

***Jets and their role in modification***  
 ***$v_4/(v_2)^2$  ratio***

**G. Eyyubova, E. Zabrodin, L. Bravina, L. Malinina**

University of Oslo

Moscow State University

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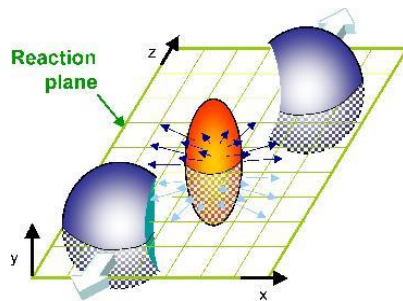
# Outline

- I.  $v_4/(v_2)^2$  ratio
- II. HYDJET++ model
- III. Results

# I. $v_4/(v_2)^2$ ratio

Anisotropic flow

$$\frac{dN}{d\varphi} = \frac{1}{2\pi} \left( 1 + \sum_{n=1}^{\infty} 2v_n(p_t) \cos[n(\varphi - \psi_r)] \right)$$



# Predictions

*N. Borghini, J.-Y. Ollitrault, PLB 642 (2006) 227*

- Within the *approximation* that the particle momentum  $\mathbf{p}$  and the fluid velocity  $\mathbf{v}$  are parallel (valid for *large momentum*  $p_{\perp}$  and *low freeze-out temperature*  $T$ )

$$dN/d\varphi = \exp(2\varepsilon p_{\perp} \cos(2\varphi)/T)$$

- Expanding to order  $\varepsilon$ , the  $\cos(2\varphi)$  term is

$$v_2 = \varepsilon p_{\perp}/T$$

- Expanding to order  $\varepsilon^2$ , the  $\cos(4\varphi)$  term is

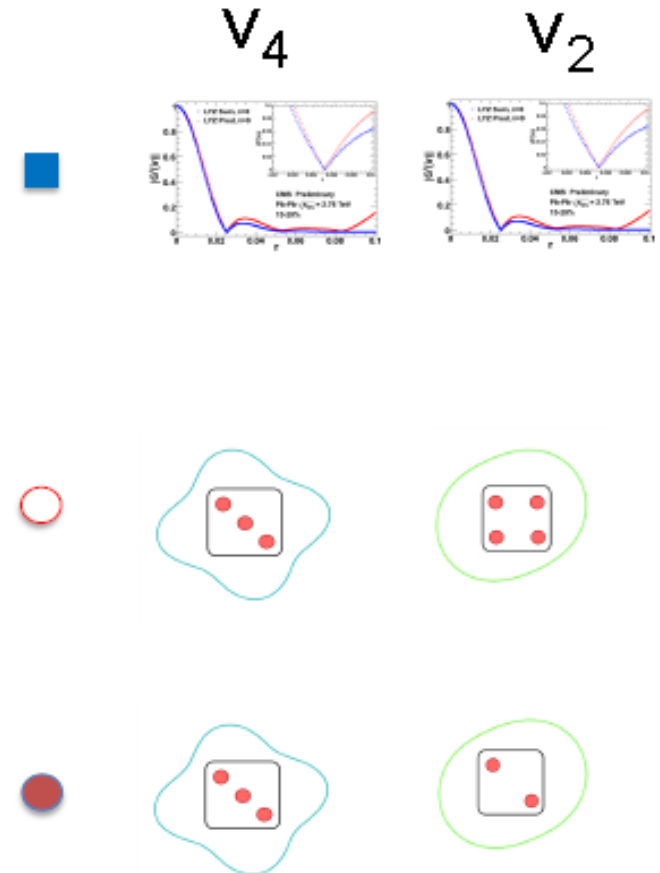
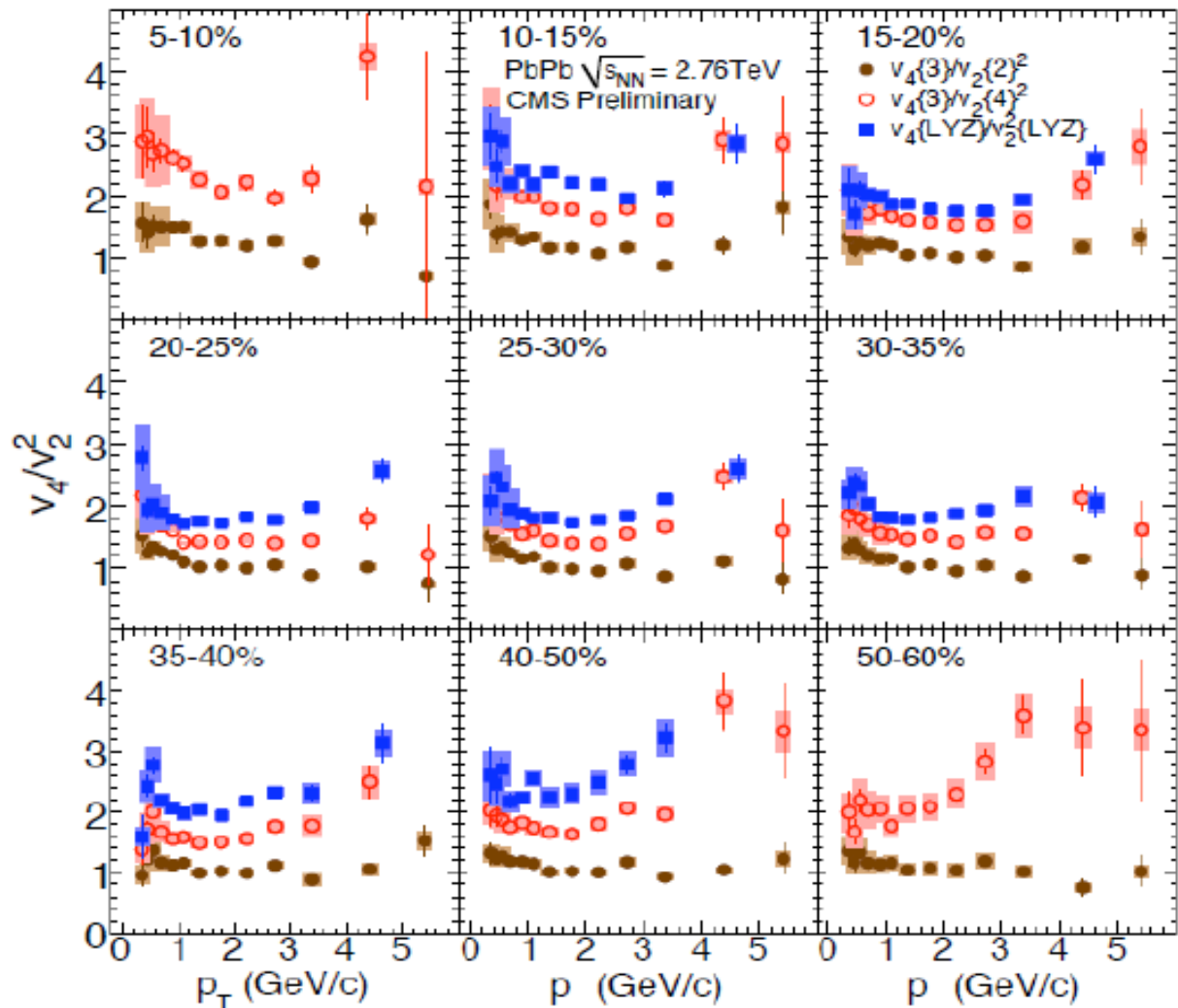
$$v_4 = \frac{1}{2} (v_2)^2$$

Hydrodynamics has a universal prediction for  $v_4/(v_2)^2$  !

Should be independent of equation of state, initial conditions, centrality, rapidity, particle type

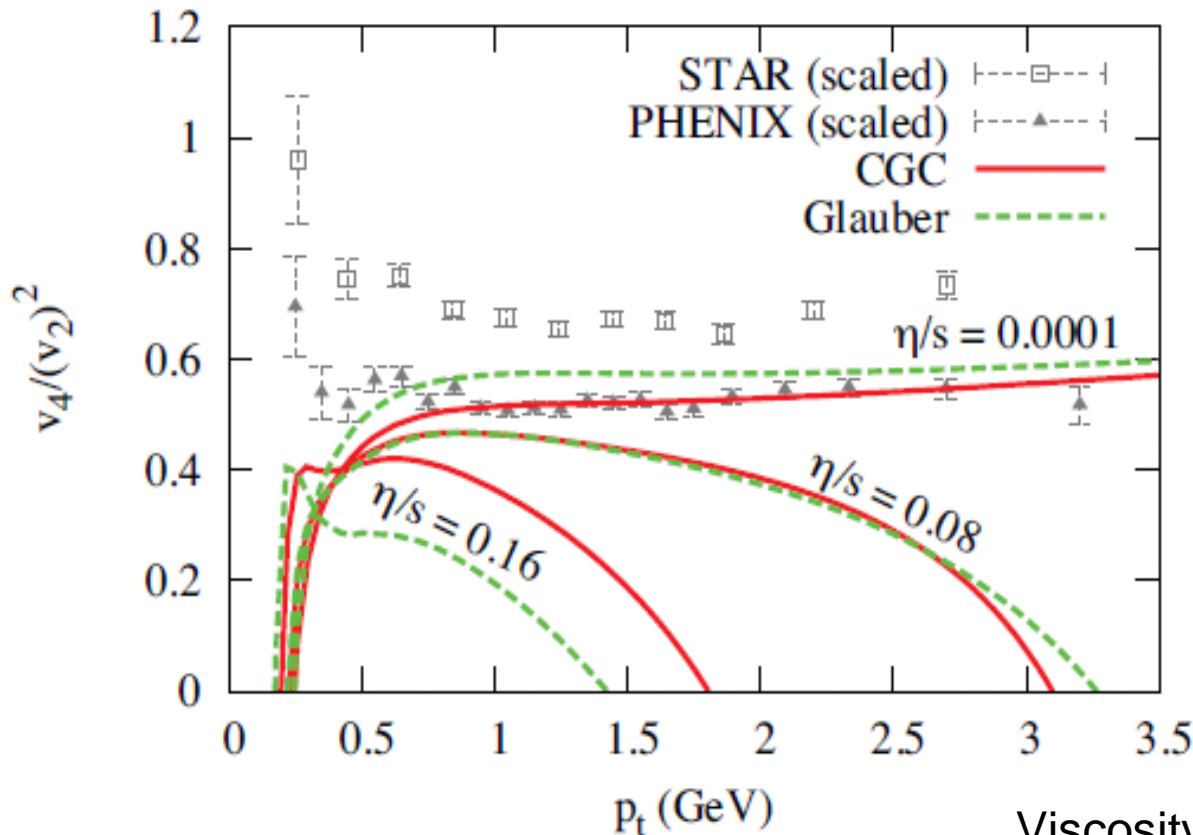
# Experiment

$v_4 / v_2^2(p_T)$  at mid-rapidity  $|\eta| < 0.8$



Significantly higher than RHIC: experimental method dependent

# Effects of initial profile and viscosity

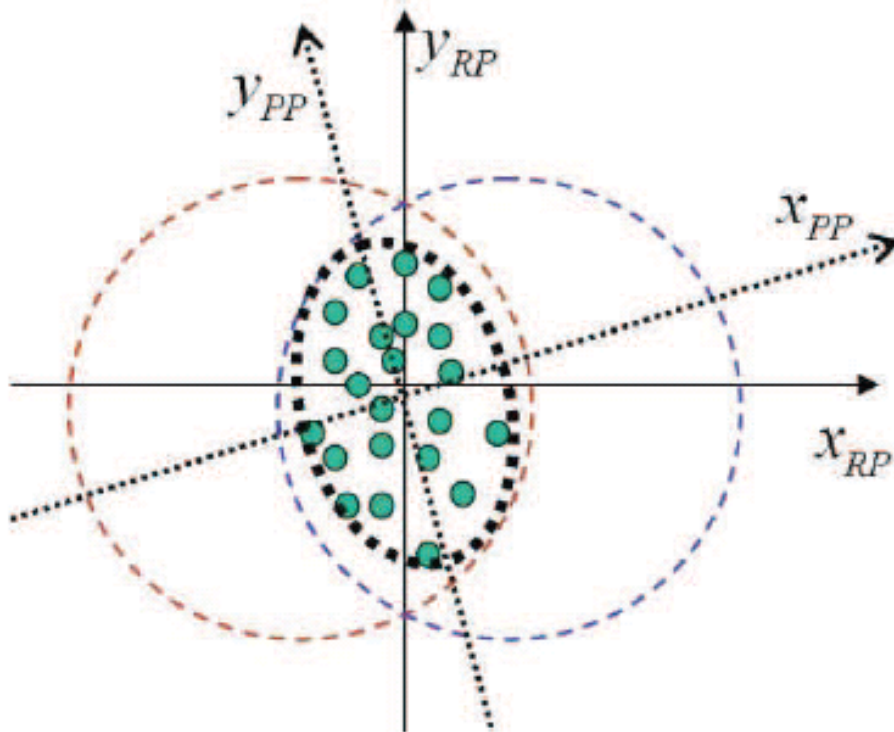


Initial profile has little effect although eccentricities differ.

results strongly depend on viscosity

Viscosity lowers  $v_4/(v_2)^2$  for a realistic  $T_f$

# Eccentricity fluctuations



Depending on where the participant nucleons are located within the nucleus at the time of the collision, the actual shape of the overlap area may vary: the **orientation and eccentricity** of the ellipse defined by participants fluctuates.

Assuming that  $v_2$  scales like the eccentricity, **eccentricity fluctuations** translate into  **$v_2$  fluctuations**

Eccentricity fluctuation can be computed in MC Glauber model or derived from experiment by comparing different methods for flow calculation.



# Why $\varepsilon$ fluctuations change $v_4/v_2^2$

Experimentally, no direct measure of  $v_2$  and  $v_4$

$v_2$  and  $v_4$  are measured via azimuthal correlations

$$v_2 \text{ from } \langle \cos(2\phi_1 - 2\phi_2) \rangle = \langle (v_2)^2 \rangle$$

$$v_4 \text{ from } \langle \cos(4\phi_1 - 2\phi_2 - 2\phi_3) \rangle = \langle v_4 (v_2)^2 \rangle$$

Experimentally measured

$$\frac{v_4}{v_2^2} = \frac{\langle v_4 (v_2)^2 \rangle}{\langle (v_2)^2 \rangle^2} = \frac{1}{2} \frac{\langle (v_2)^4 \rangle}{\langle (v_2)^2 \rangle^2} > \frac{1}{2}$$

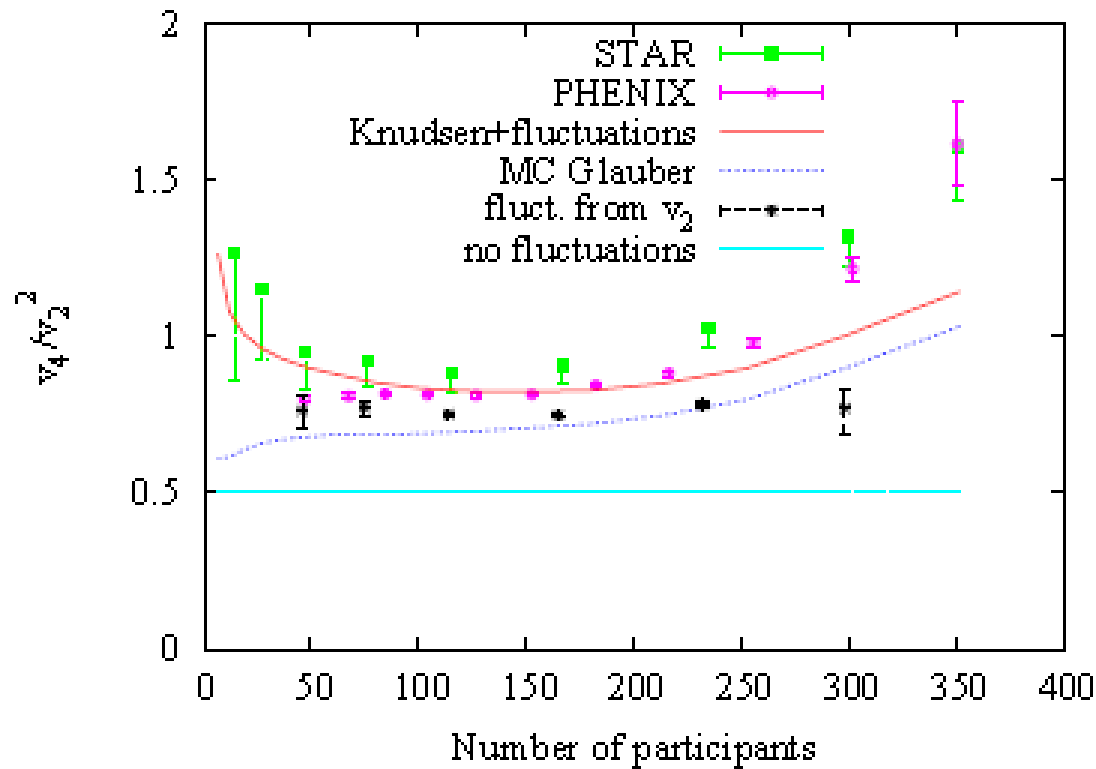
fluctuations

hydro

Similar results obtained using Event Plane method



# Effects of flow fluctuations and partial thermalization



Stars: with fluctuations inferred from the difference between  $v_2\{2\}$  and  $v_2\{LYZ\}$ .  
Dotted line: eccentricity fluctuations from a Monte-Carlo Glauber

[M. Luzum](#), [C.Gombeaud](#), [J.Y Ollitrault](#), [Phys.Rev.C81:054910,2010](#).

## II. HYDJET++ model

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The Ratio was proposed to be investigated within HYDJET++ by K. Redlich at last TORIC workshop (Sardinia, 2010)

# HYDJET++ Monte-Carlo model for relativistic heavy ion collisions

- HYDJET++ (HYDroynamics + JETs) merges two components :
- soft hydro-type component
  - hard multi-parton component

*N.S.Amelin, R.Lednisky, T.A.Pocheptsov, I.P.Lokhtin, L.V.Malinina, A.M.Snigirev, Yu.A.Karpenko, Yu.M.Sinyukov, Phys. Rev. C 74 (2006) 064901*

*N.S.Amelin, R.Lednisky, I.P.Lokhtin, L.V.Malinina, A.M.Snigirev, Yu.A.Karpenko, Yu.M.Sinyukov, I.C.Arsene, L.Bravina, Phys. Rev. C 77 (2008) 014903*

*I.P.Lokhtin, A.M.Snigirev, Eur. Phys. J. 45 (2006) 211*

*K.Tywoniuk, I.Arsene, L.Bravina, A.Kaidalov and E.Zabrodin, Phys. Lett. B 657 (2007) 170*

## **HYDJET++(hard): PYQUEN (PYthia QUENched)**

PYQUEN event generator is used for simulation of rescattering, radiative and collisional energy loss of hard partons in expanding quark-gluon plasma

HYDJET++ includes nuclear shadowing correction for parton distributions  
Impact-parameter dependent parameterization of *nuclear shadowing*

**HYDJET++(soft): FASTMC generator**      Not really hydro evolution  
But fast MC procedure

- A hydrodynamic expansion of the fireball is supposed ends by a sudden system breakup at given  $T$  and chemical potentials. Momentum distribution of produced hadrons keeps the thermal character of the equilibrium distribution.
- multiplicities are determined assuming thermal equilibrium
- hadrons are produced on the hypersurface represented by a parameterization of relativistic hydrodynamics with given freeze-out conditions
- chemical and kinetic freeze-outs are separated
- decays of hadronic resonances are taken into account (360 particles )

## HYDJET++ (hard): input parameters

initial QGP temperature  $T_0$ , at LHC:  $T_0=1$  GeV, at RHIC(200 AGeV)  $T_0=0.300$  GeV  
QGP formation time  $\tau_0$ , at LHC:  $\tau_0=0.1$  fm/c, at RHIC(200 AGeV)  $\tau_0=0.4$  fm/c  
number of active quark flavors in QGP  $N_f$  (+ minimal  $p_T$  of hard process  $P_{tmin}$ )

## HYDJET++ (soft): input parameters

1-5. Thermodynamic parameters at chemical freeze-out:  $T^{ch}$ ,  $\{\mu_B, \mu_S, \mu_C, \mu_Q\}$  (option to calculate  $T^{ch}$ ,  $\mu_B$  and  $\mu_S$  using phenomenological parameterization  $\mu_B(\sqrt{s})$ ,  $T^{ch}(\mu_B)$  is foreseen).

6-7. Strangeness suppression factor  $\gamma_S \leq 1$  and charm enhancement factor  $\gamma_c \geq 1$  (options to use phenomenological parameterization  $\gamma_S(T^{ch}, \mu_B)$  and to calculate  $\gamma_c$  are foreseen).

8-9. Thermodynamical parameters at thermal freeze-out:  $T^{th}$ , and  $\mu_\pi$  - effective chemical potential of positively charged pions.

10-12. Volume parameters at thermal freeze-out: proper time  $\tau_f$ , its standard deviation (emission duration)  $\Delta\tau_f$ , maximal transverse radius  $R_f$ .

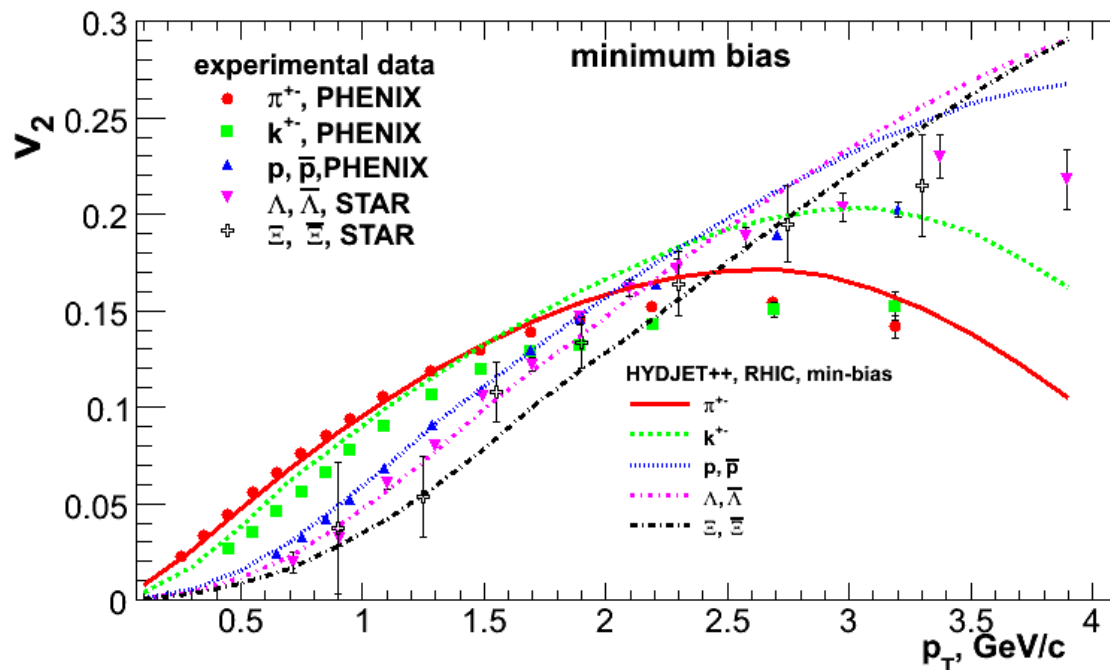
13. Maximal transverse flow rapidity at thermal freeze-out  $\rho_u^{max}$ .

14. Maximal longitudinal flow rapidity at thermal freeze-out  $\eta^{max}$ .

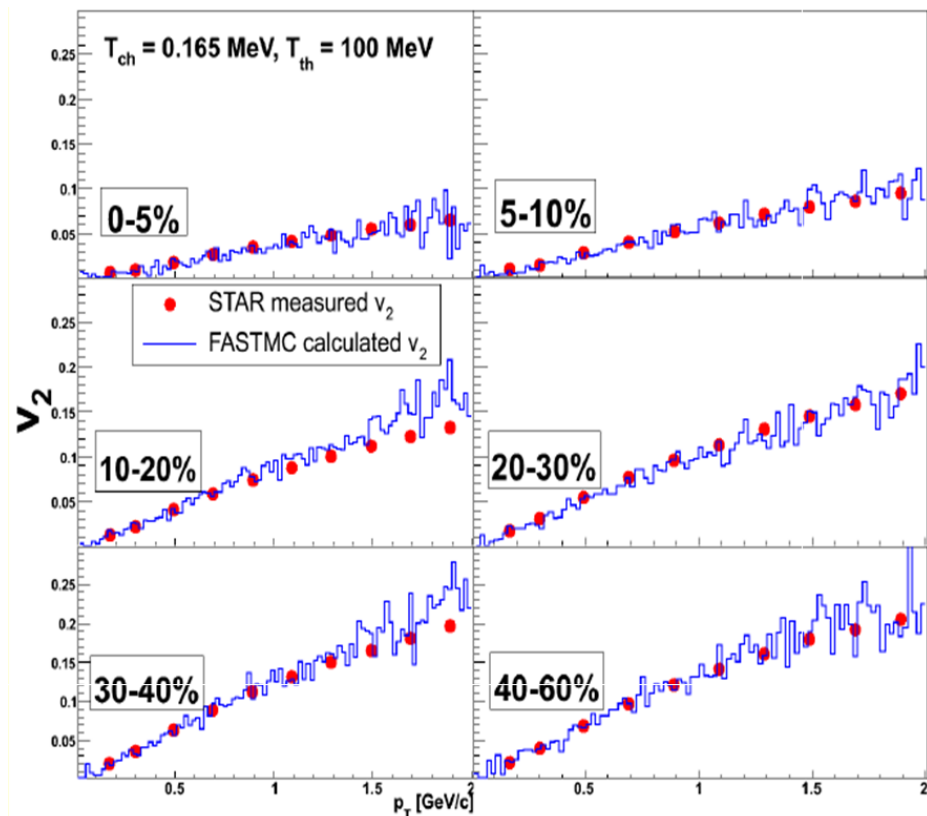
15. Flow anisotropy parameter:  $\delta(\mathbf{b}) \rightarrow u^\mu = u^\mu(\delta(\mathbf{b}), \varphi)$

16. Coordinate anisotropy:  $\varepsilon(\mathbf{b}) \rightarrow R_f(\mathbf{b}) = R_f(0) [V_{eff}(\varepsilon(0), \delta(0)) / V_{eff}(\varepsilon(\mathbf{b}), \delta(\mathbf{b}))]^{1/2} [N_{part}(\mathbf{b}) / N_{part}(0)]^{1/3}$

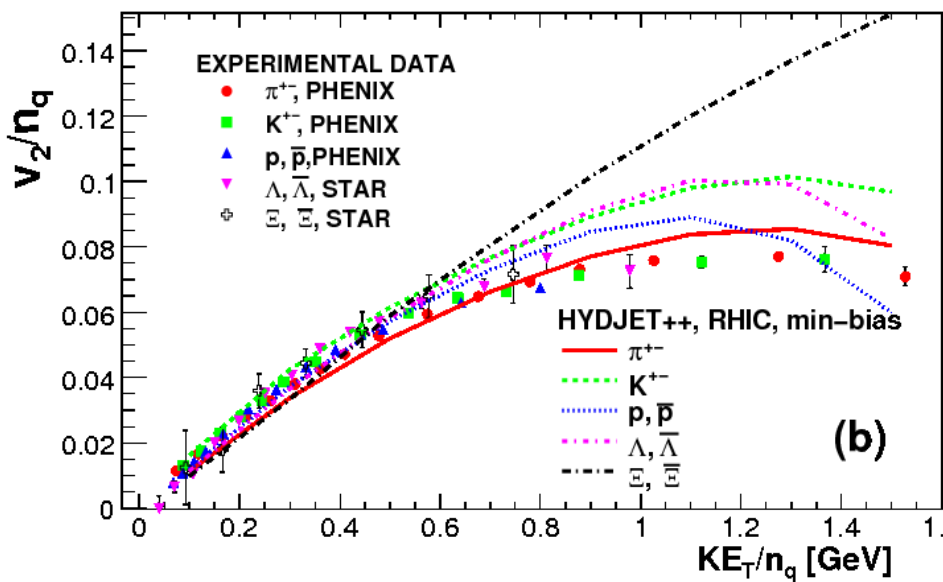
# RHIC data vs. HYDJET++ model



## Elliptic flow



G. Eyyubova et al., PRC 80 (2009) 064907;  
N.S. Amelin et al., PRC 77 (2008) 014903

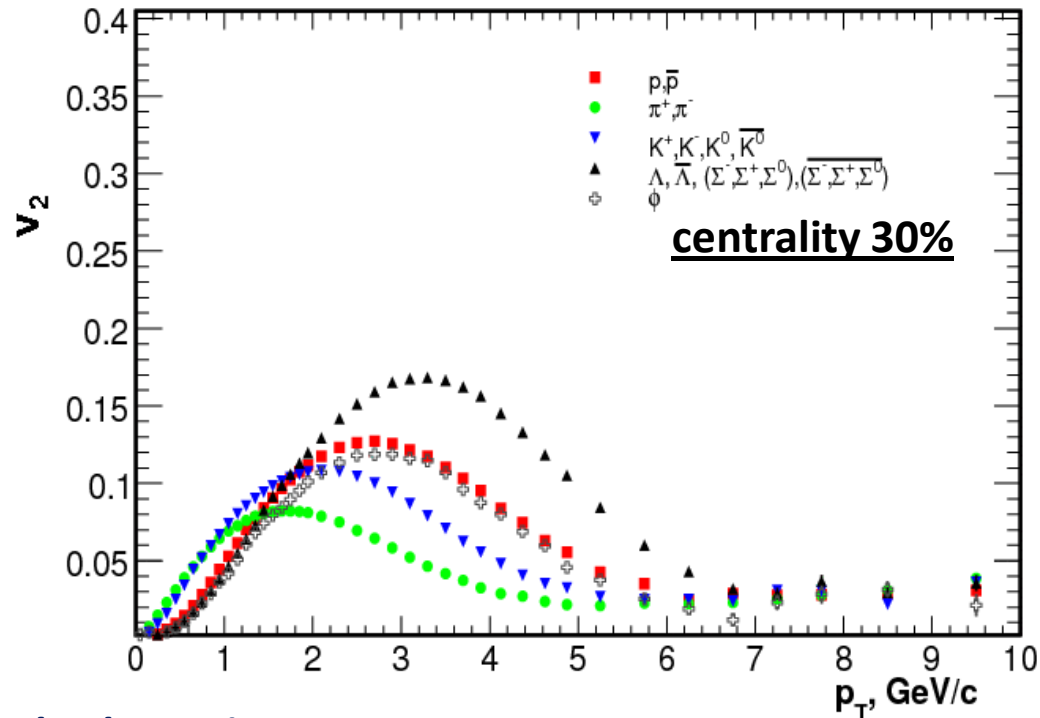


G. Eyyubova, L.V. Bravina, V.L. Korotkikh,  
I.P.Lokhtin, L.V. Malinina, S.V. Petrushanko,  
A.M. Snigirev, E. Zabrodin, Phys. Rev. C 80  
(2009) 064907



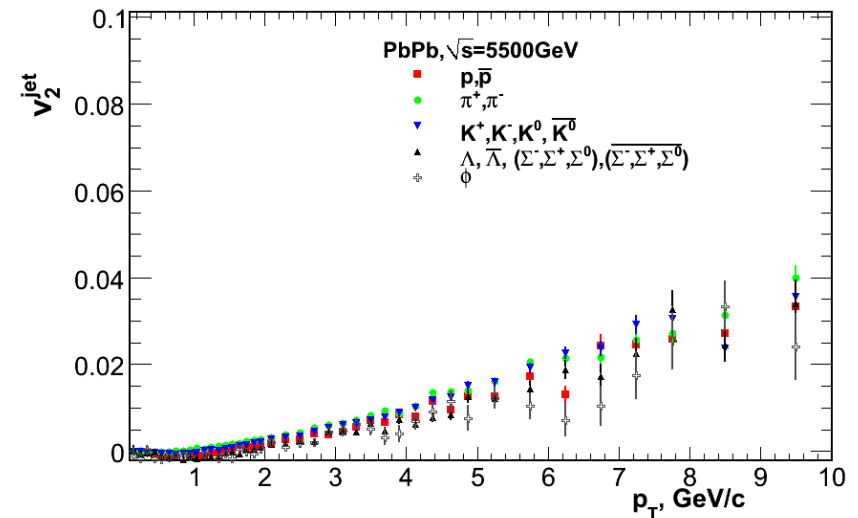
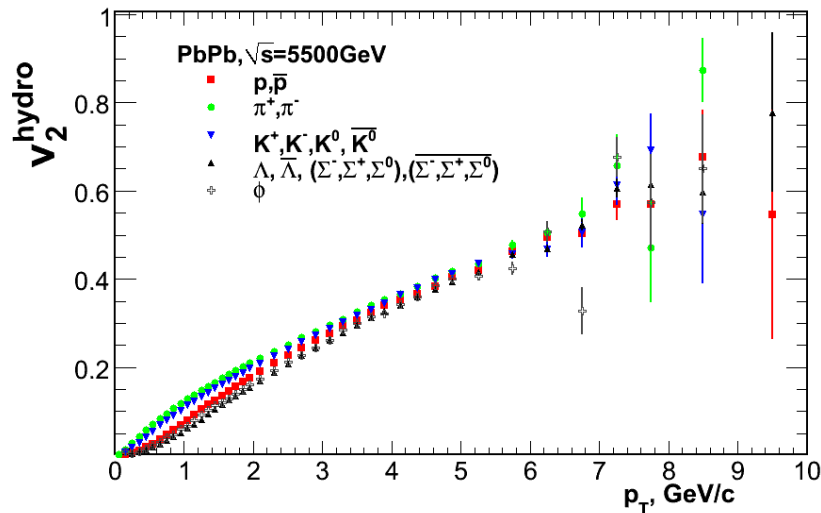
# III. Results

# Interplay between hydro and jet part in the model



*Hydrodynamics*

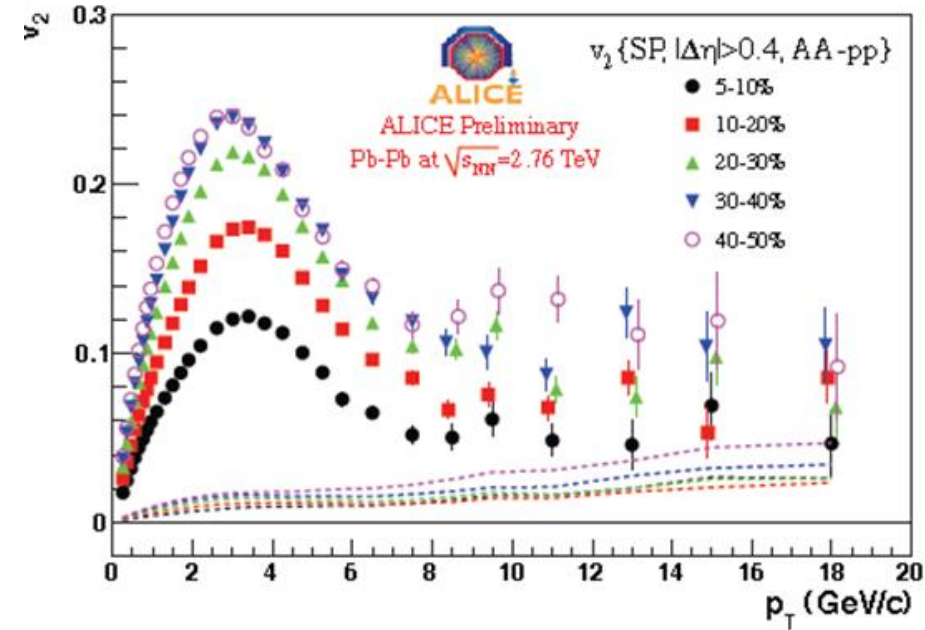
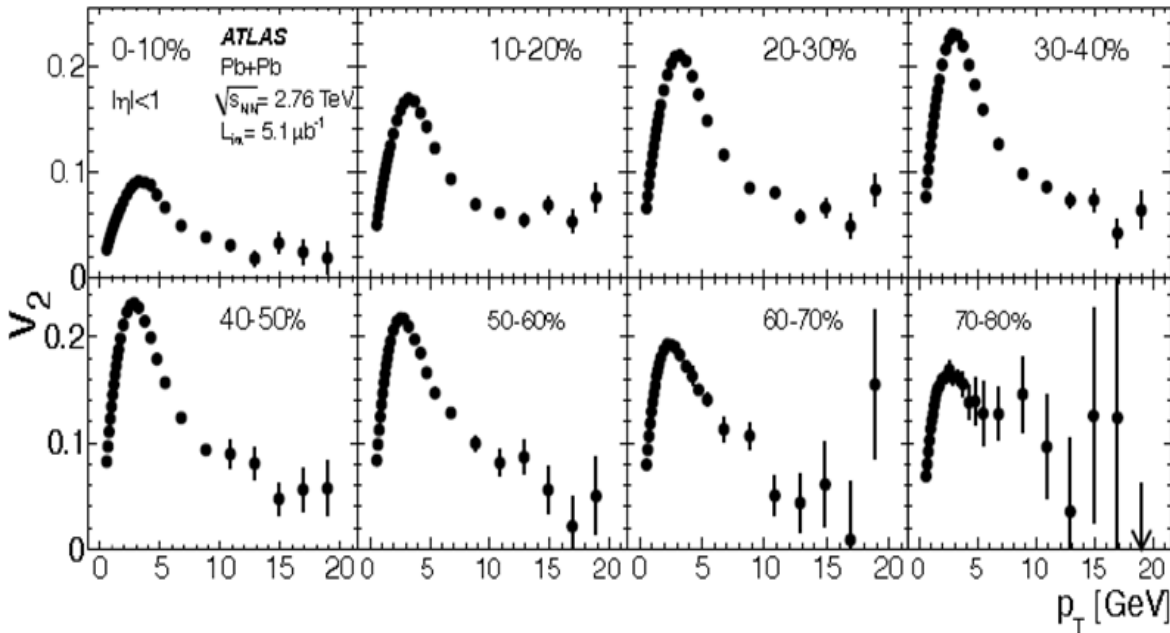
*Jet part + quenching*



# Experimental results

Centrality and  $p_T$  dependence

ATLAS, CMS and ALICE have measured  $v_2$



Rapid rise up to 3-4 GeV/c

Decrease up to 8-9 GeV/c

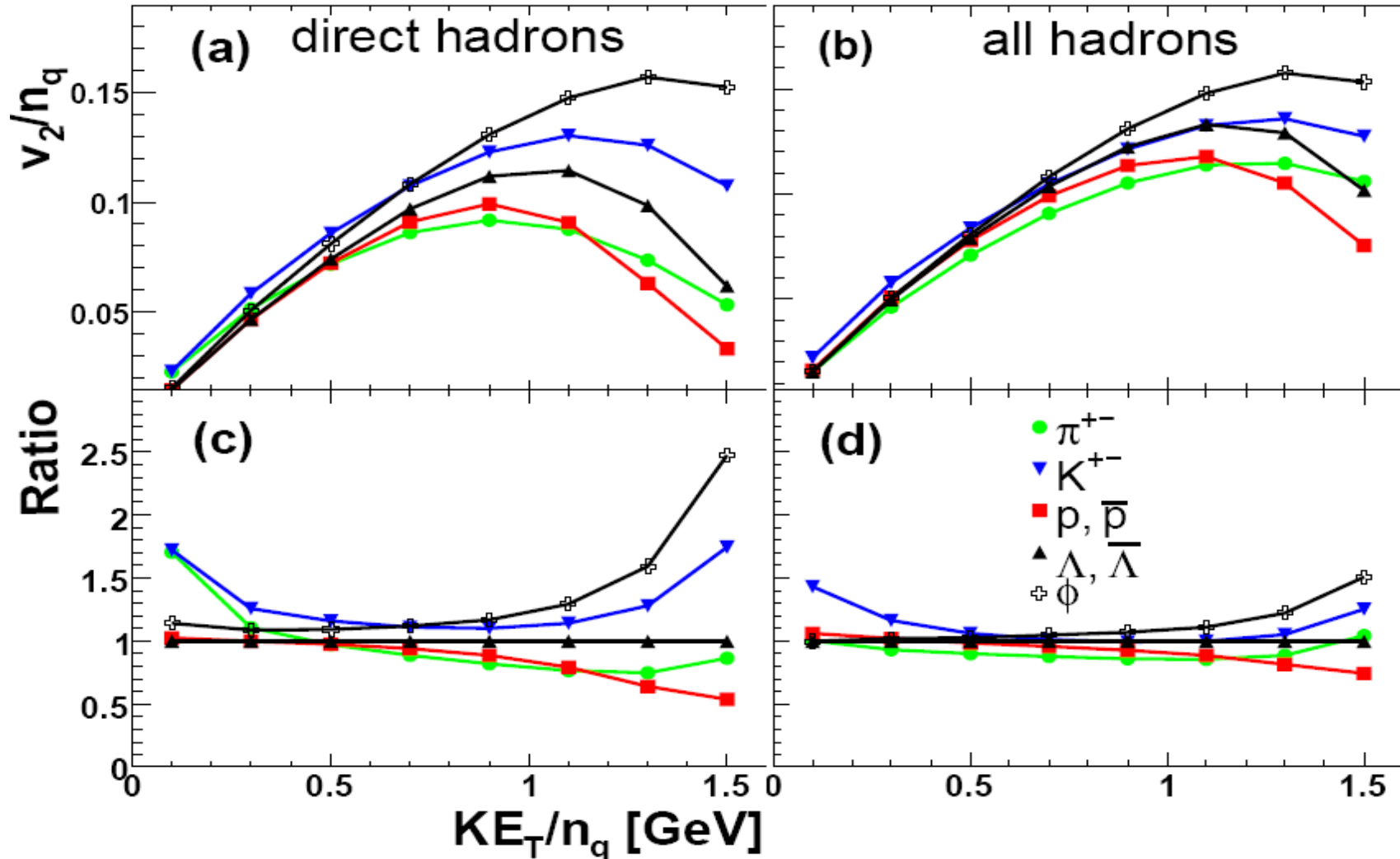
Weak  $p_T$  dependence up to 20 GeV/c

## Number of constituent quark scaling at RHIC

[G. Eyyubova](#), [L. Bravina](#), [V.L. Korotkih](#), [I.P. Lokhtin](#), [L.V. Malinina](#), [S.V. Petrushanko](#), [A.M. Snigirev](#), [E. Zabrodin](#), [Phys.Rev.C80:064907,2009](#).

Direct particles: scaling is not good.

All particles:  $KE_T/n_q$  scaling



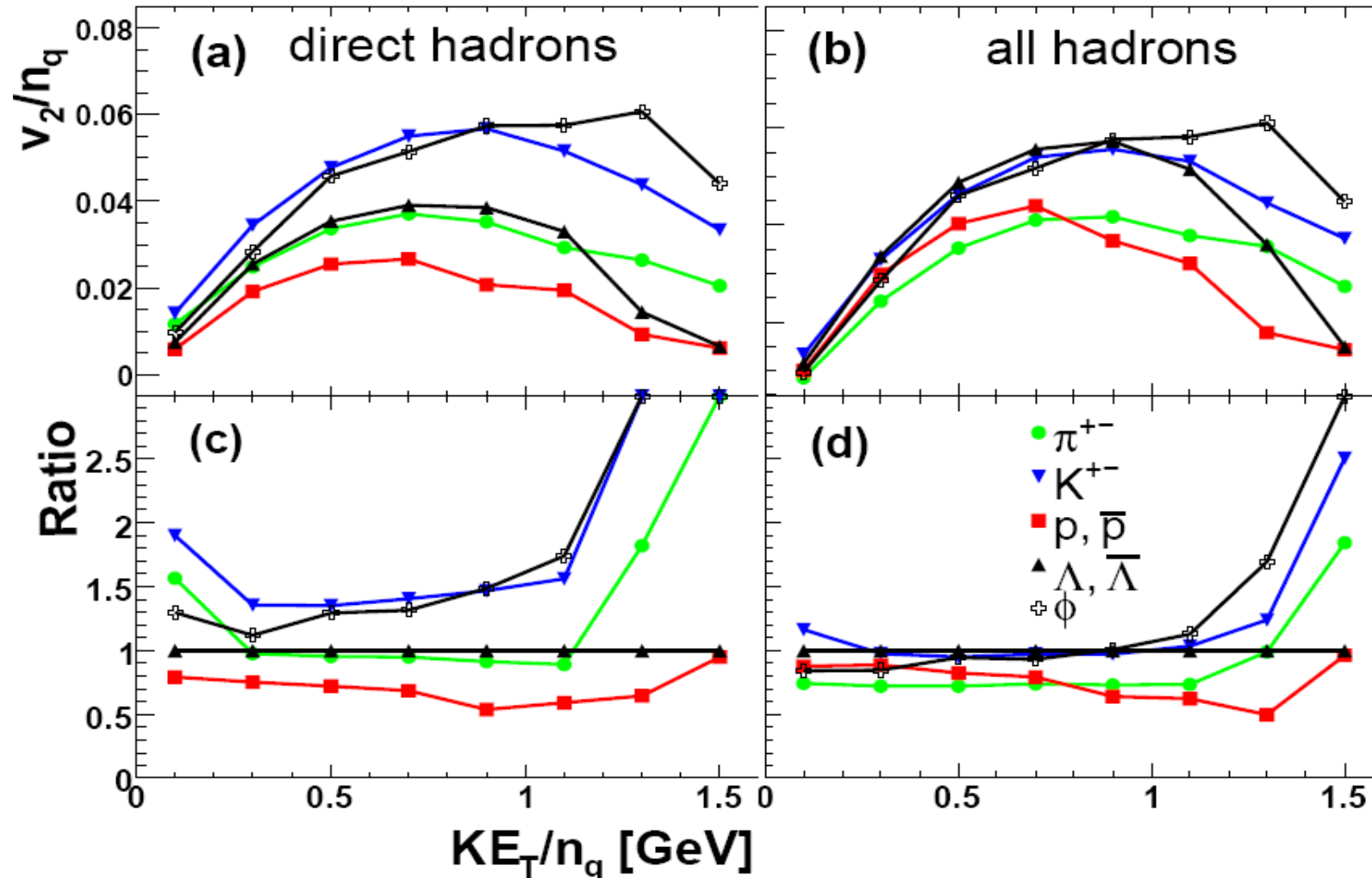
One of the explanations of  $KE_T/n_q$  scaling is partonic origin of the elliptic flow.

*However, final state effects (such as resonance decays and jets) may also lead to appearance of the scaling*

## NCO scaling at LHC

No scaling for  
direct particles

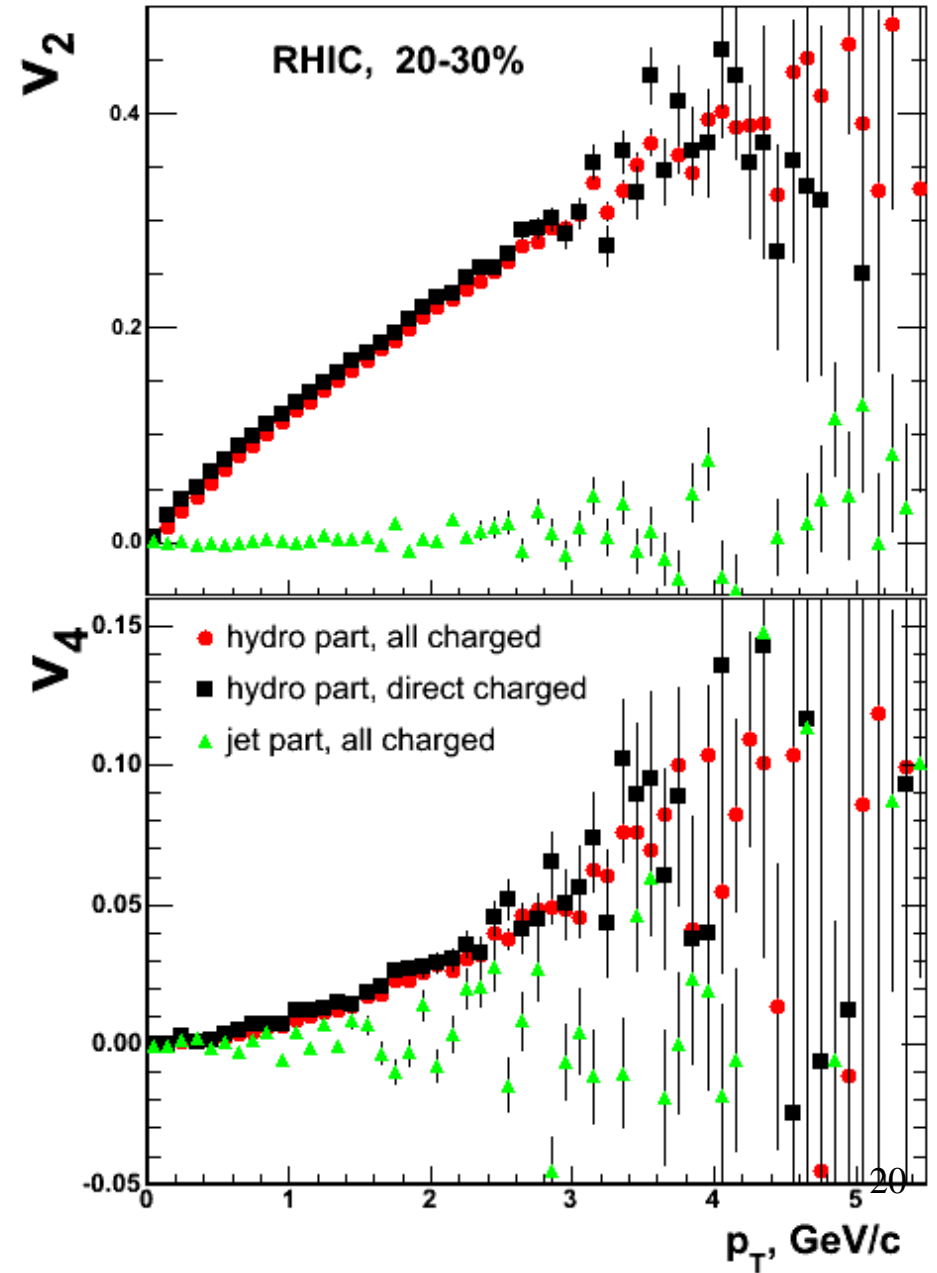
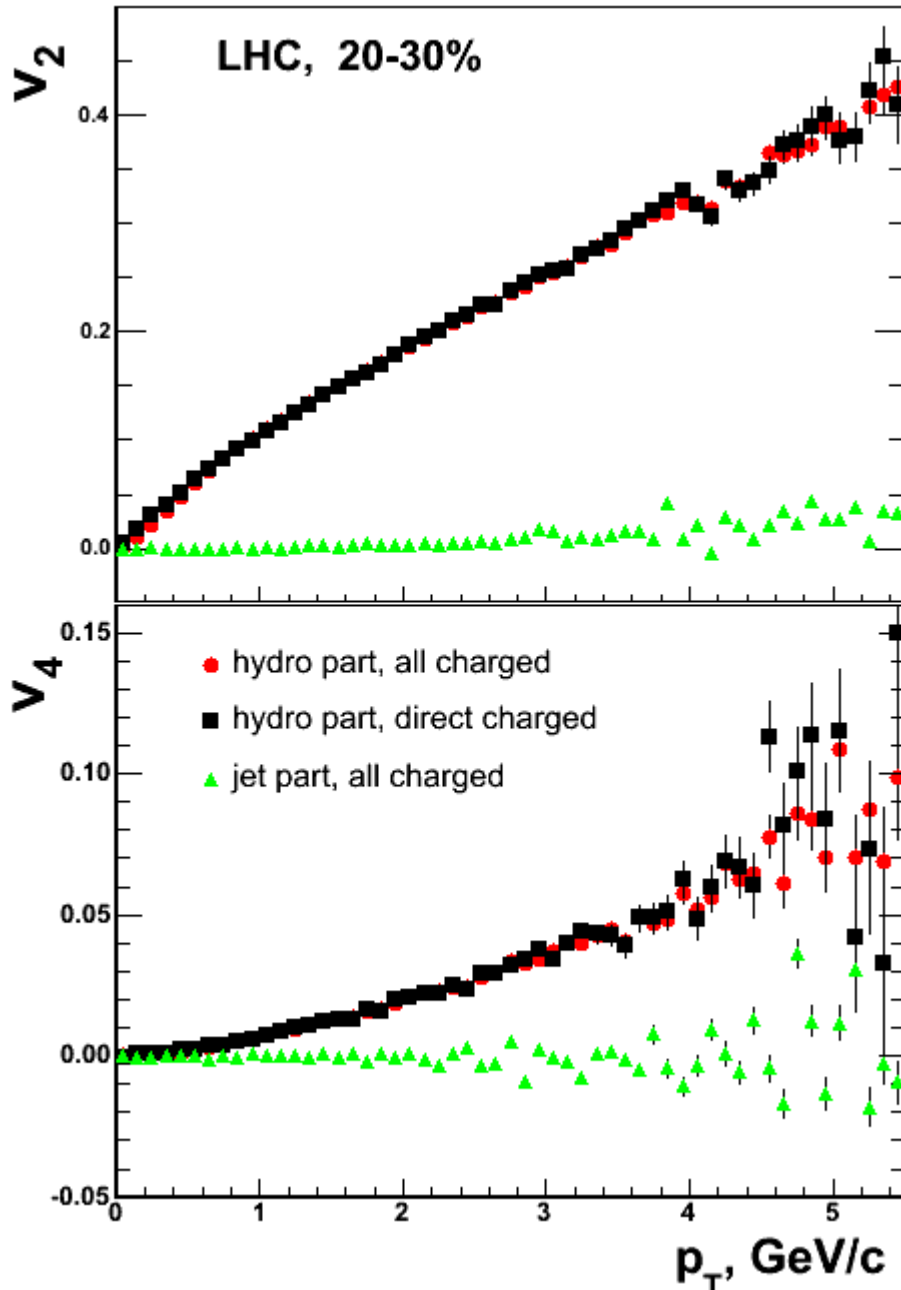
Appearance of the approximate  
scaling for all particles



**LHC: NCO scaling will be only approximate**

# HYDJET++ RESULTS

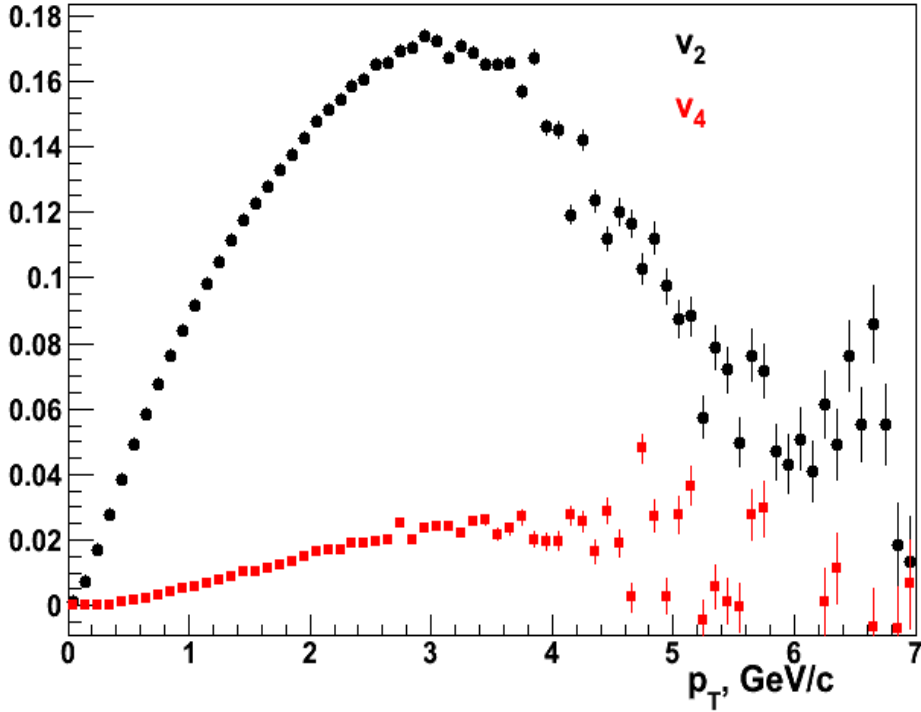
Effects to be studied: resonance decay  
hard part influence





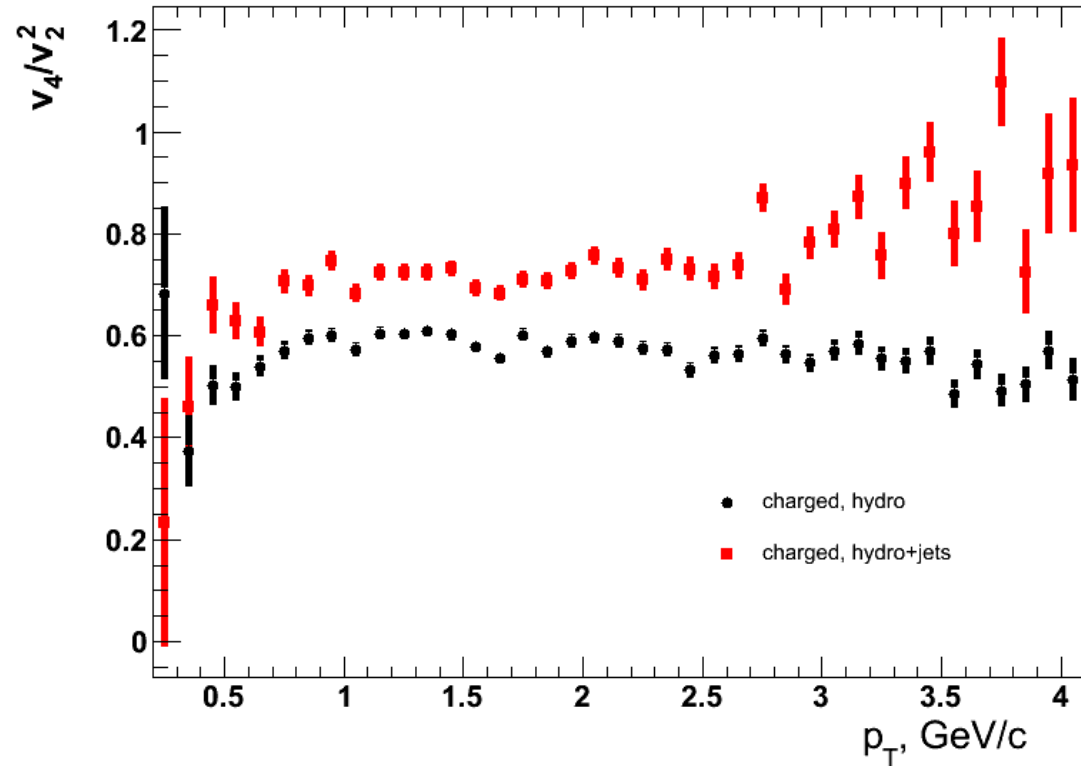
# HYDJET++ RESULTS for LHC

Flow coefficients



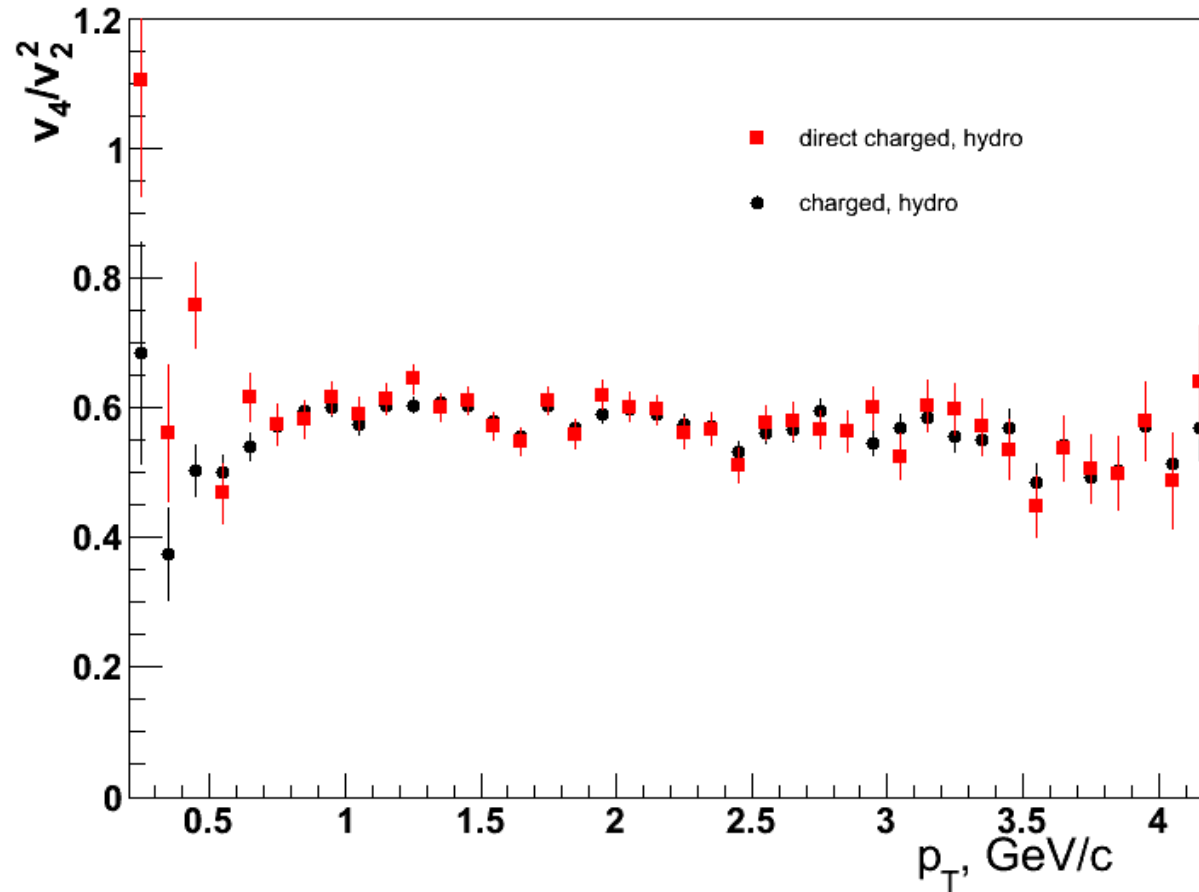
Hydro + jet parts

Ratio

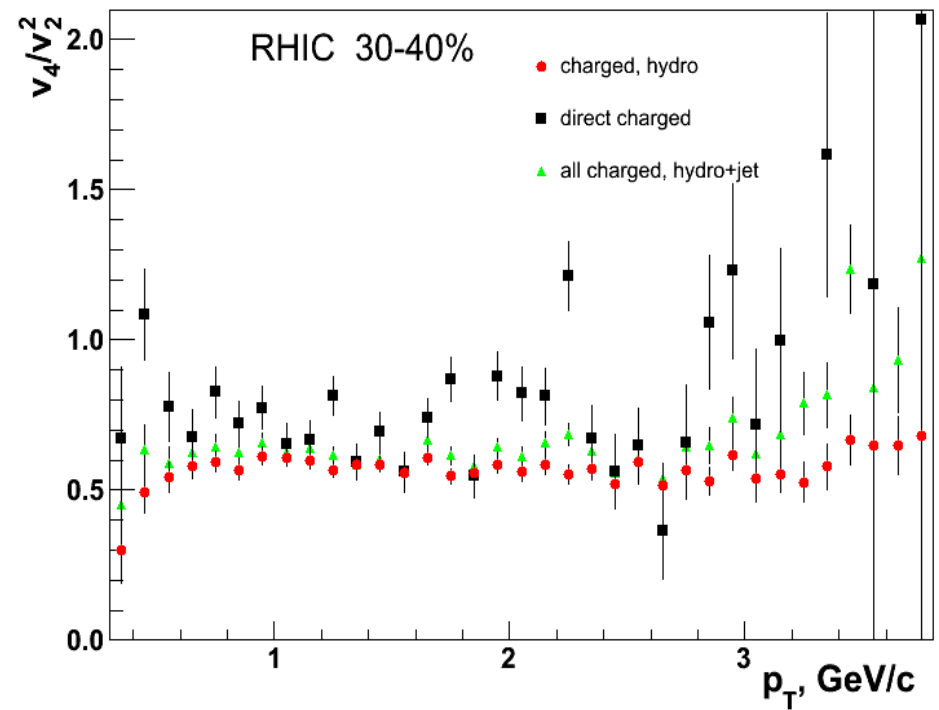
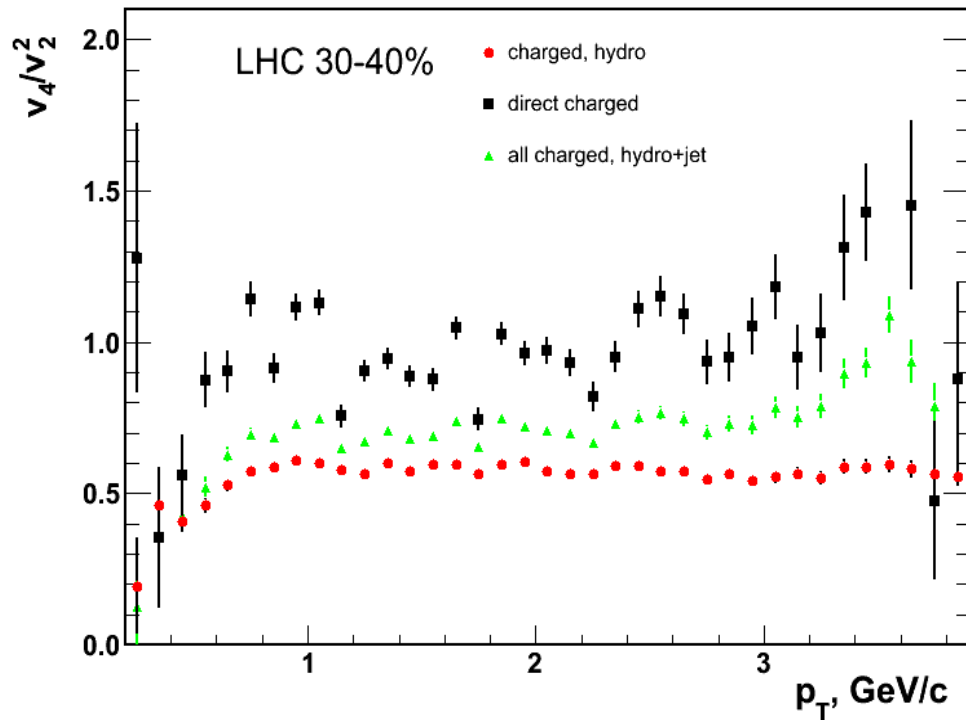


Still, the ratio is below 1

# Decays of resonances play minor role



# Contribution from jet part increases the ratio



Larger contribution of jets at LHC

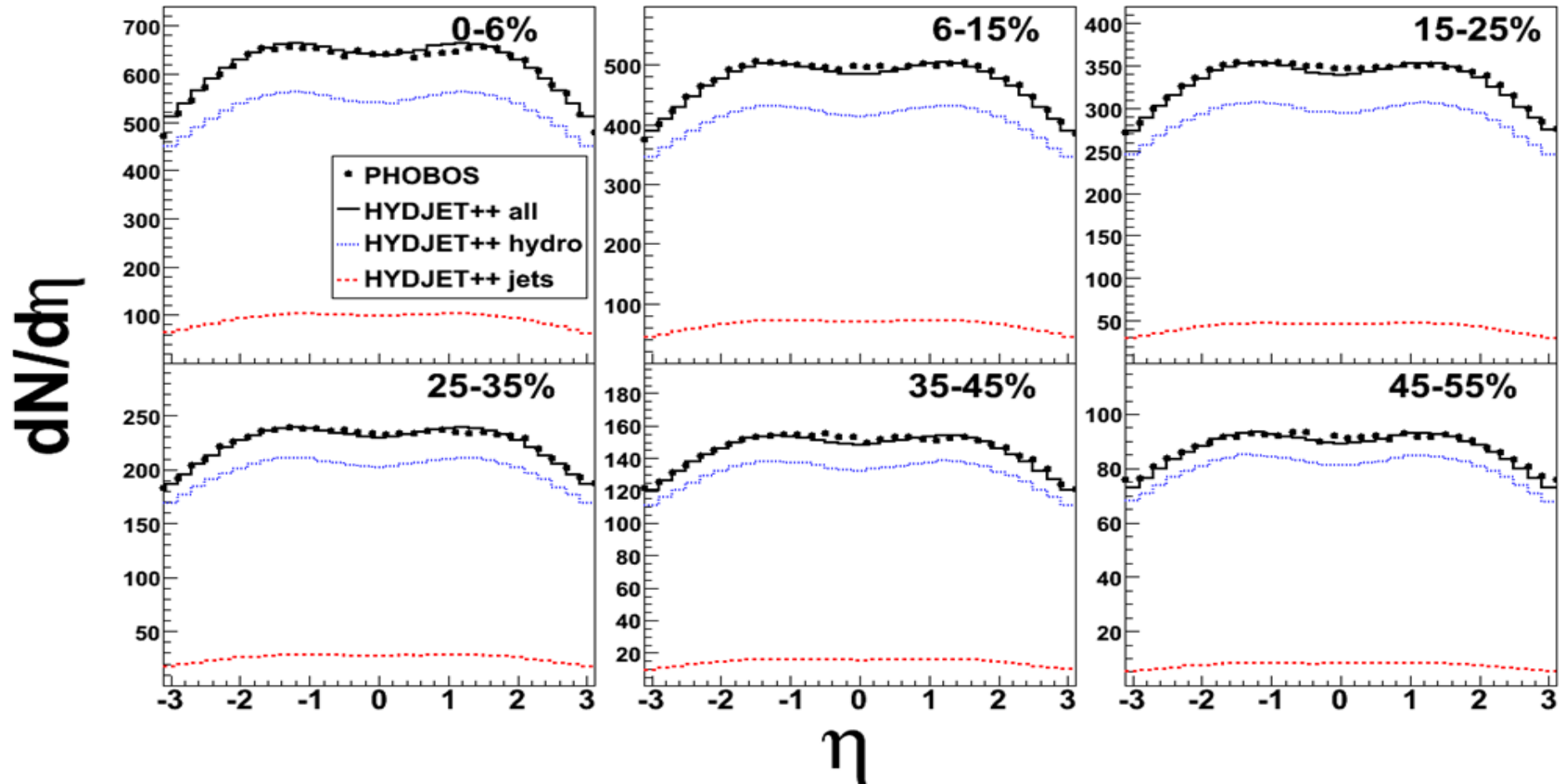
# Conclusions

The HYDJET++ model allows to investigate **hydro** and **jet** parts separately, for example, to look at reconstruction of pure hydro flow and its modification due to jet part.

- *Jets result to increase by 25% - 30% of the ratio  $v_4/(v_2*v_2)$*
- *Eccentricity fluctuations can increase the ratio by factor 1.5*
- *Jets + eccentricity fluctuations are enough to explain RHIC data*
- *For LHC we can explain 75% of the signal. Other effects are needed.*

# Backup slides

# HYDJET++: rapidity spectra vs. event centrality at RHIC



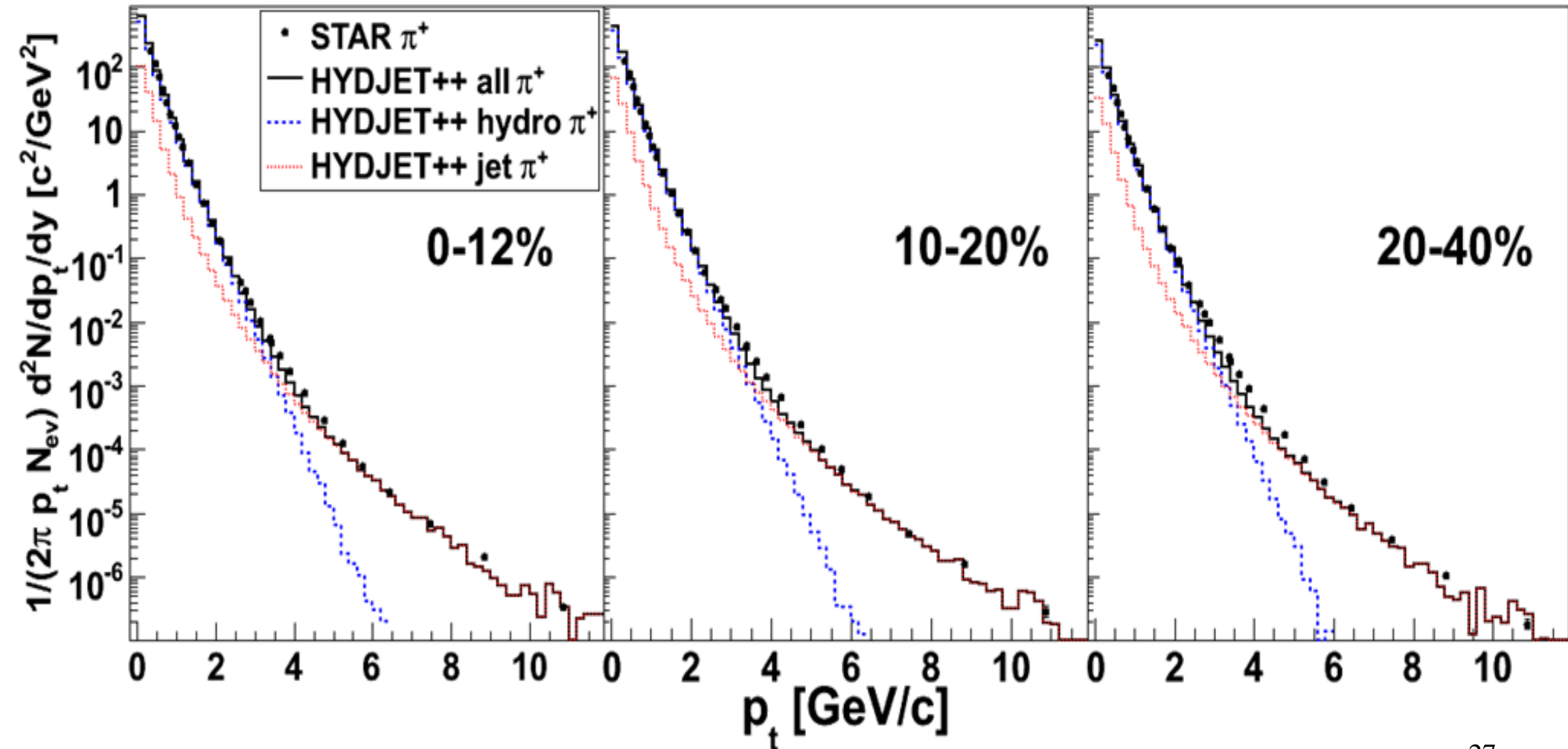
Width of the spectra allows one to fix  $\eta^{\max}=3.3$ ,

Centrality dependence of multiplicity allows one to fix  $p_{t\min}=3.4$  GeV/c and  $\mu_{\pi}=0.06$



# HYDJET++: transverse momentum spectra at RHIC

PYQUEN energy loss model parameters:  $T_0(\text{QGP})=300$  MeV,  $\tau_0(\text{QGP})=0.4$  fm/c,  $N_f=2$



# HYDJET++ (soft): hadron multiplicities

1. The hadronic matter created in heavy-ion collisions is considered as a hydrodynamically expanding fireball with EOS of an ideal hadron gas.

2. “Concept of effective volume” **T=const and  $\mu$ =const**: the total yield of particle species is

$$N_i = \rho_i(T, \mu_i) V_{eff}$$

3. Chemical freeze-out :  **$T, \mu_i = \mu_B B_i + \mu_S S_i + \mu_C C_i + \mu_Q Q_i$** ;  **$T, \mu_B$**  – can be fixed by particle ratios, or by phenomenological formulas

$$T(\mu_B) = a - b\mu_B - c\mu_B^4; \mu_B(\sqrt{s_{NN}}) = \frac{d}{1 + e\sqrt{s_{NN}}}$$

4. Chemical freeze-out: all macroscopic characteristics of particle system are determined via a set of equilibrium distribution functions in the fluid element rest frame:

$$f_i^{eq}(p^{0*}; T, \mu_i) = \frac{1}{(2\pi)^3} \frac{1}{\exp([p^{0*} - \mu_i]/T) \pm 1}$$

$$\rho_i^{eq}(T, \mu_i) = \int_0^\infty d^3 \vec{p}^* f_i^{eq}(p^{0*}; T(x^*), \mu(x^*)_i) = 4\pi \int_0^\infty dp^* p^{*2} f_i^{eq}(p^{0*}; T, \mu_i)$$

# HYDJET++ (soft): main physics assumptions

A hydrodynamic expansion of the fireball is supposed **ends by a sudden system breakup** at given  $T$  and chemical potentials. Momentum distribution of produced hadrons keeps the thermal character of the equilibrium distribution.

**Cooper-Frye formula:** 
$$p^0 \frac{d^3 N_i}{d^3 p} = \int_{\sigma(x)} d^3 \sigma_\mu(x) p^\mu f_i^{eq}(p^\nu u_\mu(x); T, \mu_i)$$

- HYDJET++ avoids straightforward 6-dimensional integration by using the special simulation procedure (like HYDJET): momentum generation in the rest frame of fluid element, then Lorentz transformation in the global frame  $\rightarrow$  uniform weights  $\rightarrow$  effective von-Neumann rejection-acceptance procedure.

## Freeze-out surface parameterizations

1. The Bjorken model with hypersurface

$$\tau = (t^2 - z^2)^{1/2} = const$$

2. Linear transverse flow rapidity profile

$$\rho_u = \frac{r}{R} \rho_u^{\max}$$

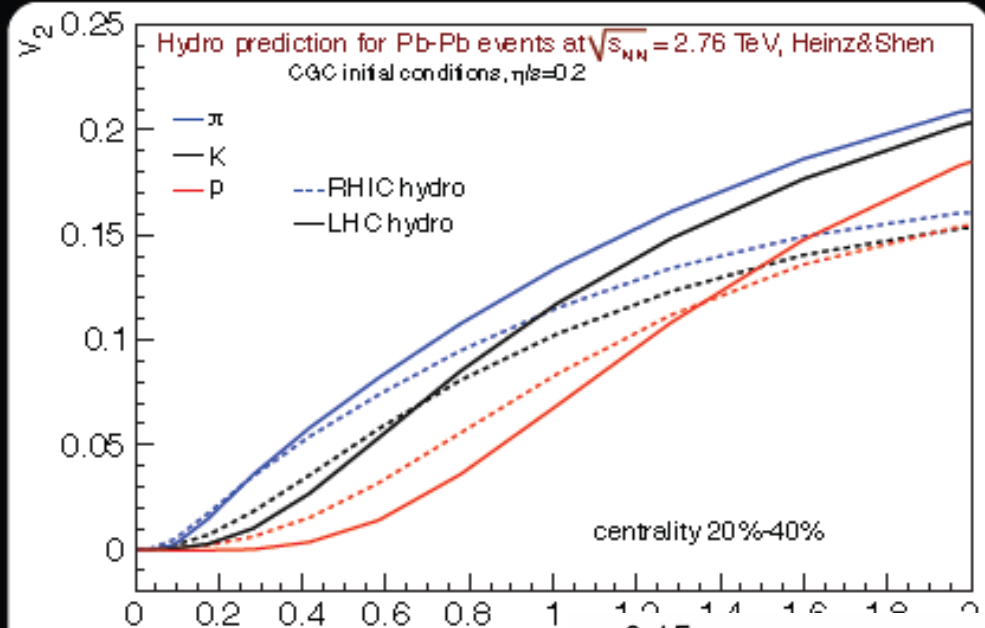
3. The total effective volume for particle production at

$$- V_{eff} = \int_{\sigma(x)} d^3 \sigma_\mu(x) u^\mu(x) = \tau \int_0^R \gamma_r r dr \int_0^{2\pi} d\phi \int_{\eta_{\min}}^{\eta_{\max}} d\eta = 2\pi\tau\Delta\eta \left( \frac{R}{\rho_u^{\max}} \right)^2 (\rho_u^{\max} \sinh \rho_u^{\max} - \cosh \rho_u^{\max} + 1)$$

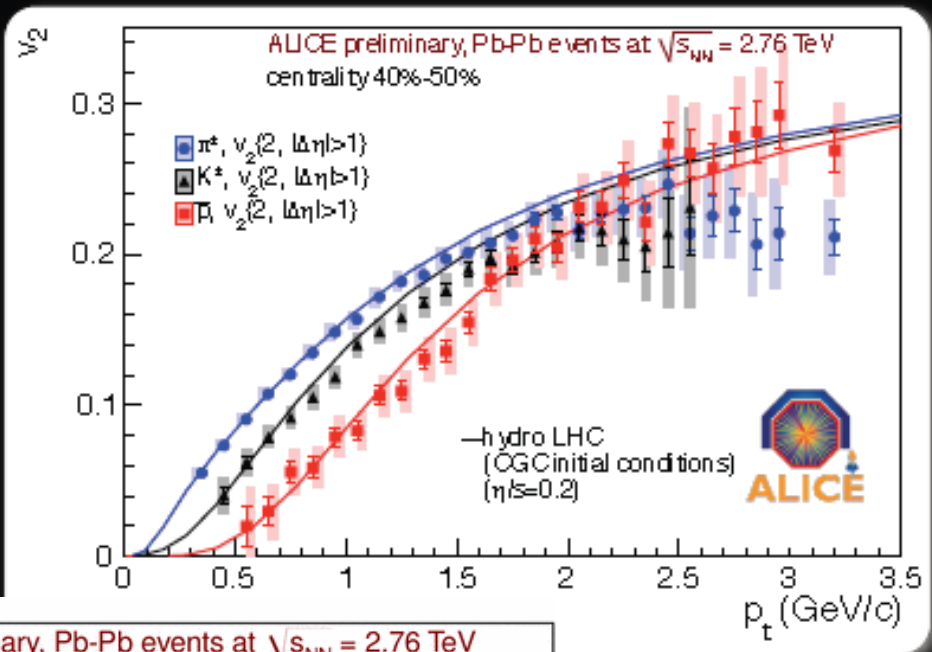
# $v_2$ for identified particles



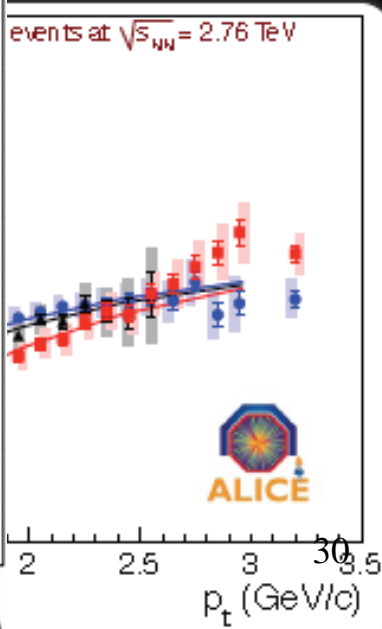
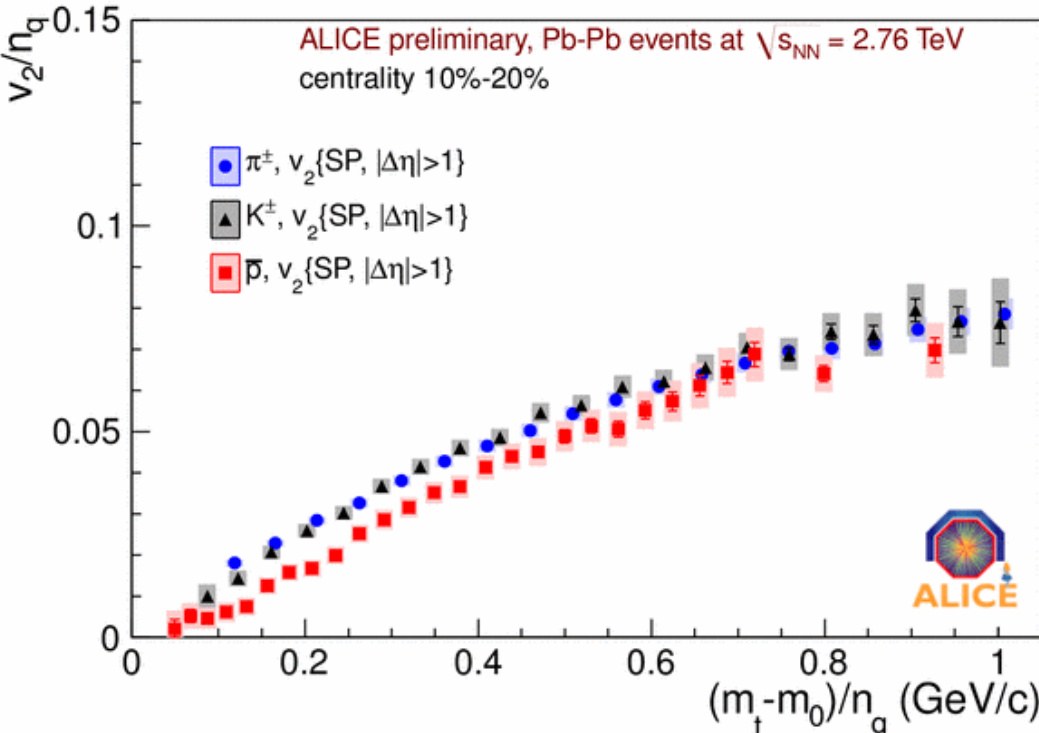
Hydro: Shen, Heinz, Huovinen & Song, arXiv:1105.3226



& Song, arXiv:1105.3226



hydro models predict  
 splitting  
 data shows mass splitting  
 well with hydro prediction  
 central collision  
 for more central collision  
 proton flow is not described  
 same calculation



see presentation