Why Do Particles and Antiparticles Flow differently?

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- Beam energy scan at RHIC
- Particle and antiparticle elliptic flows
- Hadronic potentials in nuclear medium
- Effects of hadronic potentials on elliptic flow
- Partonic potentials in QGP

Based on work with Jun Xu [PRC 85, 041901(R) (2012)]

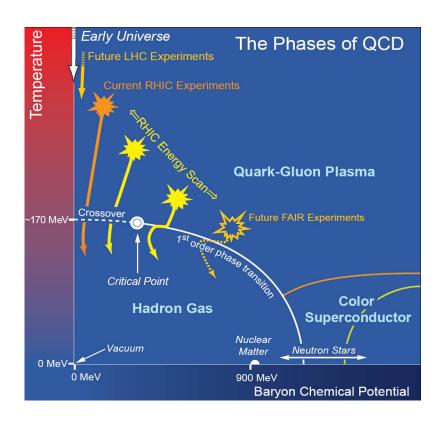
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Beam energy scan at RHIC

STAR Collaboration, arXiv: 1007.2613; 1106.5902 [nucl-ex]

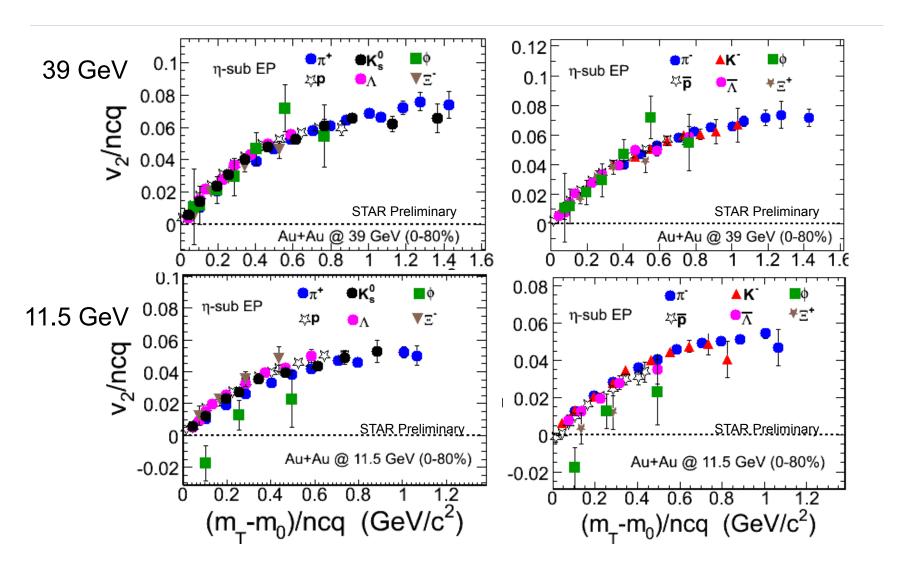
Motivations:

Study QCD phase diagram at finite baryon chemical potential: critical poin (CP), onset of de-confinement



- Experimental observations:
 - **Particle ratios**: increasing baryon chemical potential with decreasing beam energy (DBE), reaching ~ 400 MeV at $s^{1/2}_{NN} = 7.7$ GeV
 - **Dynamic charge correlations:** decreasing difference in same and opposite charges correlations with DBE (hadronic dominance?)
 - Freeze-out eccentricity: increasing with DBE (softening of EOS?)
 - Directed flow: dv₁/dy changes sign (softening of EOS?) and increasing difference in proton and antiproton dv₁/dy with DBE (hadronic dominance?)
 - Moments of net-proton distributions: both skewness and kurtosis deviate from HRG for $\rm s^{1/2}_{NN}$ < 39 GeV (presence of CP?)
 - Particle ratio fluctuations: nonzero $v_{dyn}(K/\pi)$ (correlated emission or presence of CP?)
 - Elliptic flow: breakdown of NCQ scaling and increasing difference between particles and anti-particles with DBE (hadronic dominance? chiral magnetic effect?)

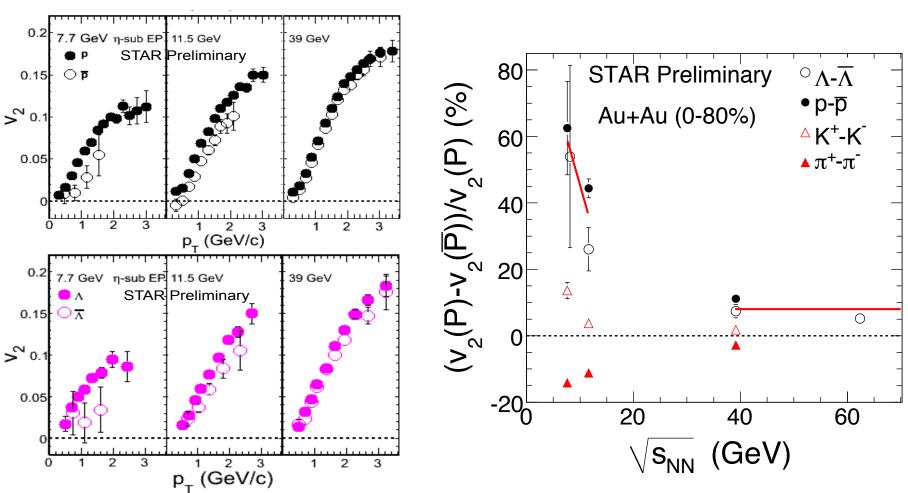
Beam energy dependence of CQN scaled elliptic flow



■ Phi meson falls off trend at $s^{1/2}_{NN}$ = 11.5 GeV (hadronic dominance?)

p (GeV/c)

Particle and antiparticle elliptic flows

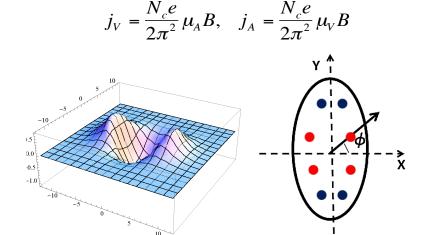


- Particle and antiparticle elliptic flows become significantly different below $s^{1/2}_{NN} < 11.5$ GeV: $v_2(baryon) > v_2(anti-baryon)$, $v_2(K^+) > v_2(K^-)$, and $v_2(\pi^+) < v_2(\pi^-)$
- P_T -integrated relative v_2 difference between particles and antiparticles: 63%, 44%, and 12% for (p, pbar), 53%, 25%, and 7% for (Λ , Λ bar), 13%, 3%, and 1% for (K^+ , K^-), -15%, -10%, and -3% for (π^+ , π^-) at 7.7, 11.5, and 39 GeV

Possible explanations for different particle and antiparticle elliptic flows

- Chiral magnetic wave [Bumier, Kharzeev, Liao & Yee, PRL 107, 052303 (2011)]
 - Stemming from the coupling of the density waves of electric and chiral charge induced by the axial anomaly in the presence of an external magnetic field
 - → Electric quadrupole momentum in QGP
 - → decreasing positive hadron and increasing negative hadron elliptic flows

$$\rightarrow V_2(\pi^+) < V_2(\pi^-)$$



- Effects on p and \overline{p} as well as K⁺ and K⁻ are masked by different absorption cross sections
- Transport versus produced particles [Dunlop, Lisa & Sorensen, PRC 84, 044914 (2011)]: Elliptic flow is larger for transport than for produced (anti) particles
- **Different particle and antiparticle transport coefficients** [Greco, Mitrovski, & Torrieri, arXiv:1201.4800v2 [nucl-th]] : antiparticles have larger absorption cross sections
- **Different particle and antiparticle potentials** [Xu & Ko, PRC 85, 041901(R) (2012)]: Potentials are repulsive for particles and attractive for antiparticles

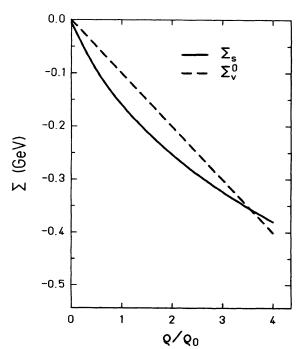
Hadron potentials in nuclear medium (I)

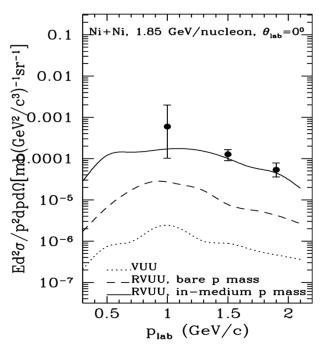
Ko & Li, JPG 22, 1673 (1996); Ko, Koch & Li, ARNPS 47, 505 (1997)

■ Nucleons and antinucleons: Relativistic mean-field model \rightarrow attractive scalar potential Σ_s and repulsive vector potential Σ_v ("+" for nucleons and "-" for antinucleons due to G-parity)

$$U_{N,\overline{N}}(\rho_{s},\rho_{b}) = \sum_{s}(\rho_{s},\rho_{b}) \pm \sum_{v}^{0}(\rho_{s},\rho_{b}) = \frac{g_{\sigma}^{2}}{m_{\sigma}^{2}}\rho_{s} \pm \frac{g_{\omega}^{2}}{m_{\omega}^{2}}\rho_{b}$$







 Deep antiproton attractive potential reduces its production threshold and thus enhances its yield in subthreshold heavy ion collisions

Hadron potentials in nuclear medium (II)

Ko & Li, JPG 22, 1673 (1996); Ko, Koch & Li, ARNPS 47, 505 (1997)

■ Kaons and antikaons: Chiral effective Lagrangian → repulsive potential for kaons and attractive potential for antikaons

$$U_{K,\bar{K}} = \omega_{K,\bar{K}} - \omega_{0}, \quad \omega_{0} = \sqrt{m_{K}^{2} + p^{2}}$$

$$\omega_{K,\bar{K}} = \sqrt{m_{K}^{2} + p^{2} - a_{K,\bar{K}} \rho_{s} + (b_{K} \rho_{B})^{2}} \pm b_{K} \rho_{B}$$

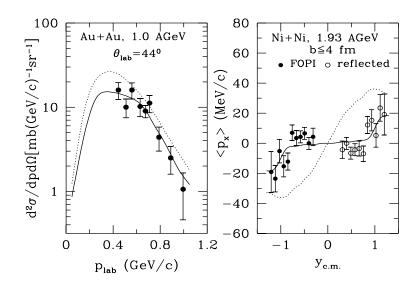
$$a_{K} = 0.22 \text{ GeV}^{2} \text{fm}^{3}$$

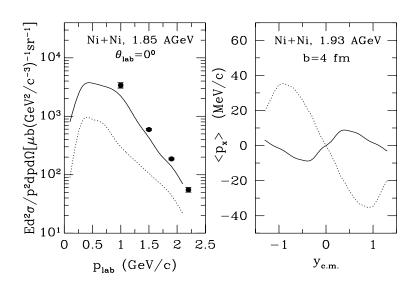
$$b_{K} = 0.33 \text{ GeV}^{2} \text{fm}^{3}$$

$$U_{\kappa,\bar{\kappa}} = \omega_{\kappa,\bar{\kappa}} - \omega_0, \quad \omega_0 = \sqrt{m_{\kappa}^2 + p^2}$$
 $a_{\kappa} = 0.22 \text{ GeV}^2 \text{fm}^3, \quad a_{\bar{\kappa}} = 0.45 \text{ GeV}^2 \text{fm}^3$

$$b_{\kappa} = 0.33 \,\mathrm{GeV^2fm^3}$$

$$\Rightarrow$$
 $U_{\kappa} = 20 \text{ MeV}, U_{\bar{\kappa}} = -120 \text{ MeV at } \rho_{0} = 0.16 \text{ fm}^{-3}$



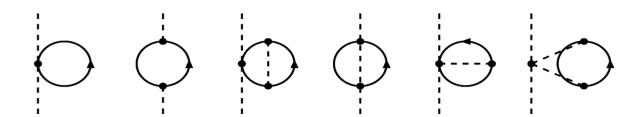


• Experimental data on spectrum and directed flow are consistent with repulsive kaon and attractive antikaon potentials

Hadron potentials in nuclear medium (III)

Kaiser & Weise, PLB 512, 283 (2001)

■ Pions: $U_{\pi} = \Pi/(2m_{\pi})$ in terms of pion selfenergies



$$\Pi^{-}(\rho_{n}, \rho_{p}) = \rho_{n} [T_{\pi N}^{-} - T_{\pi N}^{+}] - \rho_{p} [T_{\pi N}^{-} + T_{\pi N}^{+}] + \Pi_{\text{rel}}^{-}(\rho_{n}, \rho_{p}) + \Pi_{\text{cor}}^{-}(\rho_{n}, \rho_{p})$$

$$\Pi^{+}(\rho_{p}, \rho_{n}) = \Pi^{-}(\rho_{n}, \rho_{p})$$

$$\Pi^{0}(\rho_{n}, \rho_{p}) = -(\rho_{p} + \rho_{n})T_{\pi N}^{+} + \Pi_{\text{cor}}^{0}(\rho_{n}, \rho_{p})$$

Isospin even and odd πN -scattering matrices extracted from energy shift and width of 1s level in pionic hydrogen atom

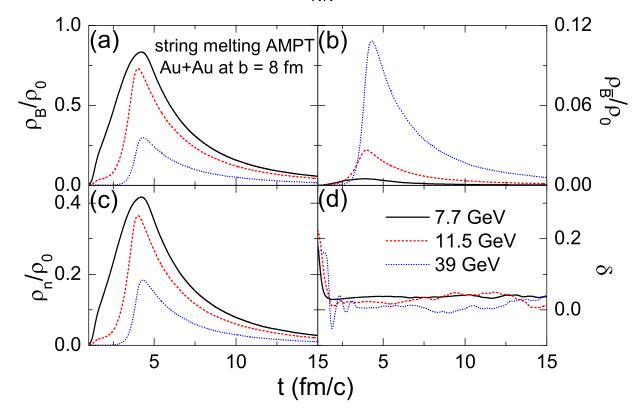
$$T_{\pi N}^{+} \approx 1.847 \,\text{fm}$$
 and $T_{\pi N}^{-} \approx -0.045 \,\text{fm}$

At normal nuclear density ρ =0.165 fm⁻³ and isospin asymmetry δ =0.2 such as in Pb,

$$U_{\pi^{-}} = 14 \text{ MeV}, \ U_{\pi^{+}} = -1 \text{ MeV}, \ U_{\pi^{0}} = 6 \text{ MeV}$$

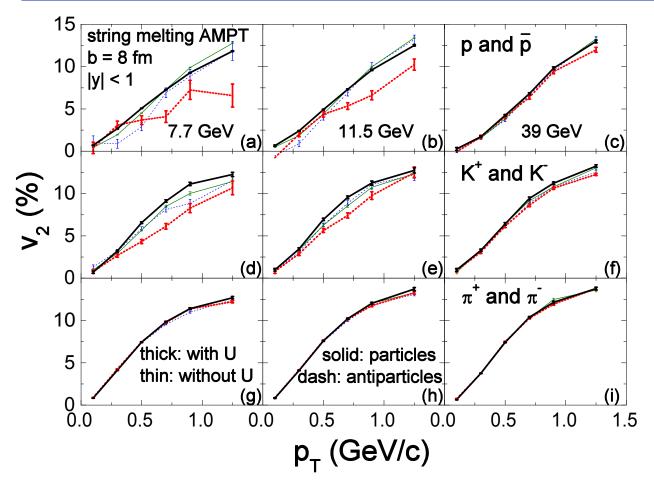
Hadron density evolutions in AMPT

Adjust parton scattering cross section and ending time of partonic stage to approximately reproduce measured elliptic flows and extracted hadronic energy density ($^{\sim}$ 0.35 GeV/fm³): isotropic cross sections of 3, 6 and 10 mb, and parton ending time of 3.5, 2.6, 2.9 fm/c for s^{1/2}_{NN}= 7.7, 11.5, and 39 GeV, respectively



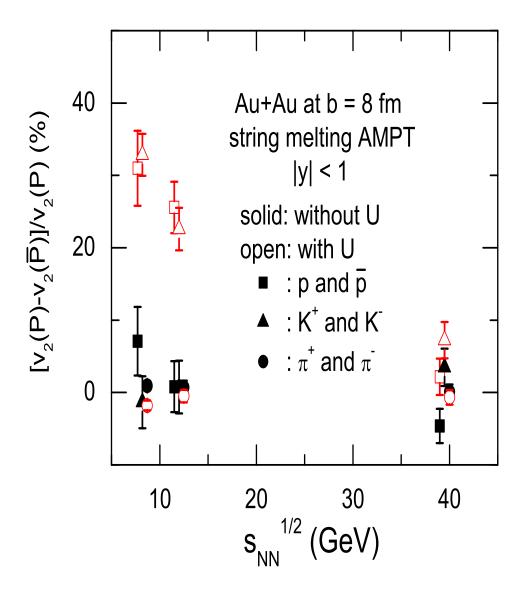
- Increasing baryon and decreasing antibaryon densities with decreasing energy
- Increasing neutron density with decreasing energy, but isospin asymmetry δ =0.02 is small due to production of Λ hyperon and pions

Particle and antiparticle differential elliptic flows



- Similar particle and antiparticle elliptic flows without hadronic potentials
- Hadronic potentials increase slightly p and pbar v_2 at p_T <0.5 GeV but reduce slightly (strongly) p (pbar) v_2 at high p_T
- Hadronic potentials increase slightly v₂ of K⁺ and reduce v₂ of K⁻
- Effects of hadronic potentials on π^+ and $\pi^ v_2$ are small

P_T-integrated particle and antiparticle elliptic flow difference



- Difference very small without hadronic potentials → different particle and antiparticle scattering and absorption cross sections have small effects
- Hadronic potentials lead to relative v₂ difference between p and pbar and between K⁺ and K⁻ of 30% at 7.7 GeV, 20% at 11.5 GeV, and negligibly small value at 39 GeV, only very small negative value between π⁺ and π⁻
- Compared to experimental values of 63%, 44%, and 12% for (p,pbar), 13%, 3%, and 1% for (K⁺,K⁻), -5%, -10%, and -13% for (π⁺,π⁻) at 7.7, 11.5, and 39 GeV, ours are smaller for (p,pbar) and (π⁺,π⁻) and larger for (K⁺,K⁻)

Quark and antiquark potentials in QGP

NJL model [Asakawa & Yazaki, NPA 504, 668 (1989)]

$$H = -i\overline{q}\gamma \cdot \nabla q + m\overline{q}q - g\left[\left(\overline{q}q\right)^{2} + \left(\overline{q}i\gamma_{5}\tau q\right)^{2}\right]$$

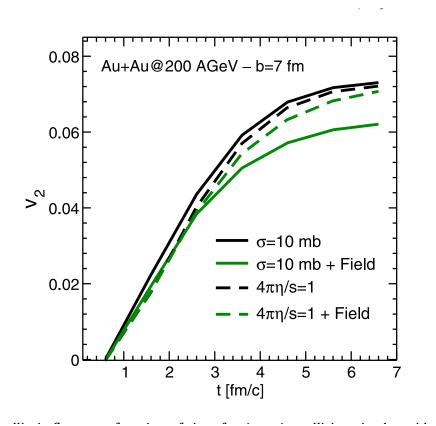
■ Fierz transformation of last term and mean-field approximation $G = \frac{4N_c + 1}{4N_c}g$

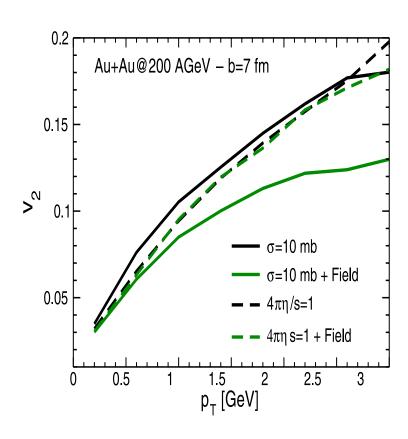
$$H_{_{MF}} = -i\overline{q}\,\gamma\cdot\nabla q + \left(m - 2G\langle\overline{q}\,q\rangle\right)\overline{q}\,q + \frac{g}{N_{_{C}}}\langle\overline{q}\,\gamma_{_{0}}q\rangle\overline{q}\,\gamma_{_{0}}q + G\langle\overline{q}\,q\rangle^{^{2}} - \frac{g}{2N_{_{C}}}\langle\overline{q}\,\gamma_{_{0}}q\rangle^{^{2}}$$

- Quark mass is modified by the quark condensate
 - Attractive scalar potential on both quark and antiquark
- Vector potential is repulsive for quark and attractive for antiquark: enhances relative v_2 difference between quarks and antiquarsk
 - Enhances relative v₂ difference between p and pbar
 - Reduces relative v₂ difference between K⁺ and K⁻
- → Would bring results with only hadronic potentials closer to experimental data

Effects of attractive scalar potential in quark matter

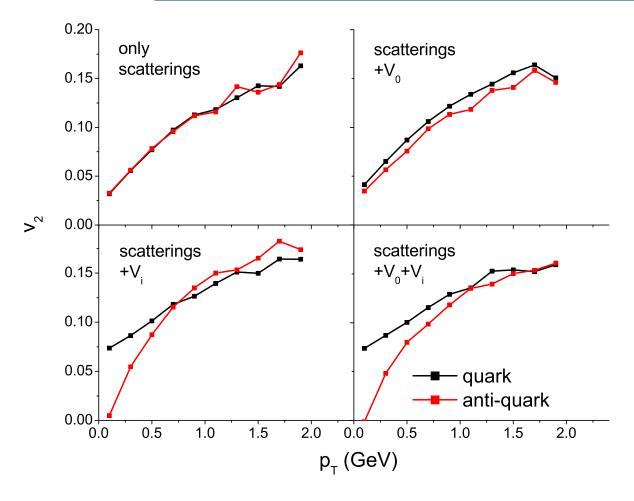
Plumari, Baran, Di Tori, Ferini, and Greco, PLB 689, 18 (2010)





- Attractive scalar potential reduces v₂ of both quark and antiquark
- Effects are reduced when parton scattering cross section is large

Effects of Vector potential in quark matter



Preliminary results from Taesoo Song

- Time (electric) component of vector potential increases quark but decreases antiquark elliptic flows
- Space (magnetic) component of vector potential has a similar effect at low p_T but an opposite effect at high p_T
- Net effect of vector potential: larger quark than antiquark elliptic flows

Summary

- Different particle and antiparticle v₂ is observed in BES at RHIC where produced matter has a large finite baryon chemical potential
- Taking into account different potentials for hadrons and antihadrons can partially account for the experimental observation
- Quarks and antiquarks are expected to be affected by scalar and vector potentials in QGP
 - reduced v₂ due to attractive scalar potential
 - vector potential becomes nonzero at finite baryon chemical potential; repulsive for quarks and attractive for anitquarks
- Information on quark and antiquark potentials at finite baryon chemical potential is useful for understanding the EOS of QGP