



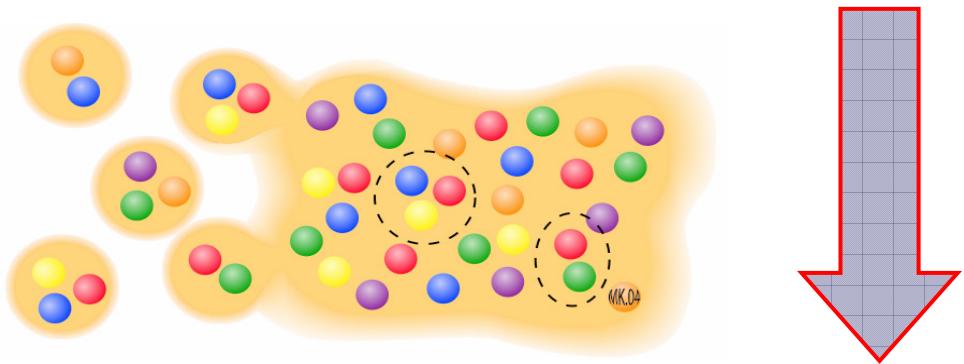
# Parton-Hadron-String Dynamics

## Overview and recent developments

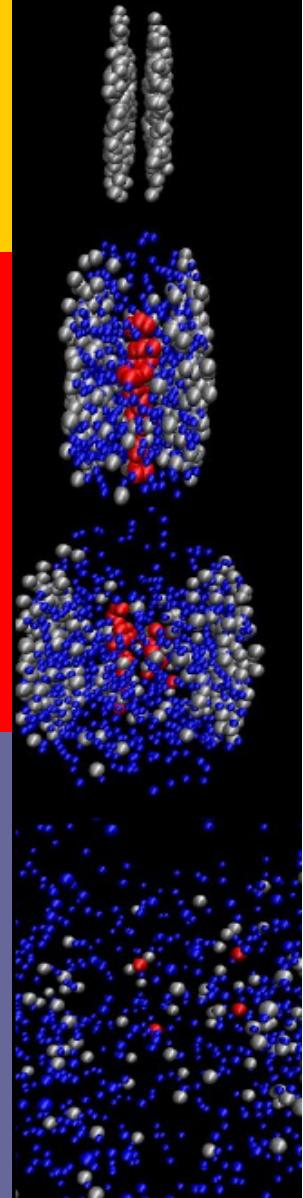
Olena Linnyk



# Transport description of the partonic and hadronic phases



Parton-Hadron-String-  
Dynamics (PHSD)



# PHSD: heavy-ion collisions

**Initial A+A collisions:** HSD, string formation and decay to pre-hadrons

**Fragmentation** of pre-hadrons into quarks using the quark spectral functions from the Dynamical Quasi-Particle Model (**DQPM**) – approximation to QCD

**Partonic phase:** quarks and gluons with constituent mass and broad spectral functions. **Widths, masses** defined by DQPM. **Elastic and inelastic parton-parton interactions** (effective cross sections adjusted to the DQPM in equilibrium):

- ✓  $q + \bar{q}$  (flavor neutral)  $\leftrightarrow$  gluon (colored)
- ✓ gluon + gluon  $\leftrightarrow$  gluon (possible due to large spectral width)
- ✓  $q + \bar{q}$  (color neutral)  $\leftrightarrow$  hadron resonances

**Hadronization:** dynamical and off-shell transitions. Massive, off-shell quarks and gluons with broad spectral functions hadronize **to off-shell hadrons**:

- ✓ gluons  $\rightarrow q + \bar{q}$ ;  $q + \bar{q} \rightarrow$  off-shell meson or ‚string‘;
- ✓  $q + q + q \rightarrow$  baryon or ‚string‘; (‚strings‘ act as doorway states)

**Hadronic phase:** hadron-string interactions and propagation by off-shell HSD

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;  
NPA831 (2009) 215; EPJ ST 168 (2009) 3; NPA856 (2011) 162

# Parton-Hadron-String Dynamics

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Main goal – description of heavy-ion collisions and properties of matter at high temperature and density as well as p+p and p(d)+A reactions at the same energy. Major features:

- ✓ Unified description of collisions at all energies from **AGS to LHC**.
- ✓ **Non-equilibrium** approach: applicable to far from equilibrium configurations as explosion-like heavy-ion collisions as well as to equilibrated matter („in the box“).
- ✓ **Dynamics**: mean fields (hadronic and partonic), scattering (elastic, inelastic,  $2 \leftarrow\rightarrow 2$ ,  $2 \leftarrow\rightarrow n$ ), resonance decays, retarded electro-magnetic fields.
- ✓ **Phase transition** (cross over) according to the lattice QCD equation of state, hadronic and partonic degrees of freedom, spacial co-existance, dynamical hadronisation.
- ✓ **Off-shell** transport: takes into account 2-particle correlations beyond the one-particle distributions.

# Boltzmann equation → off-shell transport

$$\left( \frac{\partial}{\partial t} + \vec{v}_1 \cdot \nabla_{\vec{r}} + \frac{\vec{K}}{m} \cdot \nabla_{\vec{v}_1} \right) f_1 = \int d\Omega \int d\vec{v}_2 \sigma(\Omega) |\vec{v}_1 - \vec{v}_2| (f'_1 f'_2 - f_1 f_2)$$

## GENERALIZATION



(First order gradient expansion of the Wigner-transformed Kadanoff-Baym equations)

drift term	Vlasov term	backflow term	collision term = ,loss‘ term - ,gain‘ term
$\diamond \{ P^2 - M_0^2 - Re\Sigma_{XP}^{ret} \} \{ S_{XP}^< \}$	$\diamond \{ \Sigma_{XP}^< \} \{ ReS_{XP}^{ret} \}$	$= \frac{i}{2} [ \Sigma_{XP}^> S_{XP}^< - \Sigma_{XP}^< S_{XP}^> ]$	

**Backflow term** incorporates the **off-shell** behavior in the particle propagation  
! vanishes in the quasiparticle limit  $A_{XP} = 2 \pi \delta(p^2 - M^2)$

Propagation of the Green’s function  $iS_{XP}^< = A_{XP} N_{XP}$ , which carries information not only on the number of particles, but also on their properties, interactions and correlations

$$A_{XP} = \frac{\Gamma_{XP}}{(P^2 - M_0^2 - Re\Sigma_{XP}^{ret})^2 + \Gamma_{XP}^2/4}$$

$$\diamond \{ F_1 \} \{ F_2 \} := \frac{1}{2} \left( \frac{\partial F_1}{\partial X_\mu} \frac{\partial F_2}{\partial P^\mu} - \frac{\partial F_1}{\partial P_\mu} \frac{\partial F_2}{\partial X^\mu} \right)$$

$\Gamma_{XP}$  – width of spectral function = reaction rate of a particle (at phase-space position XP)

# Off-shell equations of motion

Employ **testparticle Ansatz** for the real valued quantity  $i S_{XP}^<$  -

$$F_{XP} = A_{XP} N_{XP} = i S_{XP}^< \sim \sum_{i=1}^N \delta^{(3)}(\vec{X} - \vec{X}_i(t)) \delta^{(3)}(\vec{P} - \vec{P}_i(t)) \delta(P_0 - \epsilon_i(t))$$

insert in generalized transport equations and determine equations of motion !

**General testparticle off-shell equations of motion:**

$$\frac{d\vec{X}_i}{dt} = \frac{1}{1 - C_{(i)}} \frac{1}{2\epsilon_i} \left[ 2\vec{P}_i + \vec{\nabla}_{P_i} Re\Sigma_{(i)}^{ret} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - Re\Sigma_{(i)}^{ret}}{\Gamma_{(i)}} \vec{\nabla}_{P_i} \Gamma_{(i)} \right],$$

$$\frac{d\vec{P}_i}{dt} = -\frac{1}{1 - C_{(i)}} \frac{1}{2\epsilon_i} \left[ \vec{\nabla}_{X_i} Re\Sigma_i^{ret} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - Re\Sigma_{(i)}^{ret}}{\Gamma_{(i)}} \vec{\nabla}_{X_i} \Gamma_{(i)} \right],$$

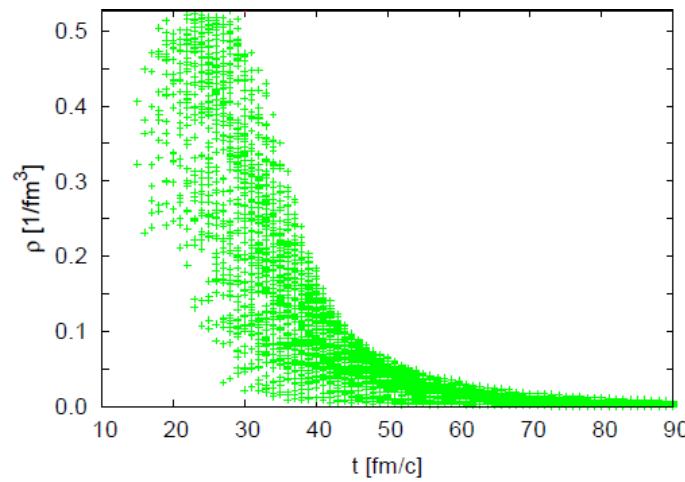
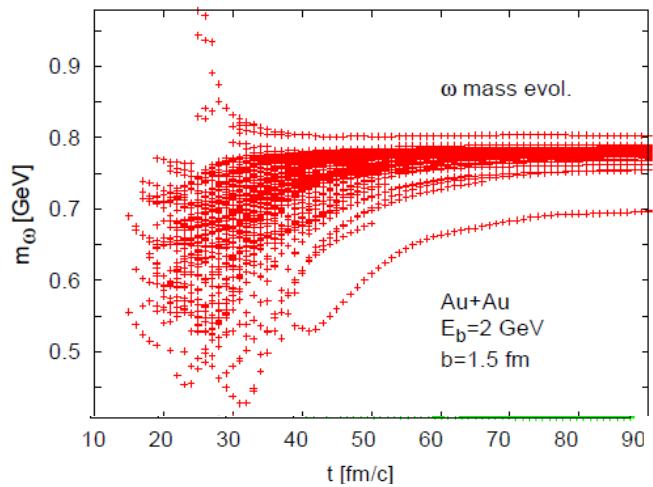
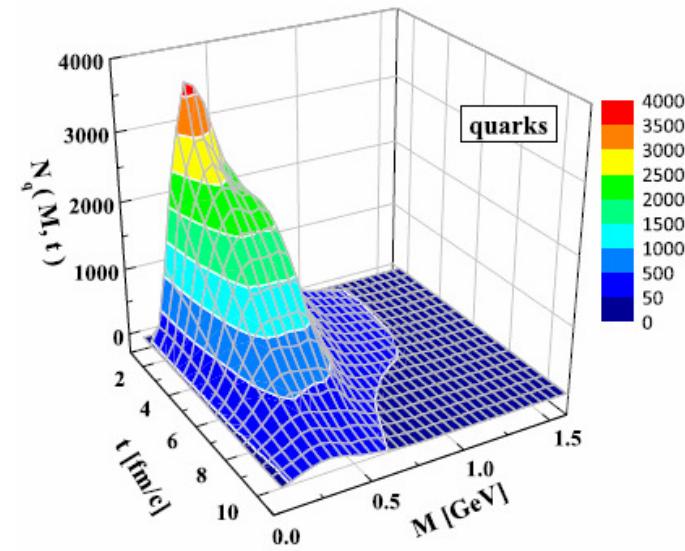
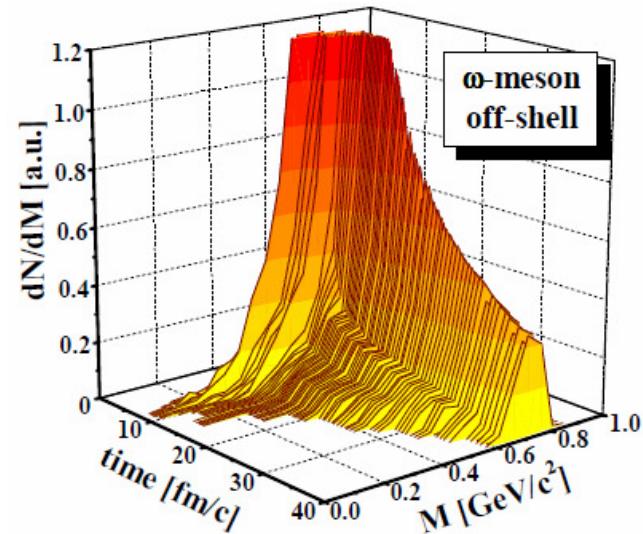
$$\frac{d\epsilon_i}{dt} = \frac{1}{1 - C_{(i)}} \frac{1}{2\epsilon_i} \left[ \frac{\partial Re\Sigma_{(i)}^{ret}}{\partial t} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - Re\Sigma_{(i)}^{ret}}{\Gamma_{(i)}} \frac{\partial \Gamma_{(i)}}{\partial t} \right],$$

with  $F_{(i)} \equiv F(t, \vec{X}_i(t), \vec{P}_i(t), \epsilon_i(t))$

$$C_{(i)} = \frac{1}{2\epsilon_i} \left[ \frac{\partial}{\partial \epsilon_i} Re\Sigma_{(i)}^{ret} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - Re\Sigma_{(i)}^{ret}}{\Gamma_{(i)}} \frac{\partial}{\partial \epsilon_i} \Gamma_{(i)} \right]$$

# Results of off-shell transport simulations

The off-shell spectral function becomes on-shell in the vacuum dynamically!



E.L. Bratkovskaya, W. Cassing, V. P. Konchakovski, O. Linnyk, NPA856(2011) 162; E.L. Bratkovskaya, W. Cassing, NPA 807 (2008) 214; H.W. Barz, B. Kampfer, Gy. Wolf, M. Zetenyi, Open Nucl. Part. Phys. J. 3 (2010) 1



# Dynamical Quasi-Particle Model (DQPM)

# The Dynamical QuasiParticle Model (DQPM)

Basic idea: Interacting quasiparticles

- massive quarks and gluons ( $g, q, q_{\bar{q}}$ ) with spectral functions :

$$\rho(\omega) = \frac{\gamma}{E} \left( \frac{1}{(\omega - E)^2 + \gamma^2} - \frac{1}{(\omega + E)^2 + \gamma^2} \right) \quad E^2 = p^2 + M^2 - \gamma^2$$

## ■ quarks

**mass:**  $m^2(T) = \frac{N_c^2 - 1}{8N_c} g^2 \left( T^2 + \frac{\mu_q^2}{\pi^2} \right)$

**width:**  $\gamma_q(T) = \frac{N_c^2 - 1}{2N_c} \frac{g^2 T}{4\pi} \ln \frac{c}{g^2}$

## ■ gluons:

$$M^2(T) = \frac{g^2}{6} \left( (N_c + \frac{1}{2}N_f) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right)$$

$$\gamma_g(T) = N_c \frac{g^2 T}{4\pi} \ln \frac{c}{g^2}$$

A. Peshier, PRD 70 (2004) 034016

$$N_c = 3, N_f = 3$$

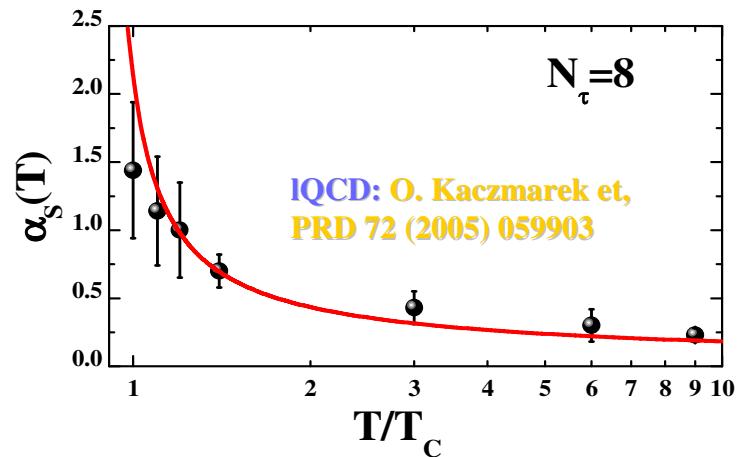
**running coupling:**  $\alpha_s(T) = g^2(T)/(4\pi)$

$$g^2(T/T_c) = \frac{48\pi^2}{(11N_c - 2N_f) \ln(\lambda^2(T/T_c - T_s/T_c)^2)}$$

► fit to lattice (lQCD) results (e.g. entropy density)

with 3 parameters:  $T_s/T_c=0.46$ ;  $c=28.8$ ;  $\lambda=2.42$

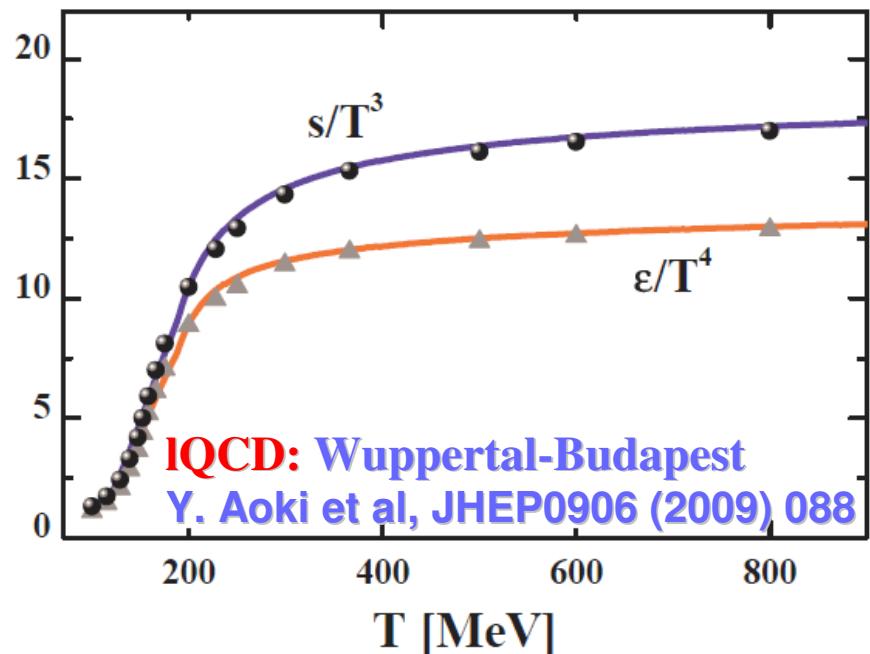
→ quasiparticle properties (mass, width)



# DQPM thermodynamics ( $N_f=3$ ) and lQCD

**entropy**  $s = \frac{\partial P}{\partial T} \rightarrow \text{pressure } P$

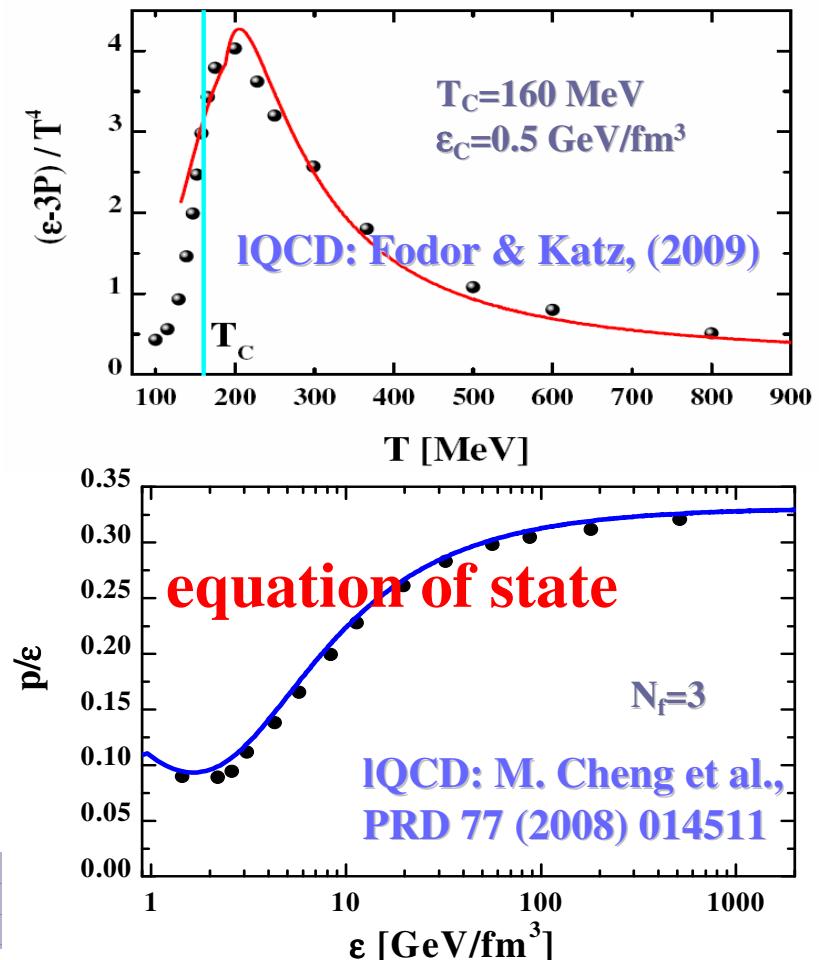
**energy density:**  $\epsilon = Ts - P$



DQPM gives a good description of lQCD!

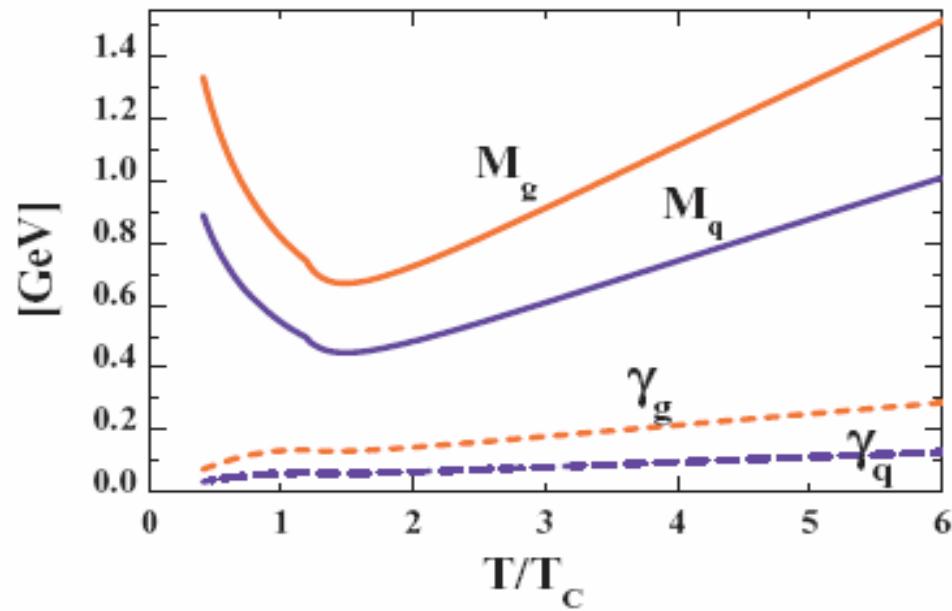
**interaction measure:**

$$W(T) := \epsilon(T) - 3P(T) = Ts - 4P$$

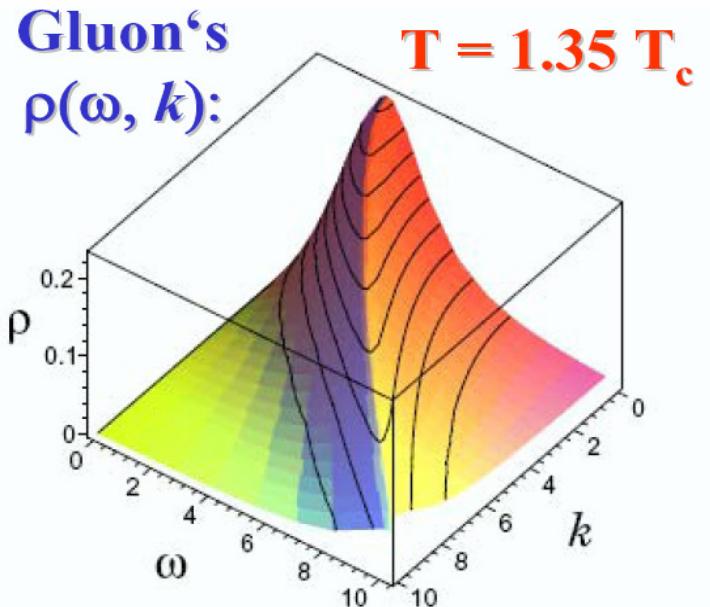


# The Dynamical QuasiParticle Model (DQPM)

- Quasiparticle properties:
  - large width and mass for gluons and quarks

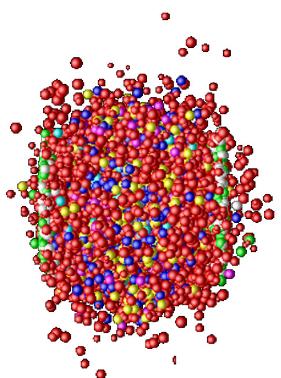


- Broad spectral function :



- DQPM matches well lattice QCD
- DQPM provides mean-fields (1PI) for gluons and quarks as well as effective 2-body interactions (2PI)
- DQPM gives transition rates for the formation of hadrons → PHSD

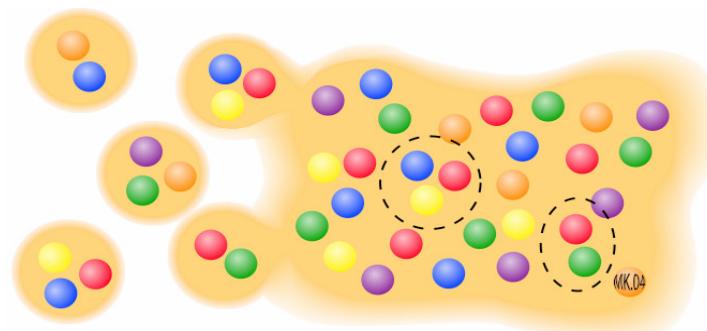
# Partonic phase summary



## Partonic phase:

- Degrees of freedom:
  - quarks and gluons (= ‚dynamical quasiparticles‘)
- Properties of partons:
  - off-shell spectral functions (width, mass) defined by DQPM
- EoS of partonic phase:
  - from lattice QCD (or DQPM)
- Elastic parton-parton interactions:
  - using the effective cross sections from the DQPM
- Inelastic parton-parton interactions:
  - ✓ quark+antiquark (flavor neutral)  $\leftrightarrow$  gluon (colored)
  - ✓ gluon + gluon  $\leftrightarrow$  gluon (possible due to large spectral width)
  - ✓ quark + antiquark (color neutral)  $\leftrightarrow$  hadron resonances
- Note: inelastic reactions are described by Breit-Wigner cross sections determined by the spectral properties of constituents ( $q, q_{\bar{q}}, g$ )
- Parton propagation:
  - with self-generated potentials  $U_q, U_g$

# Hadronization



# PHSD: hadronization

Based on DQPM; massive, off-shell quarks and gluons with broad spectral functions hadronize to off-shell mesons and baryons:



**Parton-parton recombination rate =**

$$\begin{aligned} \frac{dN_m(x, p)}{d^4x d^4p} &= Tr_q Tr_{\bar{q}} \delta^4(p - p_q - p_{\bar{q}}) \delta^4\left(\frac{x_q + x_{\bar{q}}}{2} - x\right) \\ &\times \omega_q \rho_q(p_q) \omega_{\bar{q}} \rho_{\bar{q}}(p_{\bar{q}}) |v_{q\bar{q}}|^2 W_m(x_q - x_{\bar{q}}, p_q - p_{\bar{q}}) \\ &\times N_q(x_q, p_q) N_{\bar{q}}(x_{\bar{q}}, p_{\bar{q}}) \delta(\text{flavor, color}). \end{aligned} \quad (7)$$

$W_m$  - Gaussian in phase space with  $\sqrt{\langle r^2 \rangle} = 0.66$  fm

**Hadronization happens when the effective interactions  $|v|$  become attractive,  
approx. for parton densities  $1 < \rho_p < 2.2 \text{ fm}^{-3}$   $\leq$  from DQPM**

Note: nucleon: parton density  $\rho_p^N = N_q / V_N = 3 / 2.5 \text{ fm}^3 = 1.2 \text{ fm}^{-3}$

meson: parton density  $\rho_p^m = N_q / V_m = 2 / 1.2 \text{ fm}^3 = 1.66 \text{ fm}^{-3}$

# PHSD: hadronization

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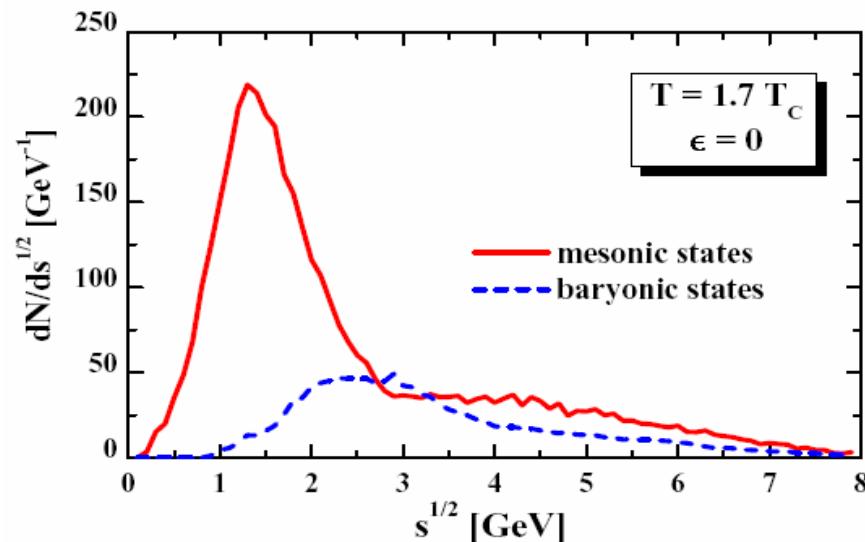
## Conservation laws:

- ✓ 4-momentum conservation → invariant mass and momentum of hadron
- ✓ flavor current conservation → quark-antiquark content of hadron
- ✓ color + anticolor → color neutrality
- ✓ Since the partons are massive the formed states are very heavy (strings) → entropy production in the hadronization!

- large parton masses → dominant production of vector mesons or baryon resonances (of finite/large width)
- hadronic resonances are propagated in HSD (and finally decay to the groundstates by emission of pions, kaons, etc.)

# Hadronization details

Mass distributions for color neutral ,mesons‘ and ,baryons‘ after parton fusion:



These ,prehadrons‘ decay according to JETSET to 0-, 1-,1+ mesons and the baryon octet/decouplet

[W. Cassing, E.L. Bratkovskaya, PRC 78 \(2008\) 034919](#)  
[W. Cassing, EPJ ST 168 \(2009\) 3](#)

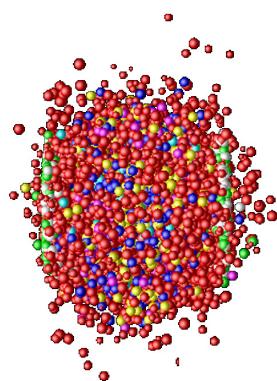
Comparison of particle ratios with the statistical model (SM):

	$p/\pi^+$	$\Lambda/K^+$	$K^+/\pi^+$
PHSD	0.086	0.28	0.157
SM $T = 160$ MeV	0.073	0.22	0.179
SM $T = 170$ MeV	0.086	0.26	0.180

TABLE I: Comparison of particle ratios from PHSD with the statistical model (SM) [31] for  $T = 160$  MeV and 170 MeV.

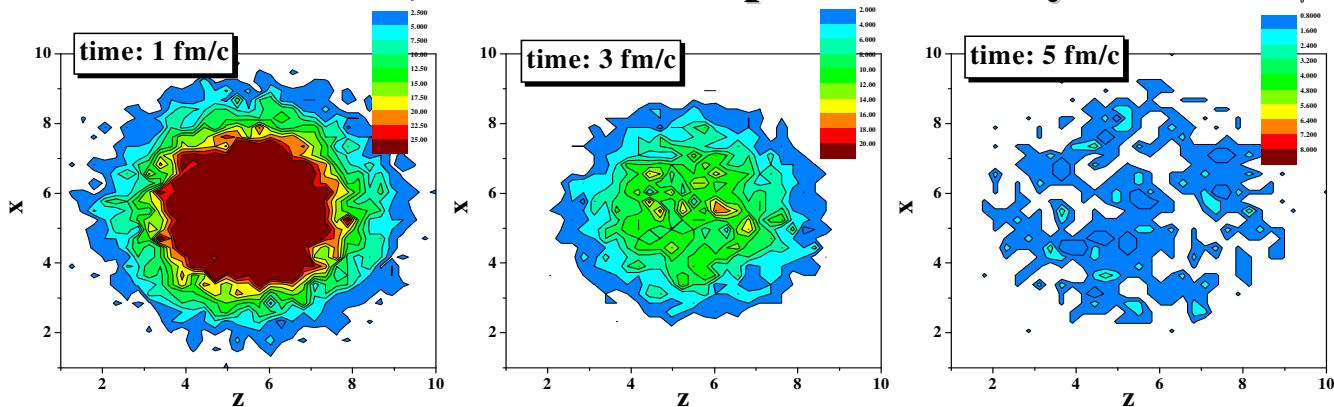


# Observables 1: Corona and spectra

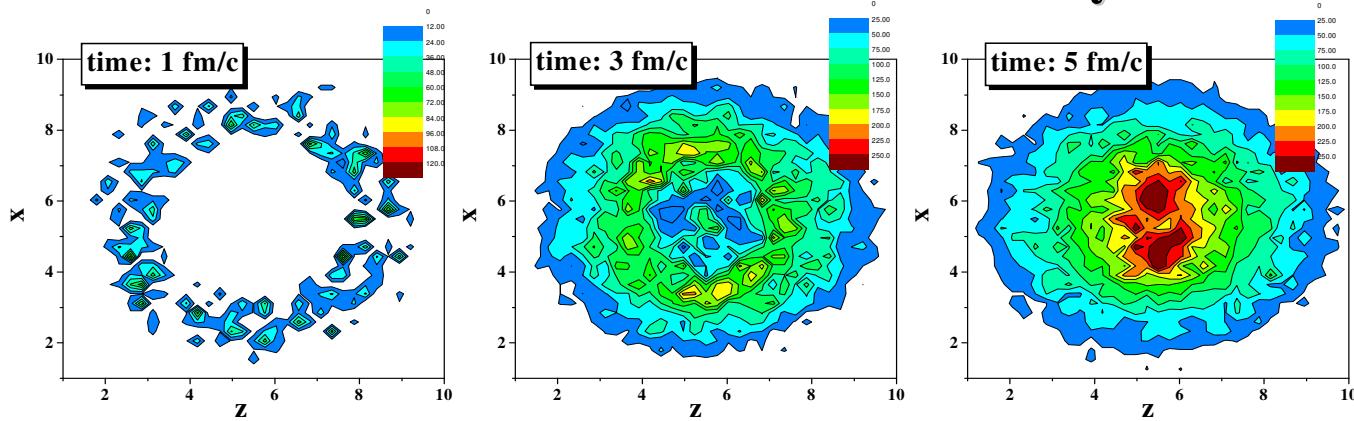


# Expanding fireball

Time-evolution of parton density



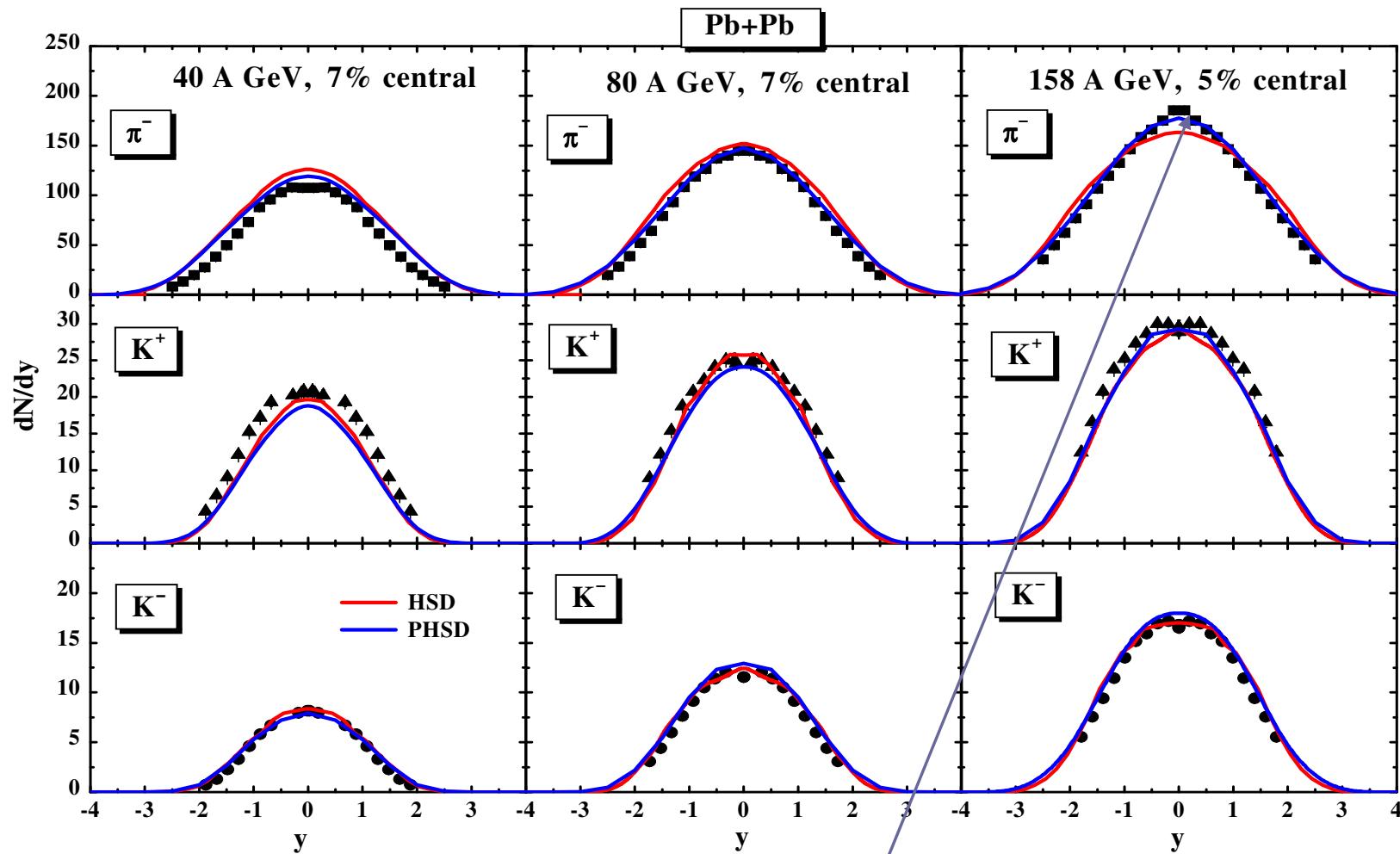
Time-evolution of hadron density



Expanding grid:  $\Delta z(t) = \Delta z_0(1+a t)$  !

**PHSD:** spacial phase ,co-existence‘ of partons and hadrons, but **NO** interactions between hadrons and partons (since it is a cross-over)

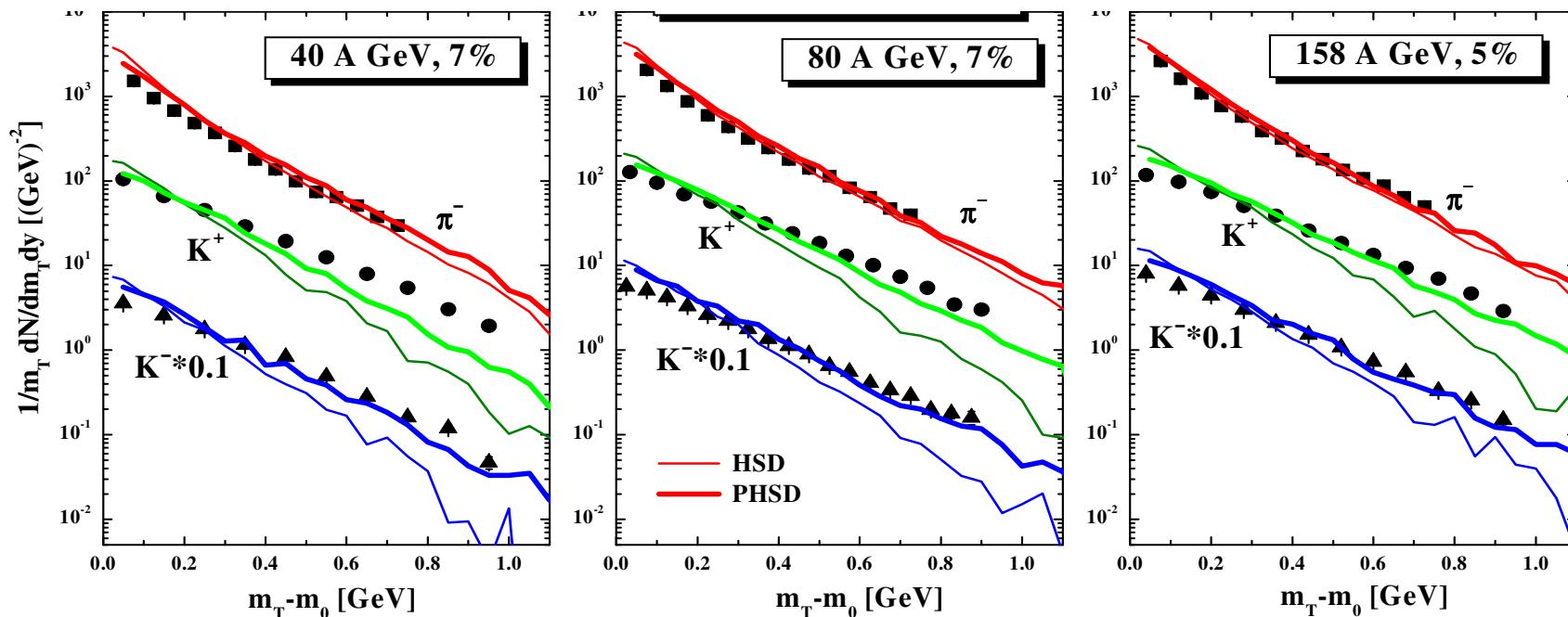
# Rapidity distributions of p, K<sup>+</sup>, K<sup>-</sup> at SPS



→ pion and kaon rapidity distributions become slightly narrower

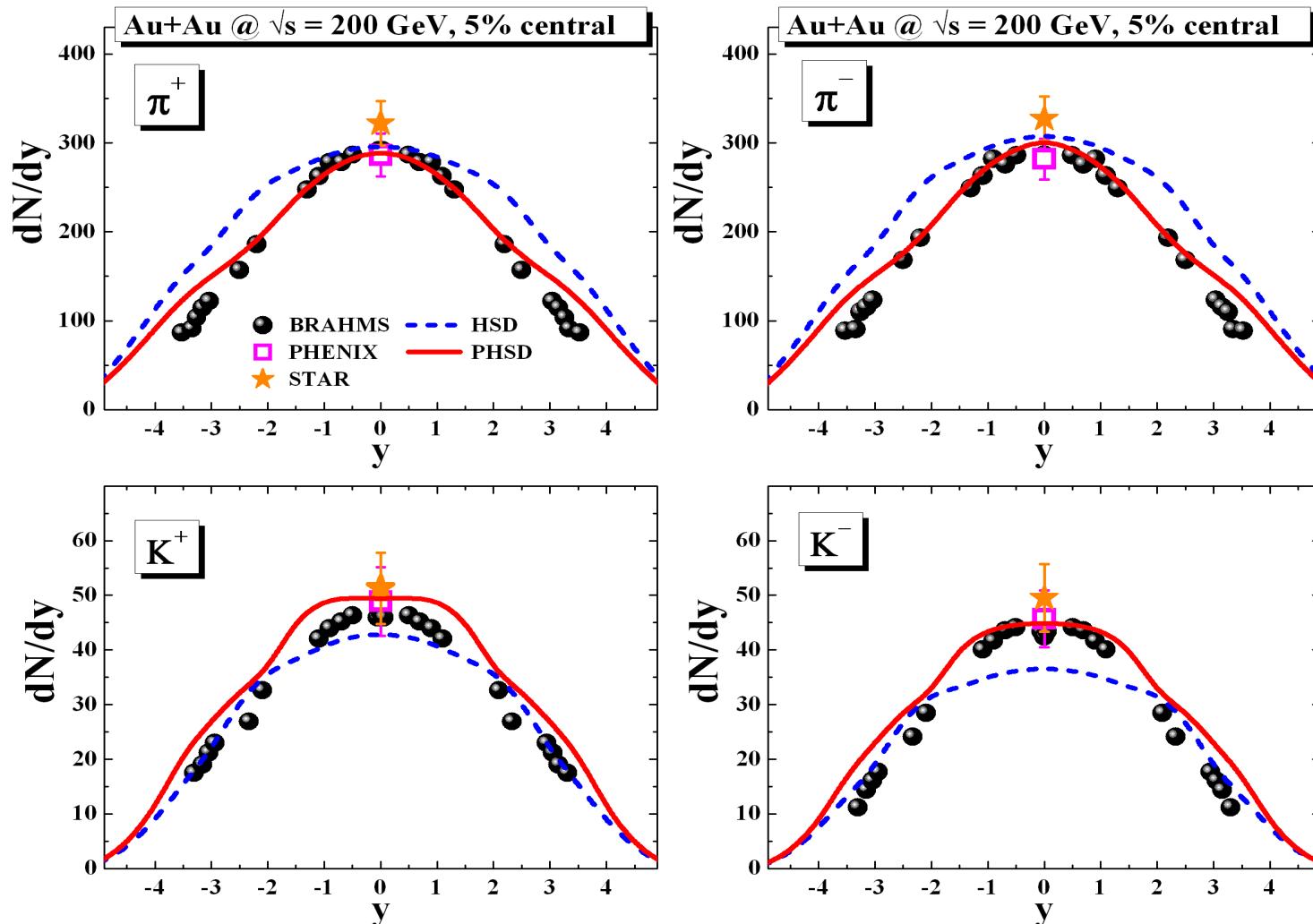
# Transverse mass spectra at SPS

## Central Pb + Pb at SPS energies



- ☺ PHSD gives harder spectra and works better than HSD at SPS (and top FAIR) energies
- ☹ However, at low SPS (and low FAIR) energies the effect of the partonic phase is NOT seen in rapidity distributions and  $m_T$  spectra

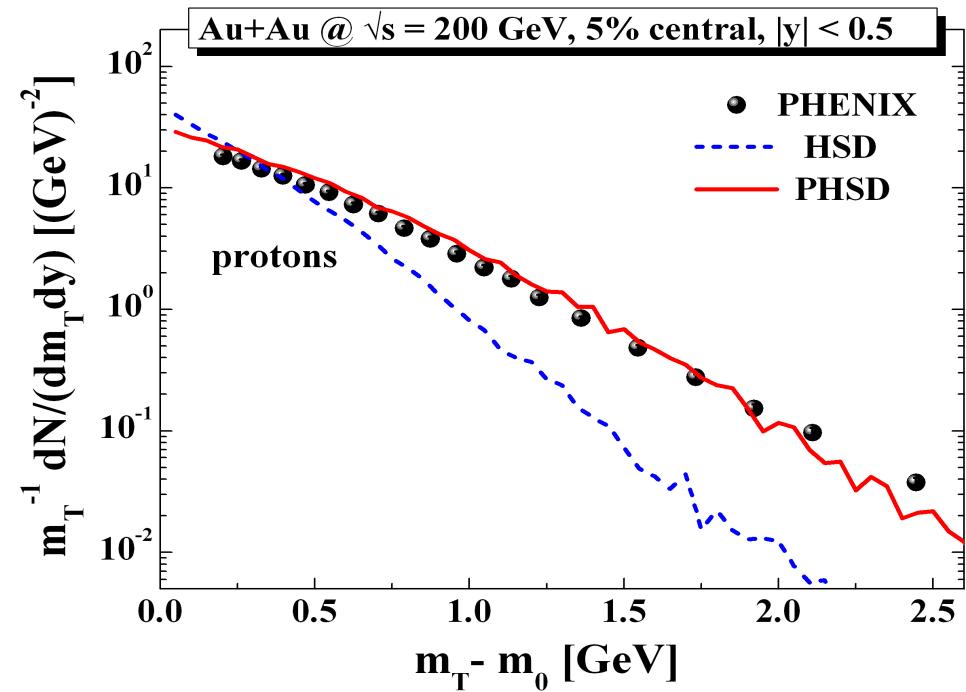
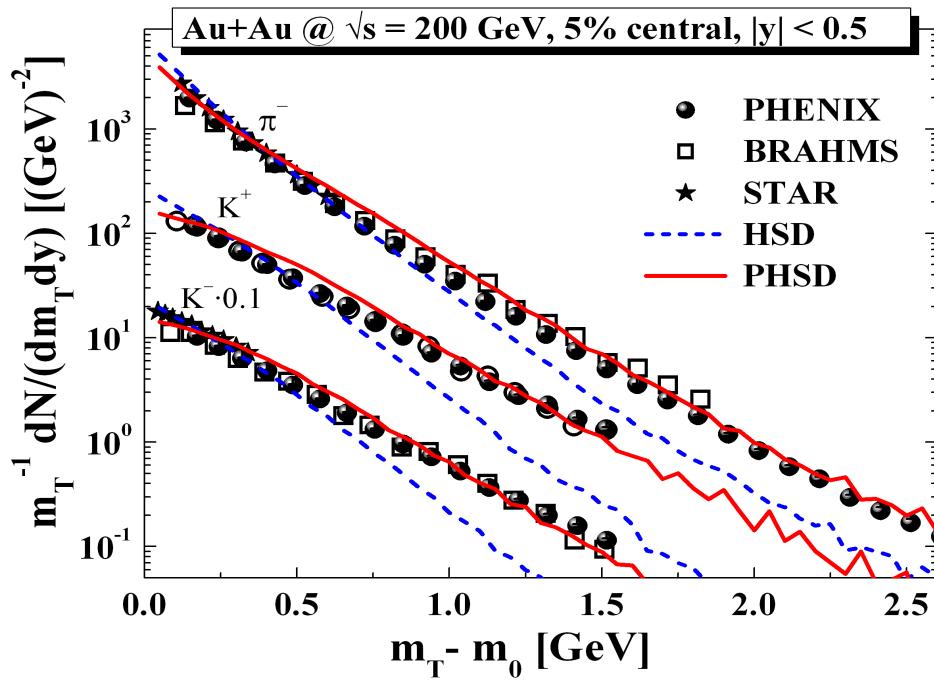
# Rapidity distributions in central Au+Au at RHIC



→ reasonable description of the data from BRAHMS, STAR, PHENIX!

# Transverse mass distributions at RHIC

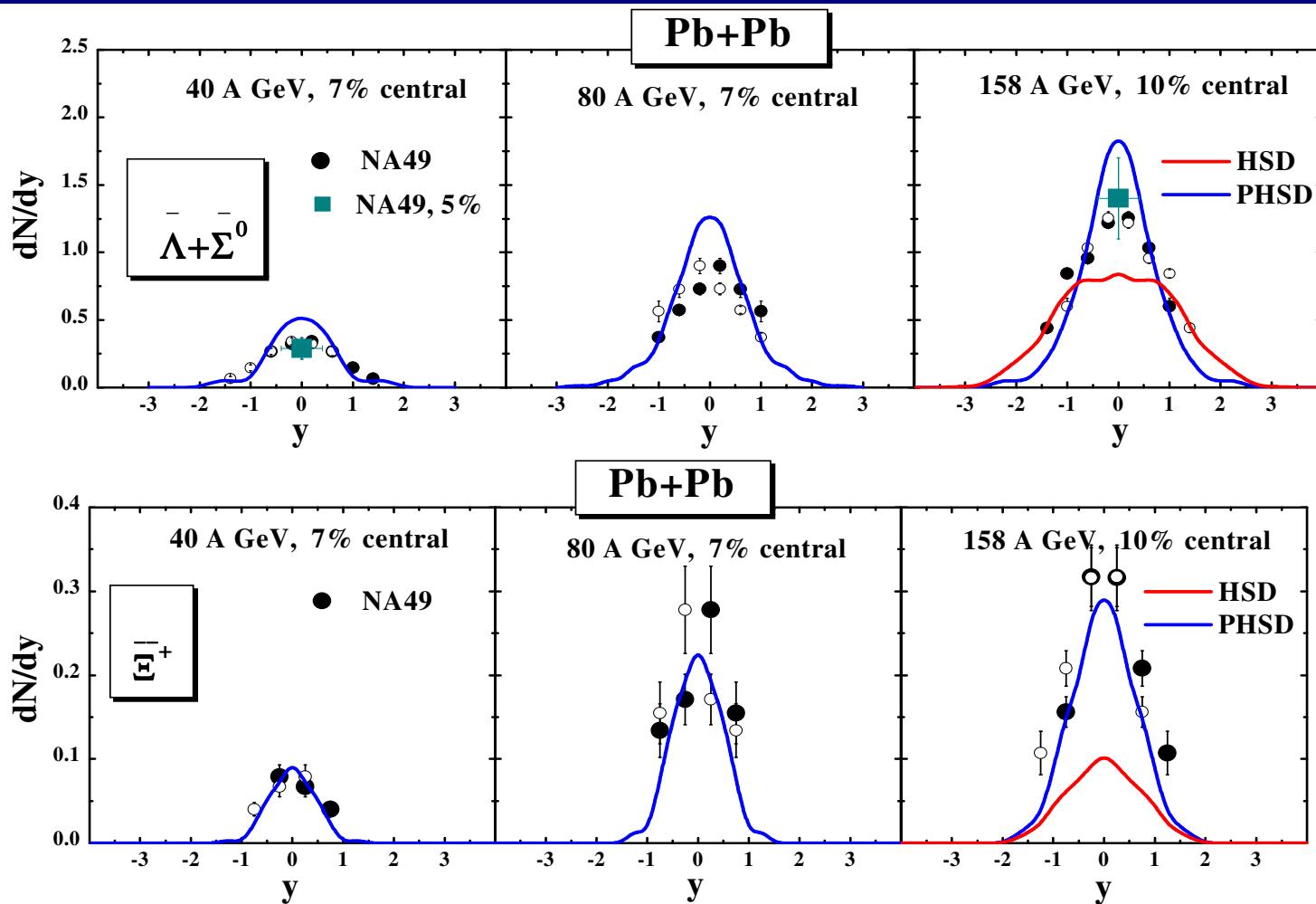
Au+Au at midrapidity  $|y| < 0.5$



→ PHSD gives harder spectra and works better than HSD at RHIC

Note: In PHSD the protons at midrapidity stem from hadronization of quarks.

# Rapidity distributions of (multi-)strange antibaryons

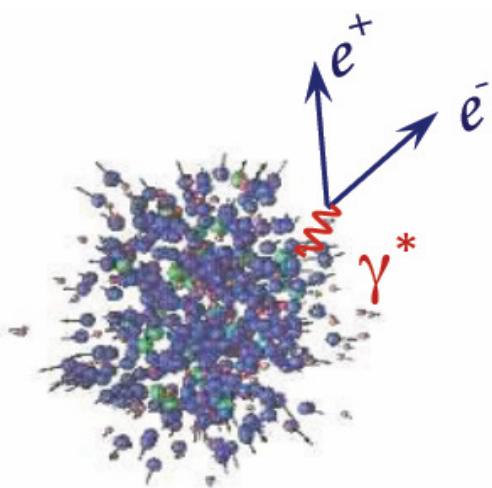


strange  
antibaryons  
 $\bar{\Lambda} + \bar{\Sigma}^0$

multi-strange  
antibaryon  
 $\Xi^- + \Xi^+$

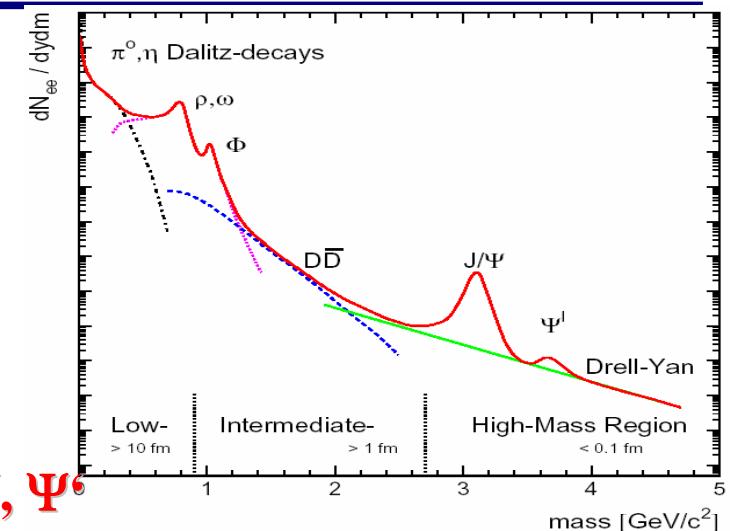
→ enhanced production of (multi-) strange anti-baryons in PHSD

# Observables 2: Dileptons



# Dilepton emission probes 2-particle correlations in contrast to 1-particle distributions

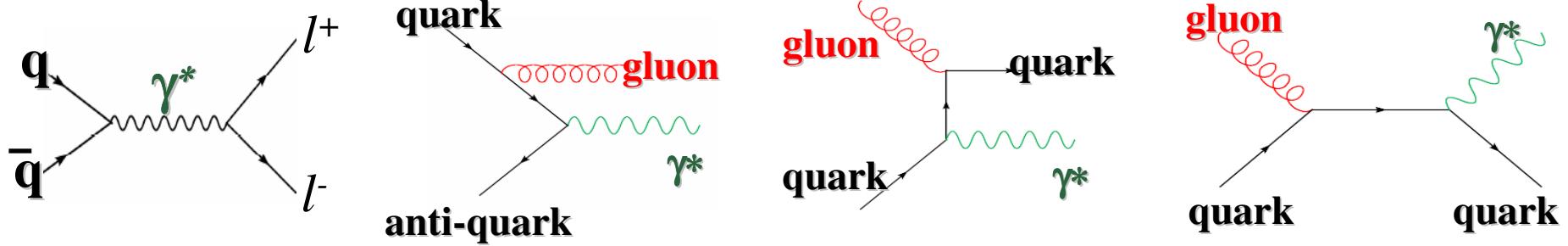
**Example: dilepton measurements access spectral functions of the particles, i.e. their interaction rates and decay properties**



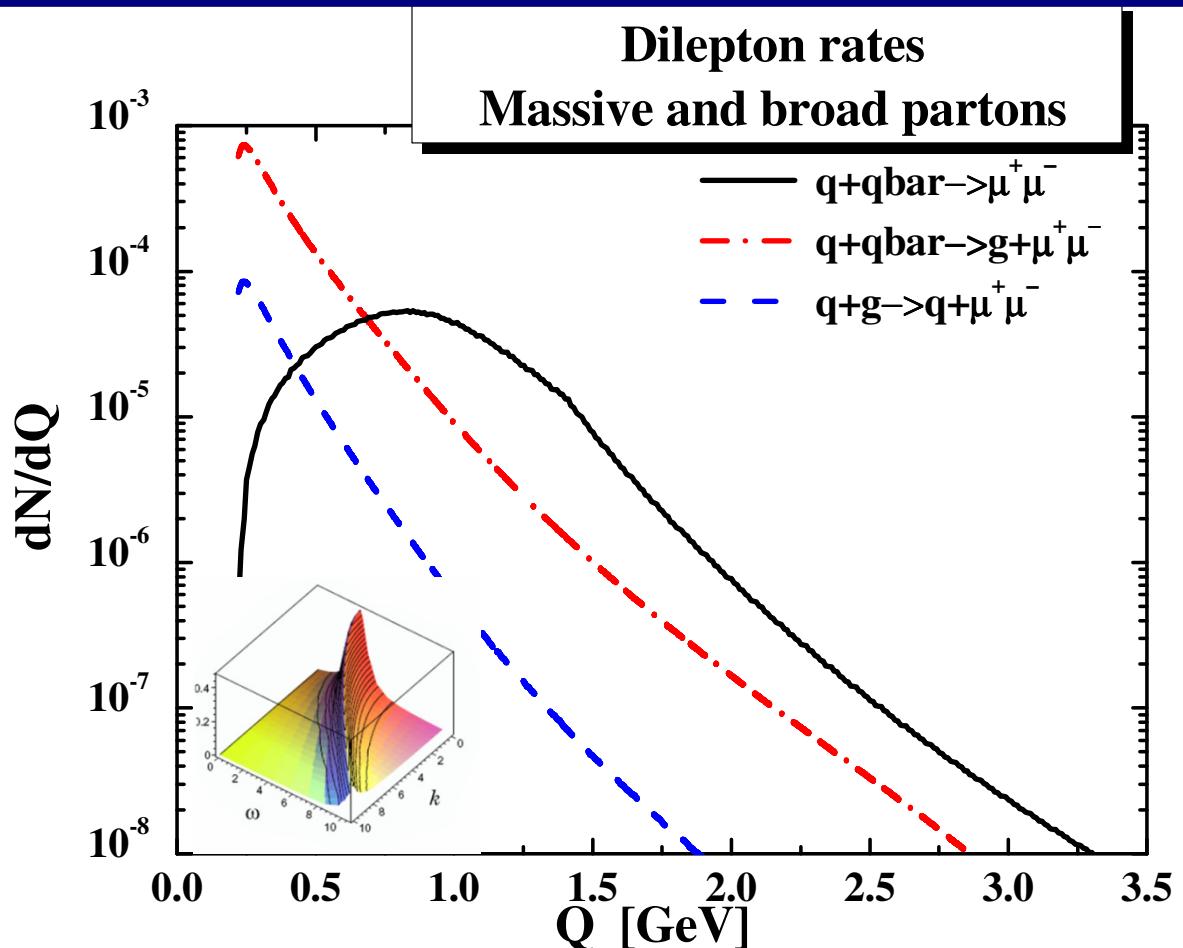
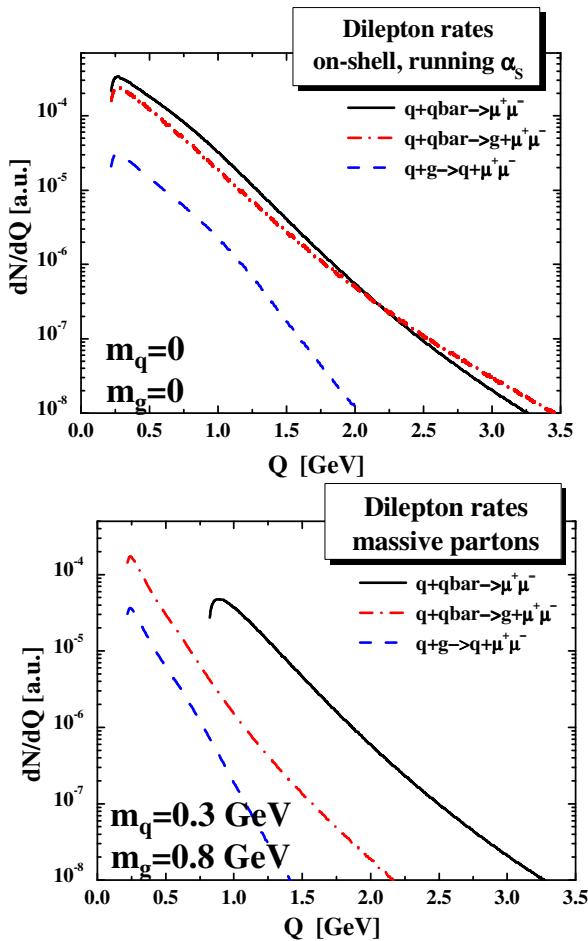
**Hadronic channels included:**

- direct and Dalitz decays of  $\pi_0, \eta, \eta^*, \rho, \omega, \phi, J/\Psi, \Psi'$
- semi-leptonic decays of (un-)correlated  $D+D_{\bar{b}ar}, B+B_{\bar{b}ar}$  pairs
- radiation from secondary mesons:  $\pi + \pi, \pi + \rho, \pi + \omega, \rho + \rho, \pi + a_1$

**Partonic channels:**



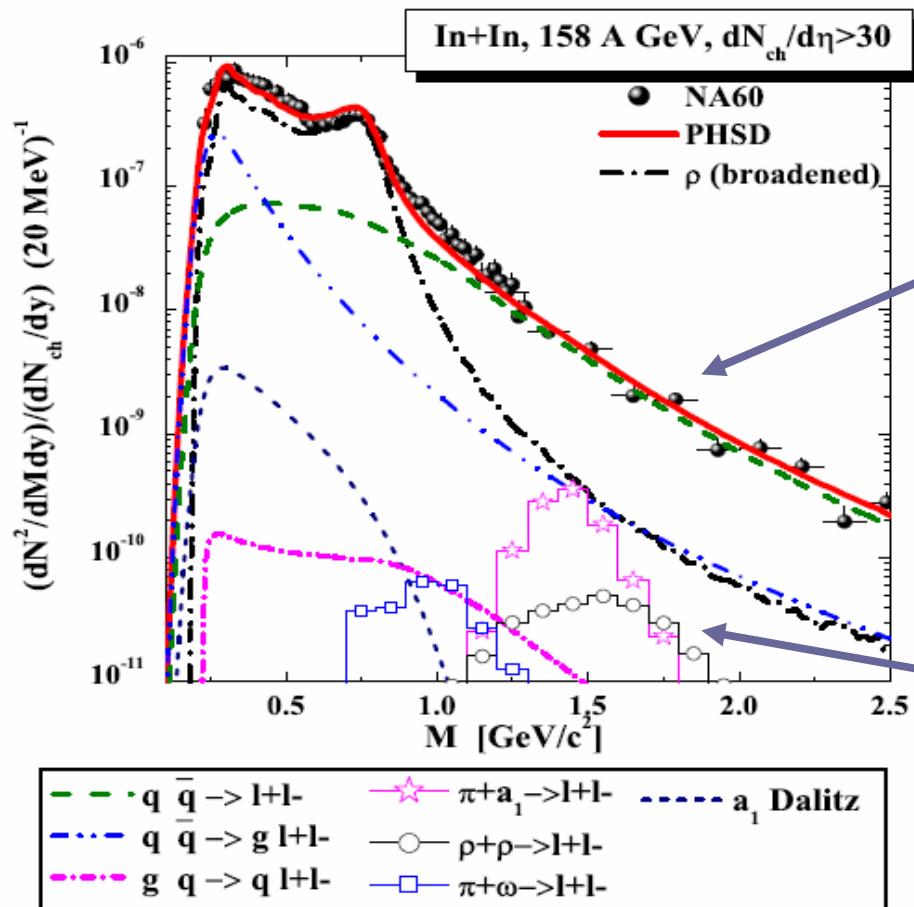
# Massive and broad quarks and gluons



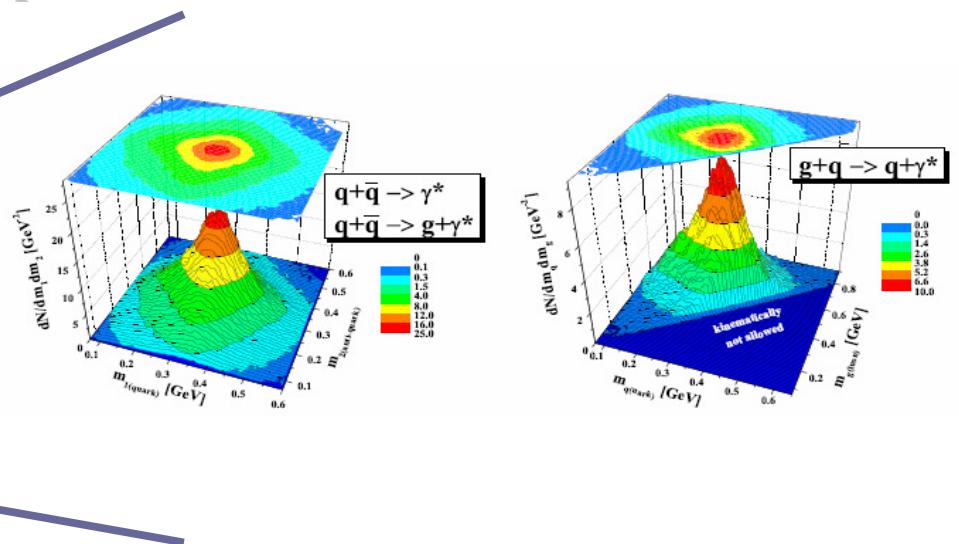
Due to broad spectral functions of partons, the threshold of the Born term is smeared, the contributions of the  $2 \rightarrow 2$  processes increased.

# Dileptons at SPS: NA60

## Acceptance corrected NA60 data

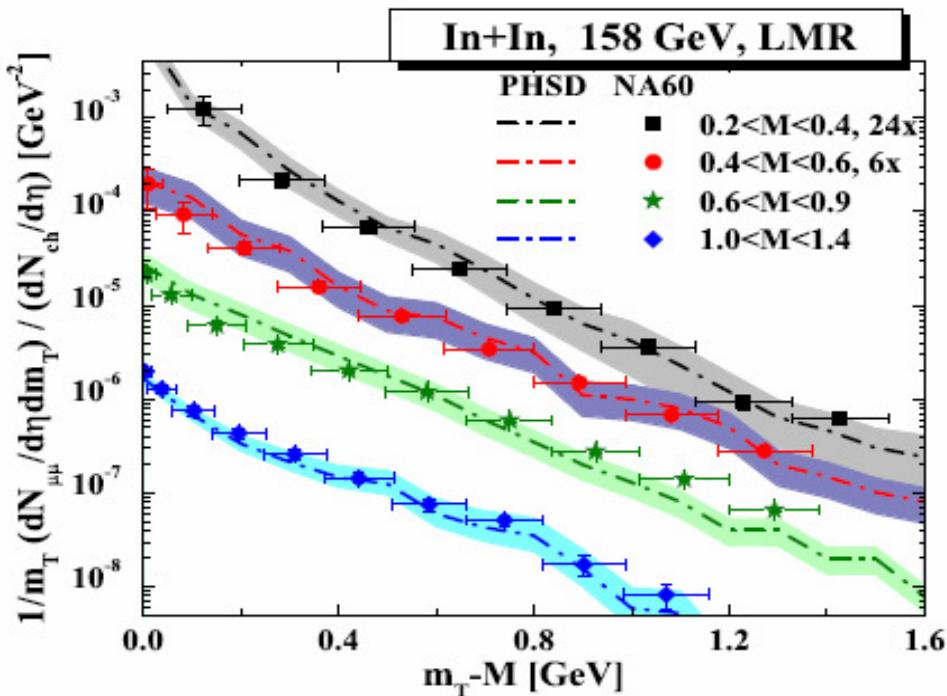


- Mass region above 1 GeV is dominated by partonic radiation

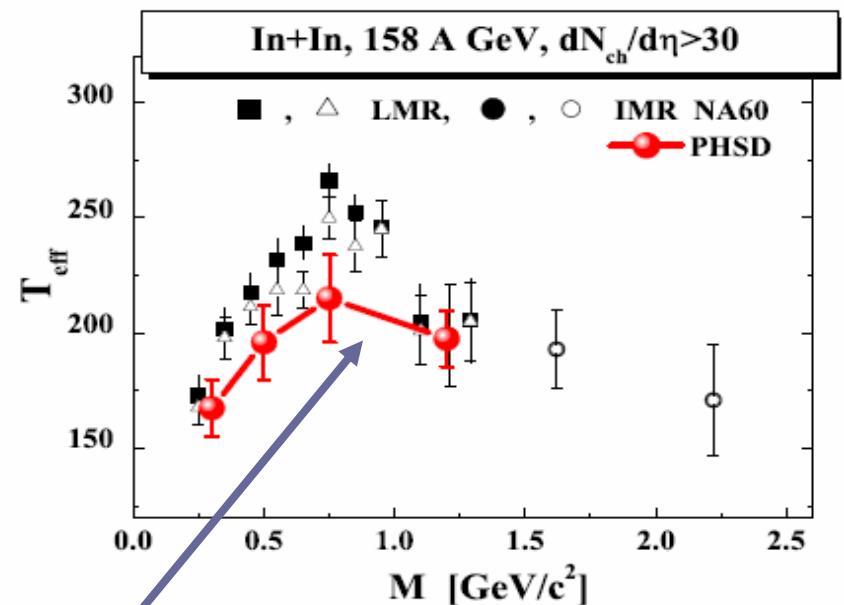


- Contributions of “4π” channels (radiation from multi-meson reactions) are small

# NA60: $m_T$ spectra



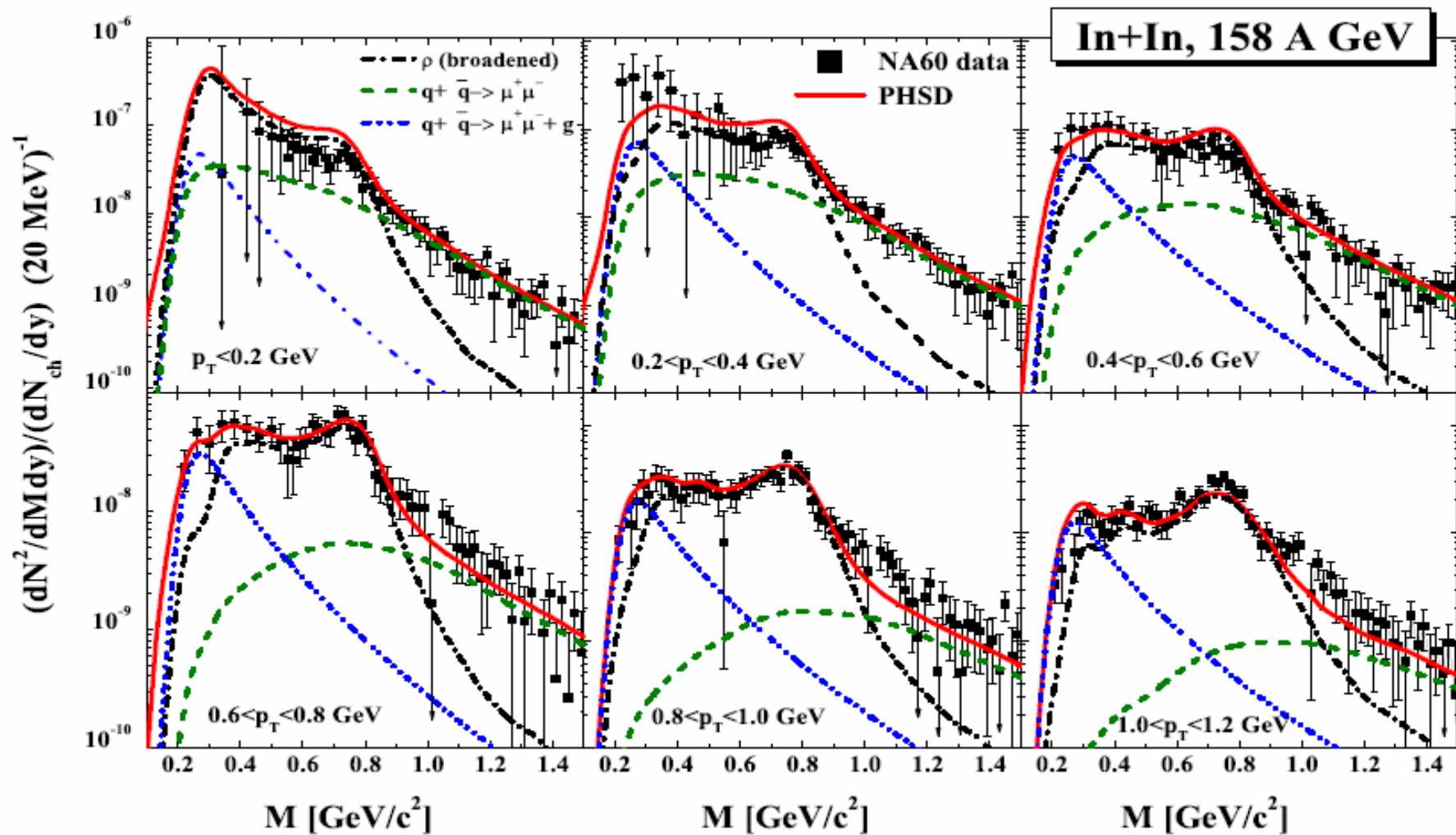
- Inverse slope parameter  $T_{\text{eff}}$  for dilepton spectra vs NA60 data



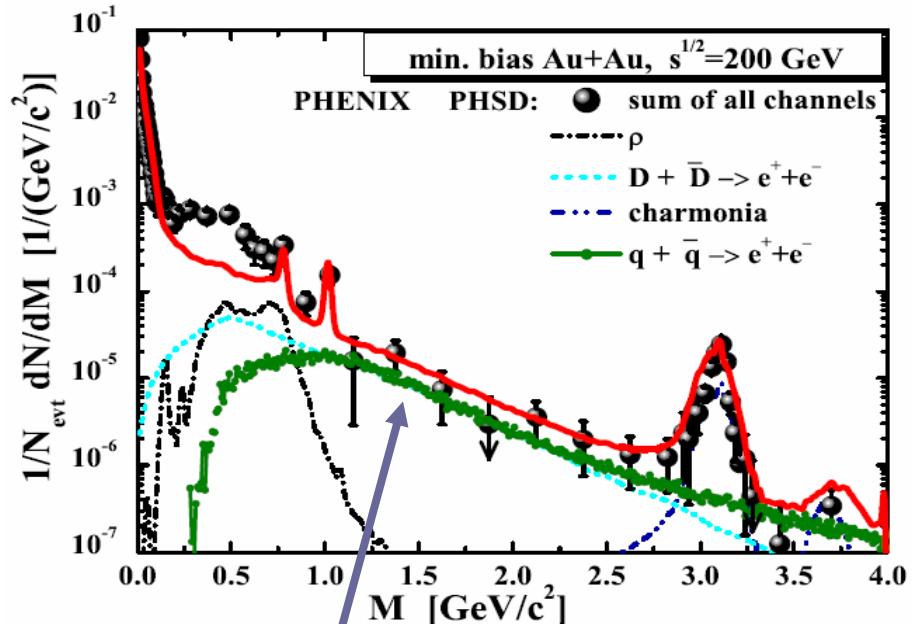
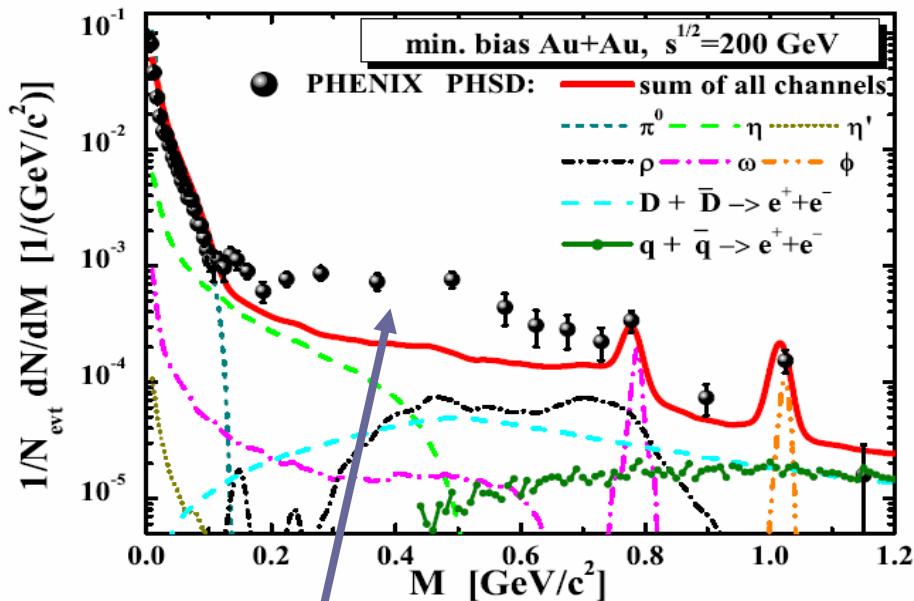
**Conjecture:**

- spectrum from sQGP is softer than from hadronic phase since quark-antiquark annihilation occurs dominantly before the collective radial flow has developed (cf. NA60)

# Dileptons at SPS: NA60



# PHENIX: dileptons from partonic channels

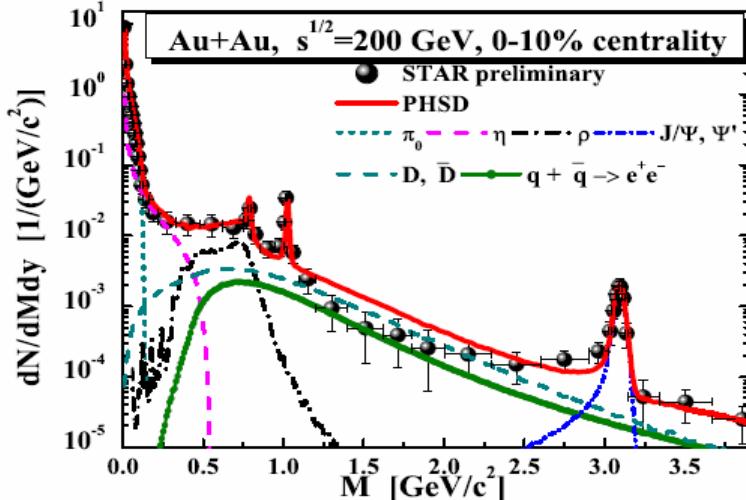
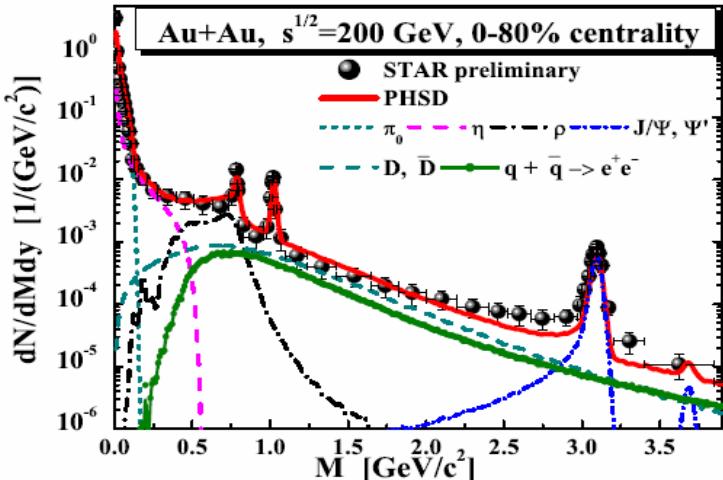
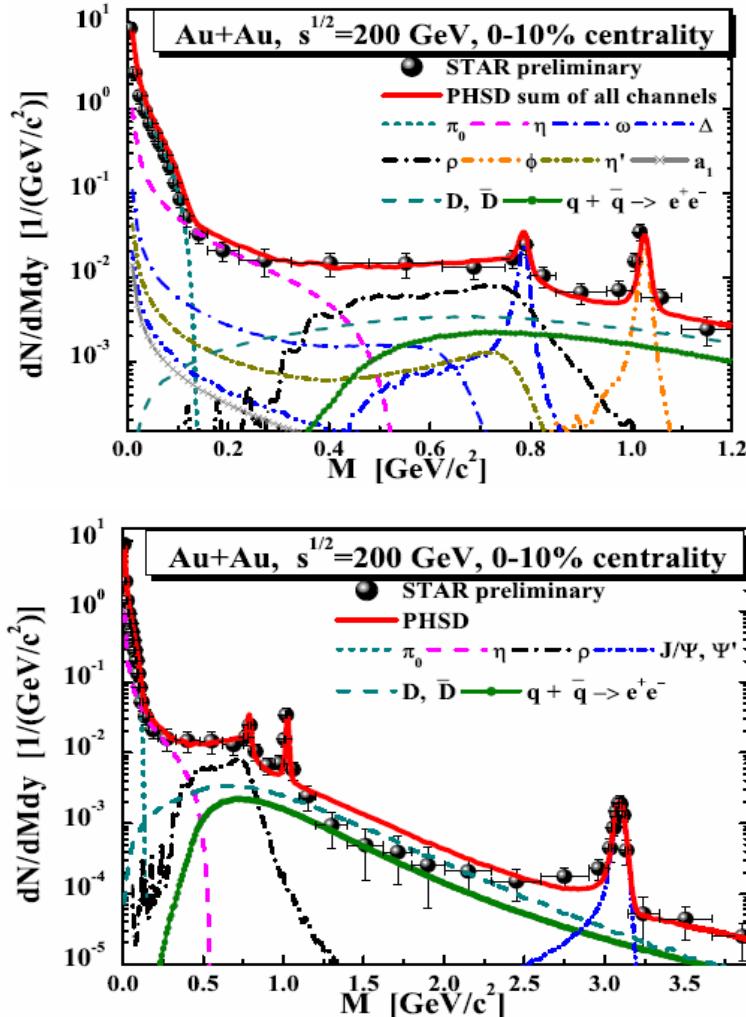
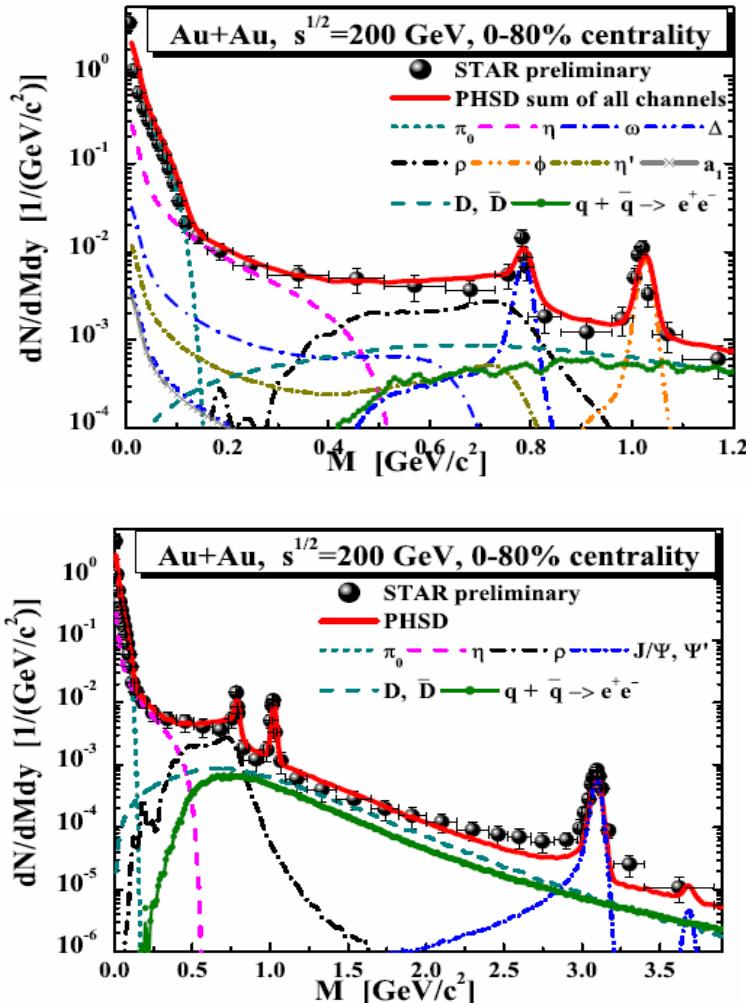


- The excess over the considered mesonic sources for  $M=0.15-0.6 \text{ GeV}$  is not explained by the QGP radiation as incorporated presently in PHSD

- The partonic channels fill up the discrepancy between the hadronic contributions and the data for  $M>1 \text{ GeV}$

→ Talk by Jaakko Manninen!

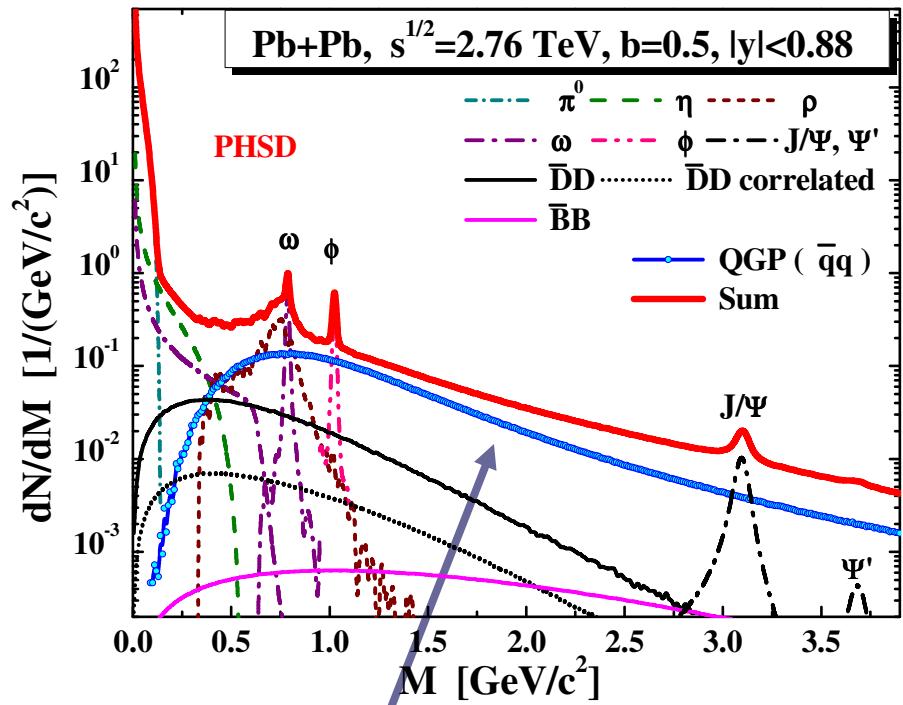
# STAR: dilepton mass spectra



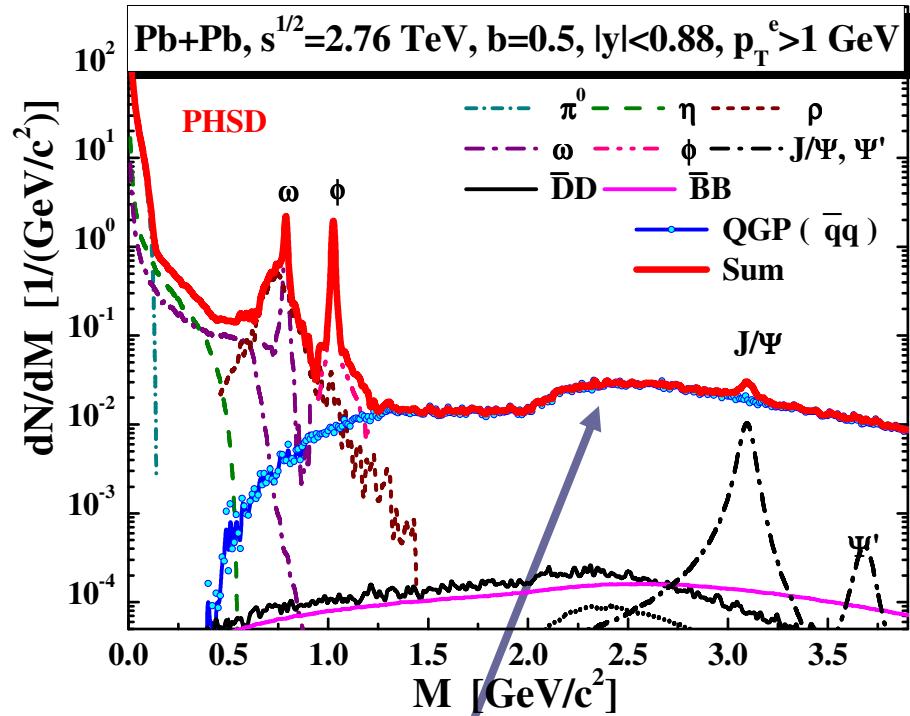
- STAR data are well described

→ Talk by Jaakko Manninen!

# LHC: dilepton mass spectra



QGP( $\overline{q}q$ ) dominates at  $M>1.2 \text{ GeV}$



$p_T$  cut enhances the signal of QGP( $\overline{q}q$ )

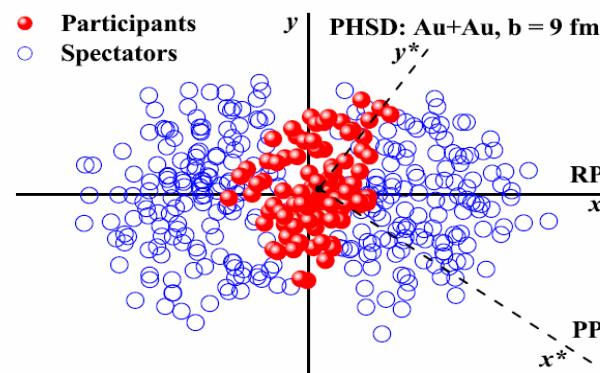
D-, B-mesons energy loss from Pol-Bernard Gossiaux and Jörg Aichelin

JPsi and Psi' nuclear modification from Che-Ming Ko and Taesoo Song

→ Talk by Jaakko Manninen!

O. Linnyk, J. Manninen et al. (2012)

# Observables 3: Flow harmonics ( $v_1$ , $v_2$ , $v_3$ , $v_4$ )



# Expanding fireball $v_2$

Elliptic flow  $v_2$  is defined by an anisotropy in momentum space:

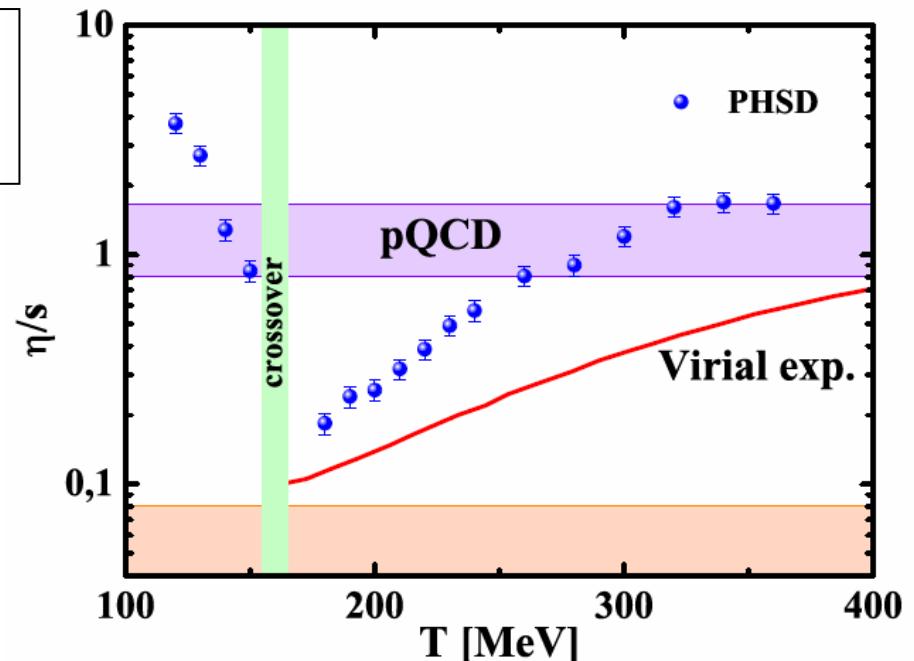
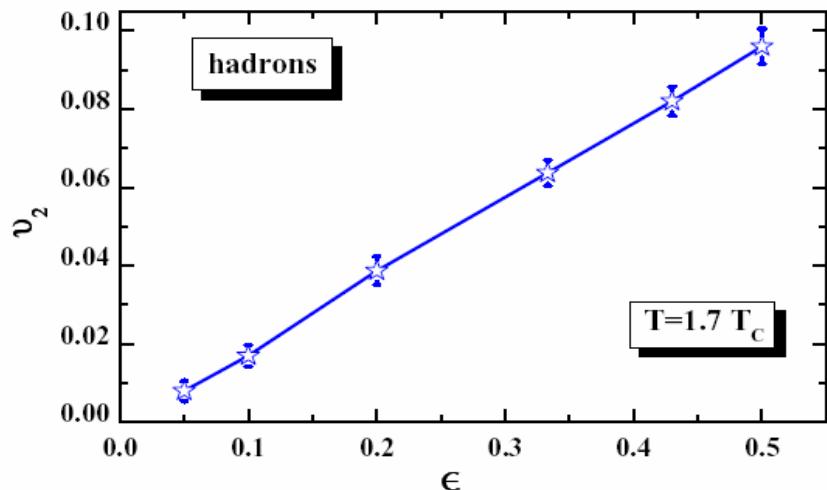
$$v_2 = (p_x^2 - p_y^2)/(p_x^2 + p_y^2)$$

Initially:  $v_2 = 0 \rightarrow$  study final  $v_2$  versus initial eccentricity  $\epsilon$  !

$$\epsilon = (\sigma_y^2 - \sigma_x^2)/(\sigma_y^2 + \sigma_x^2)$$

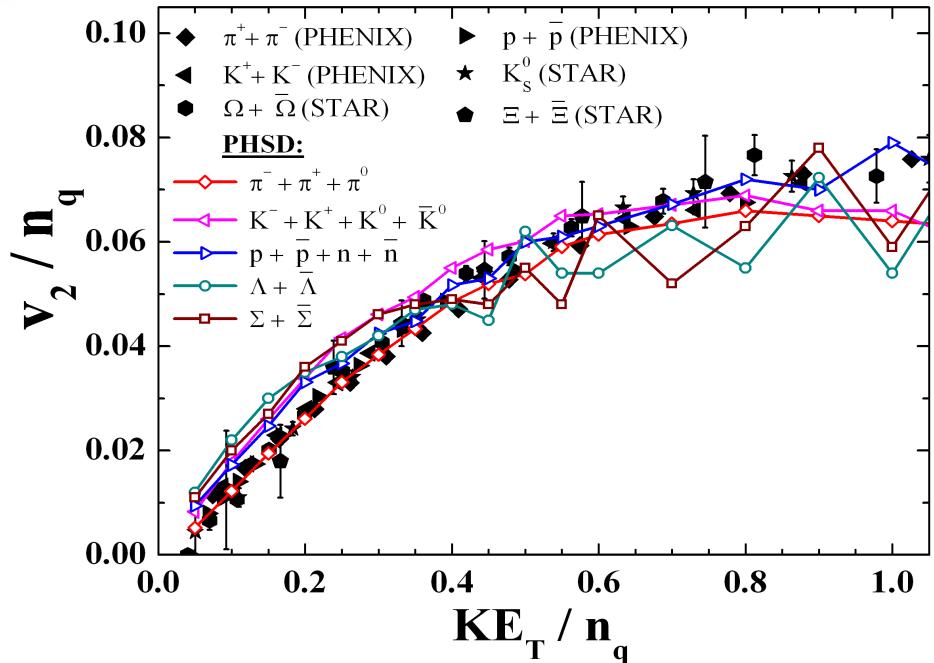
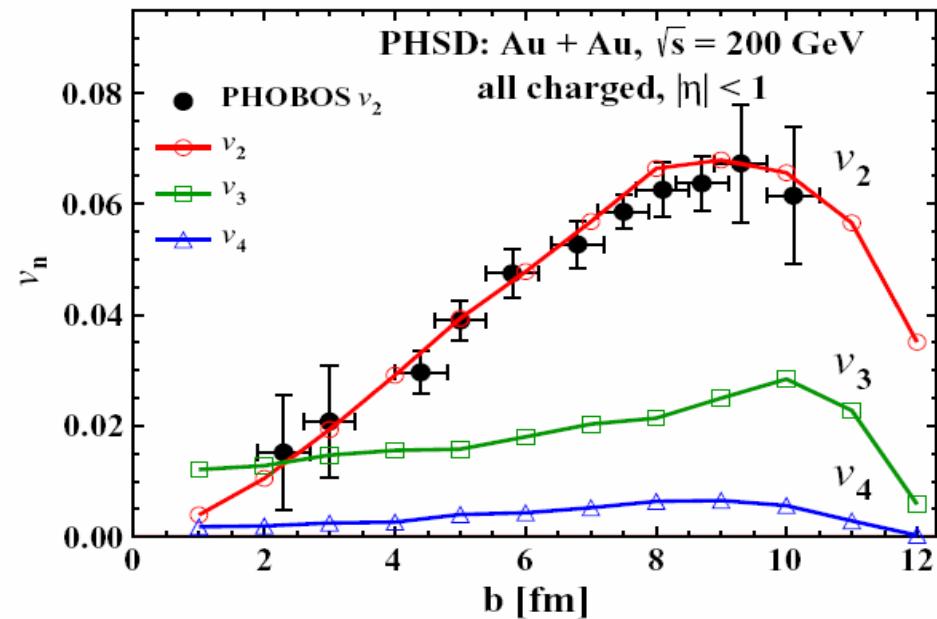
$$v_2/\epsilon = \text{const.}$$

indicates ideal hydrodynamic flow !



Expected since  $\eta/s$  is very small in the DQPM and PHSD. → Talk by Vitalii Ozvenchuk!

# Flow harmonics at RHIC

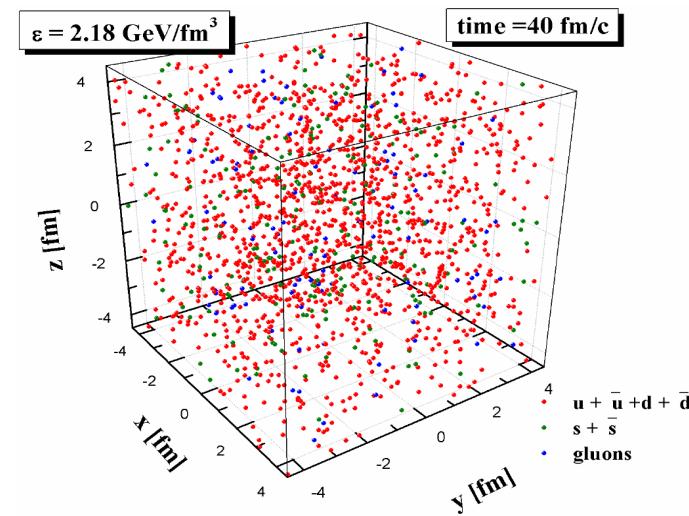


Increase of  $v_2$  with impact parameter but flat  $v_3$  and  $v_4$

The scaling of  $v_2$  with the number of constituent quarks  $n_q$  in line with data .

→ Talk by Volodya Konchakovski!

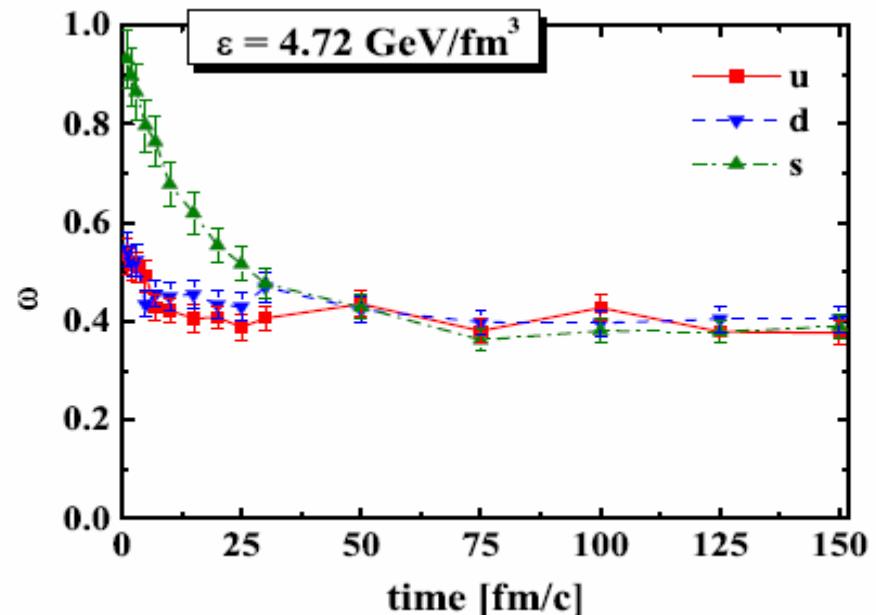
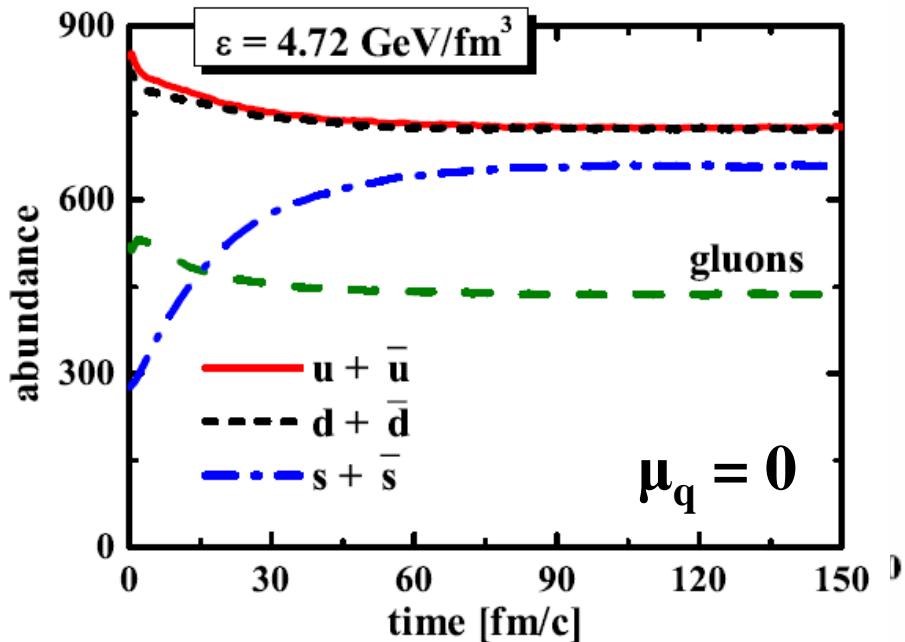
# Equilibration



# ‘Infinite’ parton matter. Equilibration.

Initialize the system in a finite box with periodic boundary conditions with some number of partons and 4-momentum distributions in line with the DQPM → energy density  $\varepsilon = E/V$  and chemical potential  $\mu_q$

Evolve the system in time until equilibrium is achieved

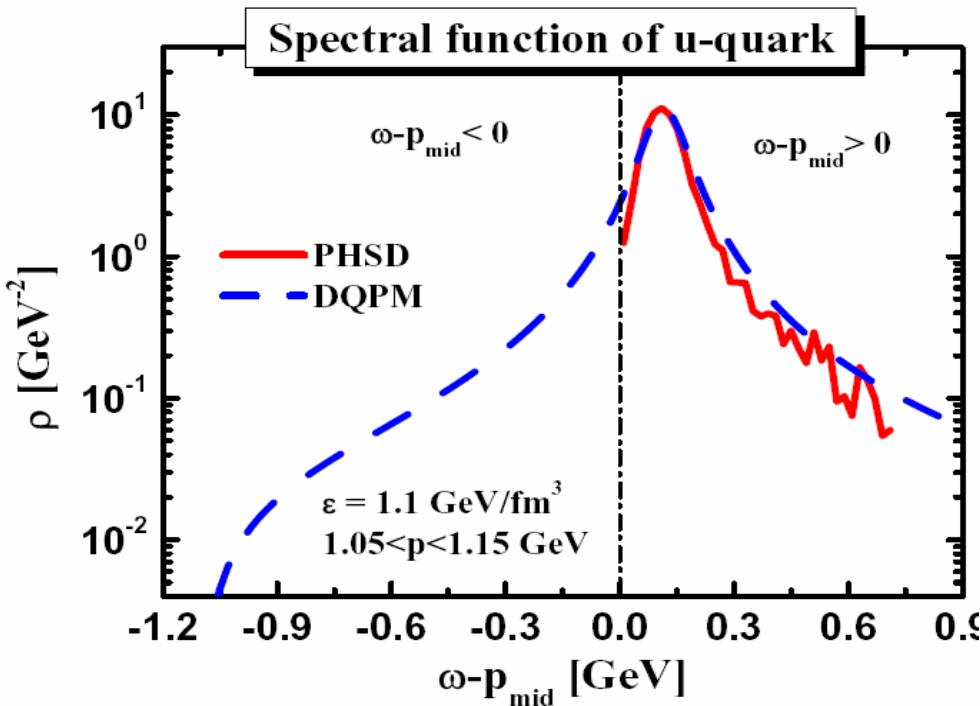


Fluctuations in parton number

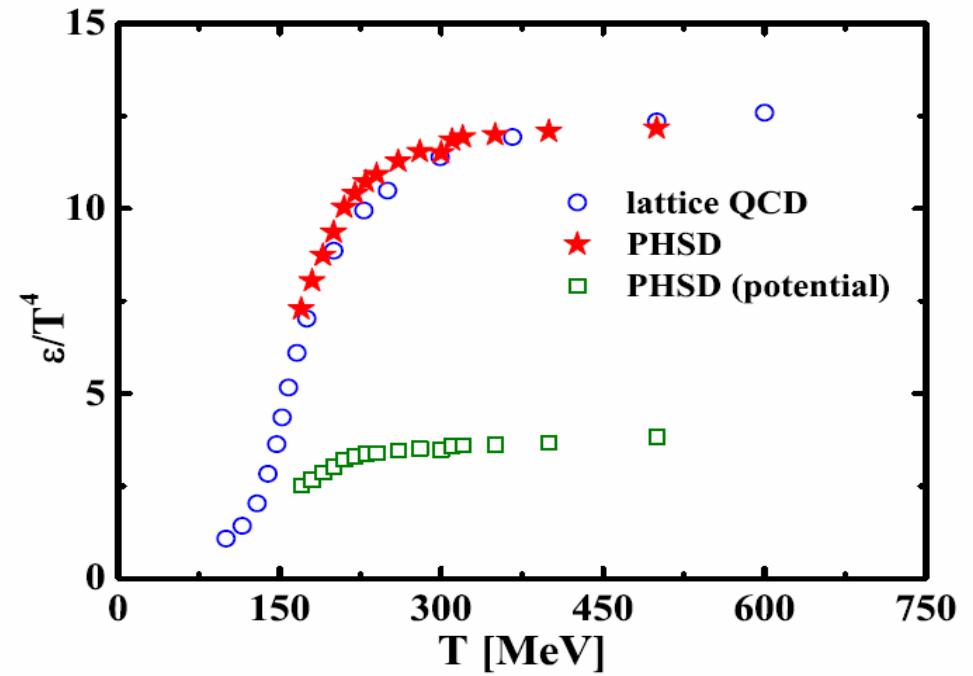
→ Talk by Vitalii Ozvenchuk!

# Equilibrium properties.

## Equilibrium spectral function of u-quark



## Equation of state

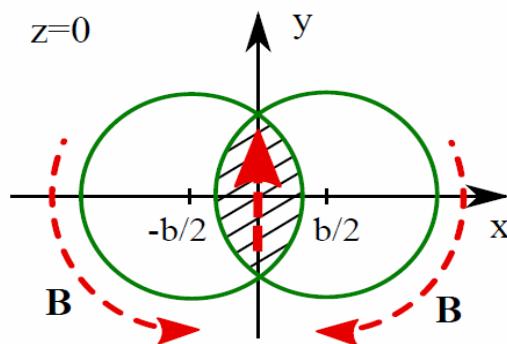


Good match between PHSD and the DQPM

Note: PHSD propagates only time-like partons

→ Talk by Vitalii Ozvenchuk!

# Electro-magnetic fields, Chiral magnetic effect



# PHSD - transport model with electromagnetic fields

Generalized transport equations in the presence of electromagnetic fields :

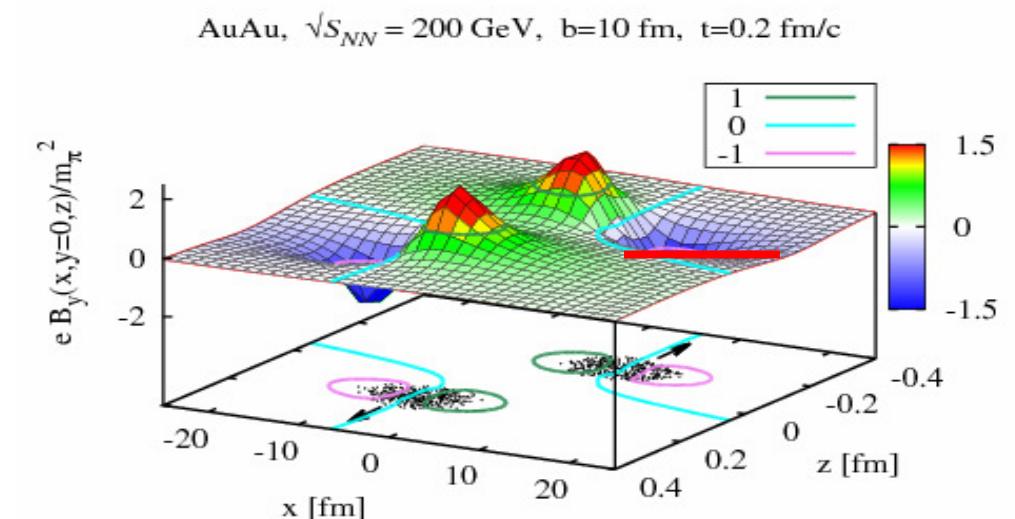
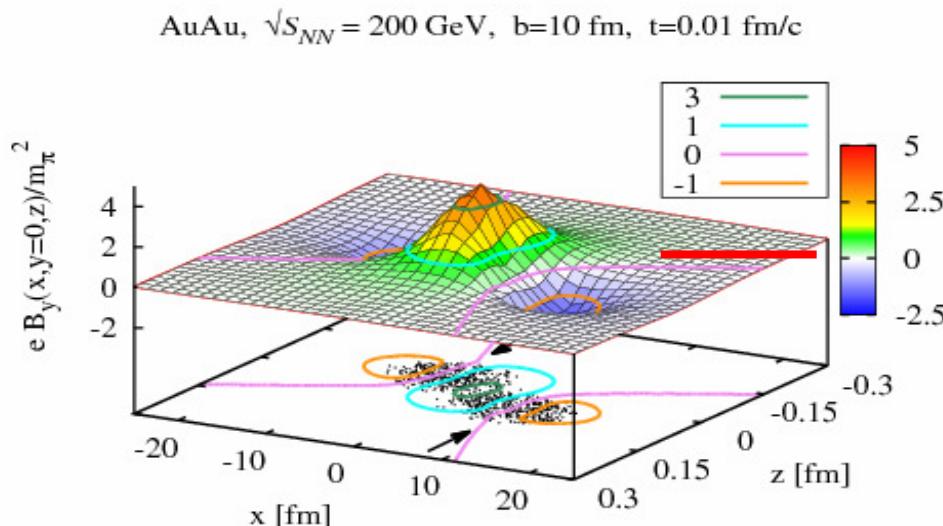
$$\dot{\vec{r}} \rightarrow \frac{\vec{p}}{p_0} + \vec{\nabla}_p U, \quad U \sim Re(\Sigma^{ret})/2p_0$$

$$\dot{\vec{p}} \rightarrow -\vec{\nabla}_r U + e\vec{E} + e\vec{v} \times \vec{B}$$

$$\vec{A}(\vec{r}, t) = \frac{1}{4\pi} \int \frac{\vec{j}(\vec{r}', t') \delta(t - t' - |\vec{r} - \vec{r}'|/c)}{|\vec{r} - \vec{r}'|} d^3 r' dt'$$

$$\Phi(\vec{r}, t) = \frac{1}{4\pi} \int \frac{\rho(\vec{r}', t') \delta(t - t' - |\vec{r} - \vec{r}'|/c)}{|\vec{r} - \vec{r}'|} d^3 r' dt'$$

Magnetic field evolution in HSD/PHSD :



→ Talk by Volodya Konchakovski!



# Conclusions

- Parton-Hadron-String-Dynamics (PHSD) theory provides a consistent description of the phase transition to the QGP in heavy-ion collisions. The dynamical quasiparticle model (DQPM) defines the input for the partonic phase in the PHSD transport in line with lattice QCD.
- Phase transition to the deconfined phase leads to narrower rapidity distributions of produced mesons, harder  $p_T$  spectra, constituent quark number scaling of  $v_2$ , enhancement of antihyperon yield. Partonic repulsive mean fields generate flow which scales with the initial space eccentricity as in an ideal hydro.
- The dilepton data provide evidence for off-shell dynamics of vector mesons and partons. QGP radiation seen in the data.
- In the ‘box’, the PHSD shows a low viscosity in the partonic phase, slow equilibration of strangeness; spectral functions in line with DQPM.

# Thank you!



**Wolfgang Cassing  
Elena Bratkovskaya**

**Volodya Konchakovski  
Jaakko Manninen  
Vitalii Ozvenchuk  
Rudy Marty**

*PHSD Team*

**Che-Ming Ko  
Taesoo Song  
Jörg Aichelin  
Pol Bernard Gossiaux  
Mark I. Gorenstein  
Viatcheslav D. Toneev  
Vadym Voronyuk**

*Collaboration*

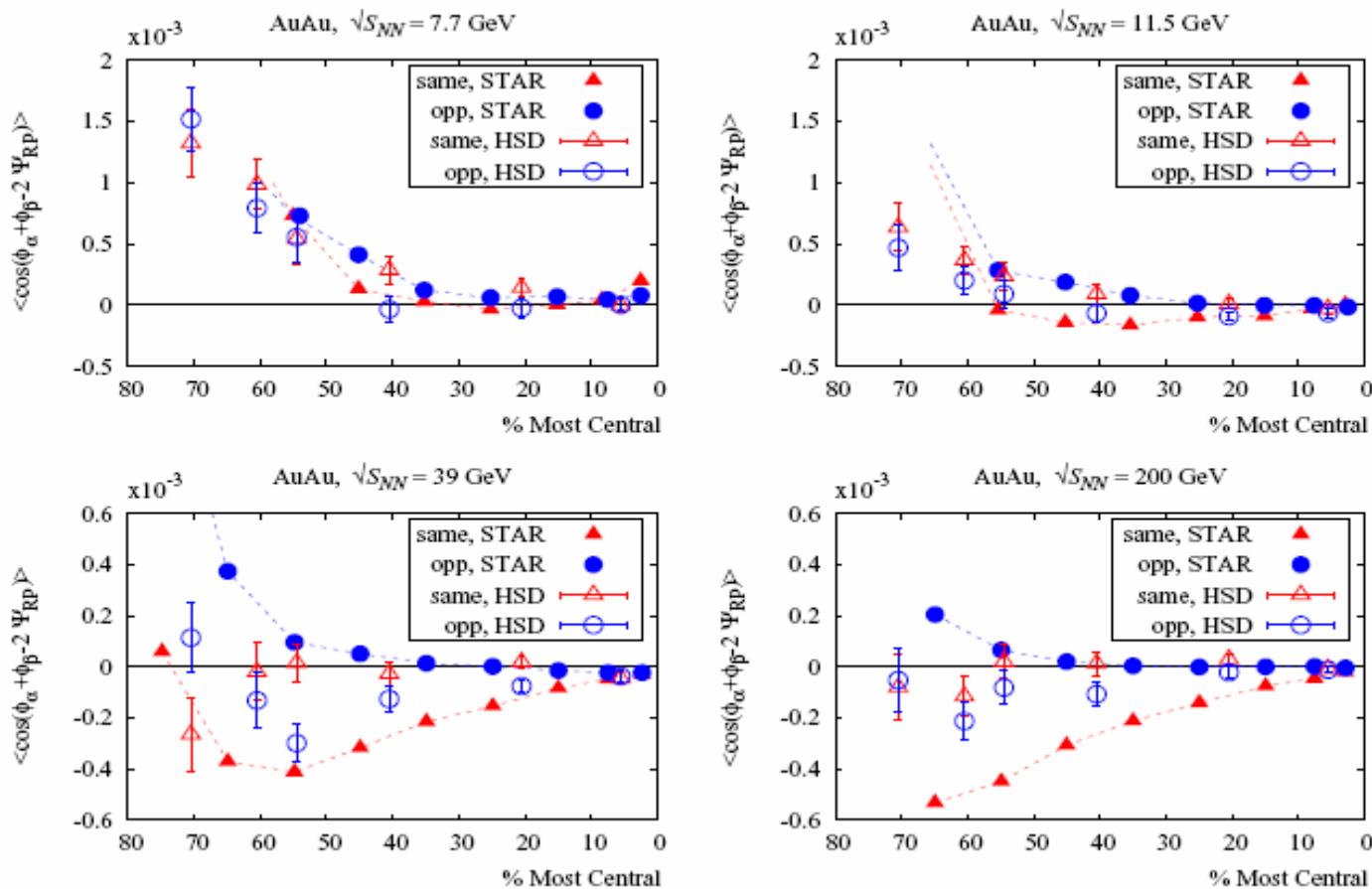


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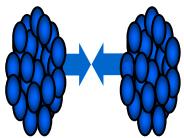
**Back up slides**

# Angular correlation wrt. reaction plane

$$\langle \cos(\psi_\alpha + \psi_\beta - 2\Psi_{RP}) \rangle$$



Angular correlation is of hadronic origin up to  $\sqrt{s} = 11 \text{ GeV} !$



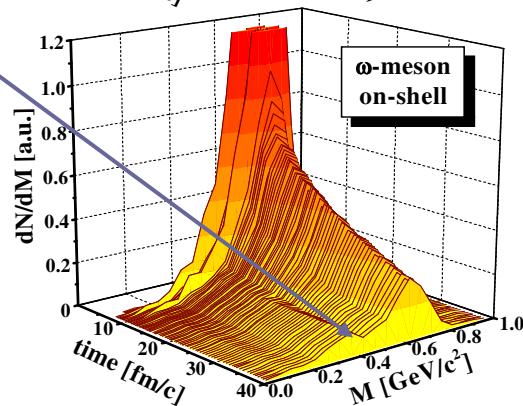
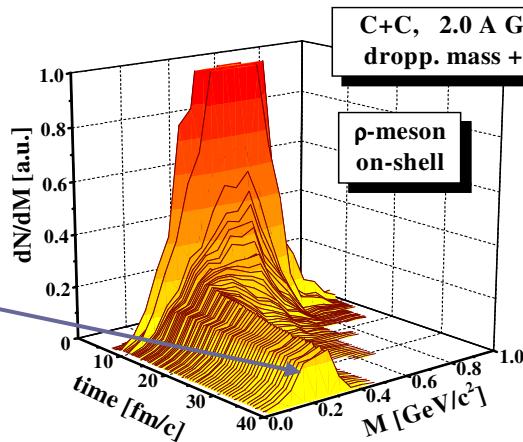
## Off-shell vs. on-shell transport dynamics

Time evolution of the mass distribution of  $\rho$  and  $\omega$  mesons for central C+C collisions ( $b=1$  fm) at  $2 A$  GeV for dropping mass + collisional broadening scenario

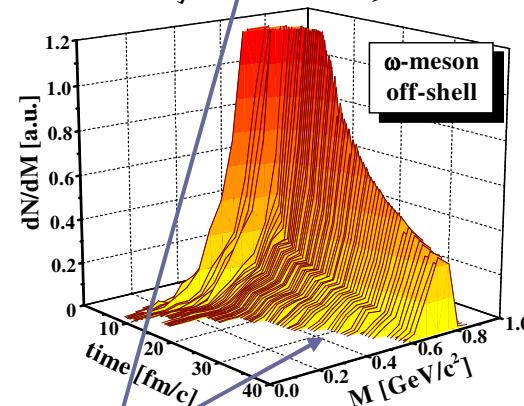
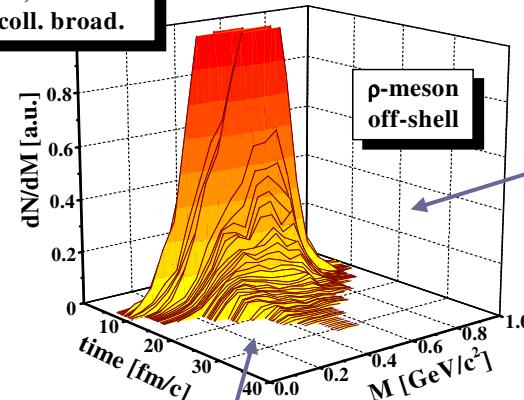
E.L.B. & W. Cassing, NPA 807 (2008) 214

### On-shell

On-shell model:  
low mass  $\rho$  and  $\omega$   
mesons live forever  
and shine dileptons!



### Off-shell



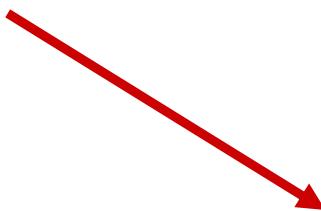
The off-shell spectral function becomes on-shell in the vacuum dynamically by propagation through the medium!

# Off-shell LO q+qbar

$$\left( \frac{d^3\hat{\sigma}(q\bar{q} \rightarrow l^+l^-)}{dQ^2 dx_F dq_T^2} \right)_{\text{on-shell}}^{\text{DY}} = \frac{4\pi\alpha^2 e_q^2}{9Q^4} \frac{x_1 x_2}{x_1 + x_2} (1 - x_1 x_2) \\ \times \delta(q_T^2) \delta(Q^2 - x_1 x_2 S_{NN}) \delta\left(x_F - \frac{x_2 - x_1}{1 - x_1 x_2}\right)$$

$$Q^2 = s = x_1 x_2 S_{NN};$$

$$x_F = (x_2 - x_1)/(1 - x_1 x_2).$$

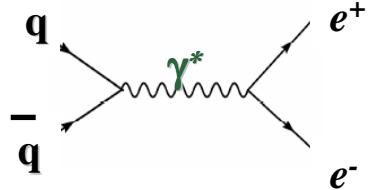


$$\left( \frac{d^3\hat{\sigma}(m_1, m_2, \vec{p}_1, \vec{p}_2)}{dQ^2 dx_F dq_T^2} \right)_{\text{off-shell}}^{\text{DY}} = \\ \kappa' \left[ 2Q^4 - Q^2 (m_1^2 - 6m_1 m_2 + m_2^2) - (m_1^2 - m_2^2)^2 \right] \\ \times \delta(Q^2 - m_1^2 - m_2^2 - 2(p_1 \cdot p_2)) \\ \times \delta\left(x_F - \frac{\sqrt{s}}{s - Q^2} (p_{2z} - p_{1z})\right) \\ \times \delta\left(q_T^2 - (\vec{p}_{1\perp} + \vec{p}_{2\perp})^2\right),$$

with

$$\kappa' = \frac{\pi\alpha^2 e_q^2}{3Q^4 N_c \sqrt{(p_1 \cdot p_2)^2 - m_1^2 m_2^2}}.$$

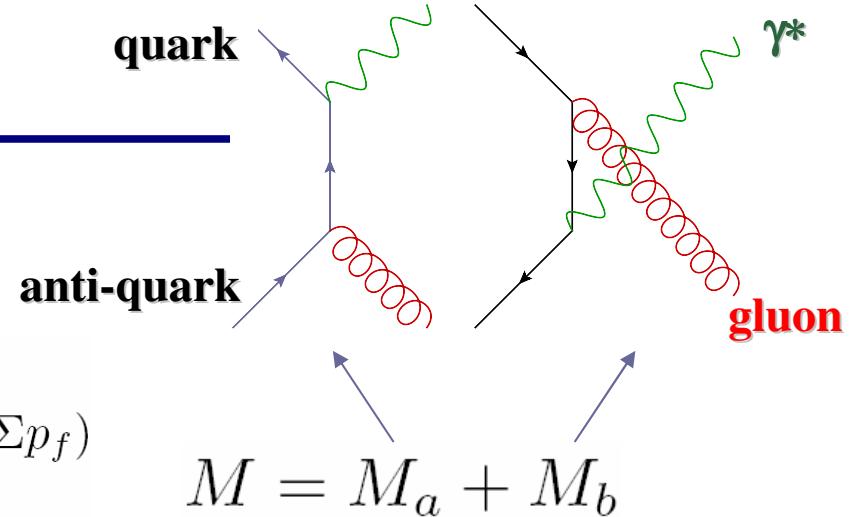
**Note: In the limit of parton masses  $\rightarrow 0$ , the perturbative QCD result is recovered**



# Off-shell NLO q+qbar

$$\frac{d\sigma(l^+l^-)}{dQ^2 dt} = \frac{\alpha}{3\pi Q^2} \frac{d\sigma(\gamma^*)}{dt} \sqrt{1 - \frac{Q_0^2}{Q^2}} \left(1 + \frac{Q_0^2}{2Q^2}\right)$$

$$d\sigma = \frac{\Sigma |\bar{M}_{i \rightarrow f}|^2 \varepsilon_1 \varepsilon_2 \Pi \frac{d^3 p_f}{(2\pi)^3}}{\sqrt{(p_1 p_2)^2 - m_1^2 m_2^2}} (2\pi)^4 \delta(p_1 + p_2 - \sum p_f)$$



$$M_a = -e_q e g_s T_{ij}^l \frac{\epsilon_\nu(q) \epsilon_{\sigma l}(k)}{p_3^2 - m_3^2} \\ \times u_i(p_1, m_1) [\gamma^\nu(\hat{p}_3 + m_3) \gamma^\sigma] v_j(p_2, m_2)$$

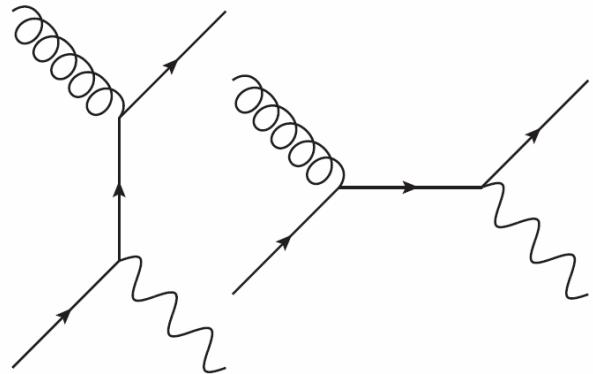
$$M_b = -e_q e g_s T_{ij}^l \frac{\epsilon_{\sigma l}(k) \epsilon_\nu(q)}{\bar{p}_3^2 - m_3^2} \\ \times u_i(p_1, m_1) [\gamma^\eta(\hat{p}_3 + m_3) \gamma^\nu] v_j(p_2, m_2)$$

$$\sum |M|^2 = \sum M_a^* M_a + \sum M_b^* M_b + \sum M_a^* M_b + \sum M_b^* M_a.$$

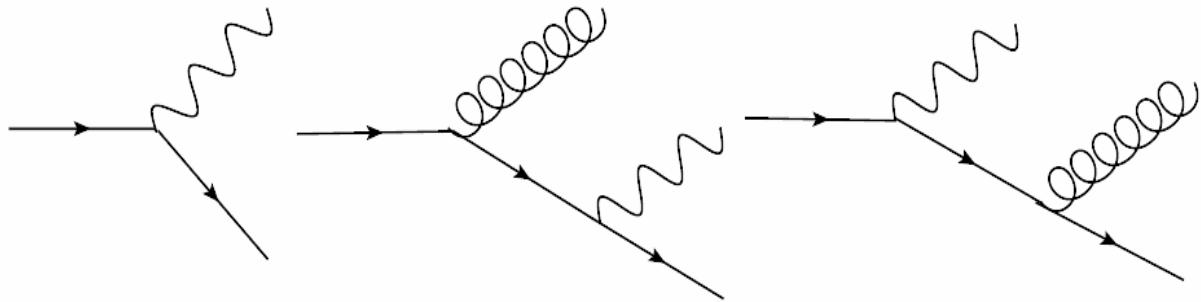
$$\sum |M_a|^2 = -\frac{e_q^2 e^2 g_s^2 \text{Tr}\{T^2\}}{(p_3^2 - m_3^2)^2} [\text{Tr} \{ \gamma_\sigma(\hat{p}_3 + m_3) \gamma_\nu(\hat{p}_1 + m_1) \gamma^\nu(\hat{p}_3 + m_3) \gamma^\sigma(\hat{p}_2 - m_2) \} \\ - \frac{1}{Q^2} \text{Tr} \{ \gamma_\sigma(\hat{p}_3 + m_3) \hat{q}(\hat{p}_1 + m_1) \hat{q}(\hat{p}_3 + m_3) \gamma^\sigma(\hat{p}_2 - m_2) \} \\ - \frac{A}{k^2} \text{Tr} \{ \hat{k}(\hat{p}_3 + m_3) \gamma_\nu(\hat{p}_1 + m_1) \gamma^\nu(\hat{p}_3 + m_3) \hat{k}(\hat{p}_2 - m_2) \} \\ + \frac{A}{k^2 Q^2} \text{Tr} \{ \hat{k}(\hat{p}_3 + m_3) \hat{q}(\hat{p}_1 + m_1) \hat{q}(\hat{p}_3 + m_3) \hat{k}(\hat{p}_2 - m_2) \}]$$

...etc. See details in  
O. L., J.Phys.G38 (2011) 025105

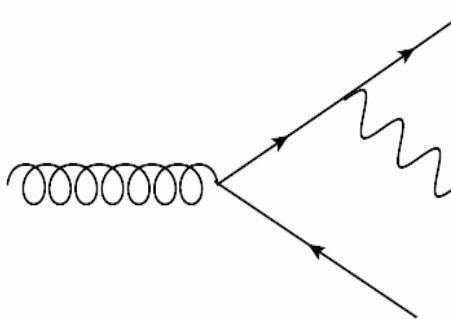
# Sub-leading diagrams



**Gluon Compton Scattering**

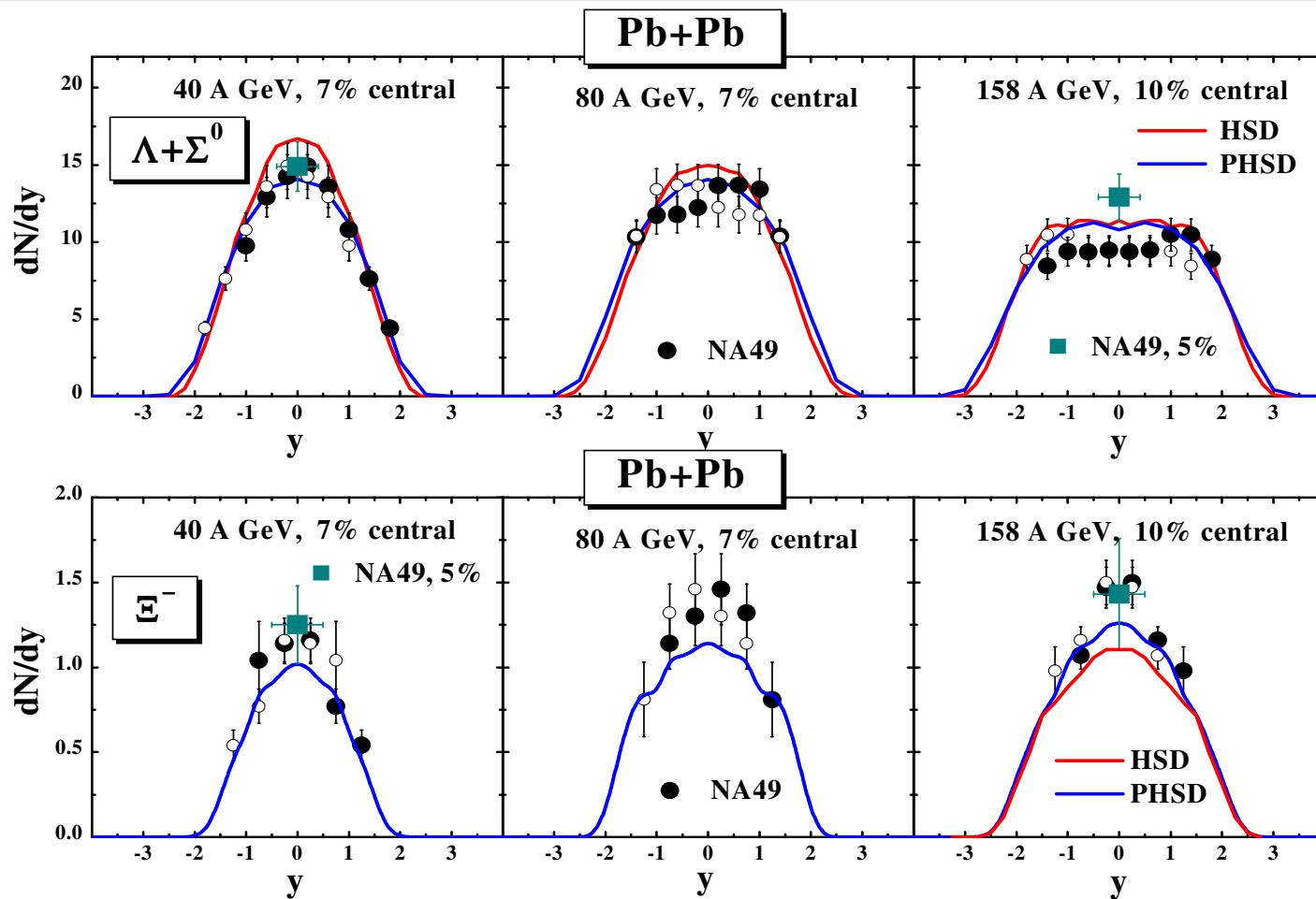


**Virtual quark decay**



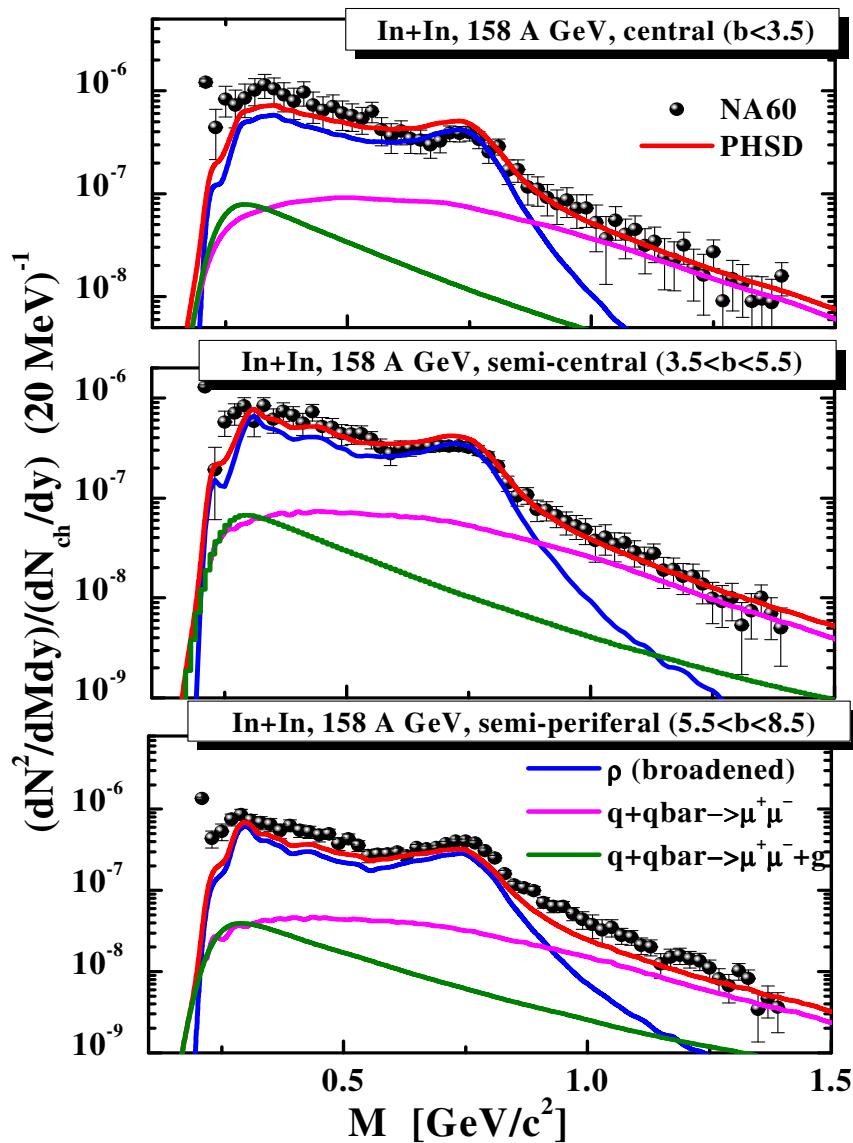
**Virtual gluon decay**

# Rapidity distributions of strange baryons



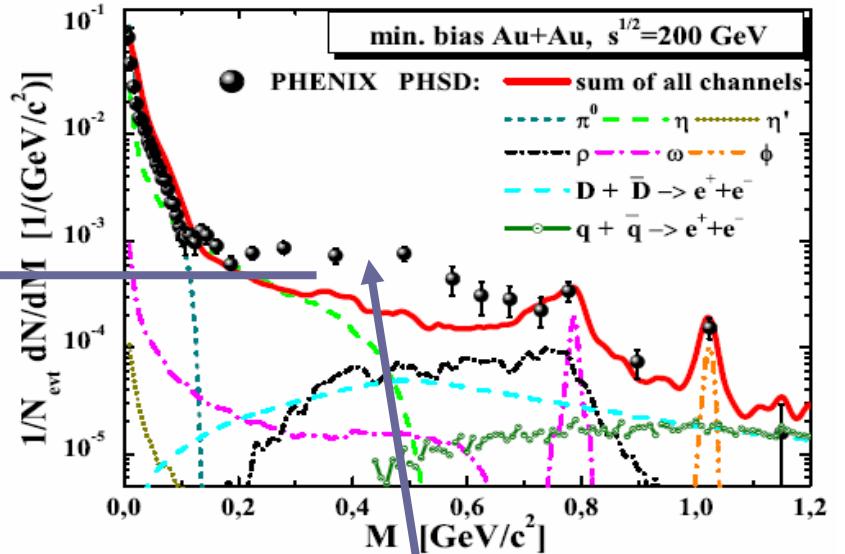
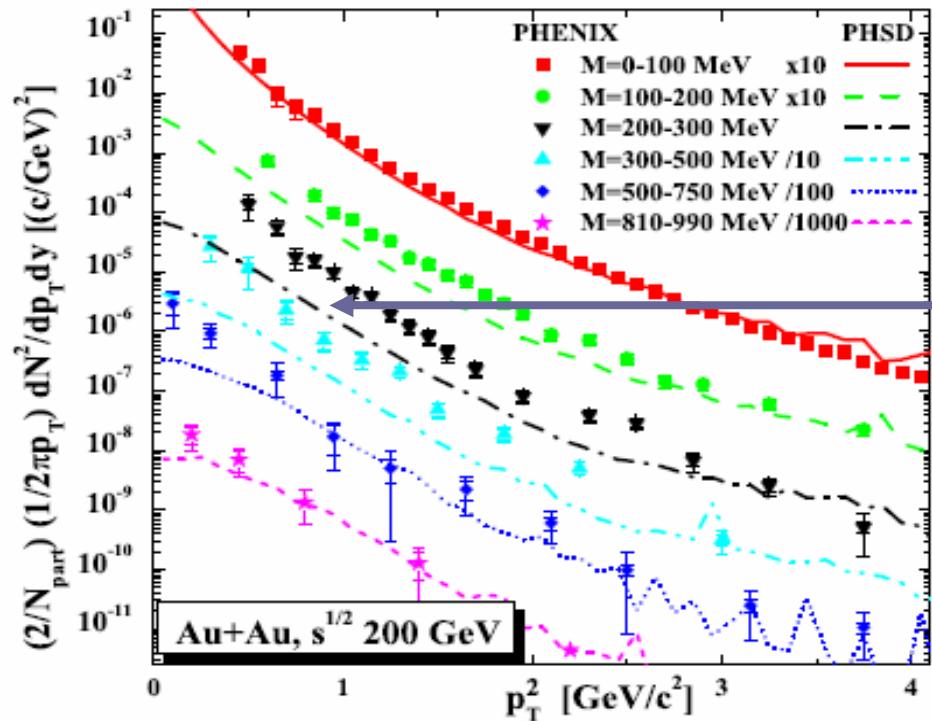
→ PHSD similar to HSD, reasonable agreement with data

# Centrality dependent NA60 data



Dominant rho-channel at  
low and quark  
annihilation at  
intermediate masses !

# PHENIX: $p_T$ spectra



- The lowest and highest mass bins are described very well
- Underestimation of  $p_T$  data for  $100 < M < 750 \text{ MeV}$  bins consistent with  $dN/dM$
- The ‘missing source’(?) is located at low  $p_T$  !

O. Linnyk, W. Cassing, J. Manninen, E.B. and C.-M. Ko, PRC  
85 (2012) 024910

# Dileptons from (in-medium) hadrons

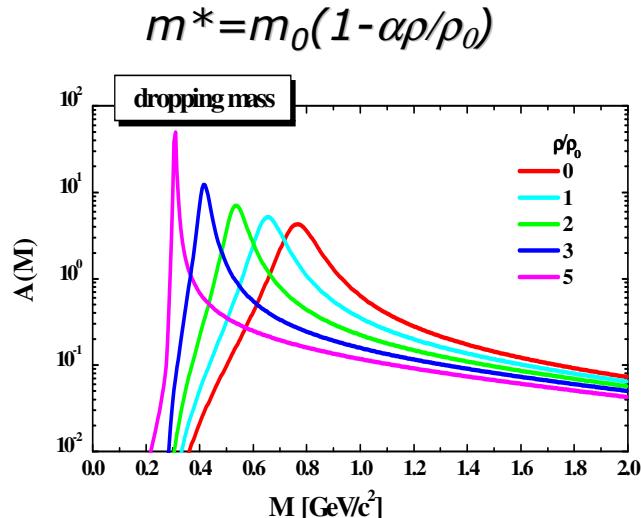
Included channels:

- direct meson (Dalitz) decays of  $\pi_0, \eta, \eta', \rho, \omega, \phi, J/\Psi, \Psi'$
- correlated D+Dbar pairs
- radiation from secondary mesons ( $\pi+\pi, \pi+\rho, \pi+\omega, \rho + \rho, \pi+a_1$ )

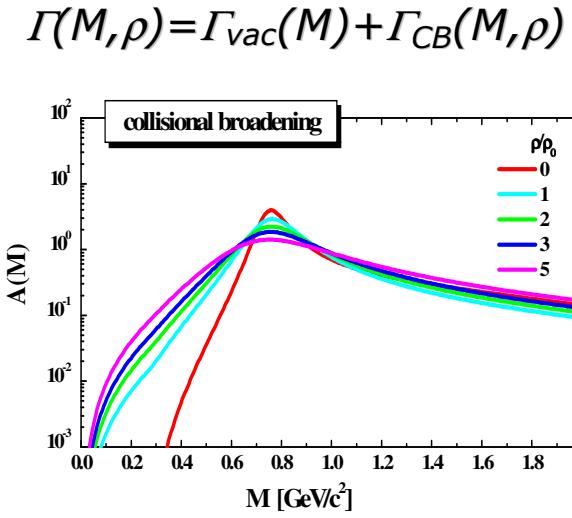
Full off-shell propagation of **in-medium spectral functions** through the hadronic medium

In-medium scenarios for  $\rho, \omega, a_1$ :

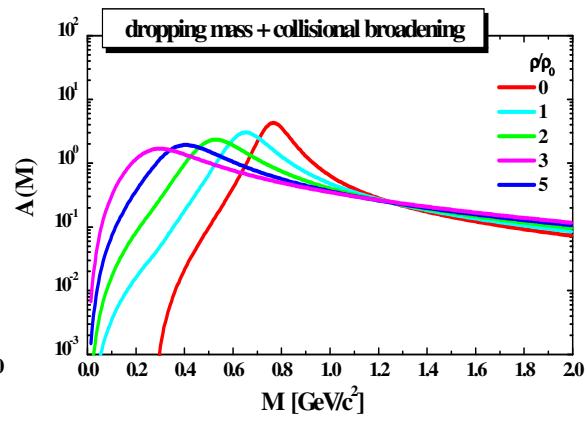
**dropping mass**



**collisional broadening**



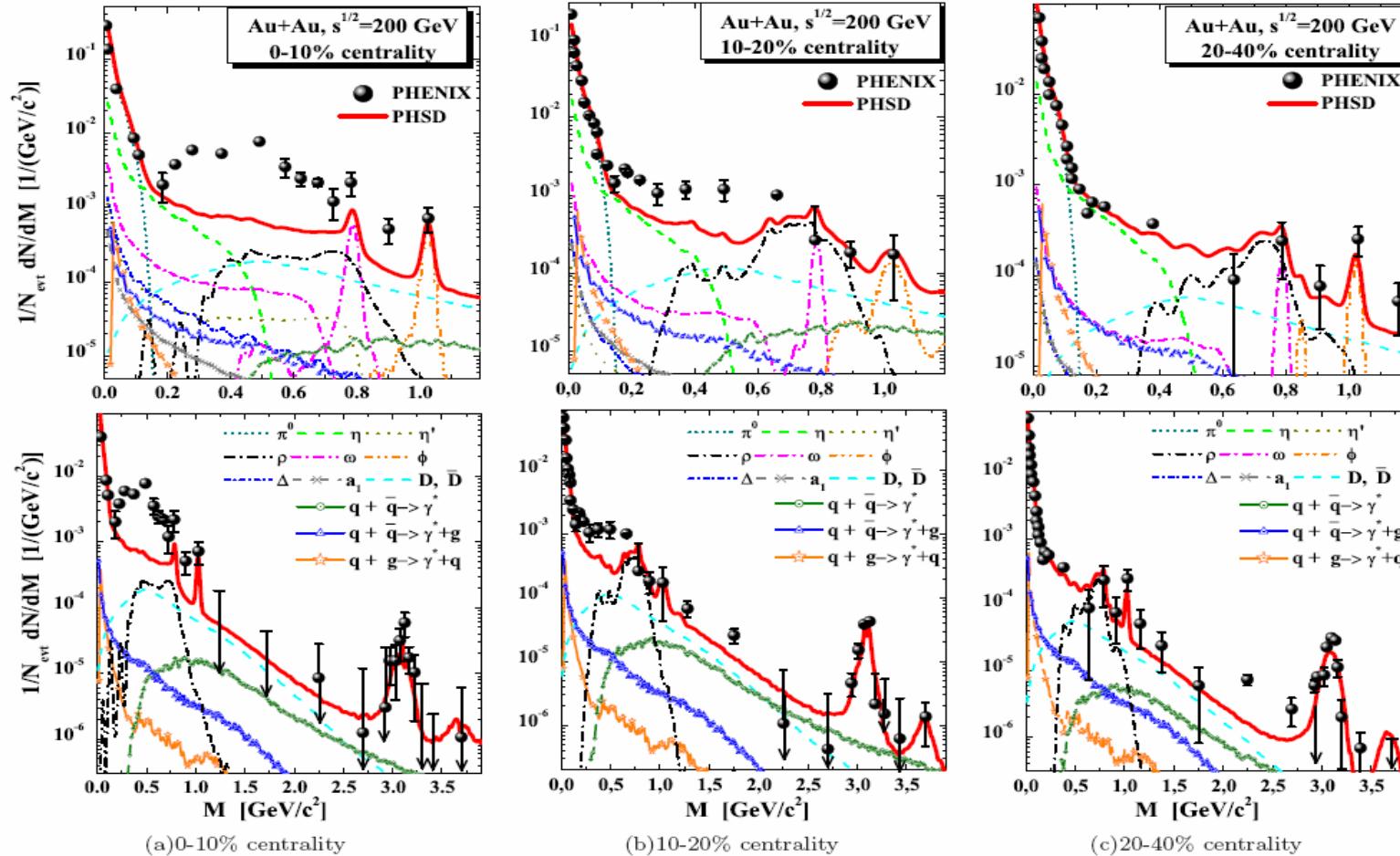
**dropping mass + coll. broad.**



(Examples for  $\rho$  spectral functions.)

E. Bratkovskaya, W. Cassing, O. L., PLB 670 (2009) 428

# PHENIX: mass spectra



- Peripheral collisions (and pp) are well described, however, central fail!

O. Linnyk, W. Cassing, J. Manninen, E.B. and C.-M. Ko, PRC  
85 (2012) 024910