

Particle production at 1-2A GeV in GiBUU transport model

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Outline

Motivation: HADES data and an abundance of pions

Giessen Boltzmann-Uehling-Uhlenbeck model (GiBUU):
Brief Introduction

Proton rapidity distributions: Comparison with FOPI data

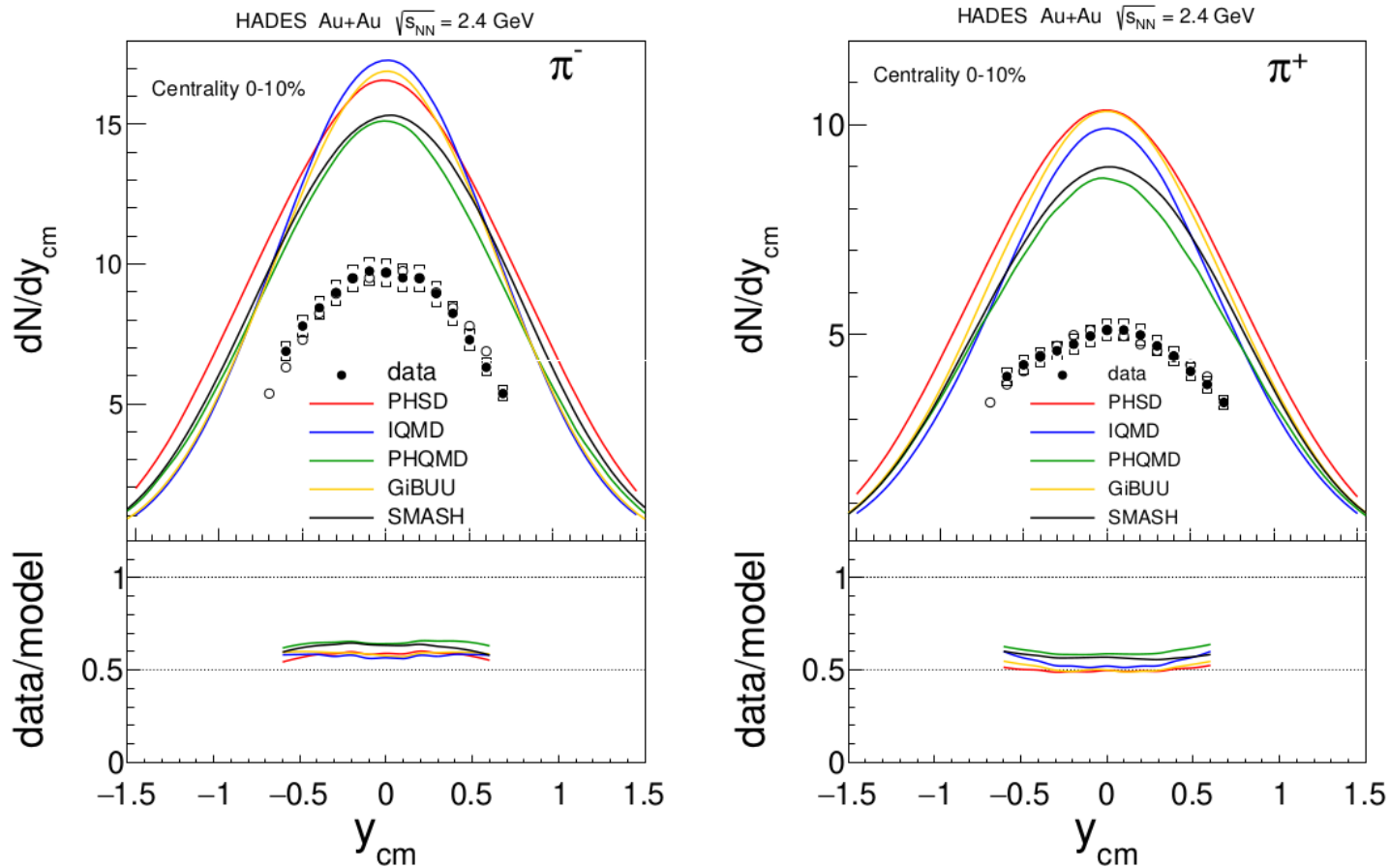
Pion p_t spectra: Comparison with FOPI and HADES data

Hadron yields and dilepton invariant mass spectra:
Comparison with HADES data

Conclusions

Motivation

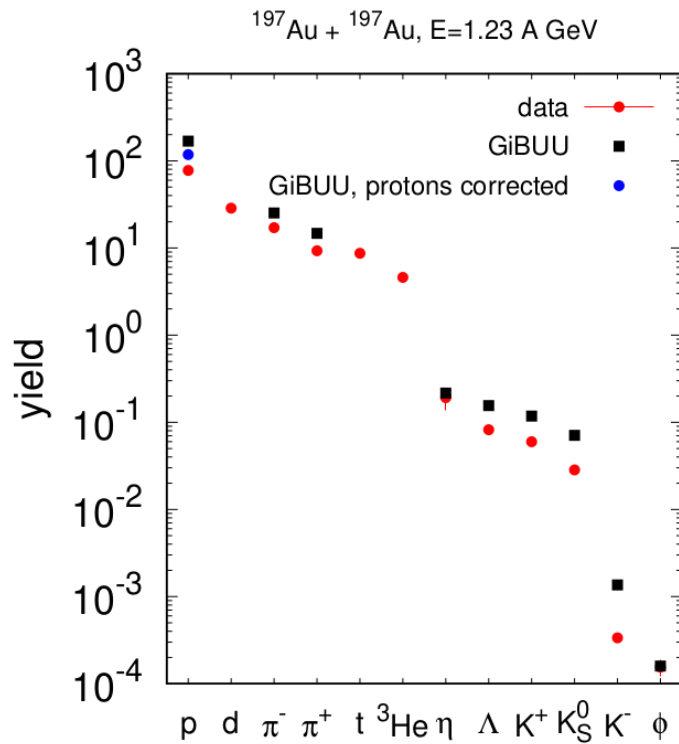
New experimental data from HADES shows that transport theories produce an excess of pions [J. Adamczewski-Musch et al., EPJA 56, 259 \(2020\)](#)



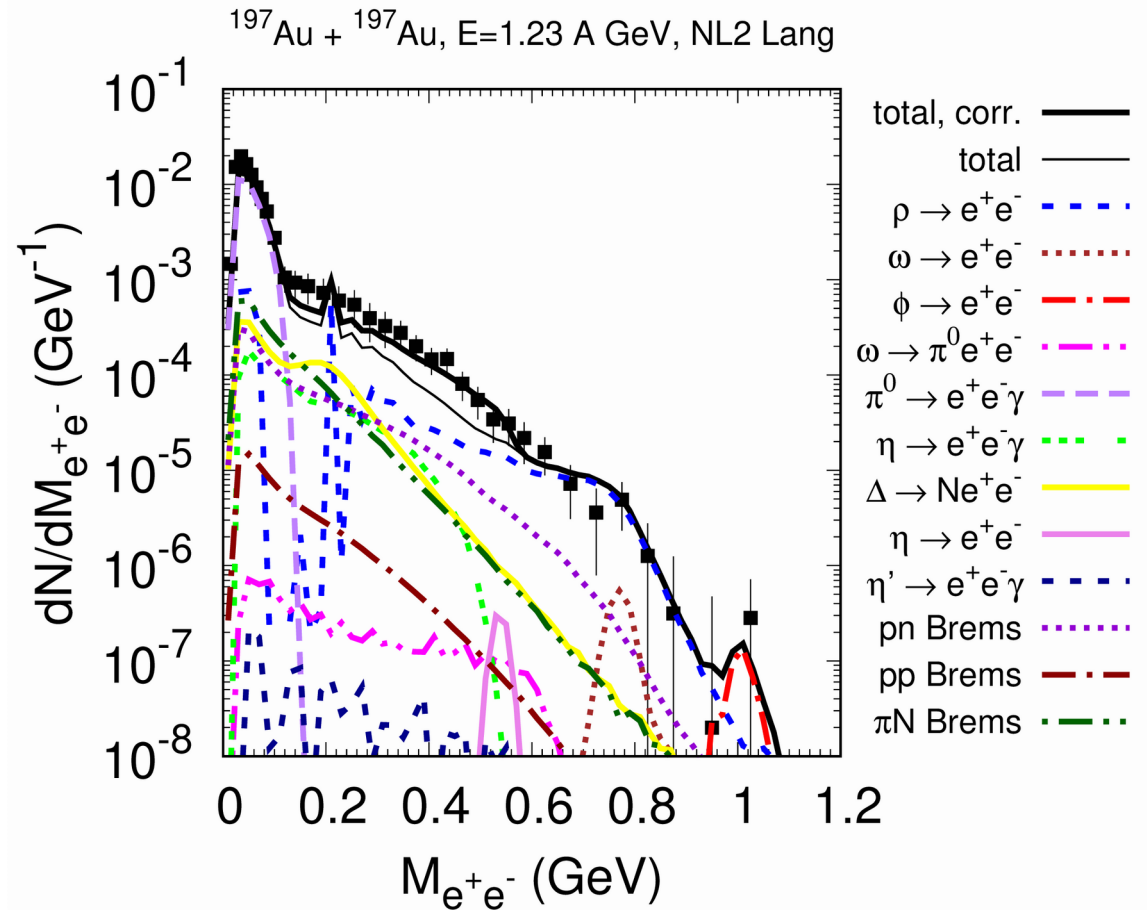
Rapidity spectra for 10% most central events

Other hadrons are overpredicted as well

However, the π^0 Dalitz decay agrees quite well with experiments
[Larionov et al., PRC 102, 064913 \(2020\)](#)



Hadron yields for the 10% or 20% most central events



Invariant mass distribution of dileptons ($e^- e^+$) for 40 % most central events

GiBUU: Brief Introduction

Lagrangian of the system

$$\begin{aligned} \mathcal{L} = & \bar{\psi}[\gamma_{\mu}(i\partial^{\mu} - g_{\omega}\omega^{\mu} - g_{\rho}\vec{\tau}\vec{\rho}^{\mu} - \frac{e}{2}(1 + \tau^3)A^{\mu}) - m_N - g_{\sigma}\sigma]\psi \\ & + \frac{1}{2}\partial_{\mu}\sigma\partial^{\mu}\sigma - U(\sigma) + \frac{1}{2}m_{\omega}^2\omega^2 + \frac{1}{2}m_{\rho}^2\rho^2 - \frac{1}{16\pi}F_{\mu\nu}F^{\mu\nu} \end{aligned}$$

The relativistic mean fields used in the Lagrangian are σ (isoscalar-scalar), ω^{μ} (isoscalar-vector) and $\vec{\rho}^{\mu}$ (isovector-vector)

$F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu}$ electromagnetic field strength tensor

$U(\sigma) = \frac{1}{2}m_{\sigma}^2\sigma^2 + \frac{1}{3}g_2\sigma^3 + \frac{1}{4}g_3\sigma^4$ Self-interaction of the scalar field

The Lagrangian leads to the following Dirac-style equations of motion (eom)

$$[\gamma_\mu (i\partial^\mu - g_\omega \omega^\mu - g_\rho \tau \rho^\mu - \frac{e}{2}(1 + \tau^3)A^\mu) - m_N - g_\sigma \sigma] \psi = 0$$

$$\partial_\mu \partial^\mu \sigma + \frac{\partial U(\sigma)}{\partial \sigma} = -g_\sigma \frac{2}{(2\pi)^3} \sum_{i=p,n,\bar{p},\bar{n}} \int \frac{d^3 p}{p_i^{*0}} m^* f_i(x, p) \quad \text{Scalar density } \rho_S$$

$$m_\omega^2 \omega^\mu = g_\omega \frac{2}{(2\pi)^3} \int d^3 p \left(\sum_{i=p,n} \frac{p_i^{*\mu}}{p_i^{*0}} f_i(x, p) - \sum_{i=\bar{p},\bar{n}} \frac{p_i^{*\mu}}{p_i^{*0}} f_i(x, p) \right) \quad \text{Baryon current } j_b^\mu$$

$$m_\rho^2 \rho^{3\mu} = g_\rho \frac{2}{(2\pi)^3} \sum_{i=p,n,\bar{p},\bar{n}} \int \frac{d^3 p}{p_i^{*0}} p_i^{*\mu} \tau_i^3 f_i(x, p) \quad \text{Isospin current } \vec{j}_I^\mu$$

$$\partial_\mu \partial^\mu A^\nu = 4\pi e \frac{1}{2} (j_b^\nu + j_I^{3\nu}) \quad \text{Electromagnetic current } j_c^\nu$$

Kinematics

$$m^* = m_N + S$$

$$S = g_\sigma \sigma$$

$$p^* = p - V$$

$$V = g_\omega \omega + g_\rho \tau^3 \rho^3 + \frac{e}{2}(1 + \tau^3)A$$

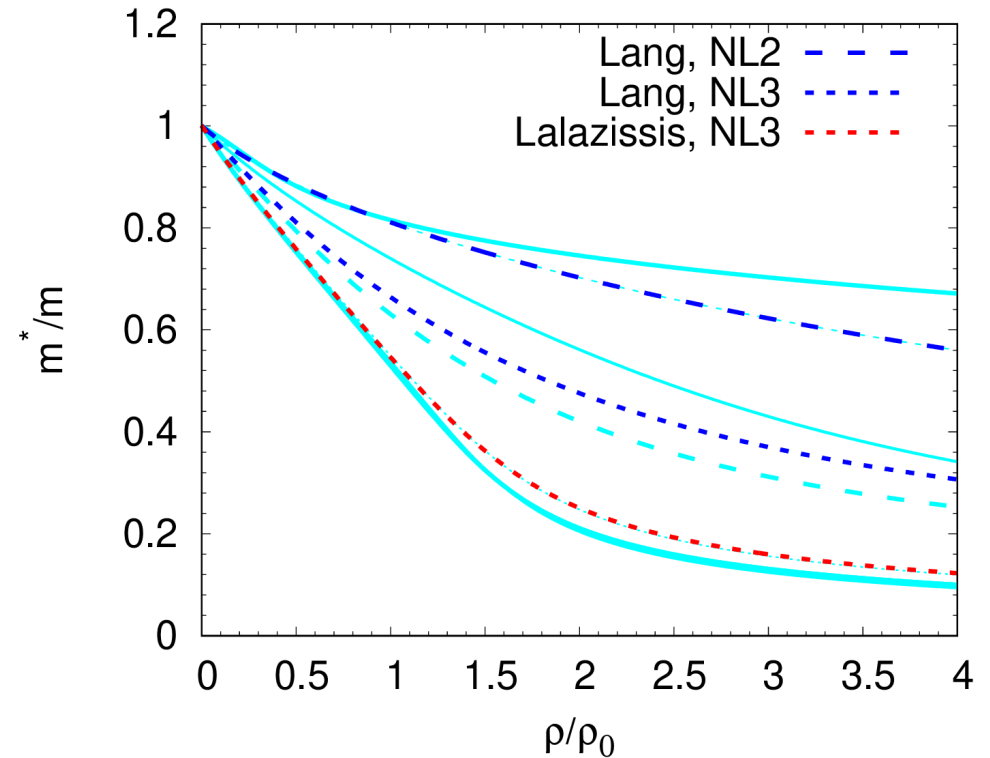
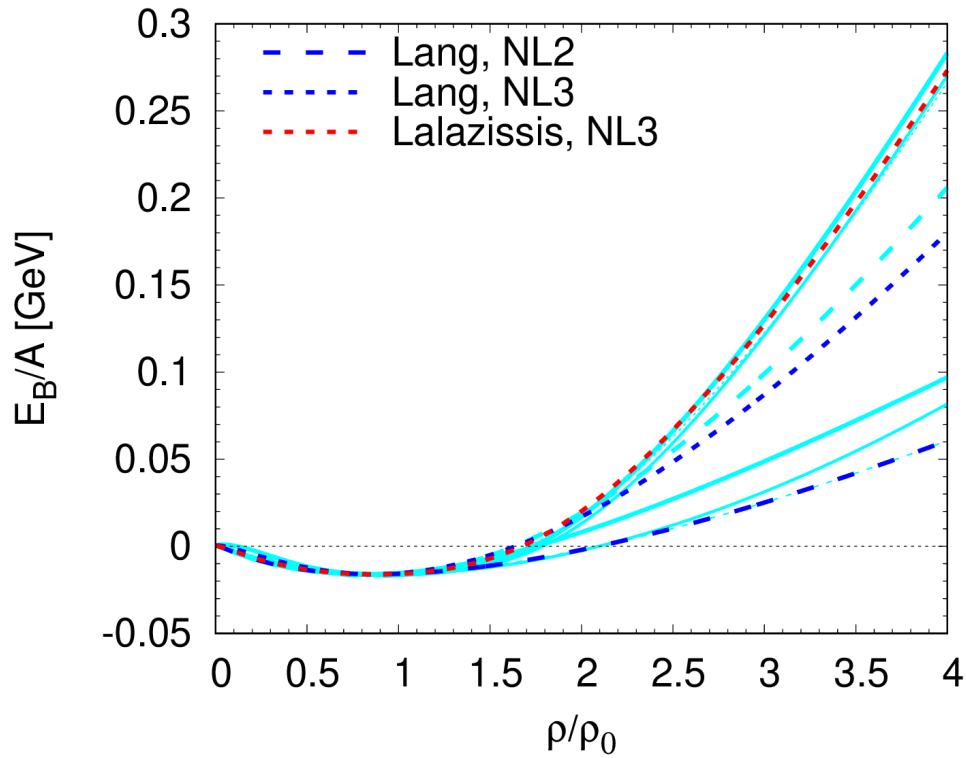
Dispersionrelation

$$(p^*)^2 - (m^*)^2 = 0$$

Nonlinear (NL) Walecka models are considered: NL3 by Lalazissis and NL2 and NL3 by Lang represent the various eos.

Background: Lang considered HIC's (A. Lang et al., NPA 541, 507 (1992)),
Lalazissis nuclear structure (G.A. Lalazissis et al., PRC 55, 540 (1997))

Smaller $\frac{m^*}{m}$ leads to repulsive optical potential: in-medium effects are enhanced



	NL2 Lang	NL3 Lang	NL3 Lalazissis
K [MeV]	210	380	272
m^*/m	0.83	0.70	0.60

The rmf's inside the nucleus lead to the modification of the baryon-baryon cross sections.

$$\begin{aligned}
 d\sigma_{12 \rightarrow 1'2' \dots N'}^* &= (2\pi)^4 \delta^{(4)} \left(p_1 + p_2 - \sum_{i=1'}^{N'} p_i \right) \frac{\prod_{i=1'}^{N'} n_i^*}{4I_{12}^*} \overline{|\mathfrak{M}_{12 \rightarrow 1'2' \dots N'}|^2} \\
 &\times \mathcal{S}_{1'2' \dots N'} \prod_{i=1'}^{N'} A_i(p_i) \frac{d^4 p_i}{(2\pi)^3 2p_i^{*0}}
 \end{aligned}$$

$n_i^* \begin{cases} = 2m_i^* \text{ for baryons} \\ = 1 \text{ for mesons} \end{cases}$

Three different cross sections are considered

- Vacuum cross sections
- All inelastic cross sections are modified (noted: σ^*)
- Only cross sections $NN \leftrightarrow NN\pi$ and $NN \leftrightarrow N\Delta$ are modified (noted: σ_{Δ}^*)

Elastic cross sections are never modified

FOPI measured the rapidity of proton-like particles for AuAu HIC's.

W. Reisdorf et al., PRL 92, 232301 (2004)

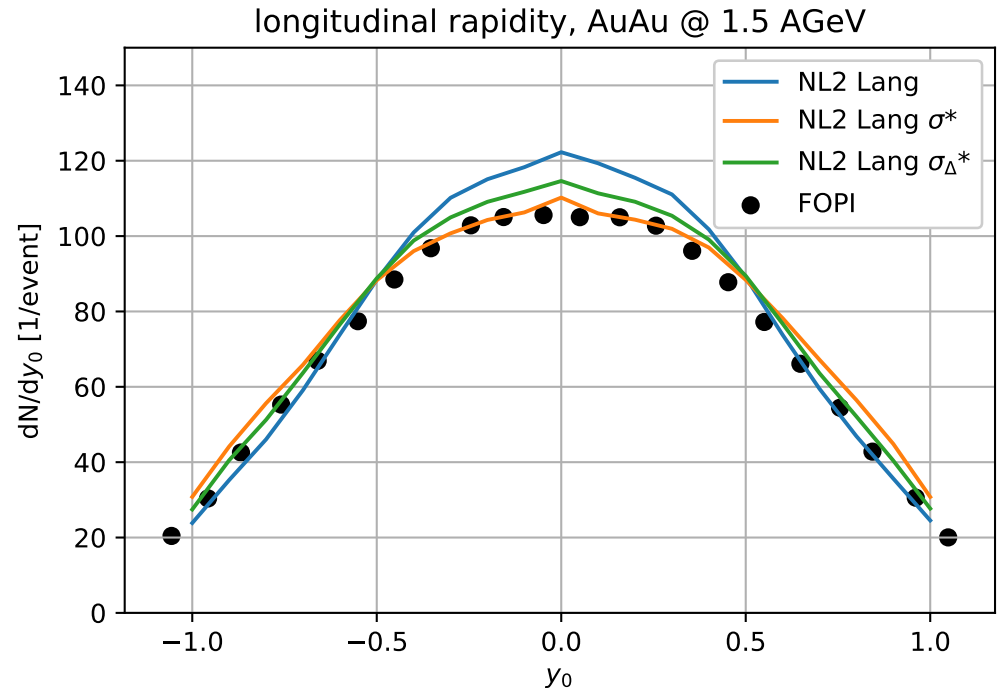
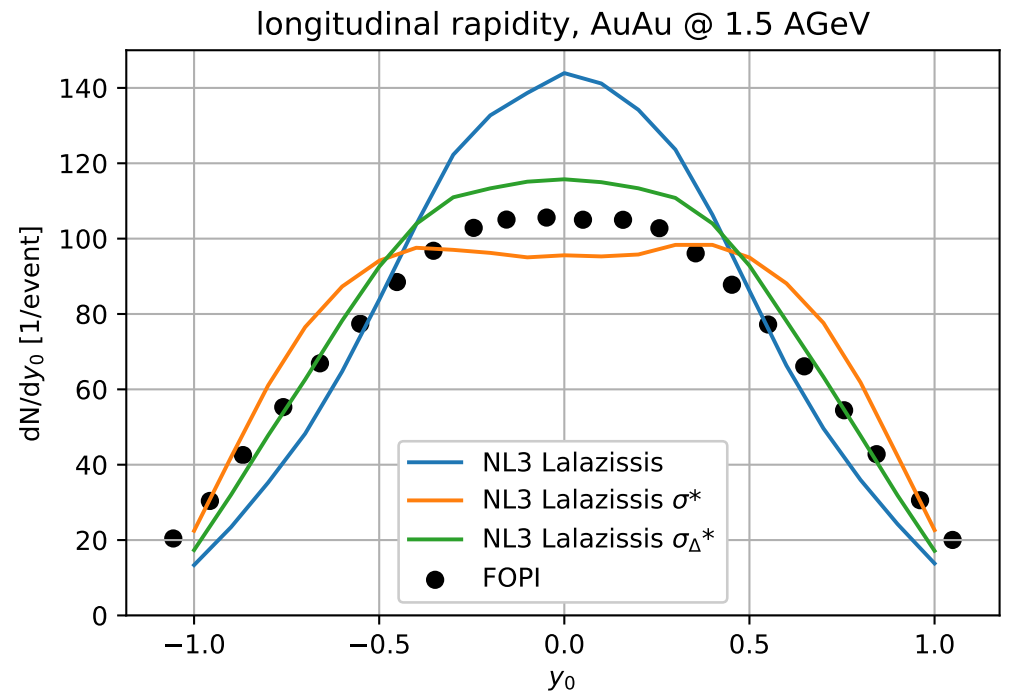
Longitudinal rapidity is given by

$$y = \frac{1}{2} \ln\left(\frac{E + p_z}{E - p_z}\right)$$

$$y_0 = (y/y_p)_{c.m.}$$

NL2 Lang with in-medium modifications describes the System best

$$b_{max} = 1.15(A_p^{1/3} + A_t^{1/3})$$

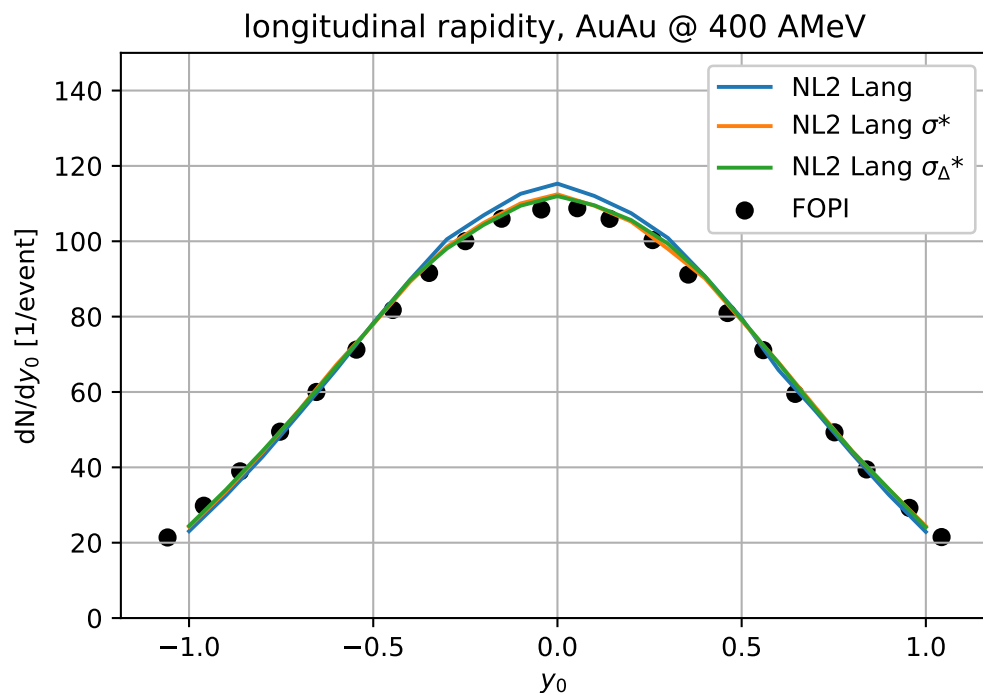
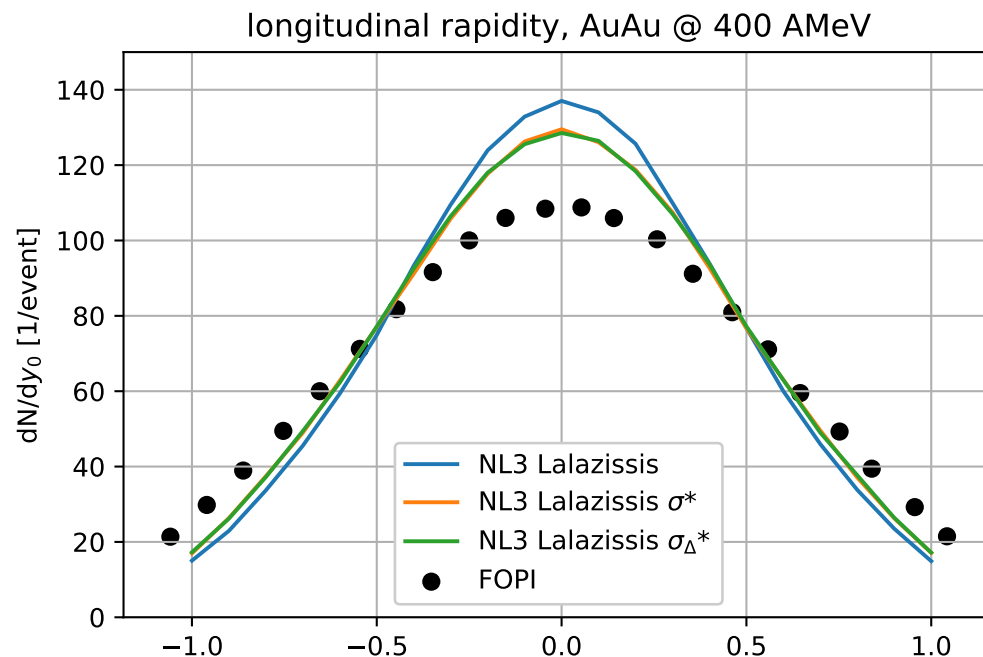


Rapidity of proton-like particles, for $b^0 < 0.15b_{max}$

FOPi measured the rapidity of proton-like particles for AuAu HIC's.

W. Reisdorf et al., NPA 781, 459 (2007)

NL3 by Lalazissis overpredicts protons at midrapidity



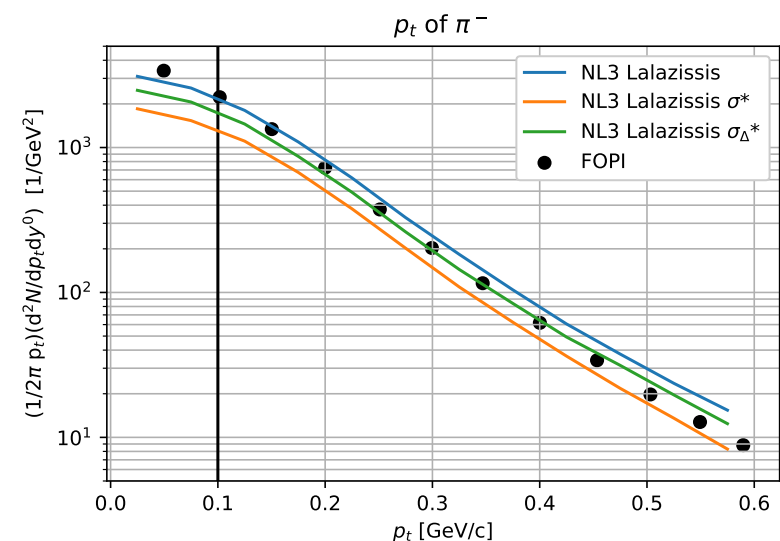
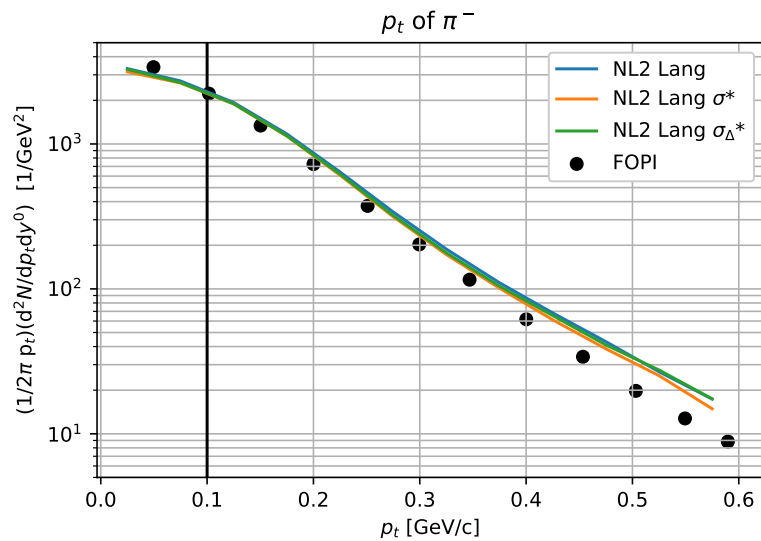
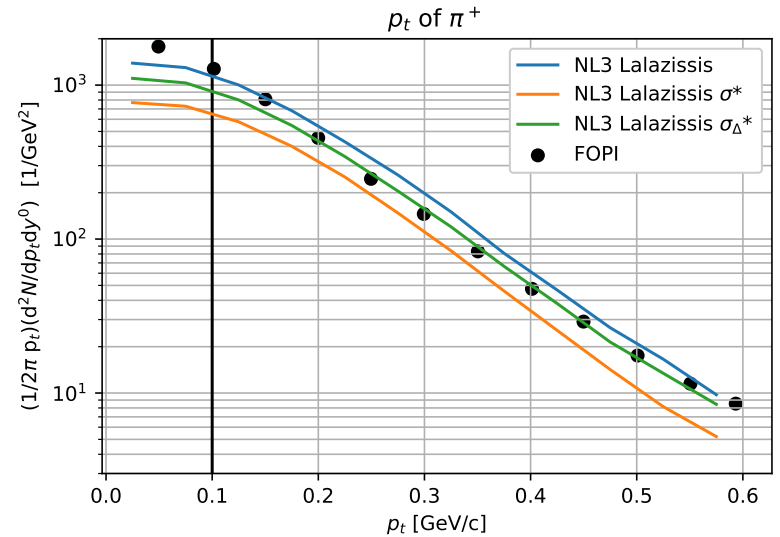
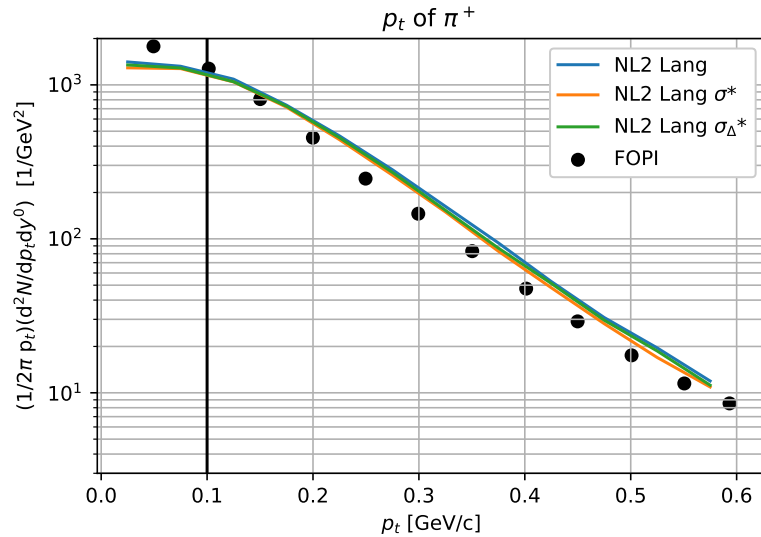
Rapidity of proton-like particles, for $b^U < 0.15b_{max}$

The eos NL2 describes the distribution of proton-like particles well, even at lower energies

FOPI also measured the p_t spectra of charged pions. AuAu @ 1.5 AGeV
 W. Reisdorf et al., NPA 781, 459 (2007)

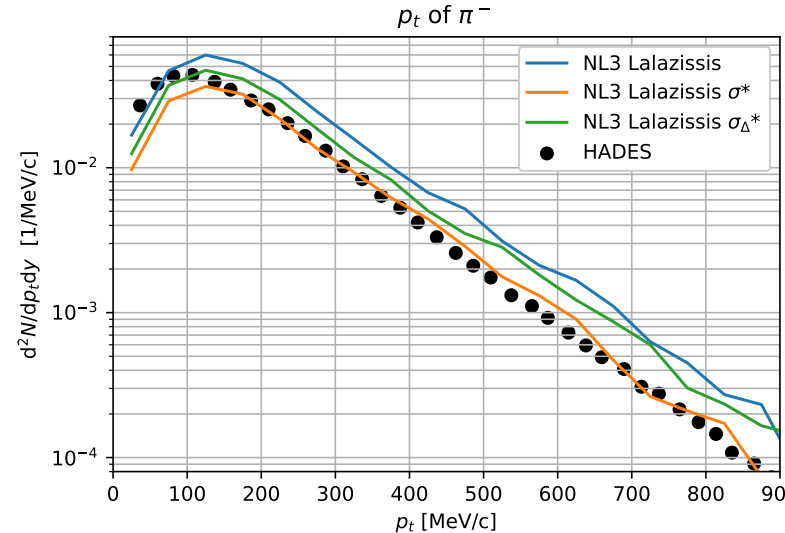
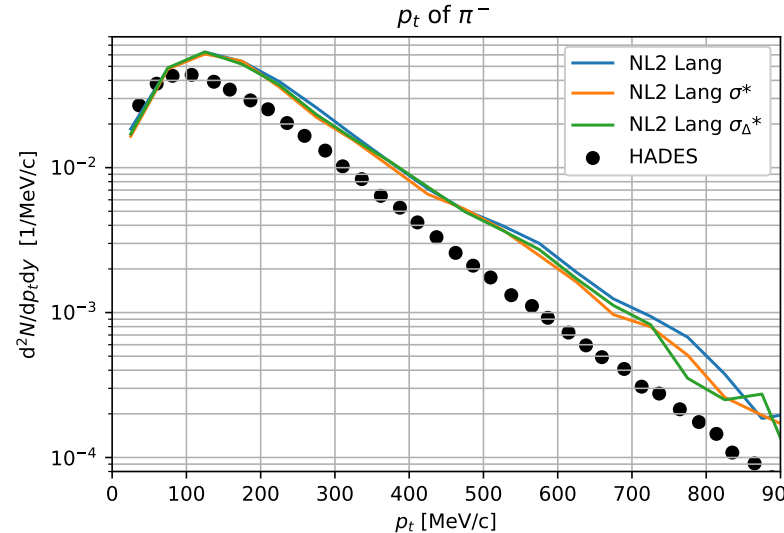
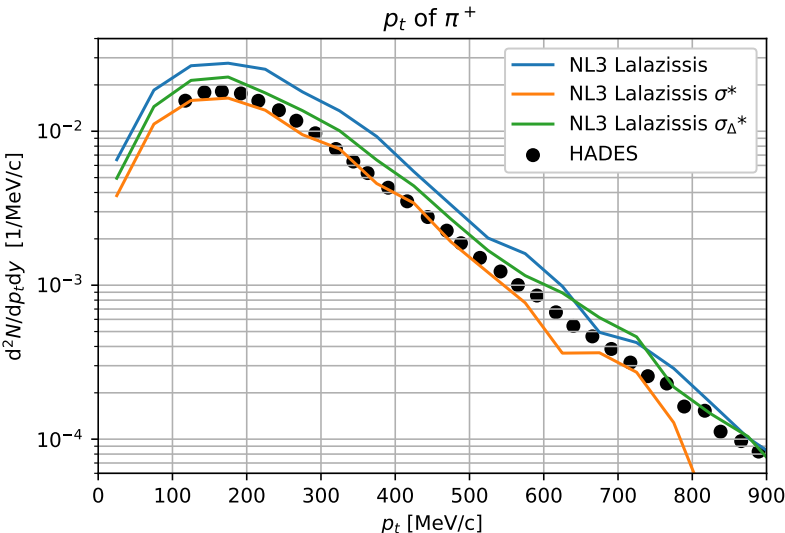
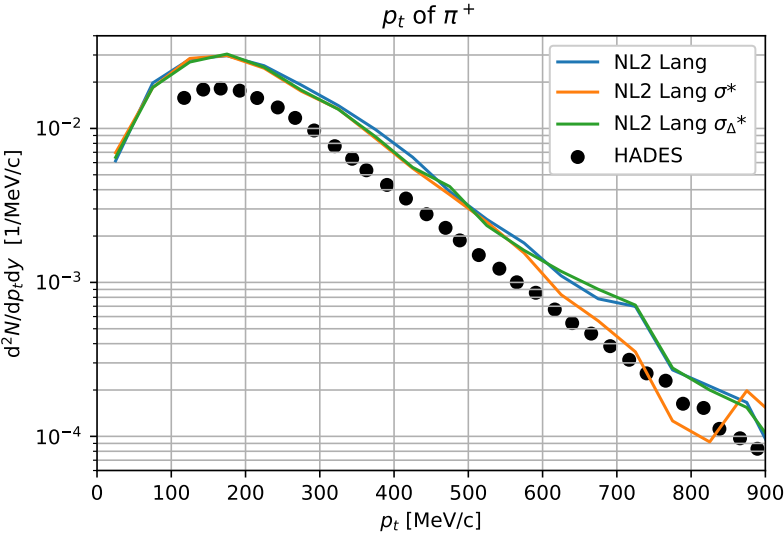
For pions NL3 by Lalazissis provides the best agreement with experiment.

Transverse momentum spectra of charged pions for $b^0 < 0.15b_{max}$ integrated over rapidity. Data to the left of black line are extrapolated.



HADES measured the pion rapidity spectra and the transverse momentum spectra of charged pions. AuAu @ 1.23 AGeV J. Adamczewski-Musch et al., EPJA 56, 259 (2020)

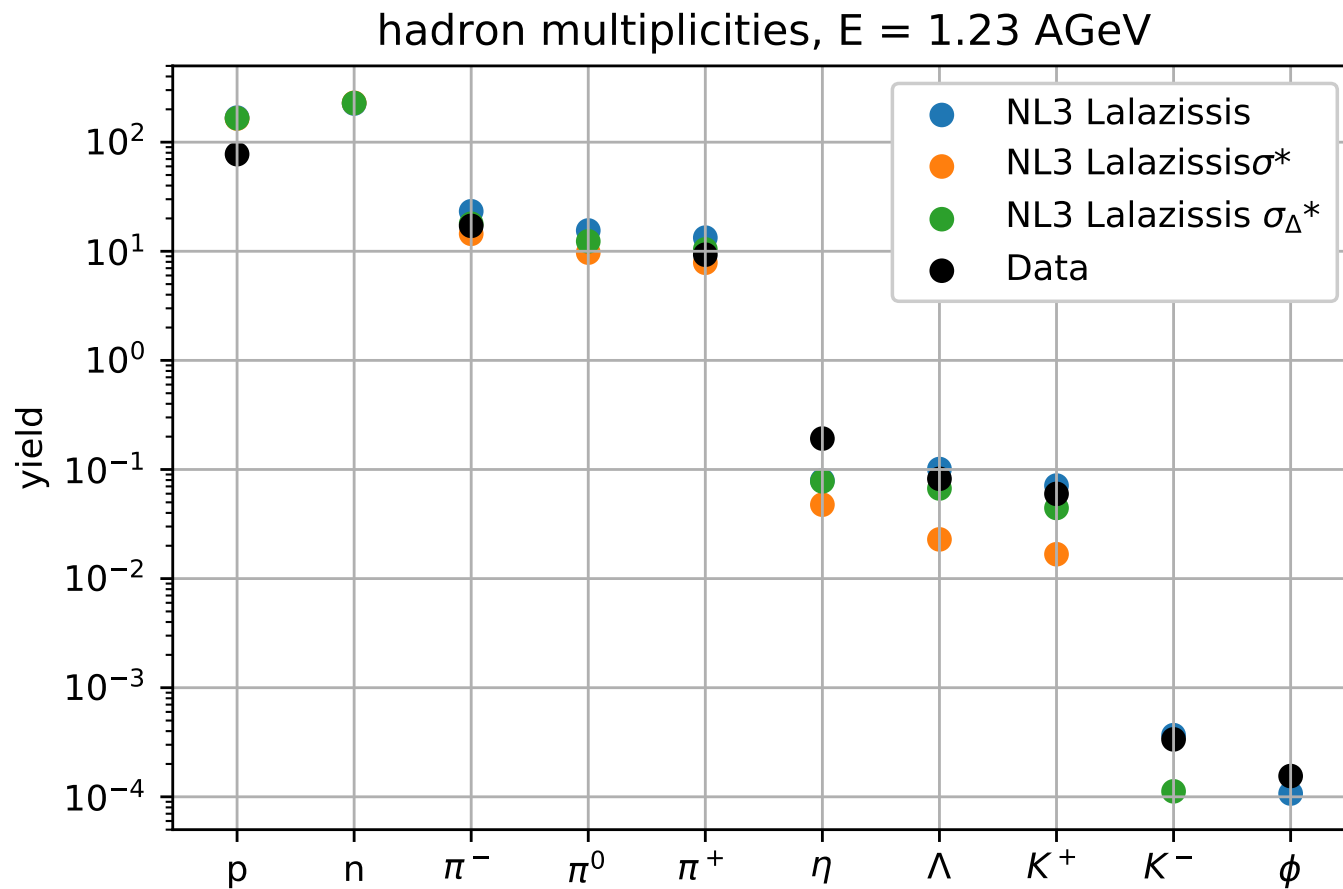
Transverse momentum spectra of charged pions for 10 % most central events at midrapidity.



The yield for various hadrons can be reproduced well

By only modifying the cross sections related to Δ strangeness is comparable with experiments

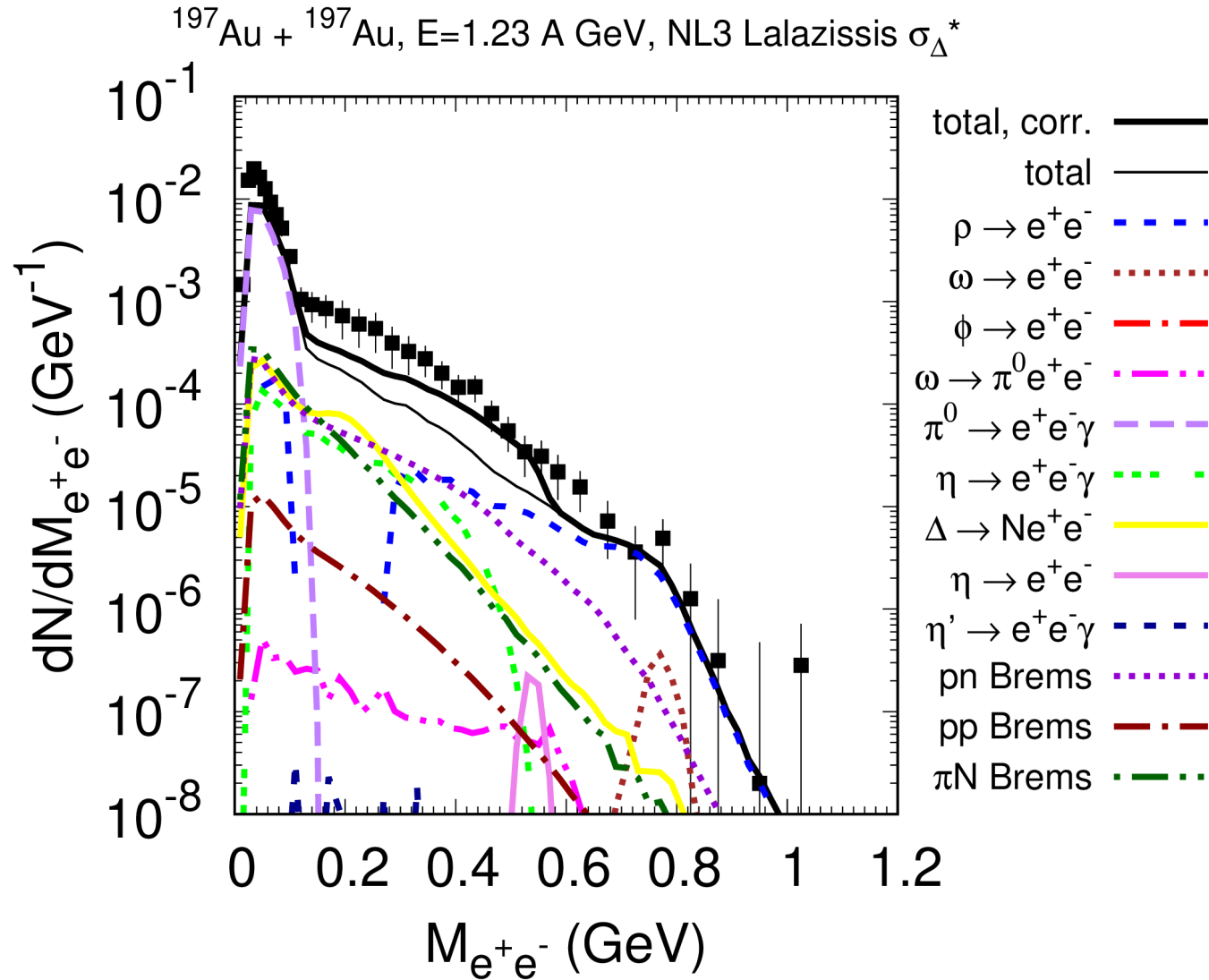
Larionov et al., PRC 102, 064913 (2020)



Hadron yields for the 10% or 20% most central events. AuAu @ 1.23 AGeV

Surprisingly, the π^0 Dalitz decay is now underpredicted

J. Adamczewski-Musch et al. (HADES), Nature



Invariant Mass spectra of dileptons for 40 % most central events

conclusion

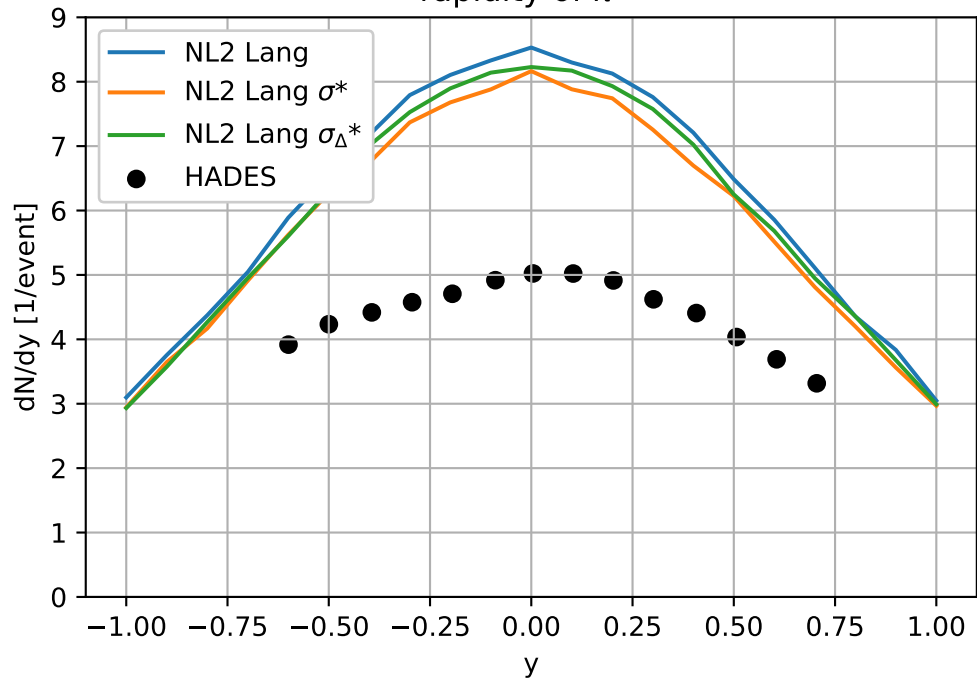
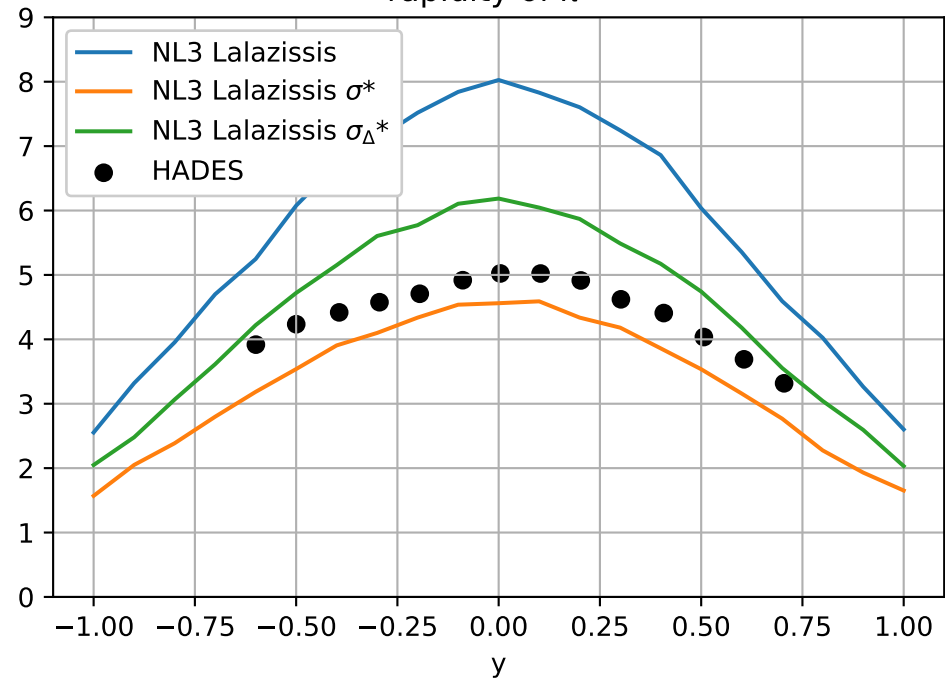
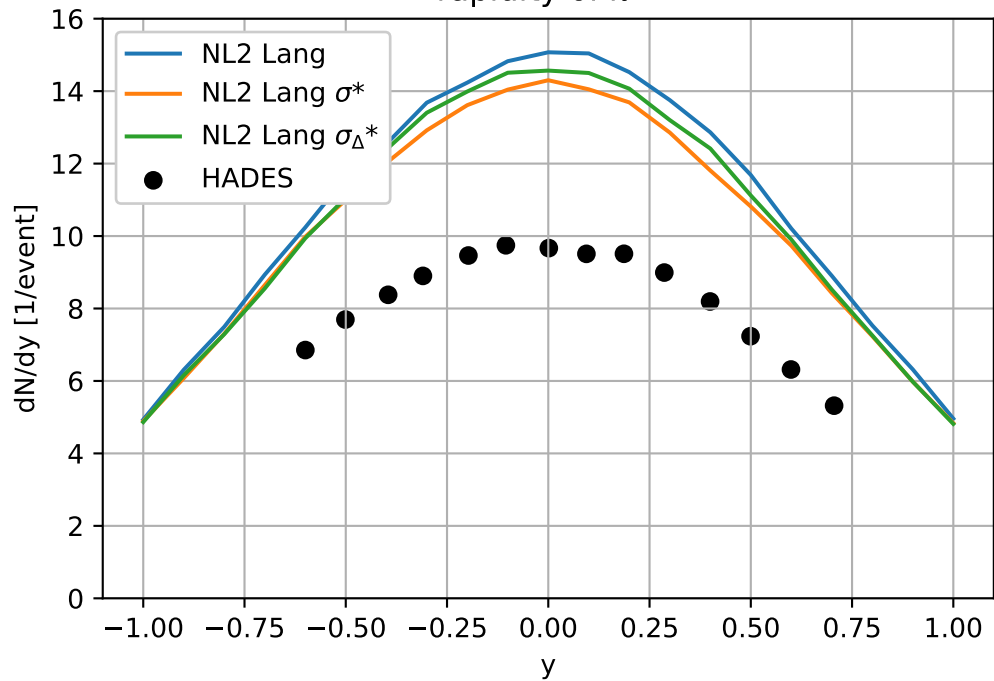
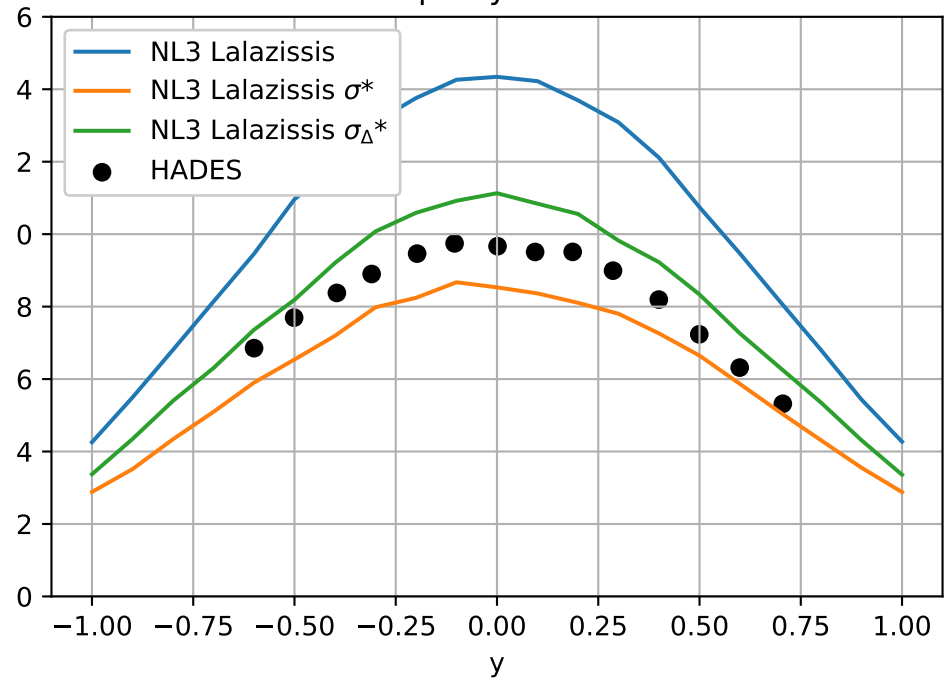
NL2 by Lang describes proton distributions in HIC's well, but creates an abundance of pions

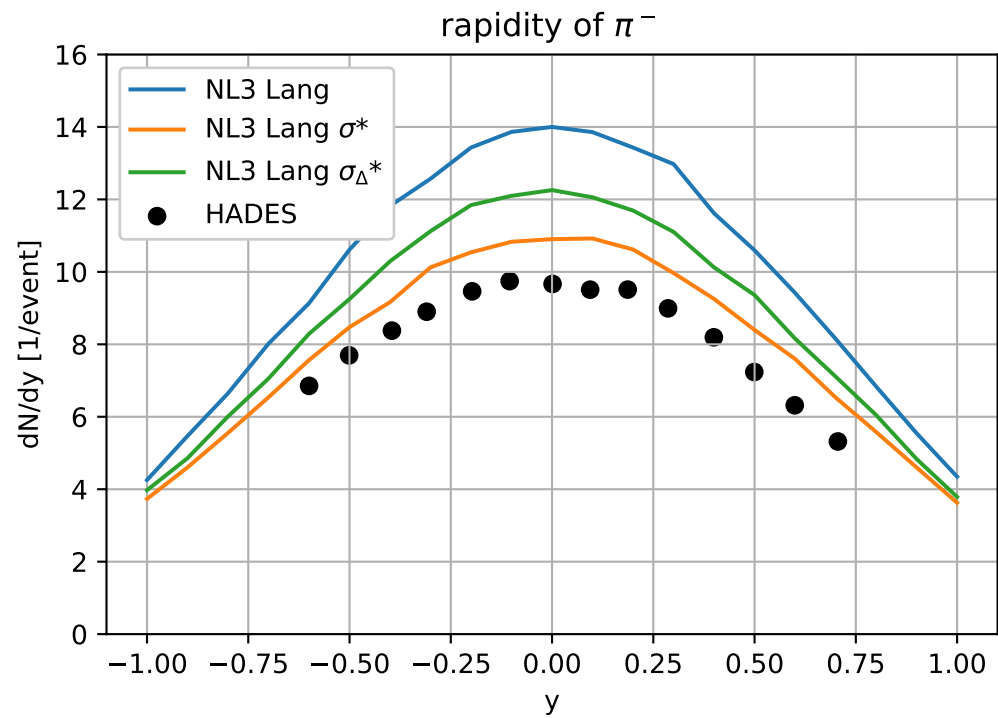
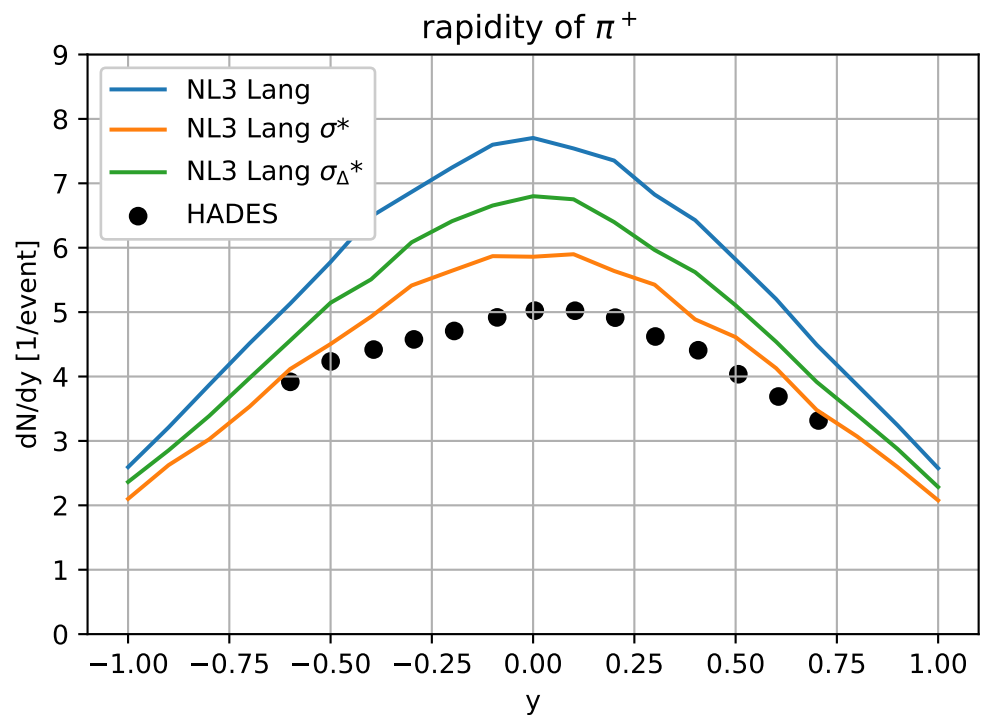
To lower pion yields, NL3 by Lalazissis with modifications of the Δ cross sections are used

NL2 by Lang performs better at lower Energies (400 AMeV)

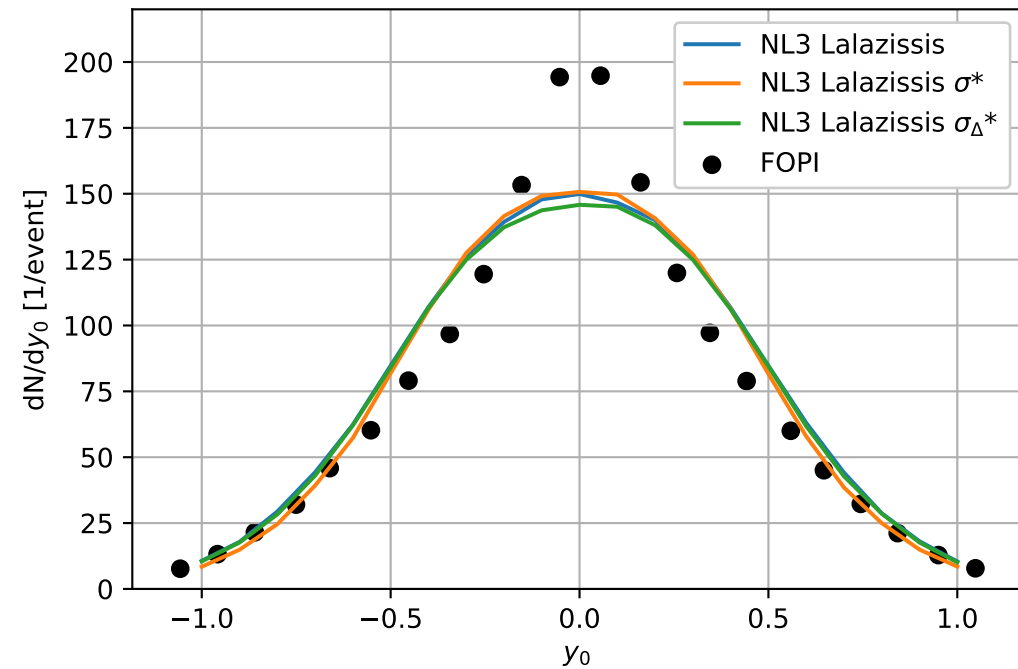
Reproducing the π^0 Dalitz decay leads to an excess of pions. Lowering the pion yield also lowers the π^0 Dalitz decay.

Backup

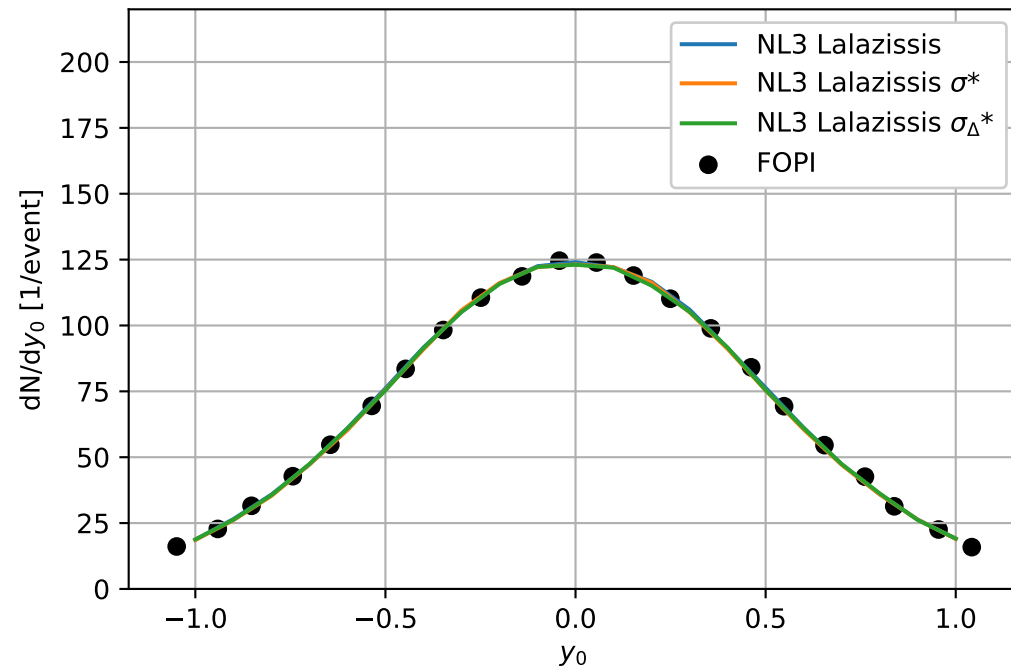
rapidity of π^+ rapidity of π^+ rapidity of π^- rapidity of π^- 



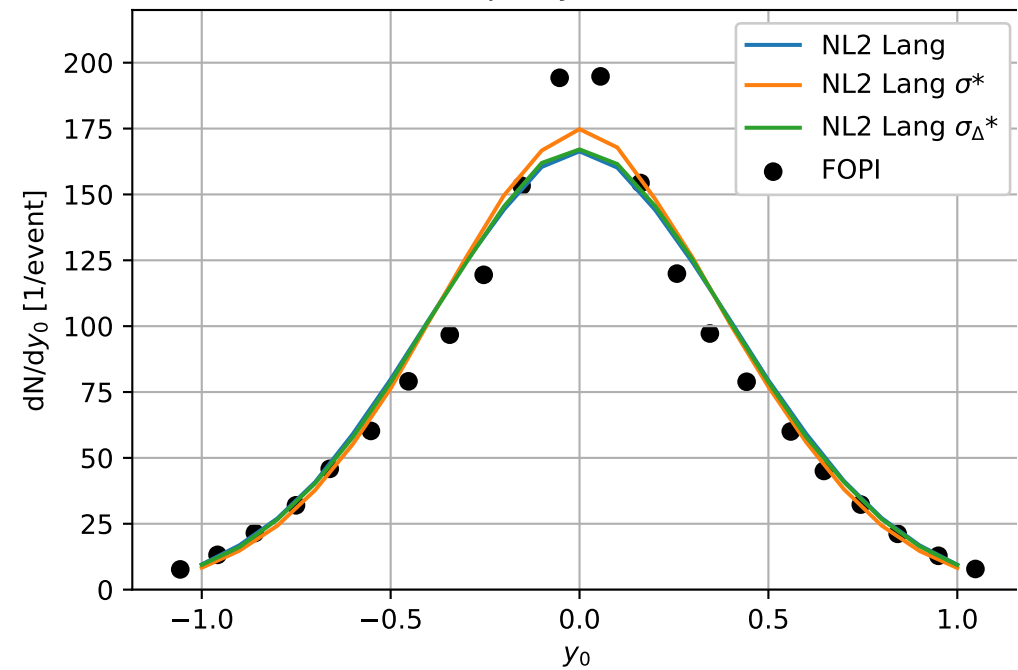
transverse rapidity, AuAu @ 1.5 AGeV



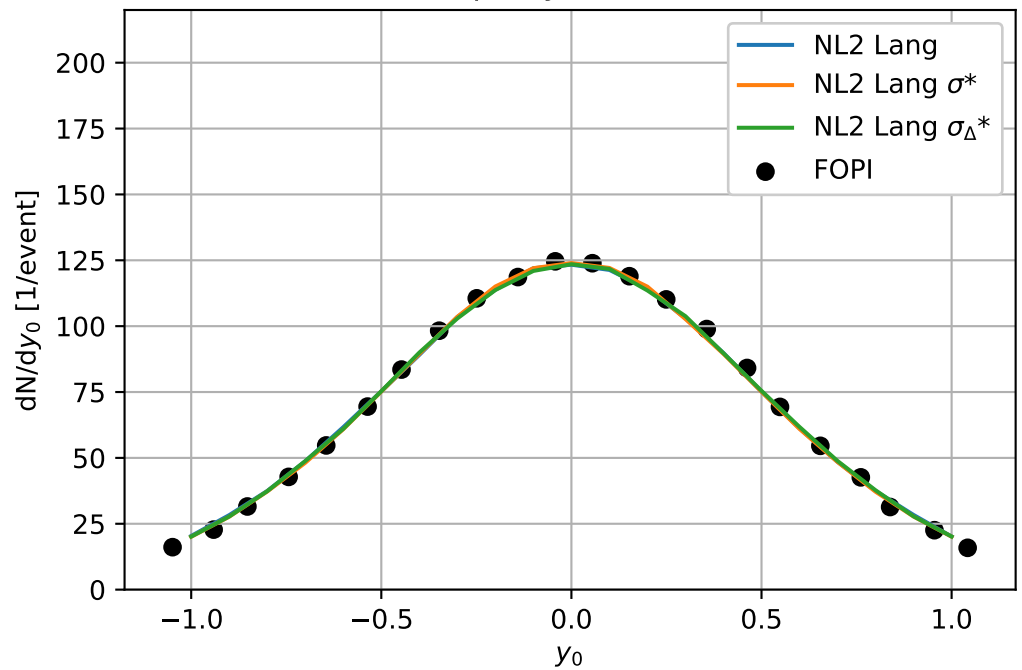
transverse rapidity, AuAu @ 400 AMeV



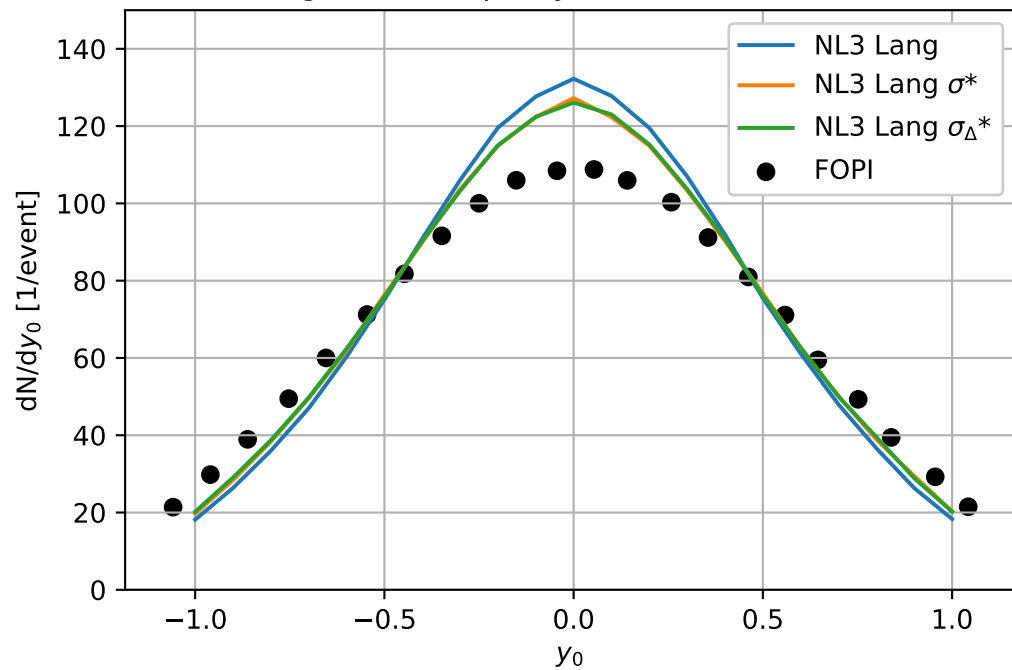
transverse rapidity, AuAu @ 1.5 AGeV



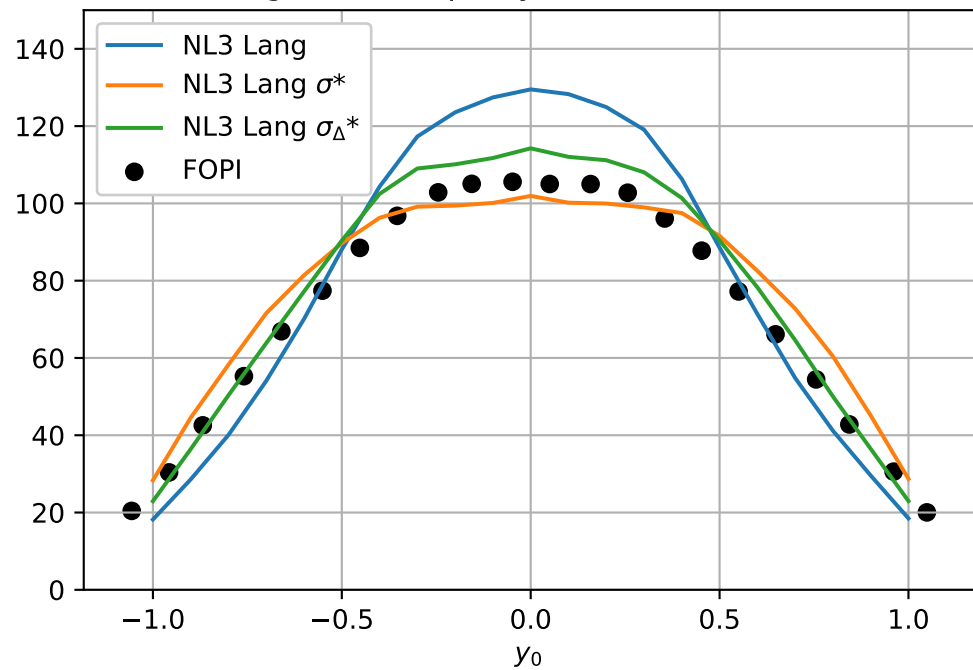
transverse rapidity, AuAu @ 400 AMeV



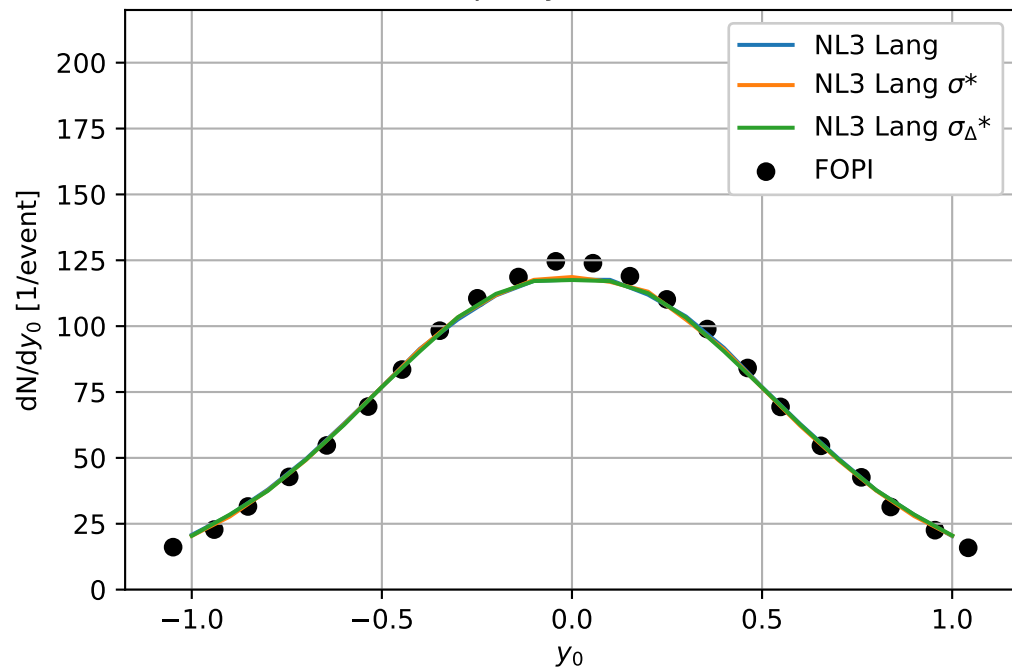
longitudinal rapidity, AuAu @ 400 AMeV



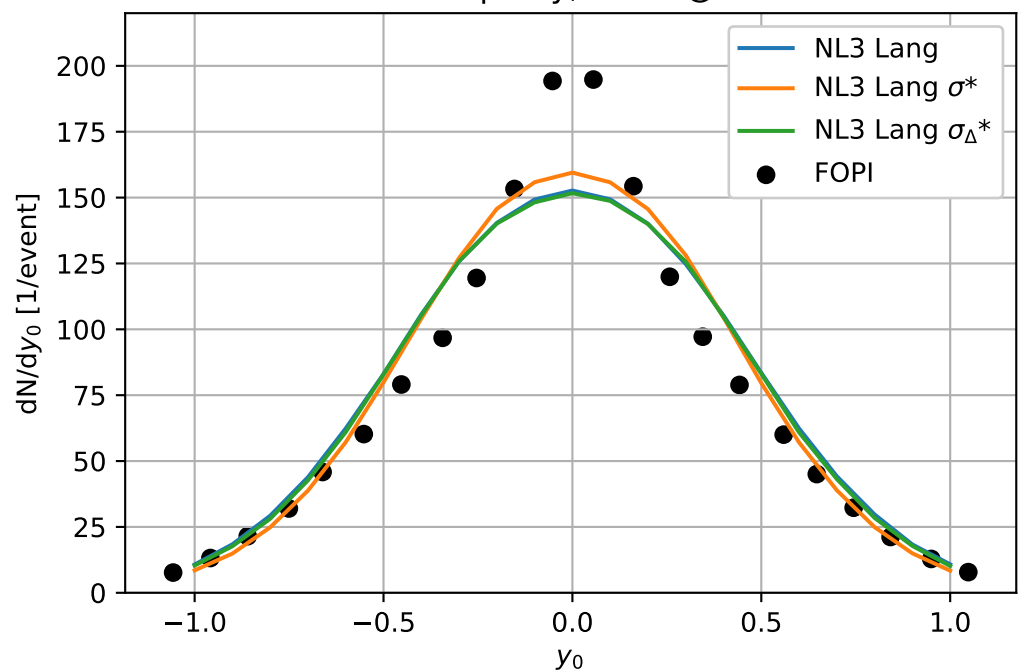
longitudinal rapidity, AuAu @ 1.5 AGeV

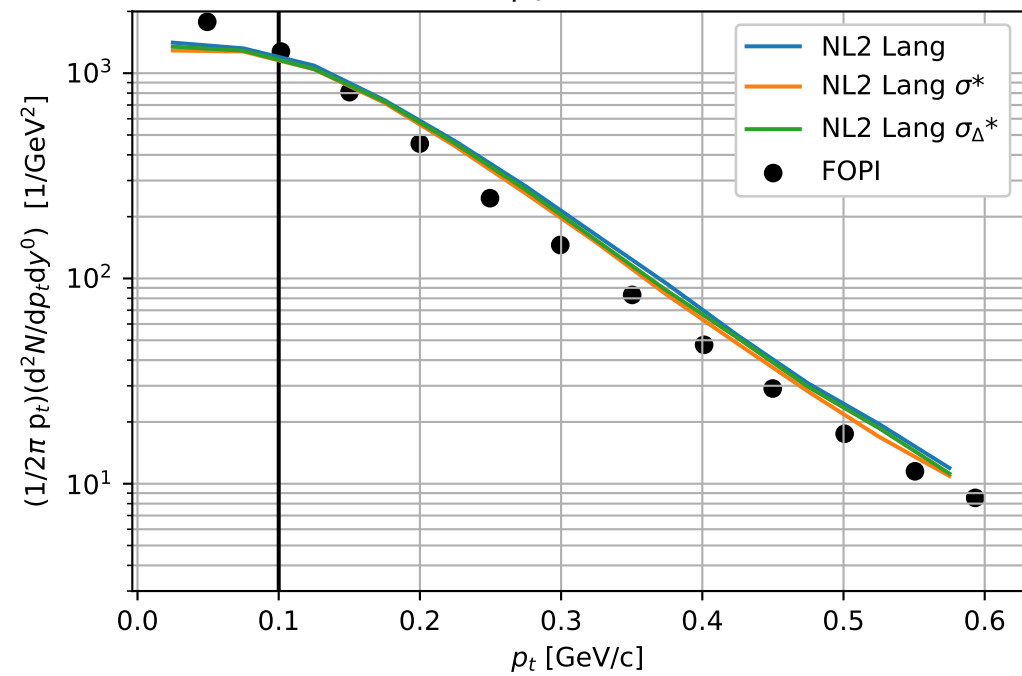
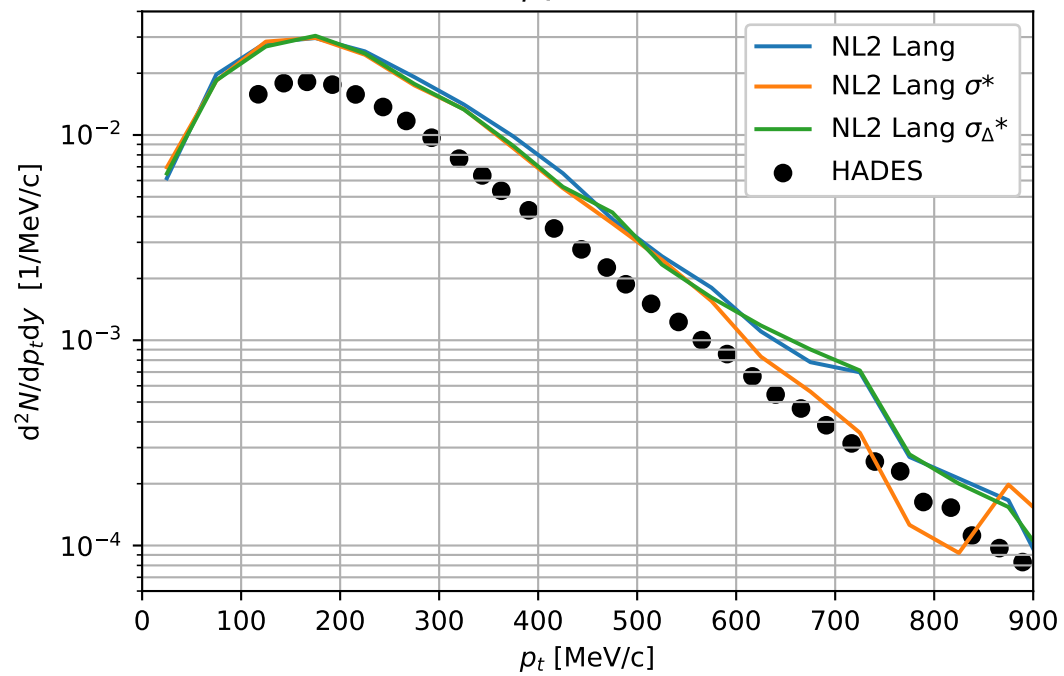
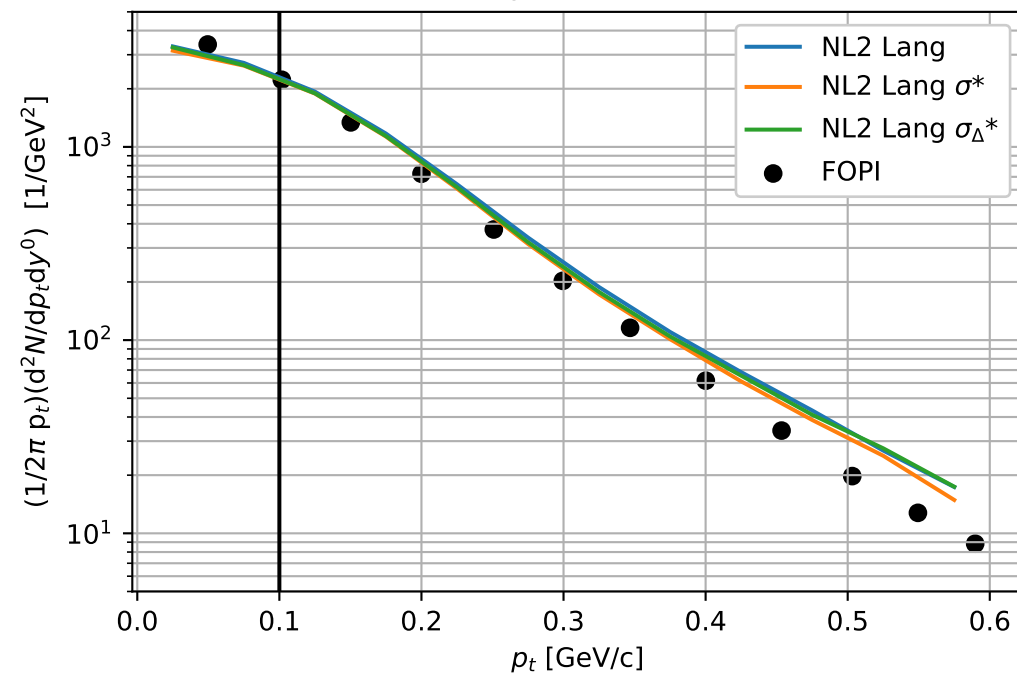


transverse rapidity, AuAu @ 400 AMeV



transverse rapidity, AuAu @ 1.5 AGeV



p_t of π^+  p_t of π^+  p_t of π^-  p_t of π^- 