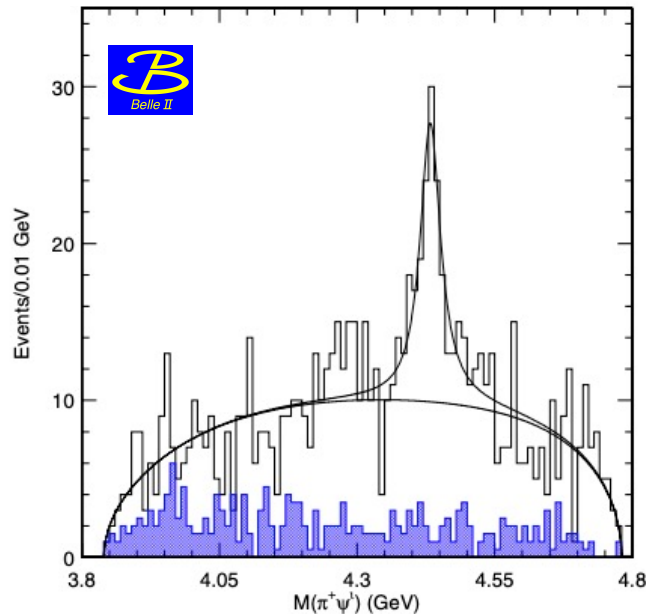
$$e^+e^- \rightarrow h_c\pi^+\pi^-$$



Two structures now resolved: $Y(4260) \rightarrow Y(4230)$, $Y(4360) \rightarrow Y(4390)$

The $Z(4430)$ and further (charged) Z_c states

[Belle, Phys. Rev. Lett., 100 (2008) 142001]



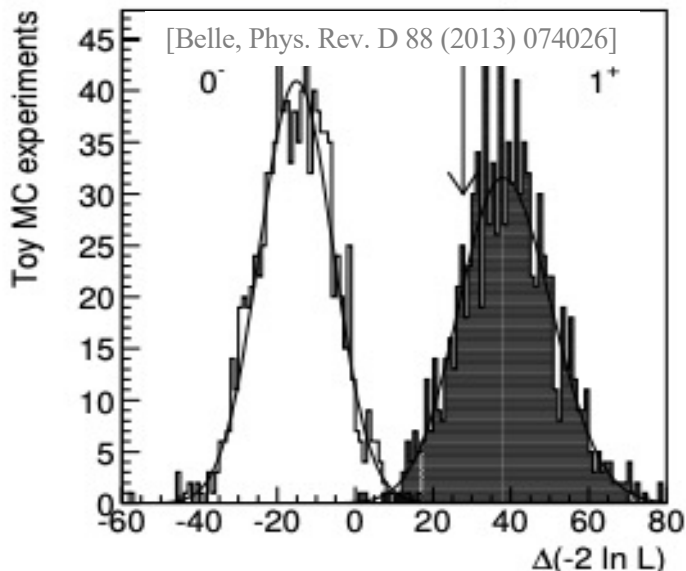
- First observed by Belle in 2008
 - $B \rightarrow K^\mp Z(4430)^\pm \rightarrow K^\mp \pi^\pm \psi'$
 - relatively narrow state, 6.5σ
 - first charmonium-like state with a non-zero electric charge
- => Minimal quark content [$c\bar{c}u\bar{d}$] = manifestly exotic

- BaBar searched for it, however, does not confirm [PRD 79, 112001 (2009)]

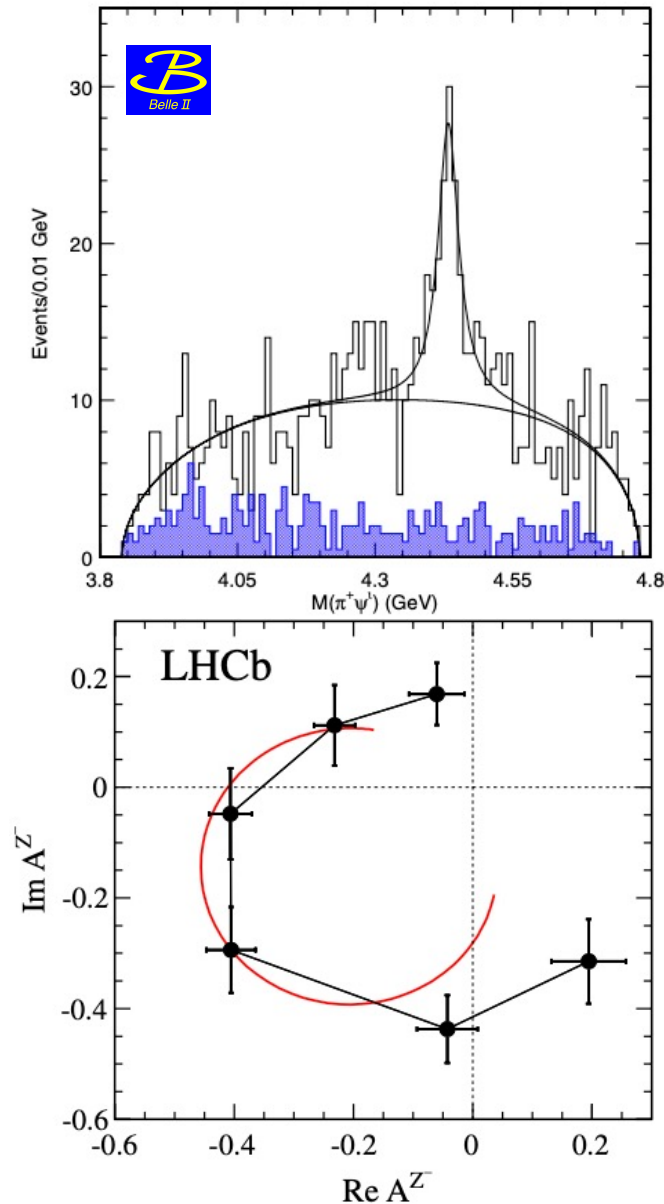
- Decay to $J/\psi/\pi$ seen in B decays by Belle [PRD 90, 112009 (2014)], and not seen by BaBar [PRD 79, 112001 (2009)]

- LHCb confirms and showed resonant behavior in argand plot [PRL 112, 222002 (2014)]

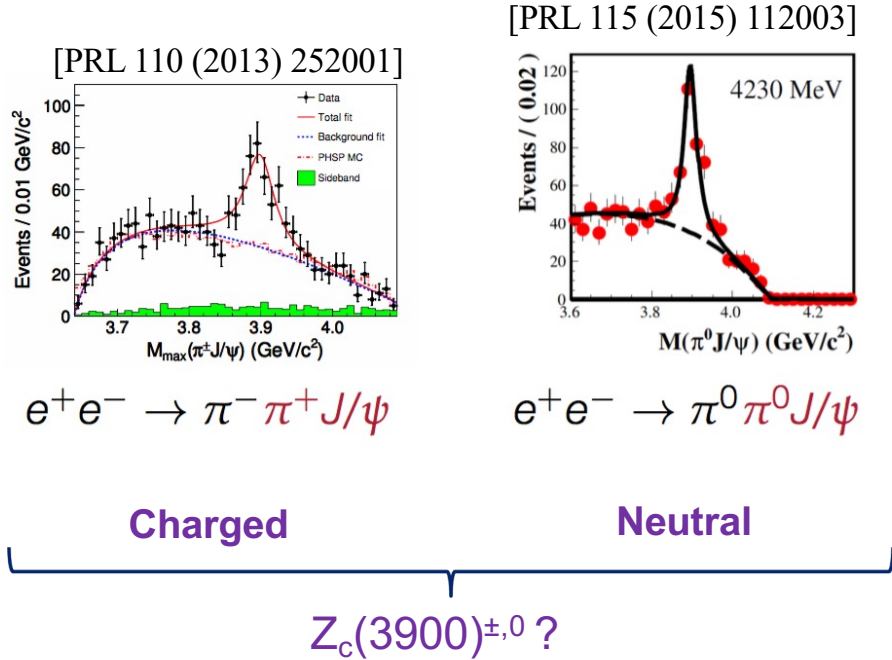
- Spin-parity constrained by Belle: $J^P = 1^+$, confirmed by LHCb [PRL 112, 222002 & PRD 92, 112009 (2015)]



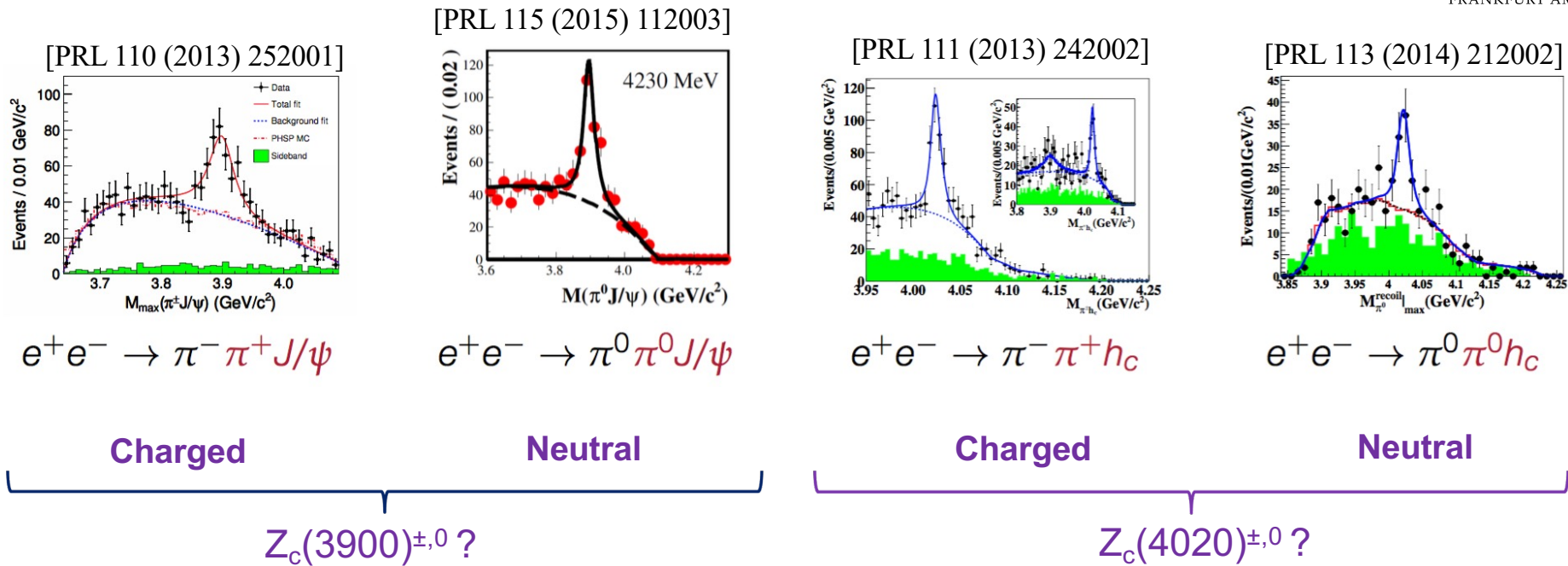
[Belle, Phys. Rev. Lett., 100 (2008) 142001]



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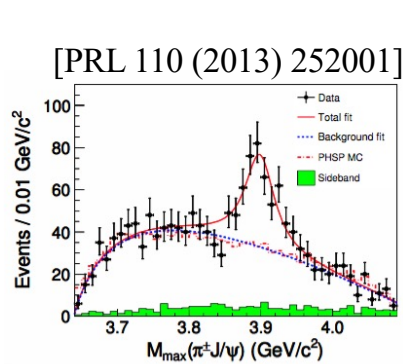


- The charged $Z_c(3900)^\pm$, and meanwhile also the neutral partner $Z_c(3900)^0$

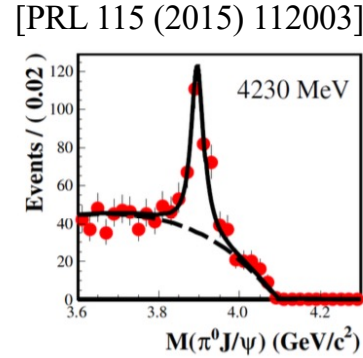


- The charged $Z_c(3900)^\pm$, and meanwhile also the neutral partner $Z_c(3900)^0$
- Two **isospin triplets** of charmonium-like exotic states established

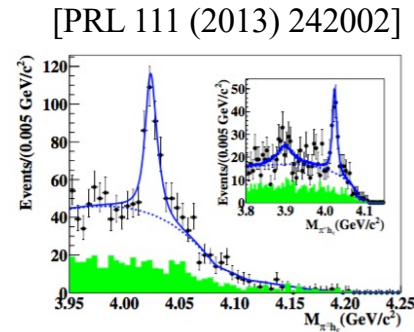
Hidden Charm



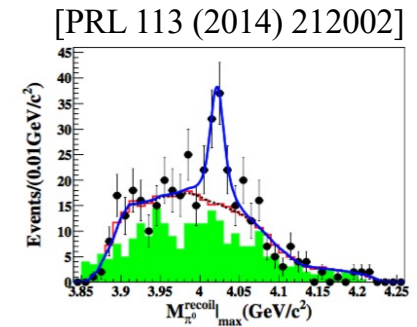
$$e^+e^- \rightarrow \pi^- \pi^+ J/\psi$$



$$e^+e^- \rightarrow \pi^0 \pi^0 J/\psi$$

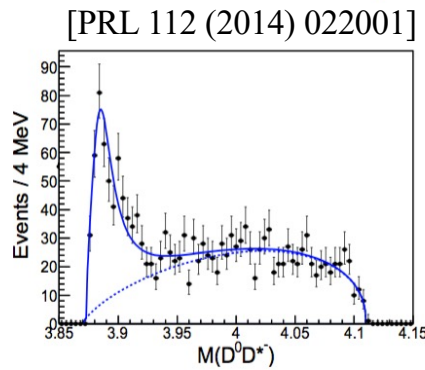


$$e^+e^- \rightarrow \pi^- \pi^+ h_c$$



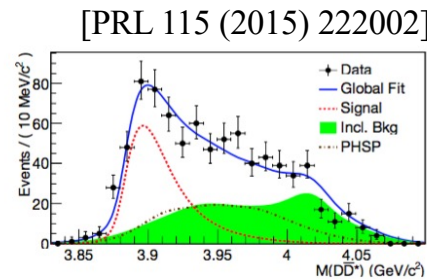
$$e^+e^- \rightarrow \pi^0 \pi^0 h_c$$

Open Charm



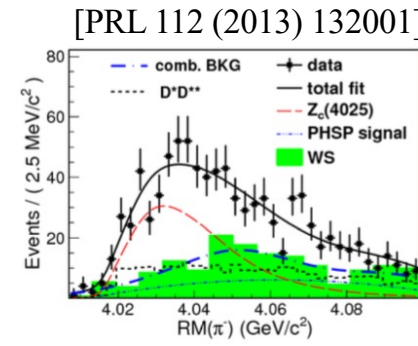
$$e^+e^- \rightarrow \pi^- (D\bar{D}^*)^+$$

Charged



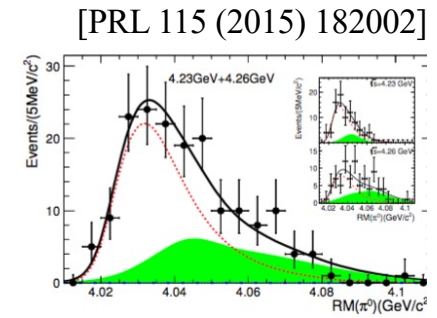
Neutral

$Z_c(3900)^{\pm,0} ?$



$$e^+e^- \rightarrow \pi^- (D^* \bar{D}^*)^+$$

Charged

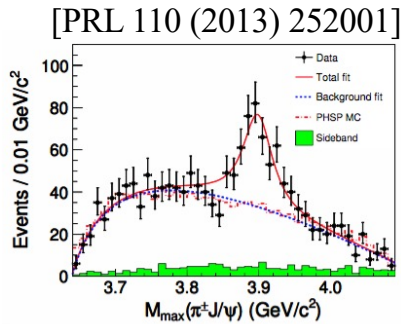


Neutral

$Z_c(4020)^{\pm,0} ?$

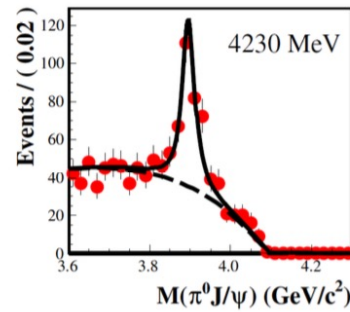
- Two **isospin triplets** of charmonium-like exotic states established
- Different decay (*hidden vs. open charm*) of same state observed?

Hidden Charm



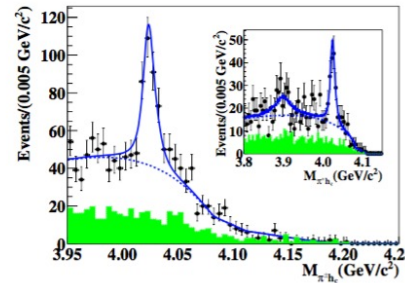
$$e^+e^- \rightarrow \pi^- \pi^+ J/\psi$$

[PRL 115 (2015) 112003]



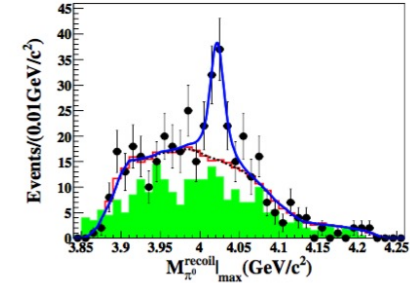
$$e^+e^- \rightarrow \pi^0 \pi^0 J/\psi$$

[PRL 111 (2013) 242002]



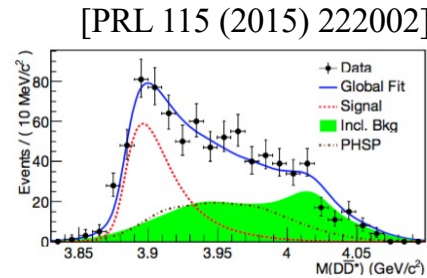
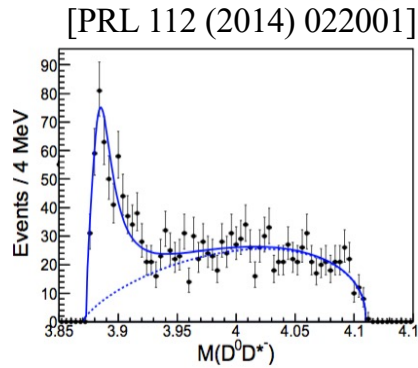
$$e^+e^- \rightarrow \pi^- \pi^+ h_c$$

[PRL 113 (2014) 212002]

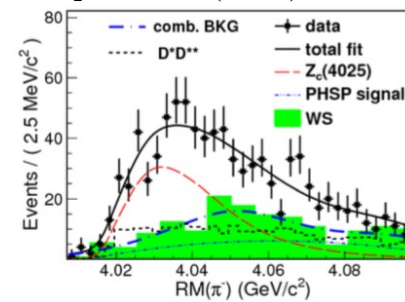


$$e^+e^- \rightarrow \pi^0 \pi^0 h_c$$

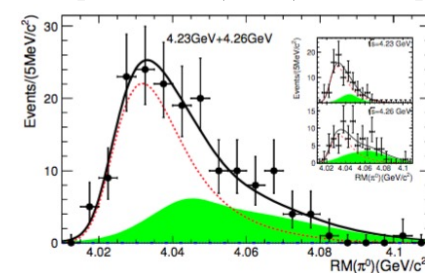
Open Charm



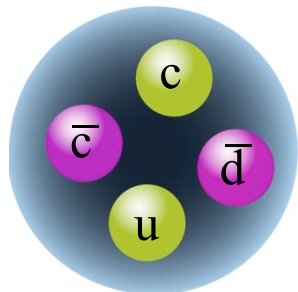
[PRL 112 (2013) 132001]



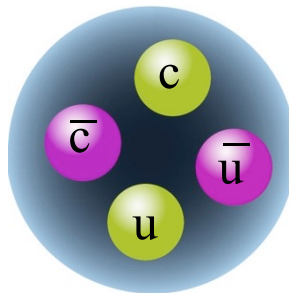
[PRL 115 (2015) 182002]



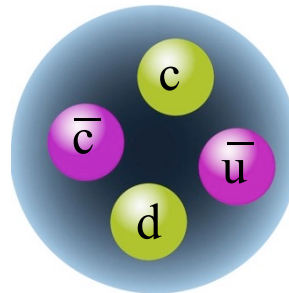
$Z_c(3900)^+$



$Z_c(3900)^0$



$Z_c(3900)^-$



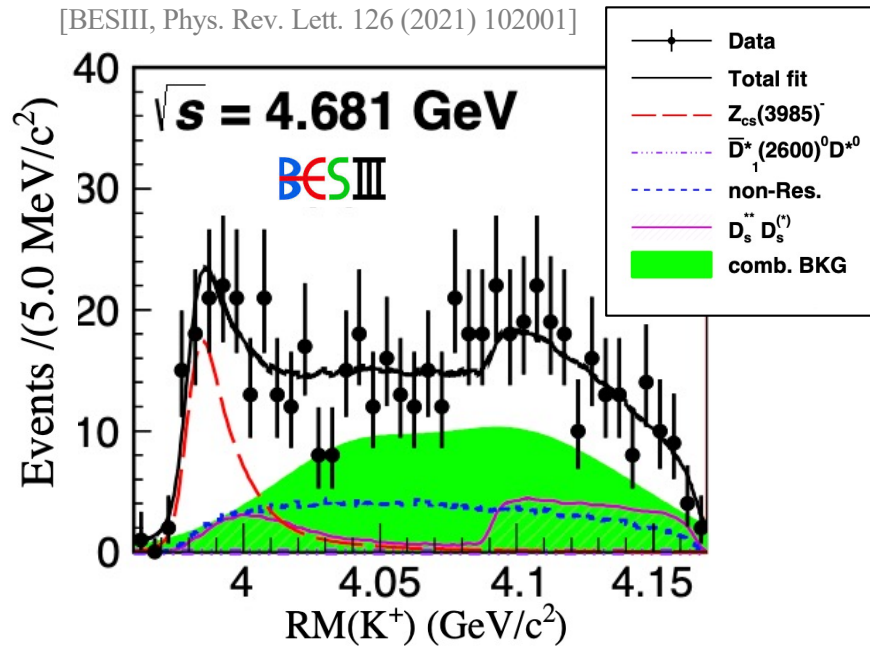
$\pi^- (D^* \bar{D}^*)^+$

Charged

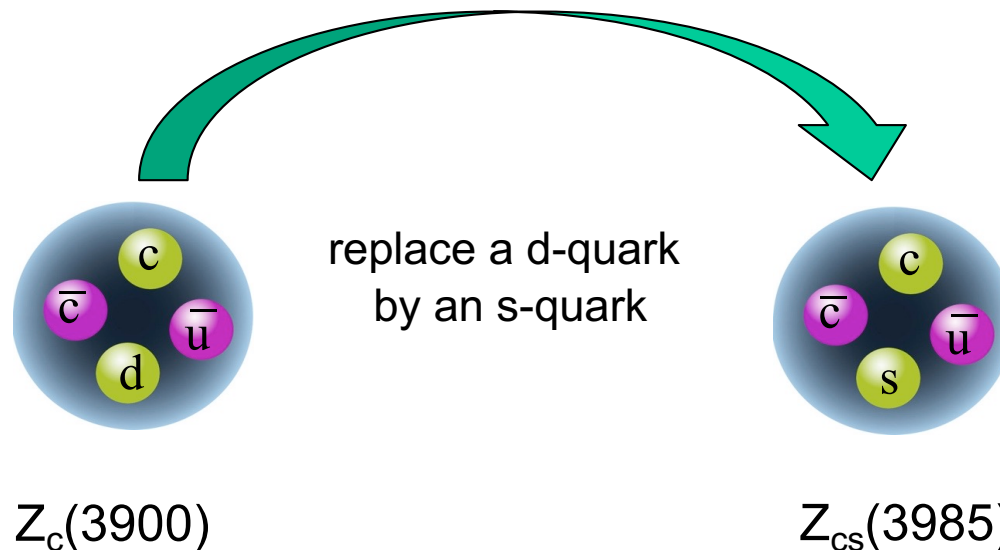
Neutral

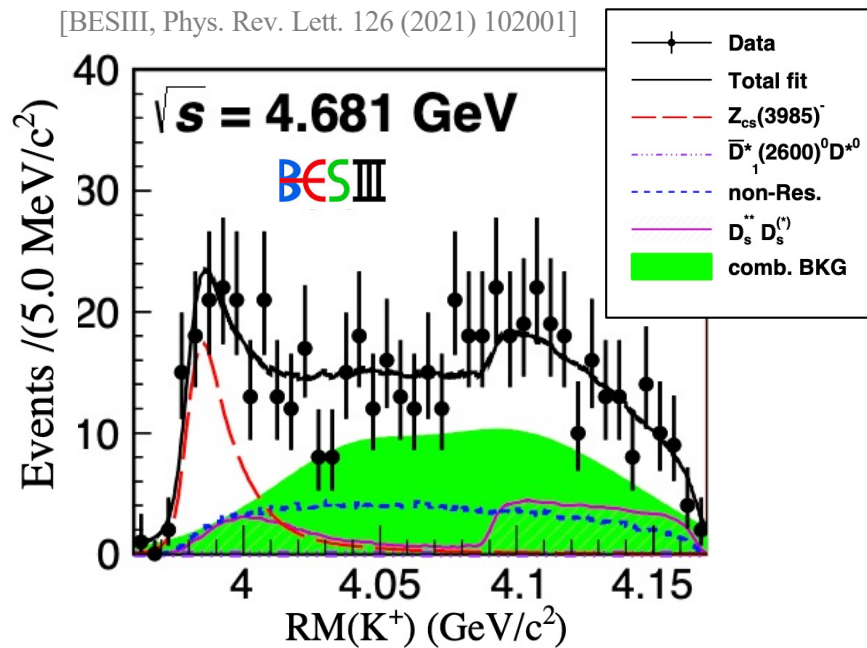
$Z_c(4020)^{\pm,0} ?$

es established
state observed?



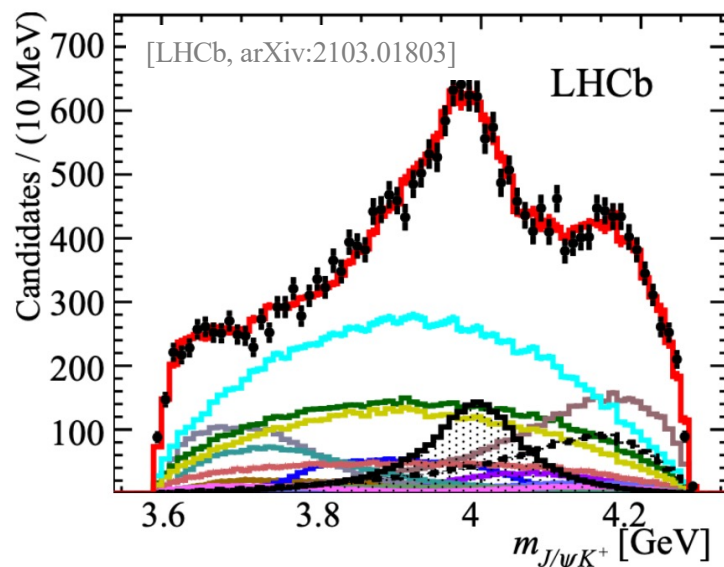
- Search for **strange partner** of $Z_c(3900)$
 - Containing s quark in **open charm** decay
 - $e^+e^- \rightarrow K^+(D_s D^* / D_s^* D)^-$
 - **Narrow** threshold enhancement (5.3σ)
 - $M = (3982.5_{-2.6}^{+1.8} \pm 2.1) \text{ MeV}/c^2$,
 $\Gamma = (12.8_{-4.4}^{+5.3} \pm 3.0) \text{ MeV}$
- Manifestly exotic charged hidden-charm tetraquark candidate with strangeness
 - With a non-zero electric charge
 - Thus, **minimal quark content** => $[c\bar{c}s\bar{u}]$





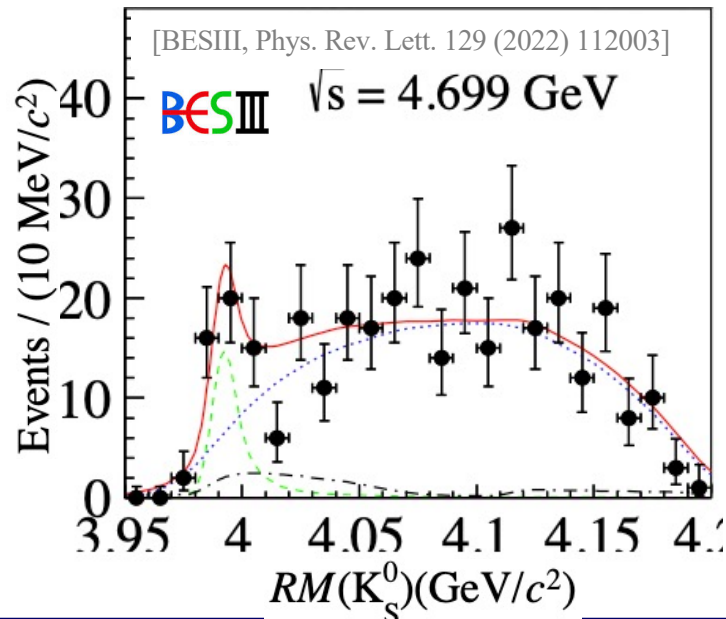
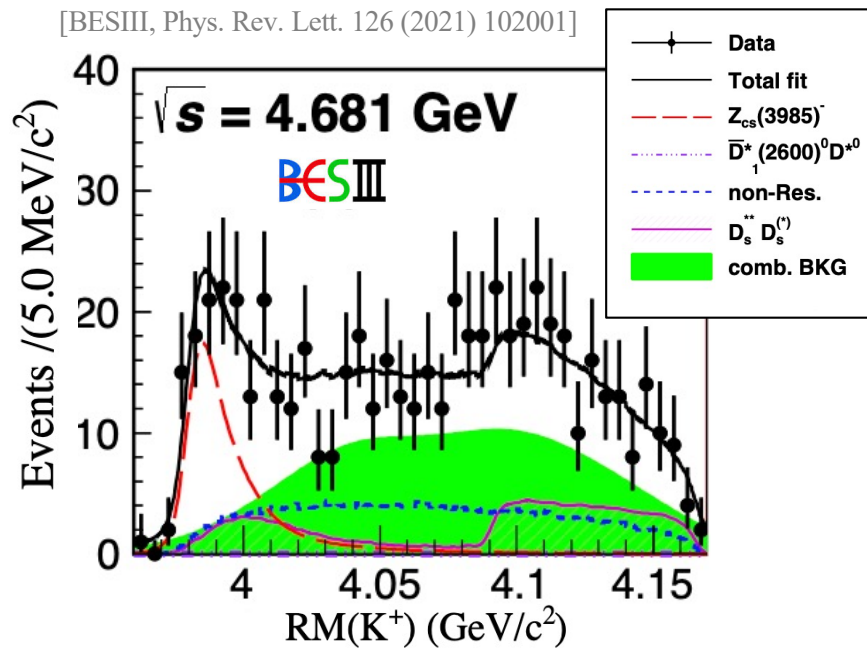
- Search for **strange partner** of $Z_c(3900)$
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- Manifestly exotic charged hidden-charm tetraquark candidate with strangeness
 - With a non-zero electric charge
 - Thus, **minimal quark content** => $[c\bar{c}s\bar{u}]$



- LHCb reports a $Z_{cs}(4000)$ in $B \rightarrow \phi(J/\psi K^+)$
 - $M = (4000.3 \pm 6^{+4}_{-14}) \text{ MeV}/c^2$,
 - $\Gamma = (131 \pm 15 \pm 26) \text{ MeV}$
 - $J^P = 1^+$, **hidden charm** final state
 - 10x broader ...

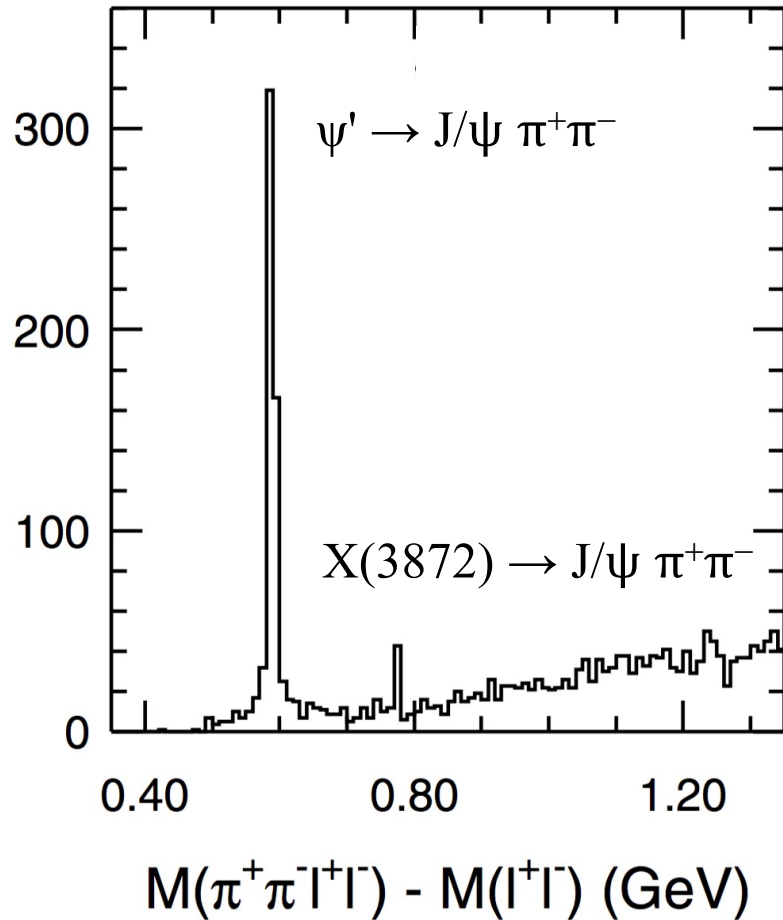
=> Same state observed in different decays (open/hidden charm) at two experiments?



- Search for **strange partner** of $Z_c(3900)$
 - Containing s quark in **open charm** decay
 - $e^+e^- \rightarrow K^+(D_s D^* / D_s^* D)^-$
 - Narrow threshold enhancement (5.3σ)
 - $M = (3982.5_{-2.6}^{+1.8} \pm 2.1) \text{ MeV}/c^2$,
 $\Gamma = (12.8_{-4.4}^{+5.3} \pm 3.0) \text{ MeV}$
 - Manifestly exotic charged hidden-charm tetraquark candidate with strangeness
 - With a non-zero electric charge
 - Thus, **minimal quark content** => $[c\bar{c}s\bar{u}]$
 - Search for neutral partner of $Z_{cs}(3985)$
 - Containing s quark in **open charm** decay
 - $e^+e^- \rightarrow K_S^0(D_s^+ D^{*-} + D_s^{*+} D^-)$
 - Narrow threshold enhancement (4.6σ)
 - $M = (3992.2 \pm 1.7 \pm 1.6) \text{ MeV}/c^2$
 $\Gamma = (7.7_{-3.8}^{+4.1} \pm 4.3) \text{ MeV}$
- => Seem to be **isospinpartners**

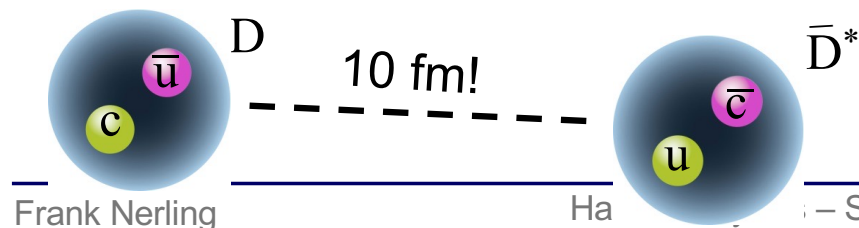
The X(3872) and further X states

[Belle Collab., PRL 91 (2003) 262001]



- First observed by Belle in 2003
 - $X(3872) \rightarrow J/\psi \pi^+ \pi^-$
 - very narrow state with $J^{PC} = 1^{++}$
- Belle & BaBar report signal in
 - $X(3872) \rightarrow D^0 \bar{D}^{*0}$
- Mass $m[X(3872)] - m[D^{*0}] - m[D^0]$
 $= (-0.07 \pm 0.12) \text{ MeV}/c^2$ (LHCb 2020)
- Width measurement:
 - $\Gamma_{X(3872)} < 1.2 \text{ MeV}$ (2011, Belle)
 - $\Gamma_{X(3872)} = 1.13 \text{ MeV}$ (2020, LHCb)

Analogy to deuteron:

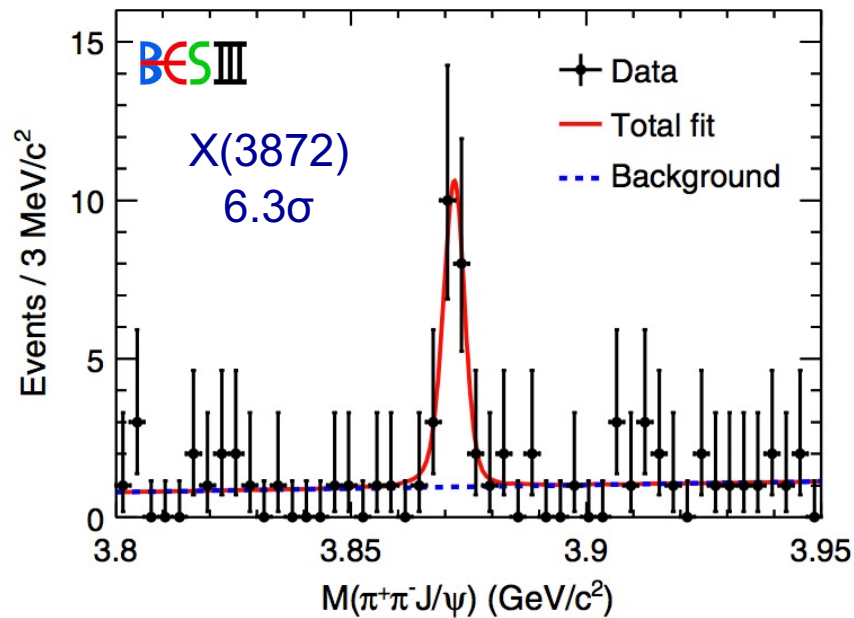


For clarification:

=> Precision measurement with sub-MeV resolution needed!

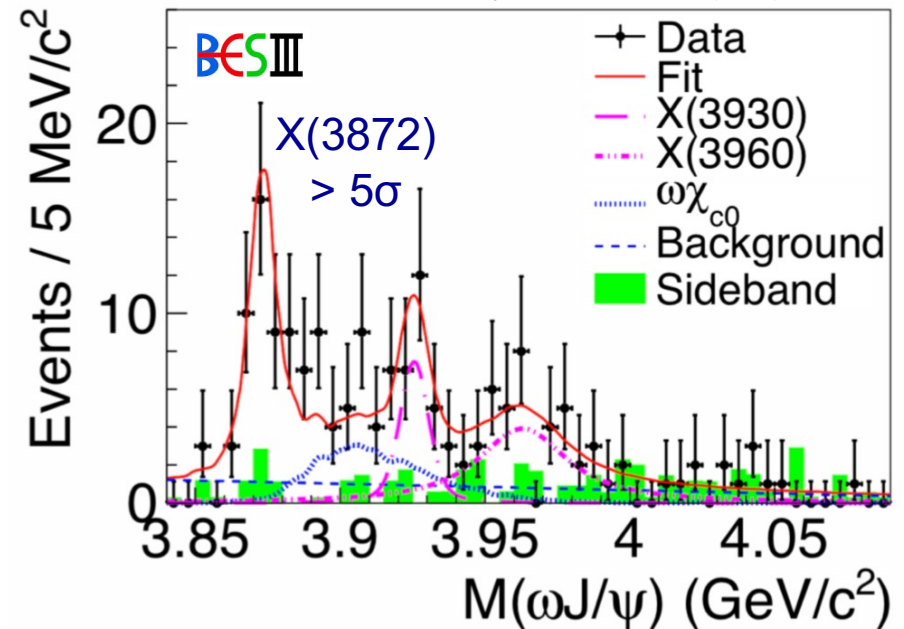
BESIII: First observation of $e^+e^- \rightarrow \gamma X(3872) \rightarrow \gamma \pi^+ \pi^- J/\psi$
First observation of $e^+e^- \rightarrow \gamma X(3872) \rightarrow \gamma \omega J/\psi$

[Phys. Rev. Lett. 112 (2014) 092001]



- $m = (3871.9 \pm 0.7 \pm 0.2) \text{ MeV}/c^2$
- $\Gamma < 2.4 \text{ MeV}$ (90% CL)

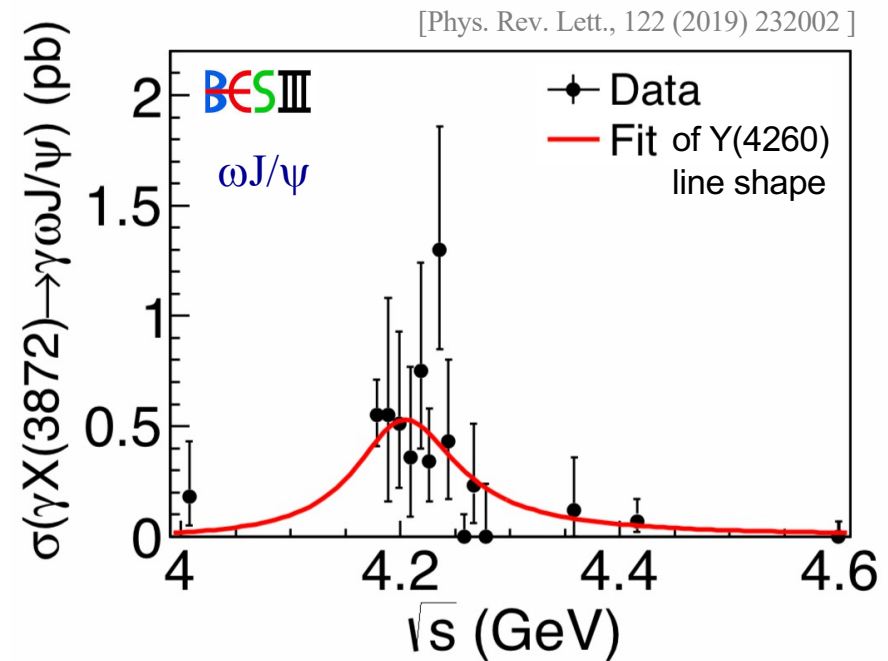
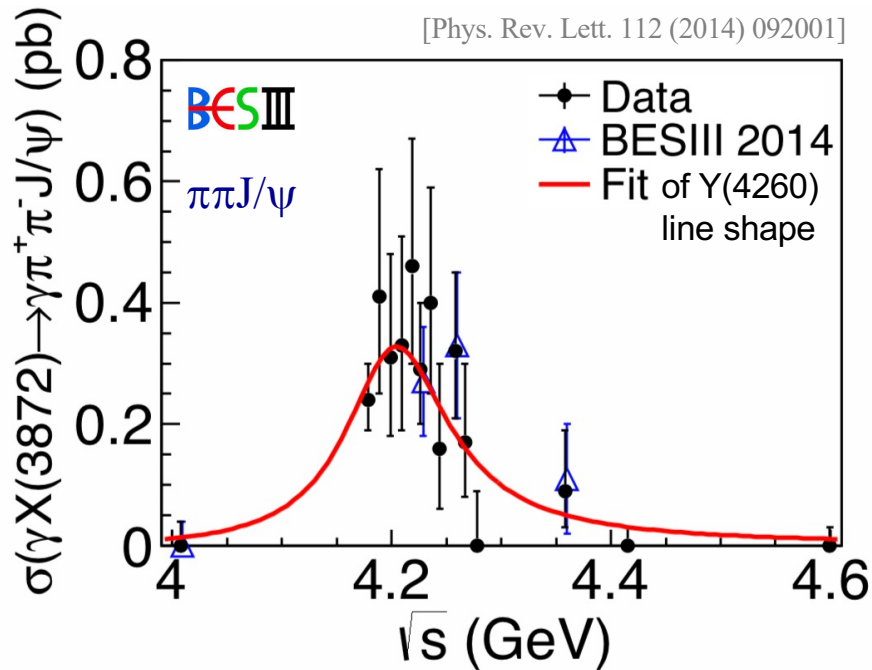
[Phys. Rev. Lett., 122 (2019) 232002]



- Fit with three Breit-Wigner resonances
=> *Evidence for two more structures*

BESIII: First observation of $e^+e^- \rightarrow Y(4260) \rightarrow \gamma X(3872) \rightarrow \gamma \omega J/\psi$
 First observation of $e^+e^- \rightarrow Y(4260) \rightarrow \gamma X(3872) \rightarrow \gamma \pi^+ \pi^- J/\psi$

cross section

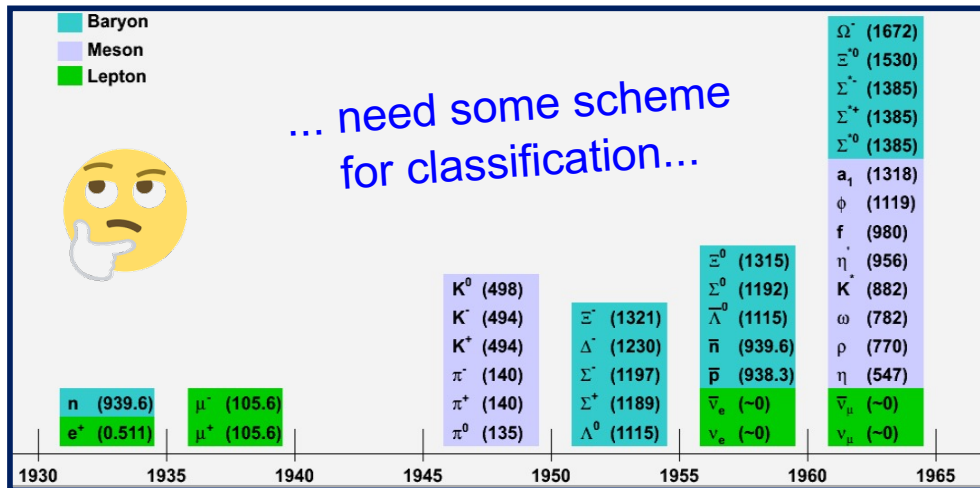


- $m = (4200.6_{-13.3}^{+7.9} \pm 3.0) \text{ MeV}/c^2$
- $\Gamma = (115_{-26}^{+38} \pm 12) \text{ MeV}/c^2$

- Shape consistent with production via a Y(4260) state

[Subm. to Phys. Rev. Lett., arXiv:1903.04695 [hep-ex]]

Again a Zoo of (exotic) hadrons ...



[LHCb-FIGURE-2021-001]

55 new hadrons at LHCb

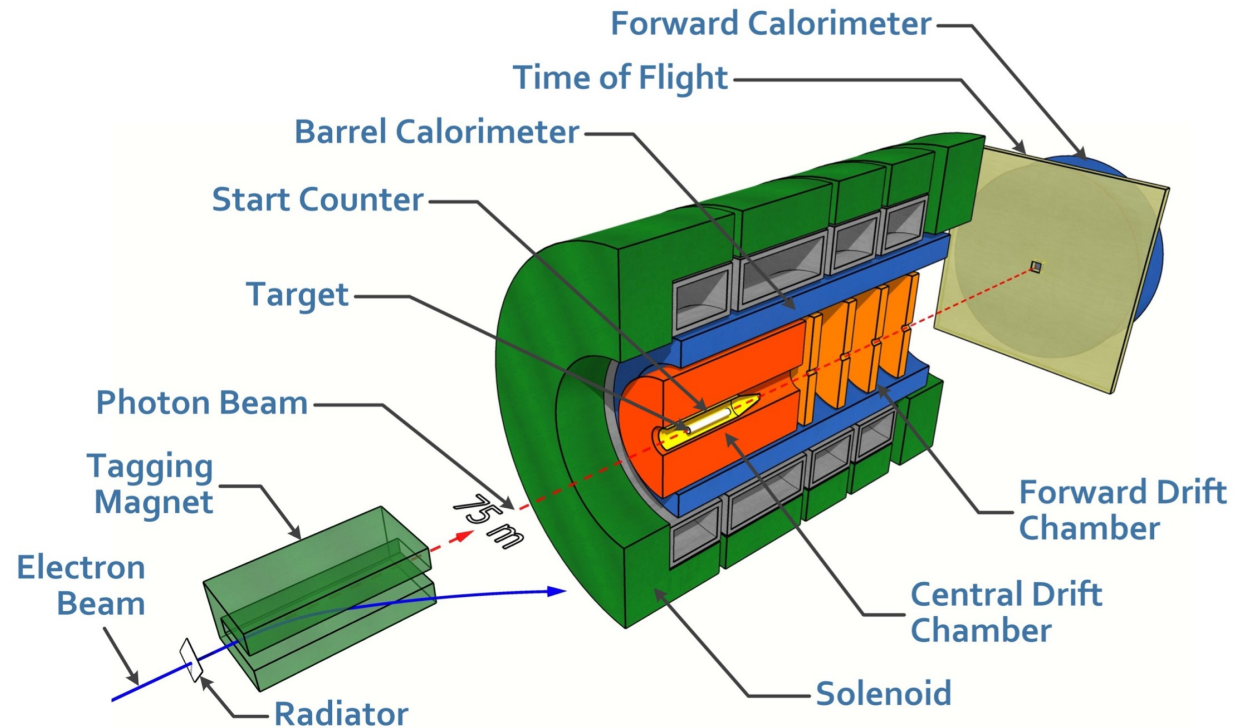
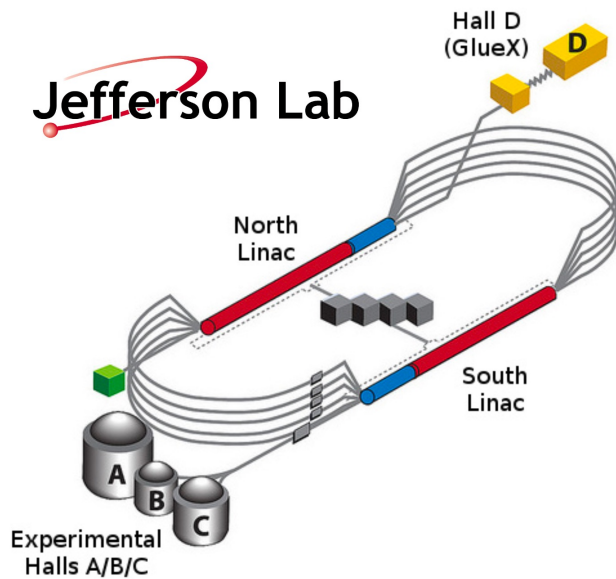


[Polyakov, EPS-HEP-2021]

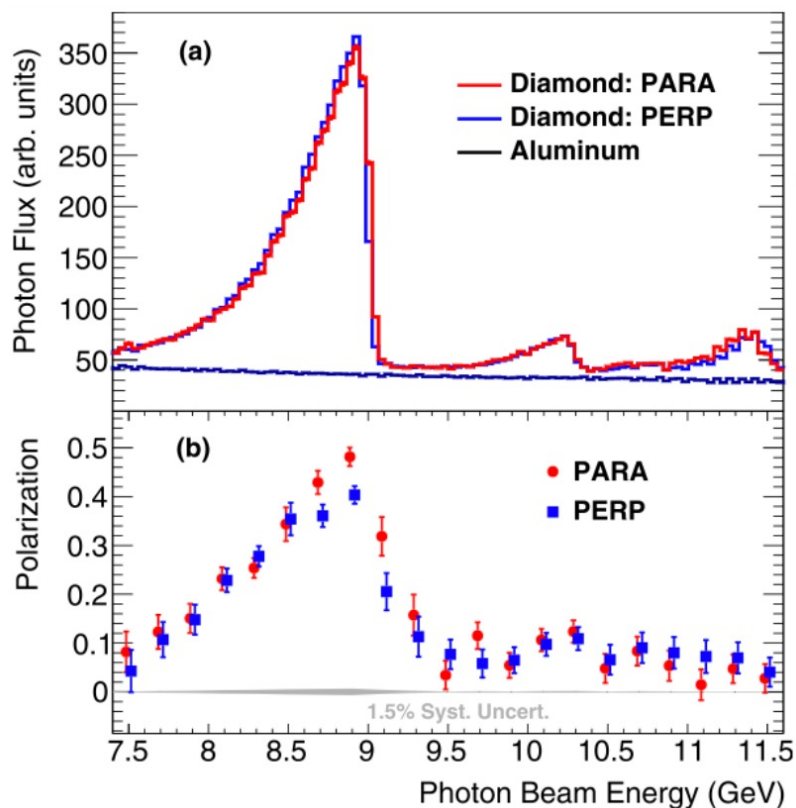
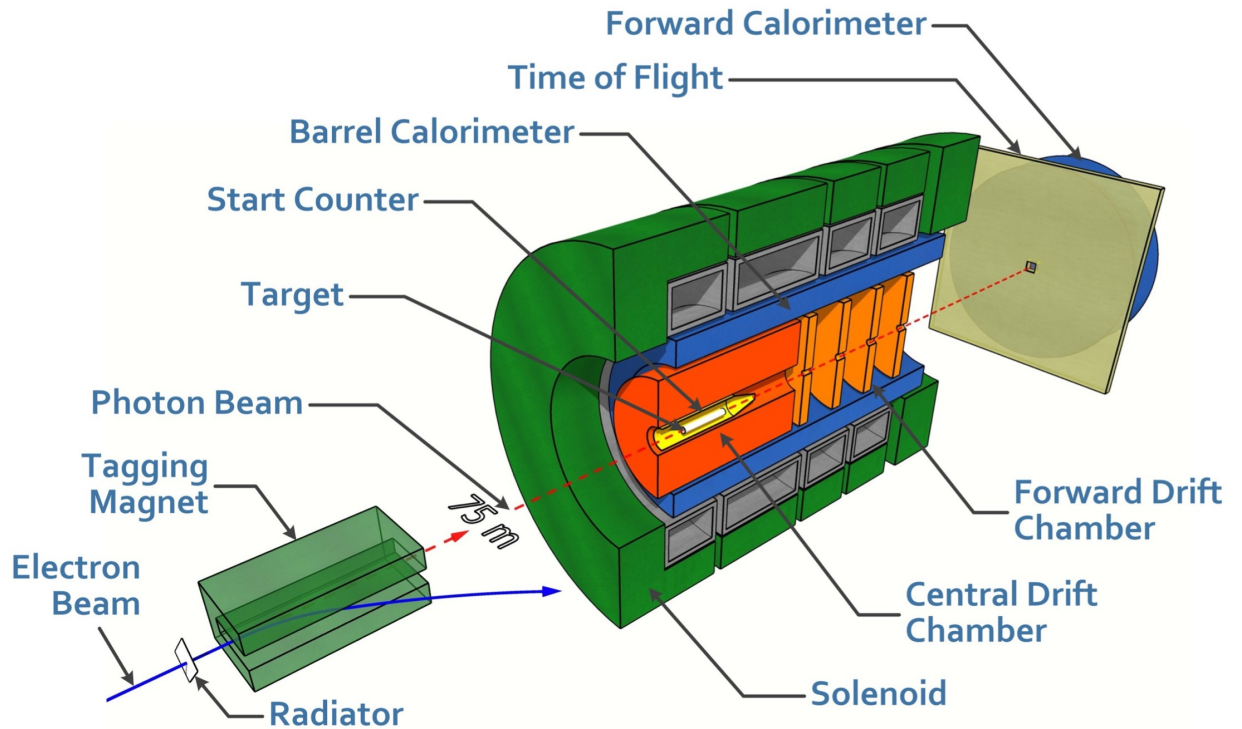
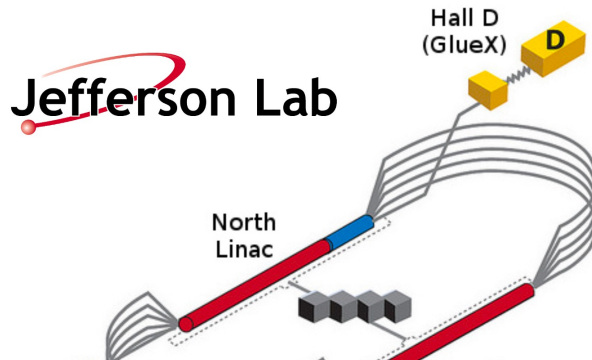
Search for the $Y(2175)$ in photo-production at GlueX



GlueX in Hall D at CEBAF, JLab



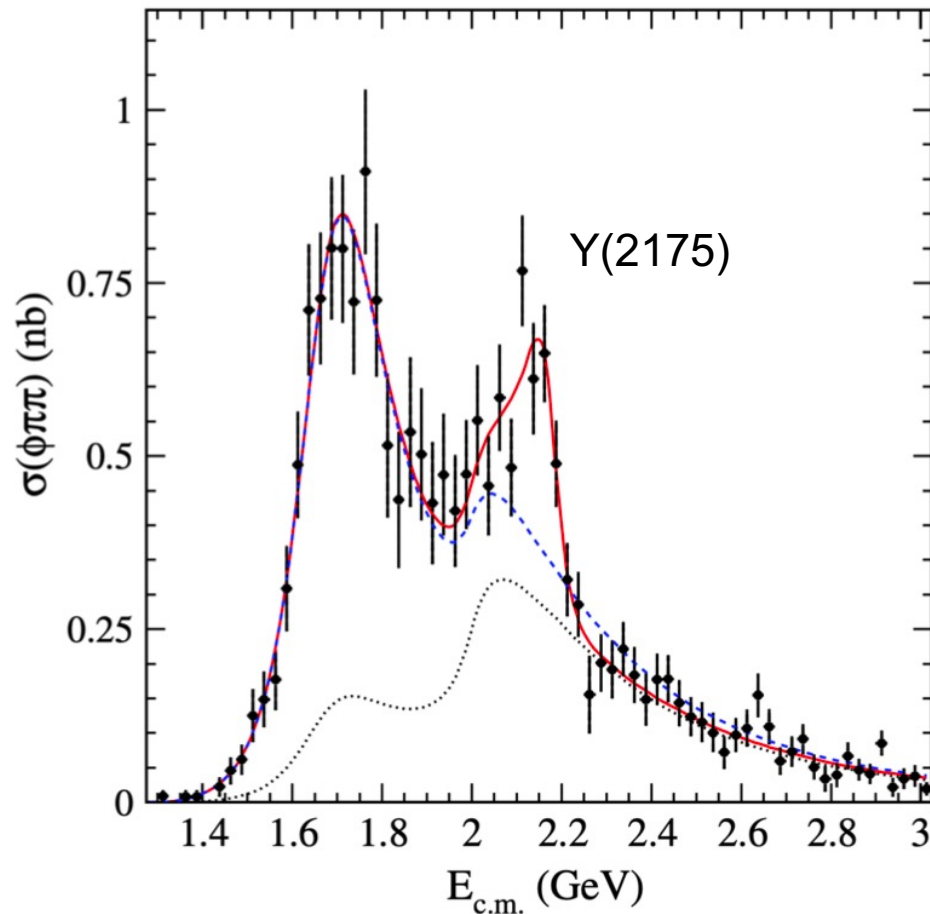
- 12 GeV electron beam from CEBAF accelerator
- Coherent Bremsstrahlung on diamond radiator
- Linear polarization in peak at ~9 GeV: $P_\gamma \sim 40\%$
- Energy tagged by scattered electrons
- Beam intensity: $1 - 5 \cdot 10^7 \gamma/s$ in peak



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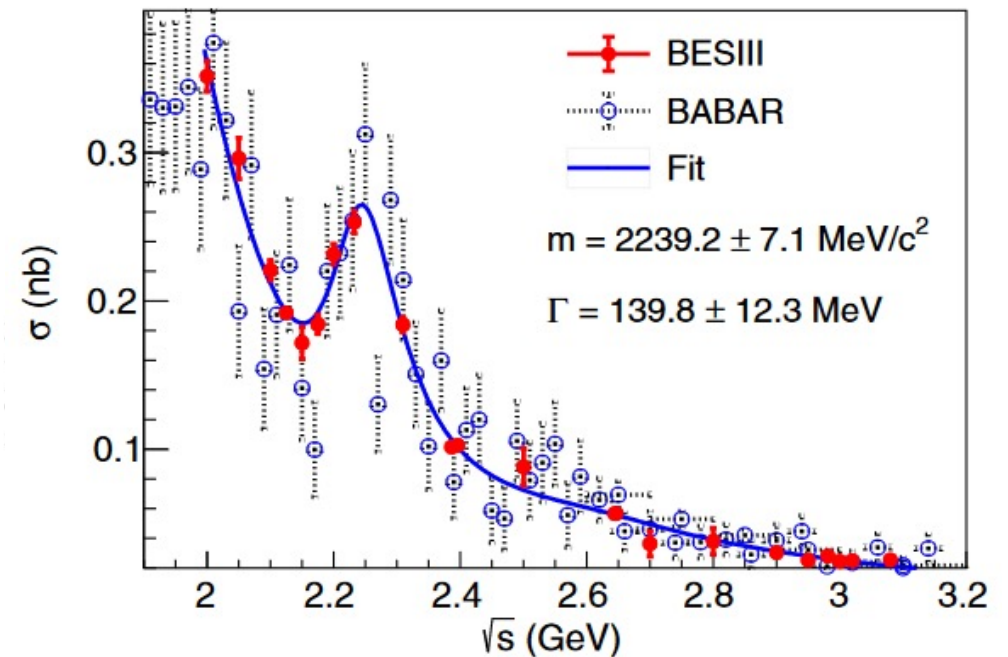
The Y(2175) – strange partner of Y(4230)

[Phys. Rev. D. 74 (2006) 091103]



First observed in ISR, BaBar

[Phys. Rev. D 99, (2019) 032001]



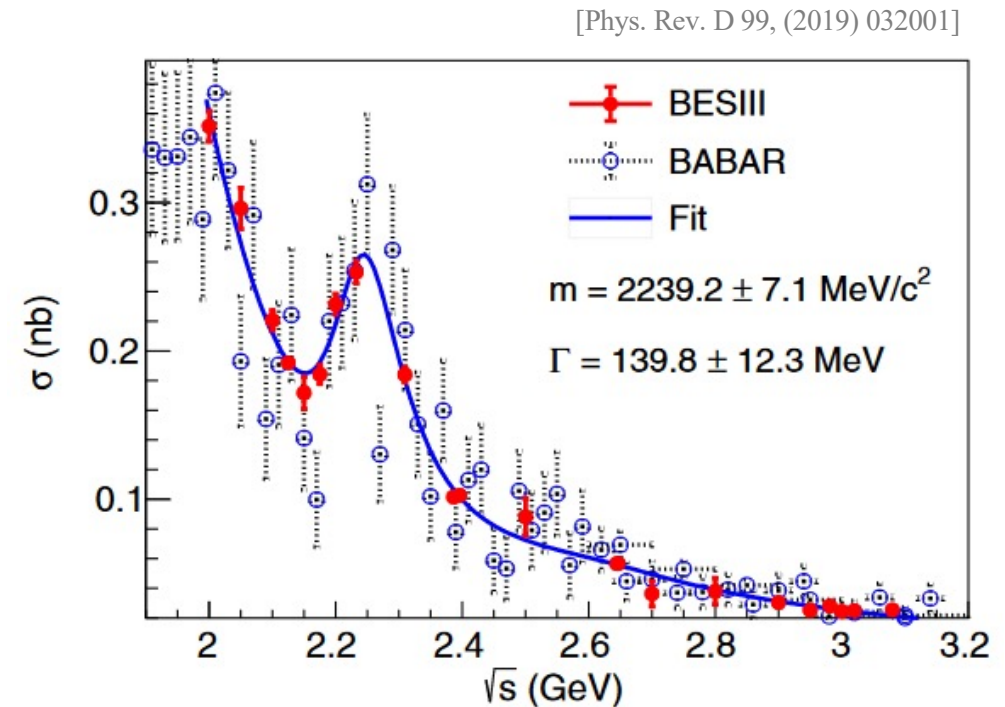
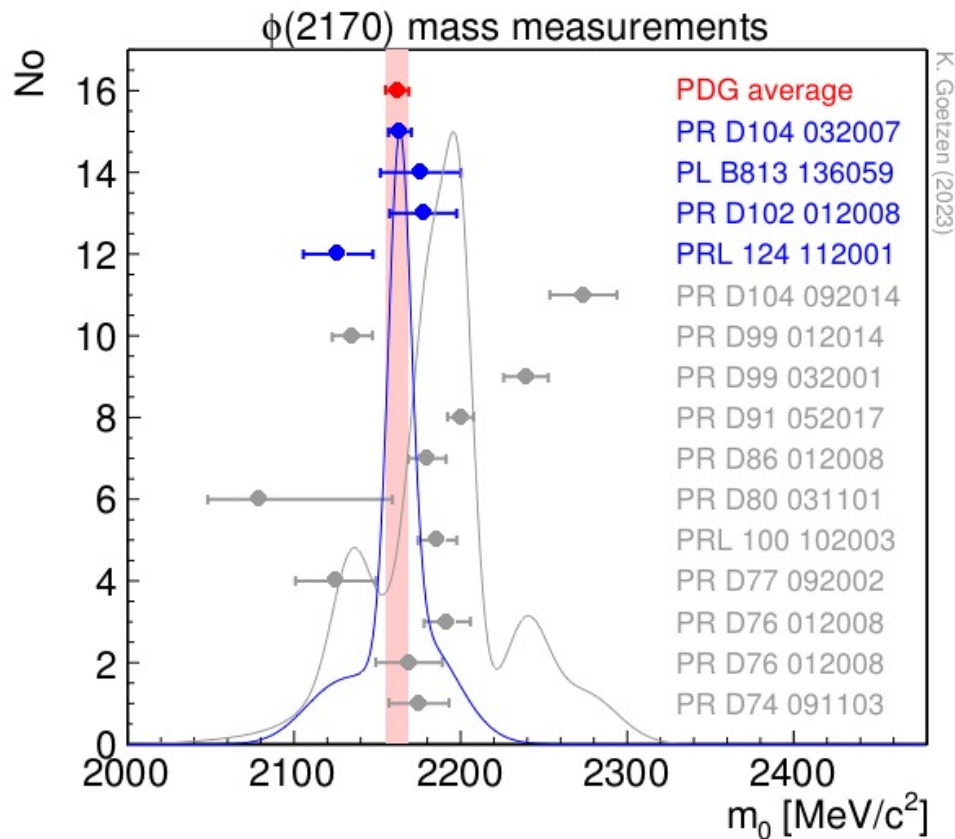
$e^+e^- \rightarrow K^+K^-$ cross section at $\sqrt{s} = 2.00 - 3.08 \text{ GeV}$

$$M = 2239.2 \pm 7.1 \pm 11.3 \text{ MeV}/c^2$$

$$\Gamma = 139.8 \pm 12.3 \pm 20.6 \text{ MeV}$$

PDG: Larger spread in individual resonance parameter measurements, e.g. above

The $Y(2175)$ – strange partner of $Y(4230)$



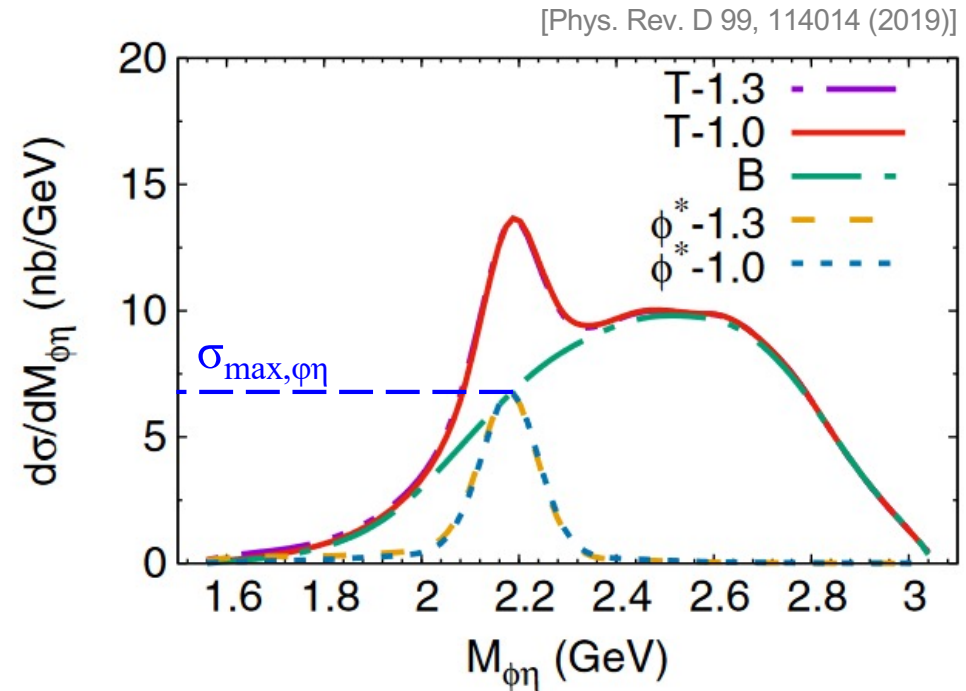
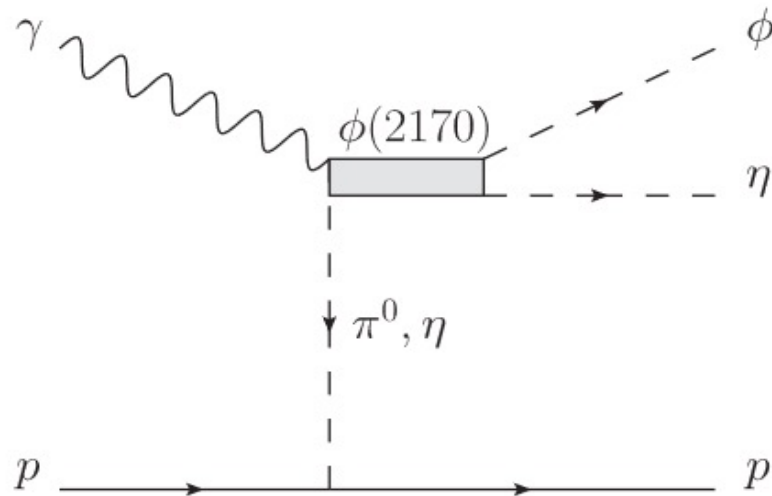
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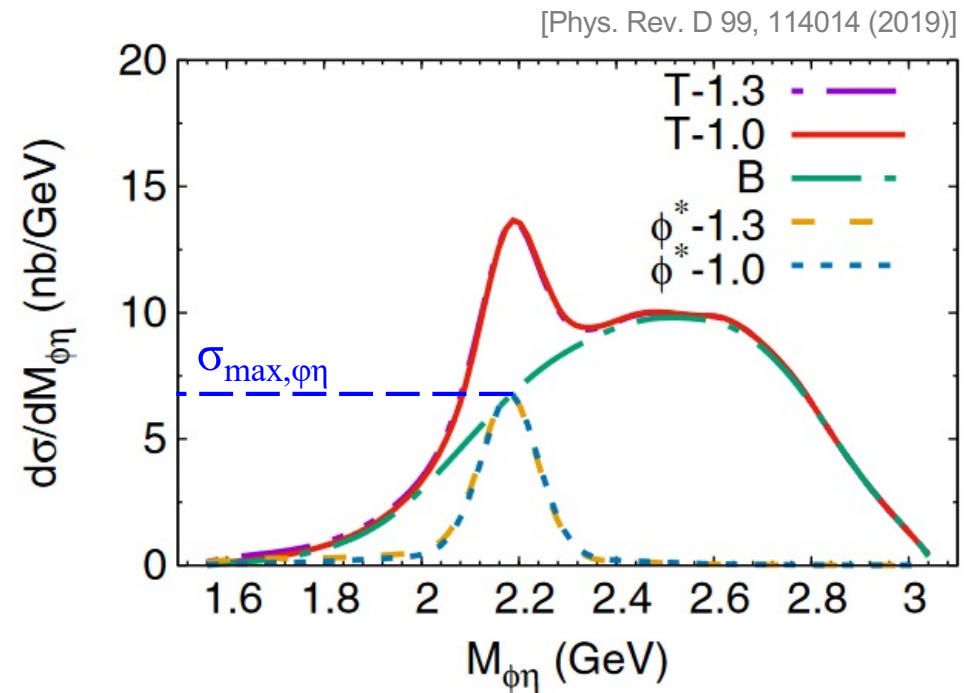
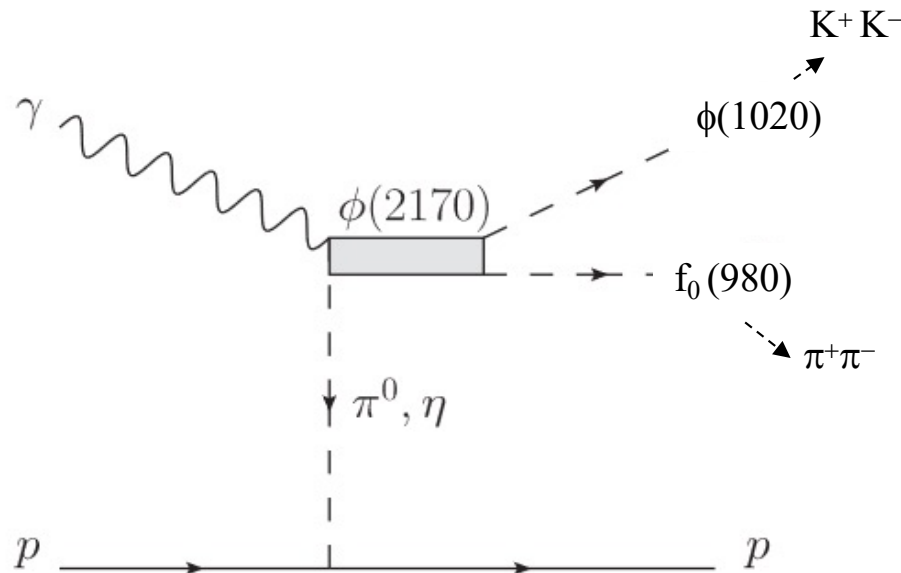
PDG: Larger spread in individual resonance parameter measurements, e.g. above

Prediction for photoproduction



- Investigation of reaction $\gamma p \rightarrow \phi \eta p$ @ $E_\gamma = 8$ GeV
- Assumption: $\Gamma(Y(2175) \rightarrow \phi \eta) \approx 6.6$ MeV (quark model)
- Peak integral: $\sigma_{\phi \eta} \approx 885$ pb (with $\sigma_{\max} \approx 7$ nb, $\Gamma = 83$ MeV/c²)

Study $\phi\pi\pi$ photoproduction



- Investigation of reaction $\gamma p \rightarrow \phi\eta p$ @ $E_\gamma = 8$ GeV
- Assumption: $\Gamma(Y(2175) \rightarrow \phi\eta) \approx 6.6$ MeV (quark model)
- Peak integral: $\sigma_{\phi\eta} \approx 885$ pb (with $\sigma_{\max} \approx 7$ nb, $\Gamma = 83$ MeV/c²)
- $\Gamma(Y(2175) \rightarrow \phi f_0(980)) / \Gamma(Y(2175) \rightarrow \phi\eta) \approx 1.37$
 - For $Y(2175) \rightarrow \phi f_0(980)$: $\sigma_{\phi f_0} \approx 1212$ pb

Timeline	$\int \mathcal{L}$ (pb ⁻¹)
2017	22
2018	103
2020	132
2023	
2024	

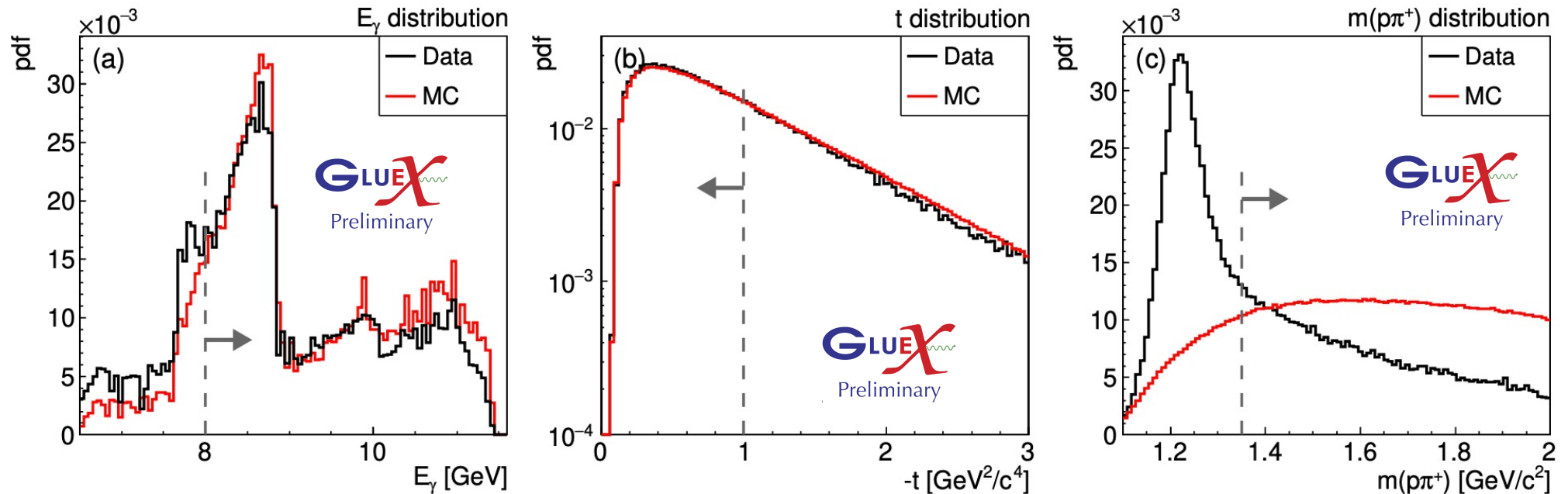
- I)
 - Apply loose PID selection (dE/dx, ToF)
 - Form $\gamma K^+K^-\pi^+\pi^- p$ candidates
 - Perform 4C of $K^+K^-\pi^+\pi^- p$ to γp_{target} system together with
 - Vertex fit of $K^+K^-\pi^+\pi^- p$ system

} event candidates

- II)
 - Apply beam energy cut $E_\gamma > 8 \text{ GeV}$
 - Apply momentum transfer cut $-t < 1 \text{ GeV}^2/c^4$ (fiducial)
 - Apply veto cut for $\Delta^{++}(1232): m > 1.35 \text{ GeV}/c^2$
 - Require $|MM^2| < 50 \text{ MeV}^2/c^4$ for missing mass squared
 - Require $\chi^2_{4C+vtx} < 70$

} event selection cuts

- III)
 - Determine $\phi(1020)$ yield using a Voigtian fctn.

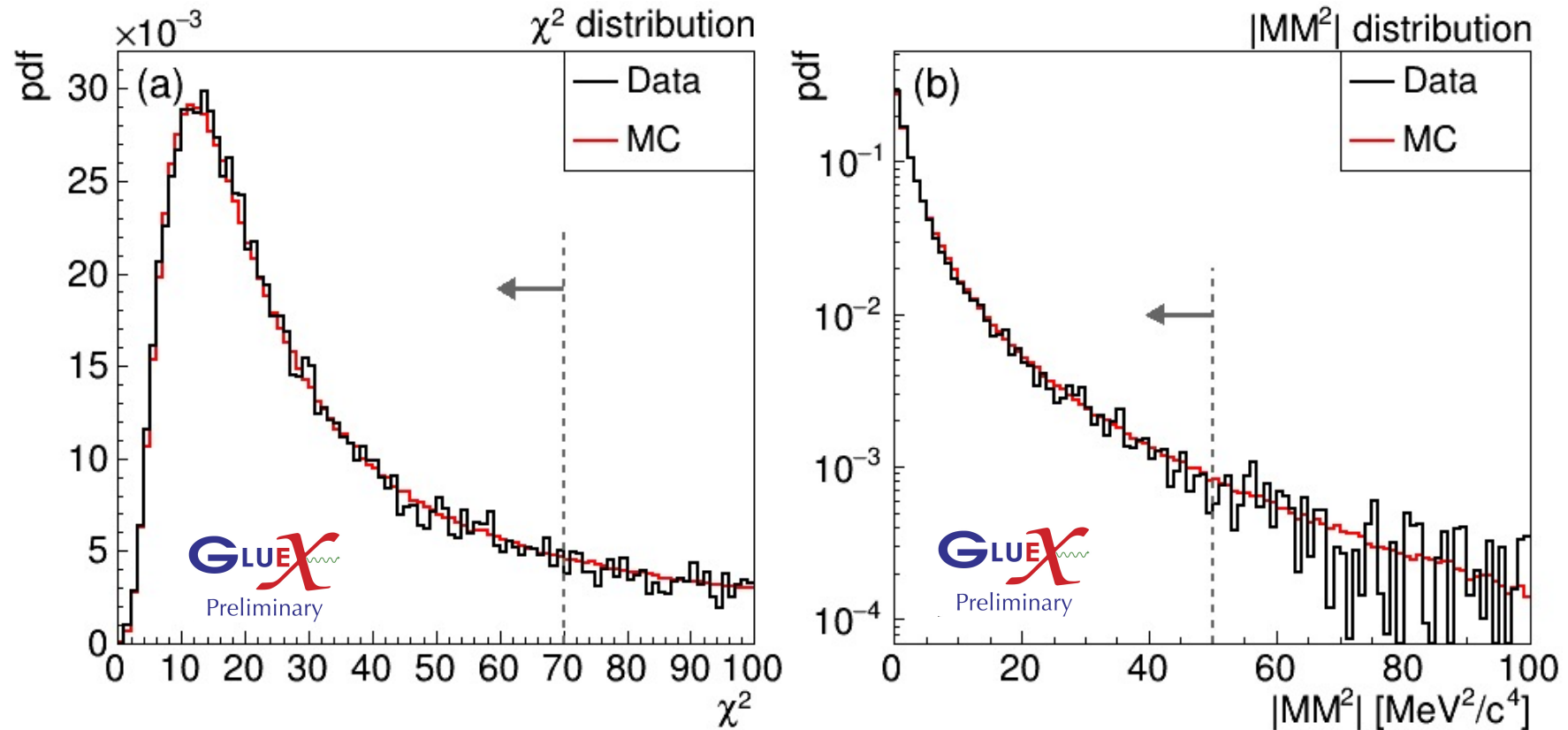


- Photon energy:
 $E_\gamma > 8 \text{ GeV}$

- Momentum transfer:
 $-t < 1 \text{ GeV}^2/c^4$

- Veto $\Delta(1232)^{++}$:
 $m(\pi^+ p) > 1.35 \text{ GeV}/c^2$

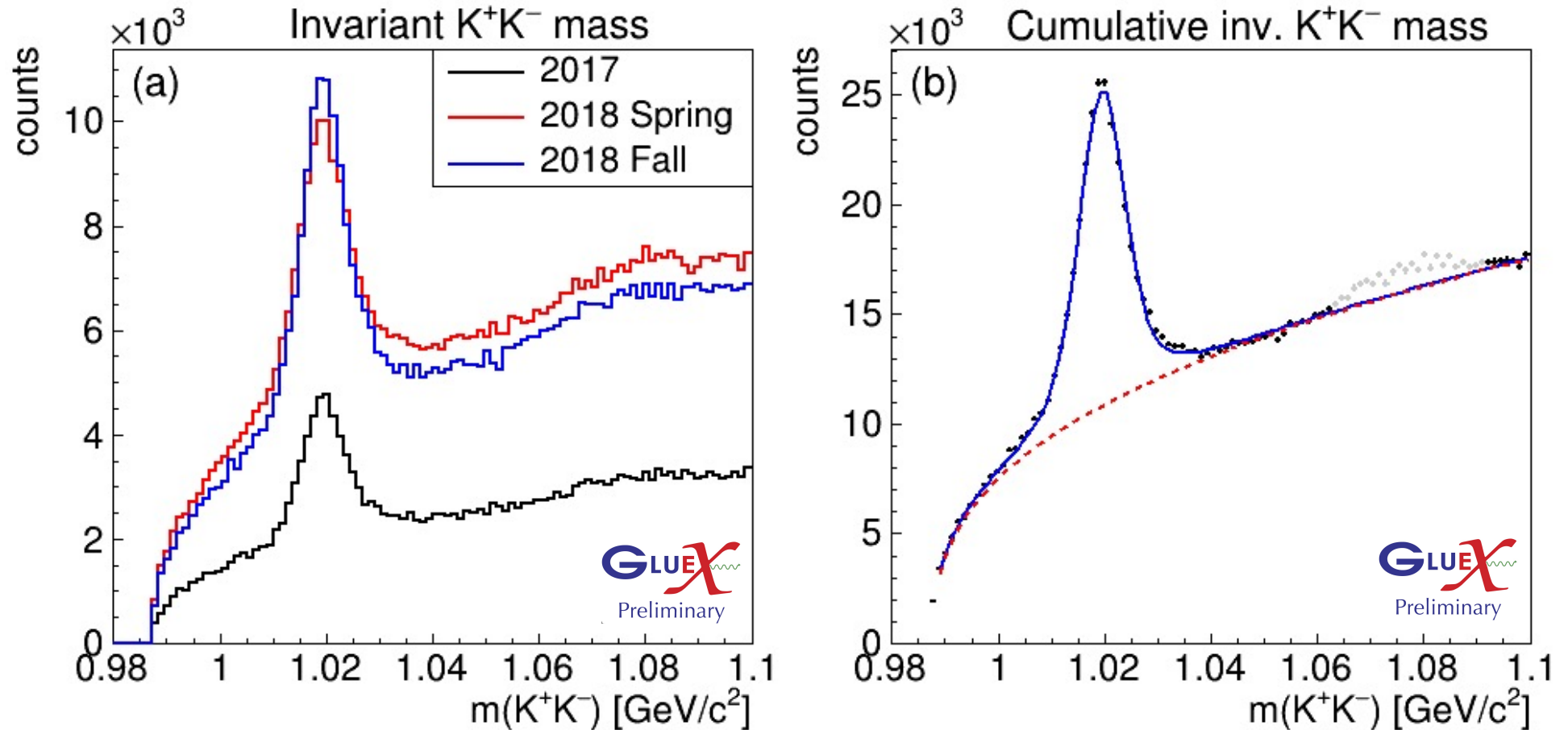
Event selection (II): Kinematics



- 4C and vertex fit quality:
 $\chi^2 < 70$ (ndf = 11)

- Missing mass:
 $|MM^2| < 50 \text{ MeV}^2/c^4$

[K. Goetzen and F. Nerling, behalf of GlueX,
Conf. Proc. HADRON2023 & MESON2023]



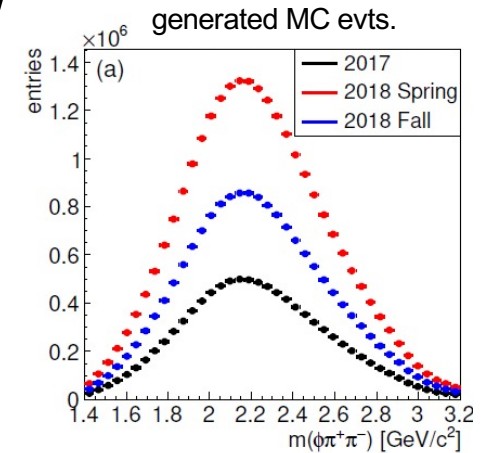
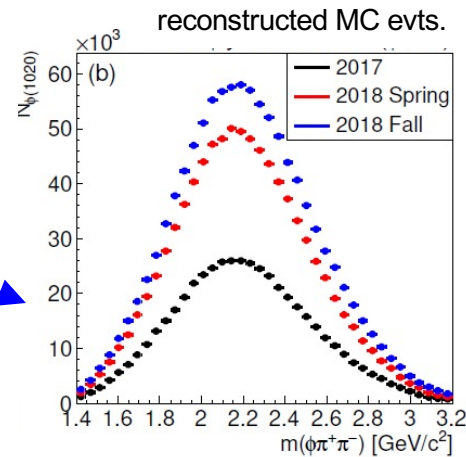
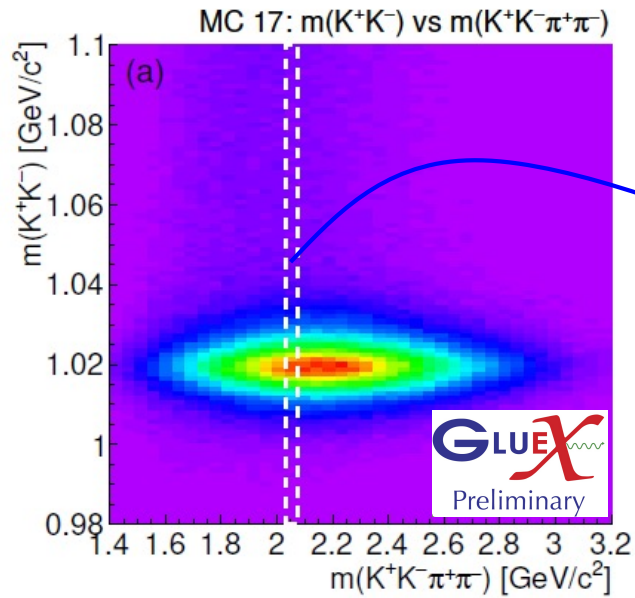
- Fit signal with function ($V =$ Voigtian):

$$f(m) = V(m; m_0, \Gamma_0, \sigma_{\text{res}}) + |m - m_t|^p \cdot e^{-\lambda m} \quad \text{for } m > m_t,$$

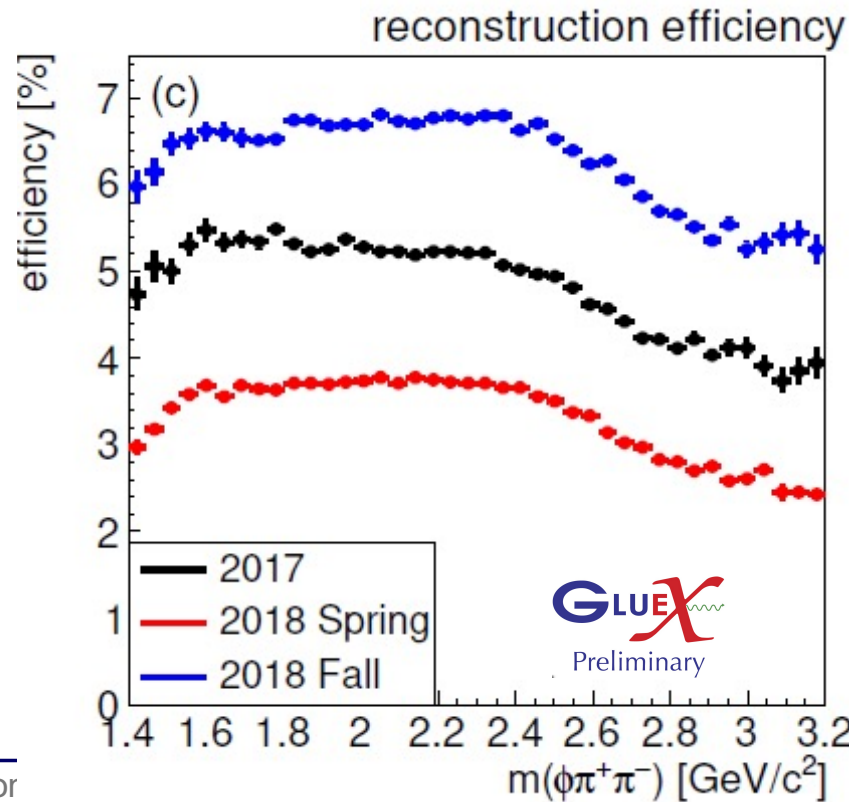
- **Fix ϕ -shape parameters** to extract distributions slice-wise

[K. Goetzen and F. Nerling, behalf of GlueX,
Conf. Proc. HADRON2023 & MESON2023]

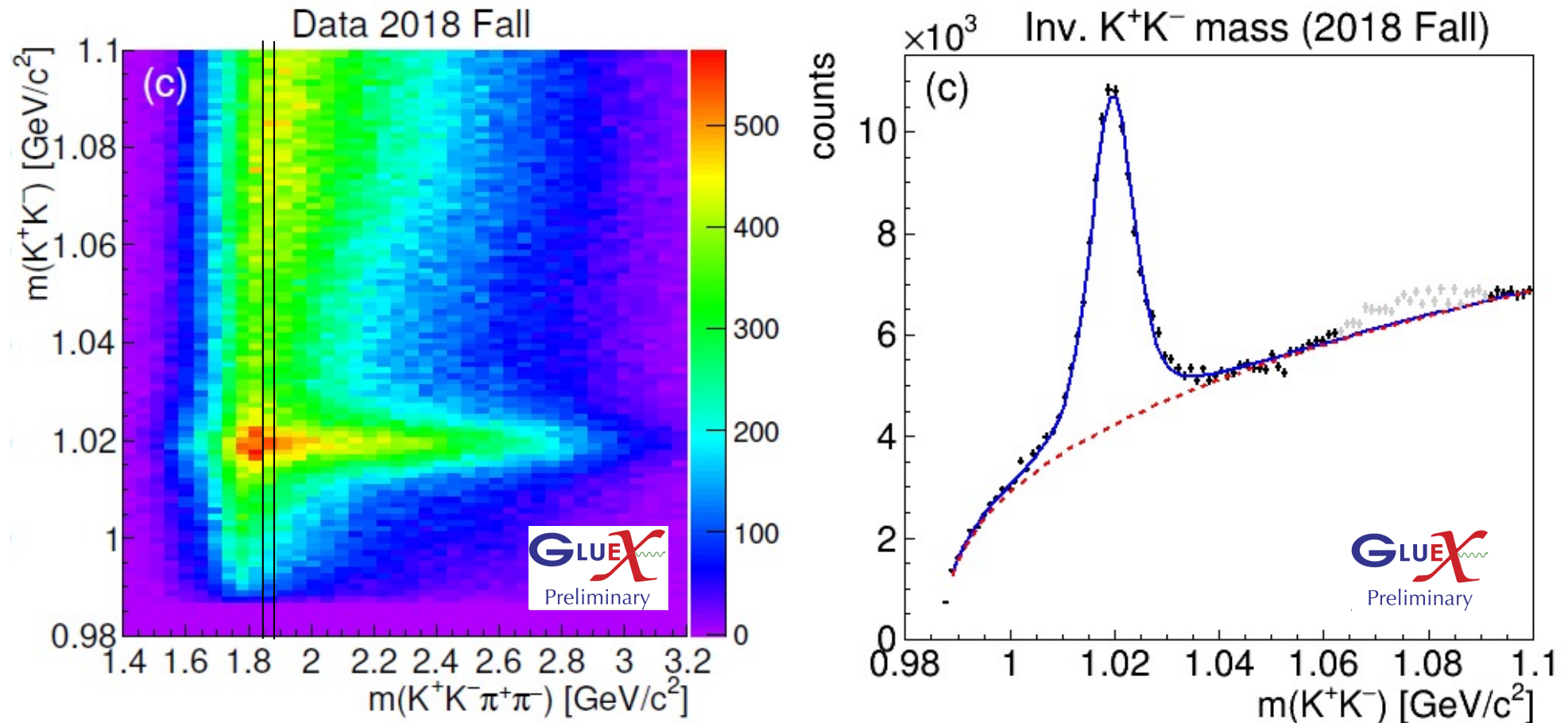
Slice-wise efficiency determination



⇒

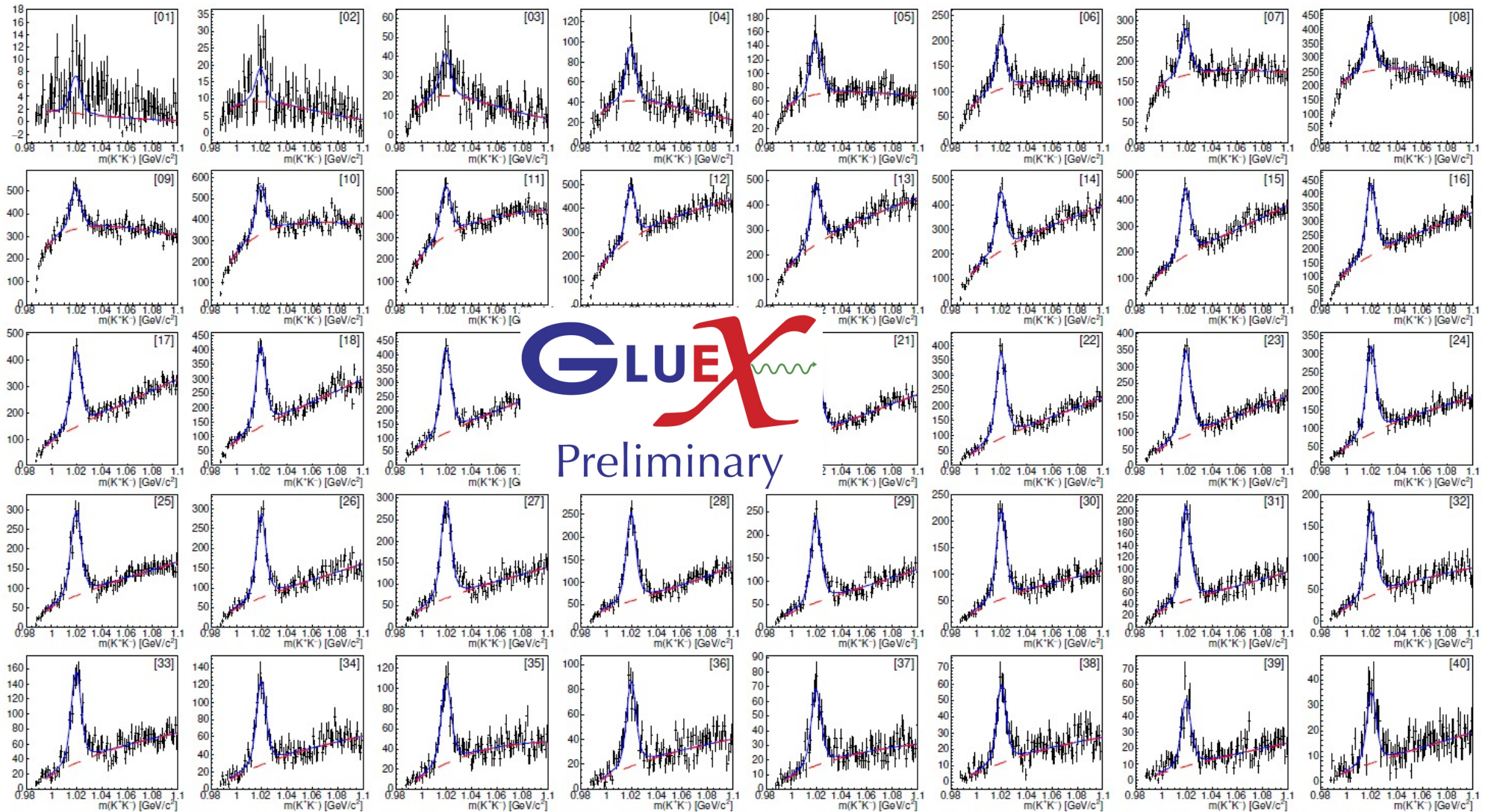


[K. Goetzen and F. Nerling, behalf of GlueX,
Conf. Proc. HADRON2023 & MESON2023]



- Fit yields in 45 MeV slices in 4-body mass with fixed signal shape
- Signal shape parameters m and σ_{res} determined from data (coarse scan)

„Slice-wise ϕ fits“, data

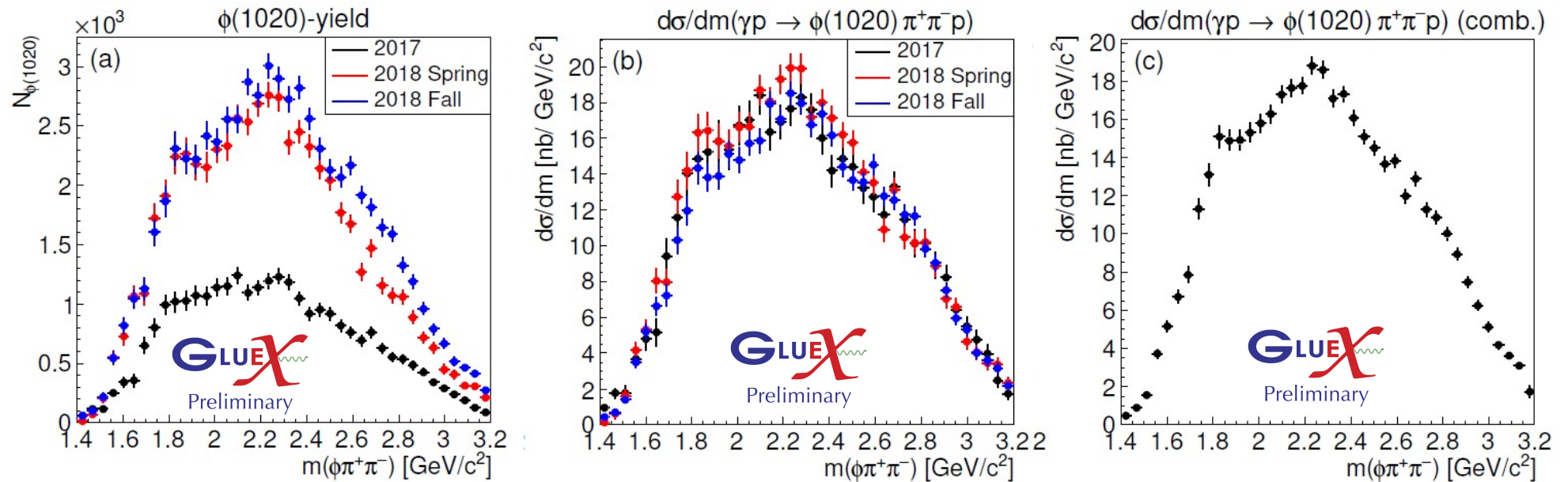


- Single slice fits data (here for 2018 Fall)

[K. Goetzen and F. Nerling, behalf of GlueX, Conf. Proc. HADRON2023 & MESON2023]

- Determine mass-dependent cross section:

$$\frac{d\sigma}{dm}(m_i) = \frac{N_\phi(m_i)}{\varepsilon(m_i) \cdot F \cdot d_{\text{target}} \cdot \mathcal{B}(\phi(1020) \rightarrow K^+ K^-)}$$

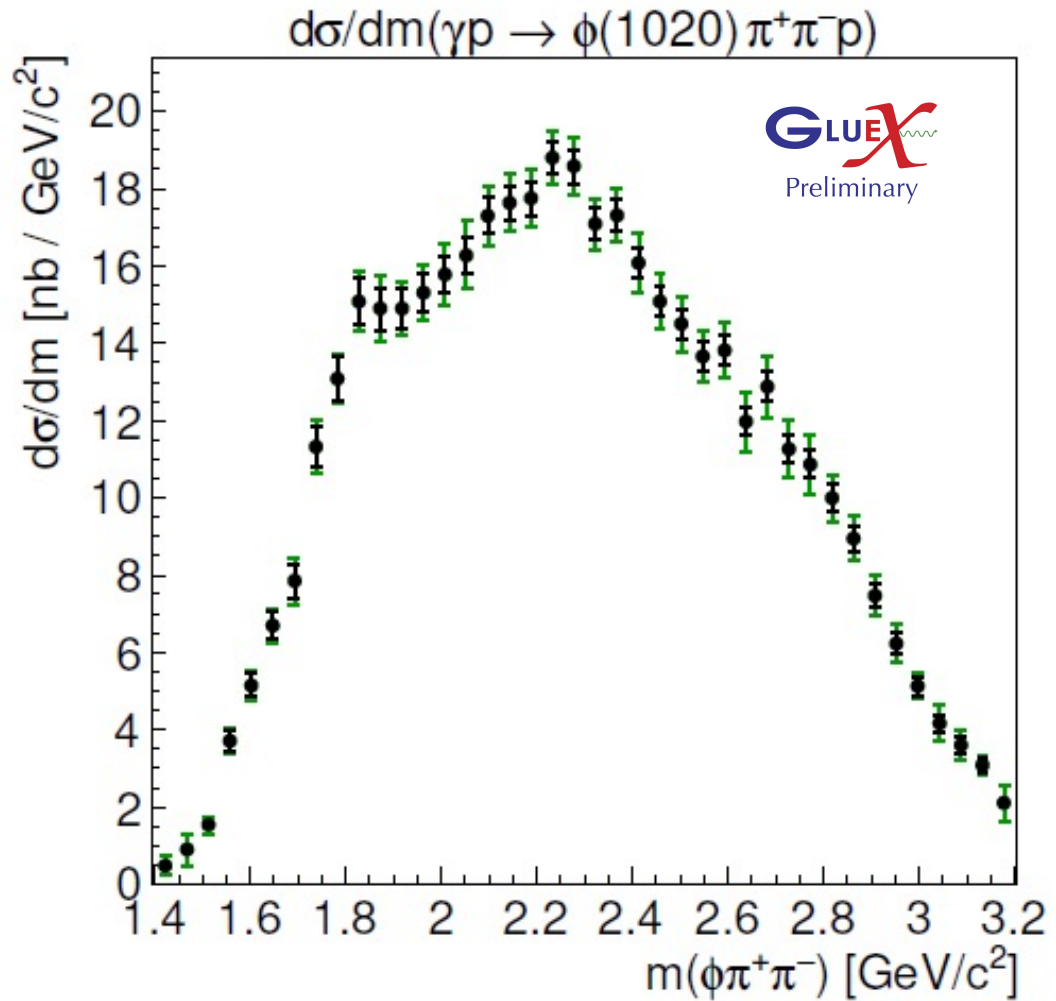


- Combine results by bin-wise via „weighted average“ method:

$$\hat{x} \pm \delta\hat{x} = \frac{\sum_i w_i x_i}{\sum_i w_i} \pm \left(\sum_i w_i^2 \right)^{-1/2} \quad \text{with } w_i = 1/\delta x_i^2$$

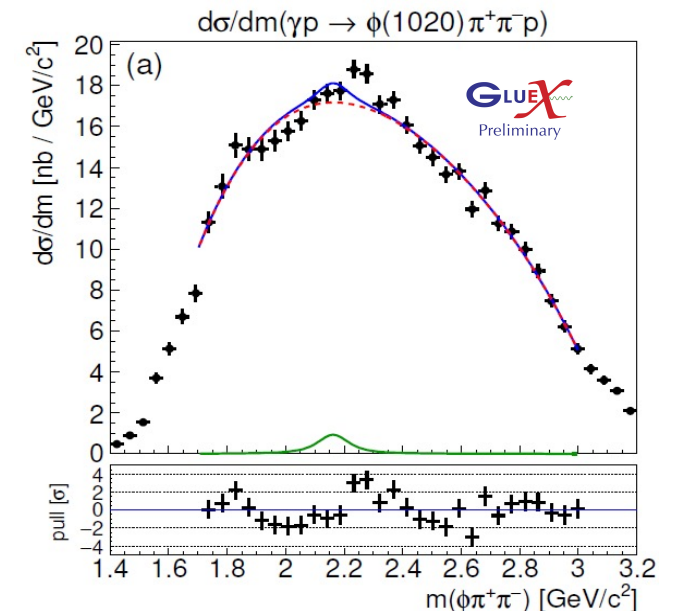
=> Take differences in cross section of default vs. varied fit as systematics

Source	$\delta_{\text{sys,avg}}$ [%]
$\phi(1020)$ branching fraction	1.0
χ^2 requirement	0.9
MM^2 requirement	0.4
Accidentals	0.5
K^+K^- binning	0.7
$\Delta(1232)^{++}$ veto	2.8
$\phi(1020)$ fit model data	0.8
$\phi(1020)$ fit model MC	0.7
$\phi(1020)$ fit range	1.6
$\phi(1020)$ veto range MC	0.5
$\phi(1020)$ integral range MC	0.1
$\phi(1020)$ param. interpolation	0.5
Total systematic uncertainty	4.7

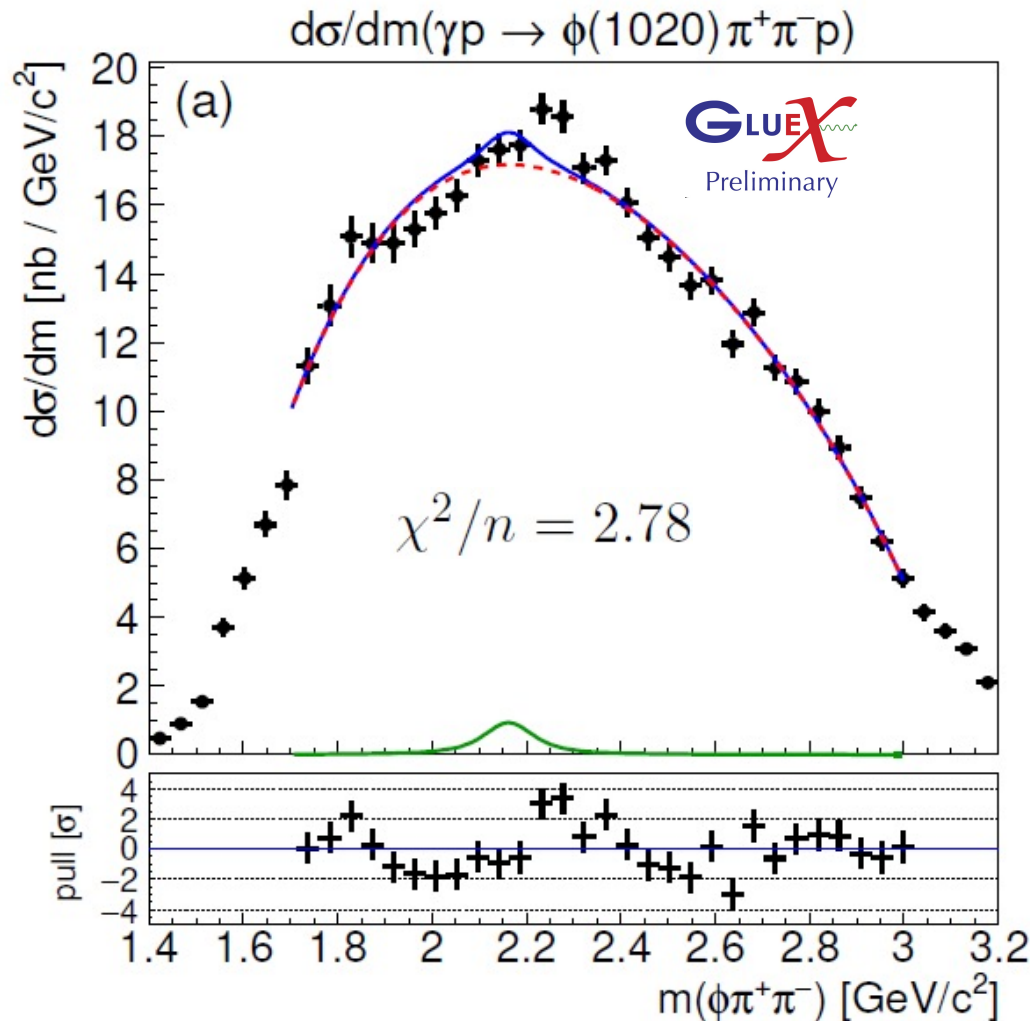


[K. Goetzen and F. Nerling, behalf of GlueX, Conf. Proc. HADRON2023 & MESON2023]

- Fit signal + background in **combined spectrum**
 - **1 Res.:** $f(m) = V(m; m_1, \Gamma_1, \sigma_{\text{res}}) + T_4(m)$
 - **2 Res.:** $f(m) = V_1(m; m_1, \Gamma_1, \sigma_{\text{res}}) + V_2(m; m_2, \Gamma_2, \sigma_{\text{res}}) + T_4(m)$
 - $V = \text{Voigtian}$, $T_4 = 4^{\text{th}}$ order Chebyshev polynomial
- Use **weighted mass resolution** from MC ($\sigma_{\text{res}} = 24.6 \text{ MeV}/c^2$)
- Repeat for each **systematic variation**
- Systematic uncertainty: Difference to nominal result
- Additional systematics are:
 - $m(\phi\pi\pi)$ fit range
 - $m(\phi\pi\pi)$ fit model (degree of bkgd polynomial)
 - $\phi(2170)$ mass m_0 (by $\pm 1\sigma$)
 - $\phi(2170)$ width Γ_0 (by $\pm 1\sigma$)
- And we take the (larger) difference as systematic uncertainty



Fixed $Y(2175)$ parameters – fit a_1



R1: Fixed PDG parameters $Y(2175)$

$$m_{\phi(2170)} = 2162 \pm 7 \text{ MeV}/c^2$$

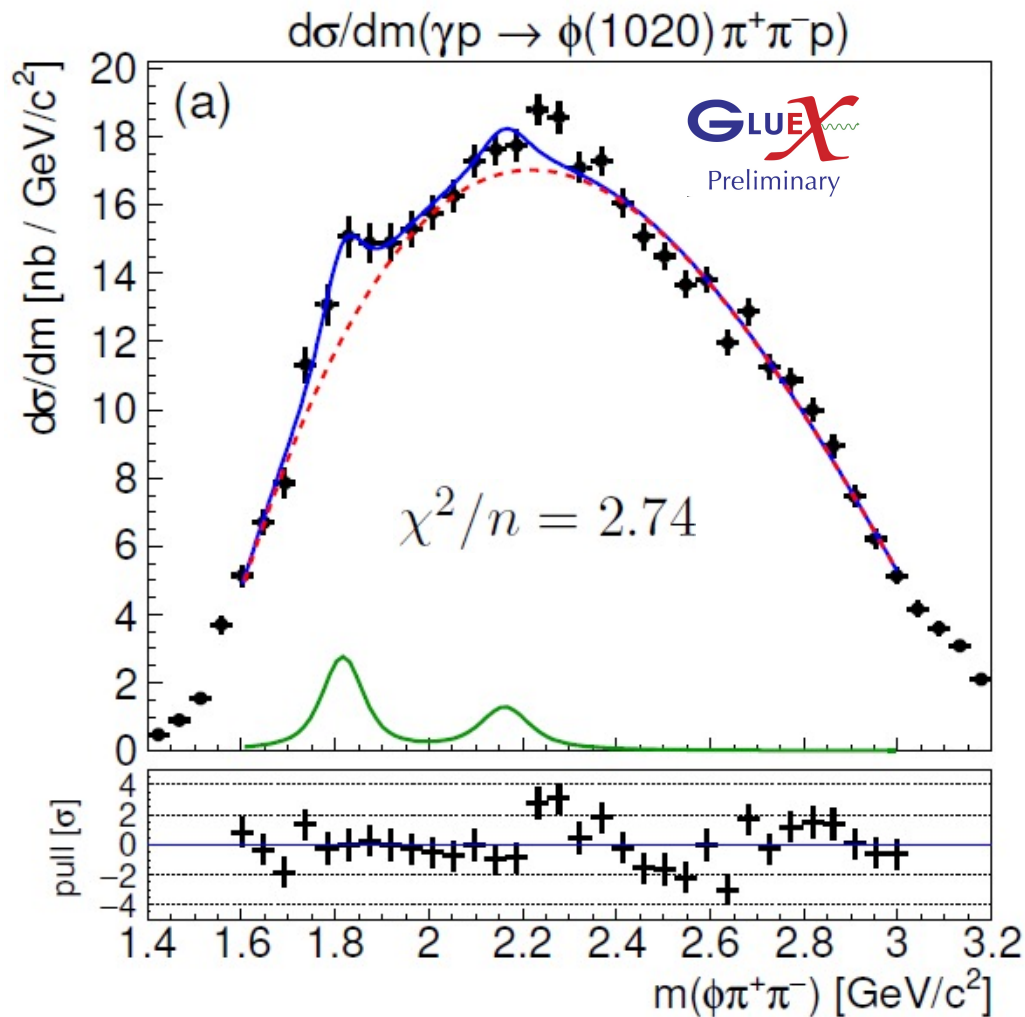
$$\Gamma_{\phi(2170)} = 100^{+31}_{-21} \text{ MeV}/c^2$$

$$\sigma_{\phi(2170)} = 174 \pm 69 \text{ (stat.)} \pm 218 \text{ (sys.) pb}$$

$$\sigma_{\phi(2170)} < 499 \text{ pb (CL90)} \quad [Z = 1.6\sigma \text{ (} 2.1\sigma)]$$

[K. Goetzen and F. Nerling, behalf of GlueX,
Conf. Proc. HADRON2023 & MESON2023]

Fixed Y(2175) parameters – fit a₂



R1: Fixed PDG parameters Y(2175)

$$m_{\phi(2170)} = 2162 \pm 7 \text{ MeV}/c^2$$

$$\Gamma_{\phi(2170)} = 100^{+31}_{-21} \text{ MeV}/c^2$$

R2: Possible structure at $m \sim 1.8 \text{ GeV}$

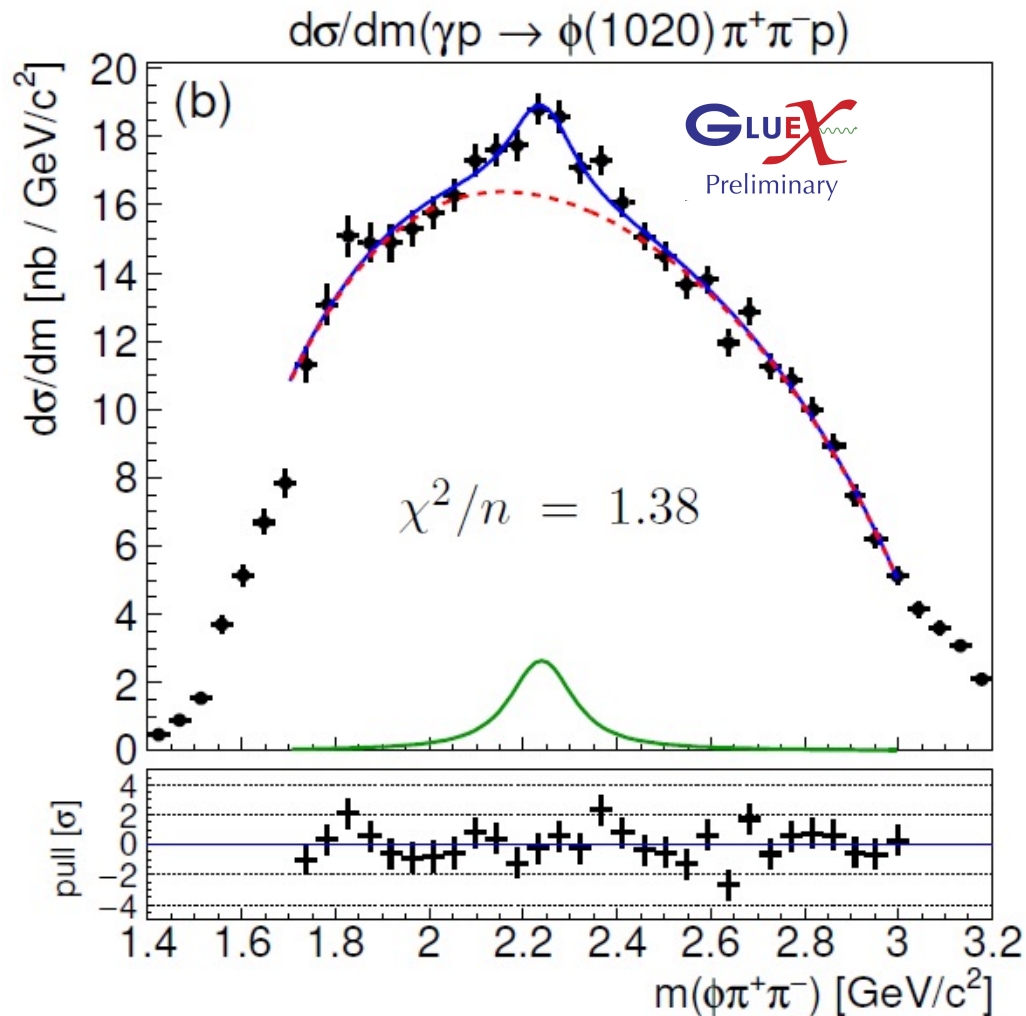
$$\sigma_{X(1800)} < 615 \text{ pb (CL90)}$$

$$\sigma_{\phi(2170)} = 232 \pm 68 \text{ (stat.)} \pm 91 \text{ (sys.) pb}$$

$$\sigma_{\phi(2170)} < 379 \text{ pb (CL90)} \quad [Z = 1.5\sigma \text{ (} 1.8\sigma)]$$

[K. Goetzen and F. Nerling, behalf of GlueX,
Conf. Proc. HADRON2023 & MESON2023]

Fixed $Y(2239)$ parameters – fit b_1

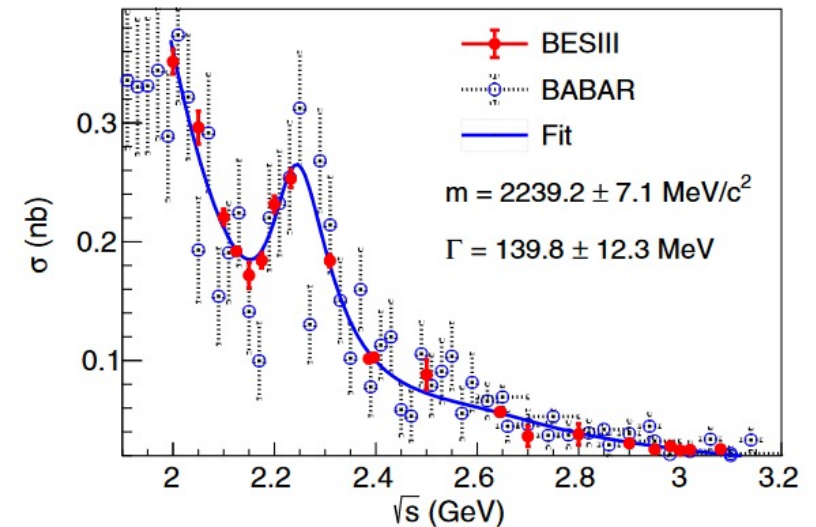


R1: Fixed parameters $Y(2239)$

$$m_{Y(2239)} = 2239.2 \pm 13.4 \text{ MeV}/c^2$$

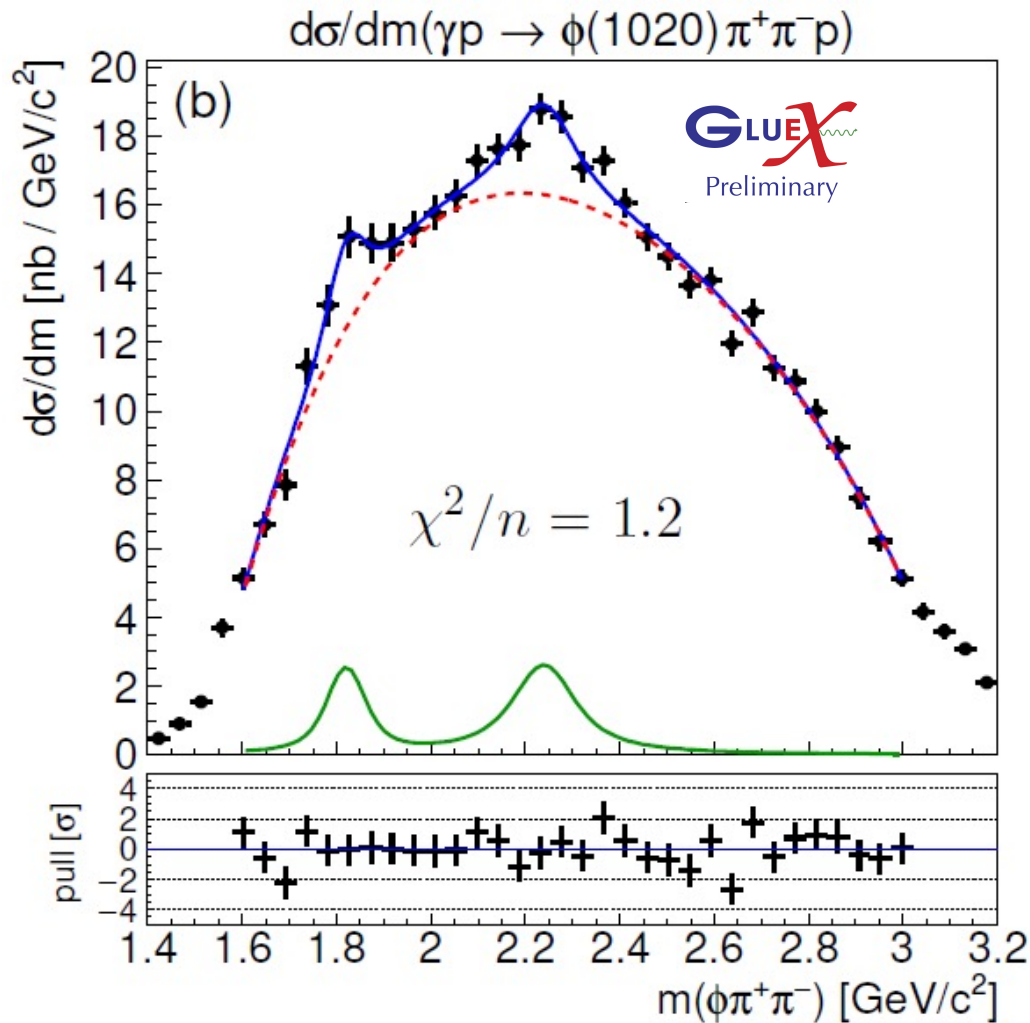
$$\Gamma_{Y(2239)} = 139.8 \pm 24.0 \text{ MeV}/c^2$$

[Phys. Rev. D 99, (2019) 032001]



$$\sigma_{Y(2239)} = 641 \pm 82 \text{ (stat.)} \pm 181 \text{ (sys.) pb}$$

$$\sigma_{Y(2239)} < 896 \text{ pb (CL90)} \quad [Z = 5.7\sigma \text{ (} 6.0\sigma)]$$



R1: Fixed parameters Y(2239)

$$m_{Y(2239)} = 2239.2 \pm 13.4 \text{ MeV}/c^2$$

$$\Gamma_{Y(2239)} = 139.8 \pm 24.0 \text{ MeV}/c^2$$

R2: Possible structure at $m \sim 1.8 \text{ GeV}$:

$$\sigma_{X(1800)} < 701 \text{ pb (CL90)}$$

$$\sigma_{Y(2239)} = 629 \pm 83 \text{ (stat.)} \pm 130 \text{ (sys.) pb}$$

$$\sigma_{Y(2239)} < 826 \text{ pb (CL90)} \quad [Z = 4.7\sigma \text{ (} 5.1\sigma)]$$

[K. Goetzen and F. Nerling, behalf of GlueX,
Conf. Proc. HADRON2023 & MESON2023]

- Analysis of reaction $\gamma p \rightarrow K^+ K^- \pi^+ \pi^- p$
- Measurement of differential $\phi \pi^+ \pi^-$ production cross section $\sigma(\gamma p \rightarrow \phi \pi^+ \pi^- p)$
- Search for $Y(2175)$ + other resonances gives

Case	Cross Section [pb]	UL [pb]	Z_{stat}	Z_{tot}
Fit a ₁ : Y(2175) fixed	$174 \pm 69 \pm 218$	499	2.1	1.6
Fit a ₂ : Y(2175) fixed	$232 \pm 68 \pm 91$	379	1.8	1.5
Fit b ₁ : Y(2239) fixed	$641 \pm 82 \pm 181$	896	6.0	5.7
Fit b ₂ : Y(2239) fixed	$629 \pm 83 \pm 130$	826	5.1	4.7

- Fit with Y(2175) PDG parameters → **no evidence** ($Z < 3\sigma$)
- Alternative fits with Y(2239) parameters (fixed) → **evidence/observation** ($Z > 3$)
- Signal strength of Y(2239) in ball-park of **predicted** $\sigma \approx 1200$ pb
- Find **2nd structure** at around $m \approx 1.8$ GeV/c²
 - UL(CL90): $\sigma < 615$ pb (fit a₂) and $\sigma < 701$ pb (fit b₂)

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**Under internal review for publication
→ paper submission to journal soon**

- **New era** of charmonium-like **exotic states** started two decades ago, and more than 20 unexpected XYZ states have been discovered
 - Supernumerary vector Y states consistently resolved (statistics)
 - *Two structures consistently resolved in all three systems*
 - *$Y(4260)$ and $Y(4360) \rightarrow Y(4230), Y(4390)$?*
 - Charged Z_c states are manifestly exotic states
 - *First complete isospin triplets established*
 - *First strange partner(s) reported, incl. neutral partner*
 - The first of the XYZ states discovered, the X(3872), still not understood
 - *Consistent picture in B decays and e^+e^- production*
 - *Line shape to be measured precisely $\rightarrow p\bar{p}$ annihilation experiment*

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 - Further understand the nature of these exotic states
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Thank you!

Outlook: „QCD at FAIR“ initiative

→ Synergies between hadron physics and heavy-ion communities

