

# Lecture

## Introduction:

# „Dynamical models for relativistic heavy-ion collisions“

## **Lectures:**

**Thursday, 11:15-12:45**

**Lecturers:** Elena Bratkovskaya, Igor Mishustin

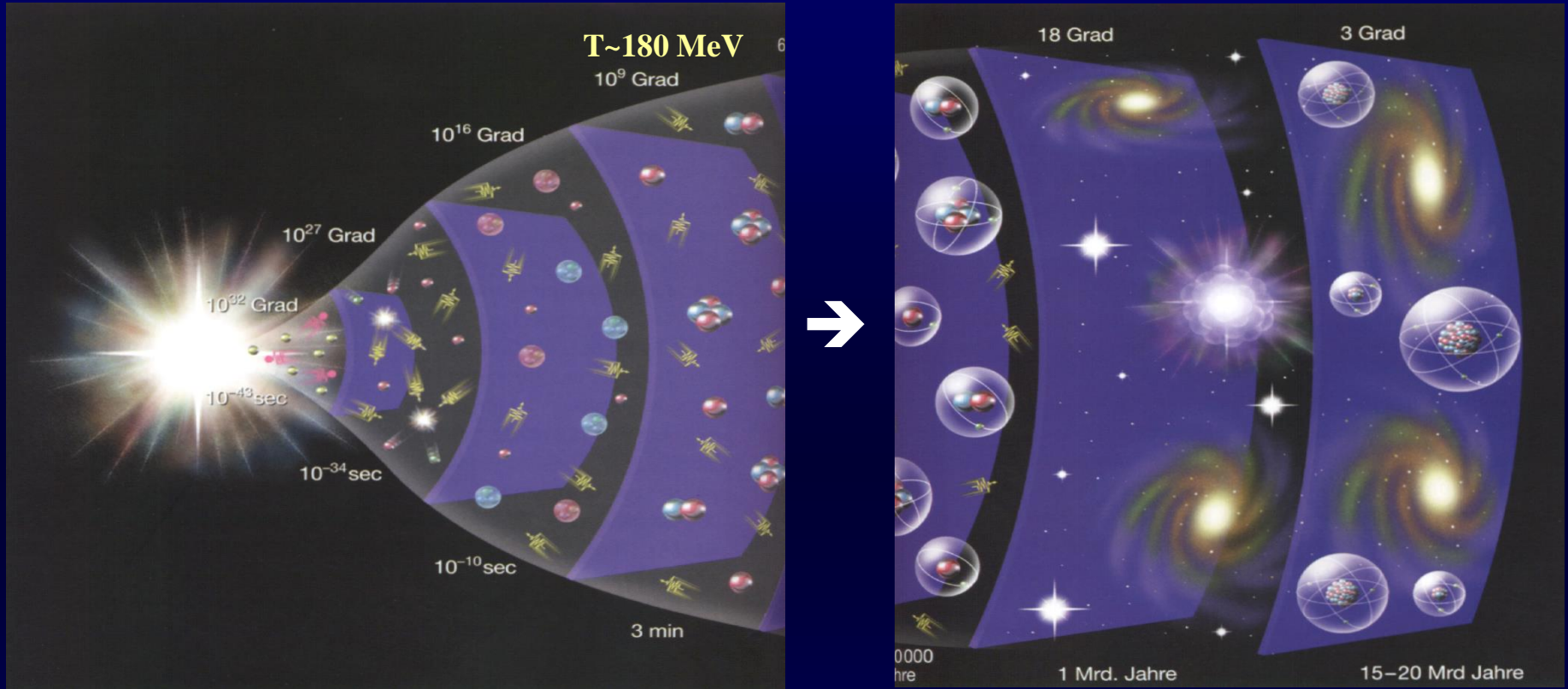
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**e-mail: mishustin@fias.uni-frankfurt.de**

**[http://theory.gsi.de/~ebratkov/LecturesSS2024/Lec\\_SS2024.html](http://theory.gsi.de/~ebratkov/LecturesSS2024/Lec_SS2024.html)**

# From Big Bang to Formation of the Universe



*time*

$10^{-3} \text{ sec}$

quarks  
gluons  
photons

3 min

nucleons  
deuterons  
 $\alpha$ -particles

30000 years

atoms

15 Mrd years

our Universe

← Can we go back in time?



# ... back in time

‚Re-create‘ the **Big Bang conditions:**

matter at high temperature and pressure

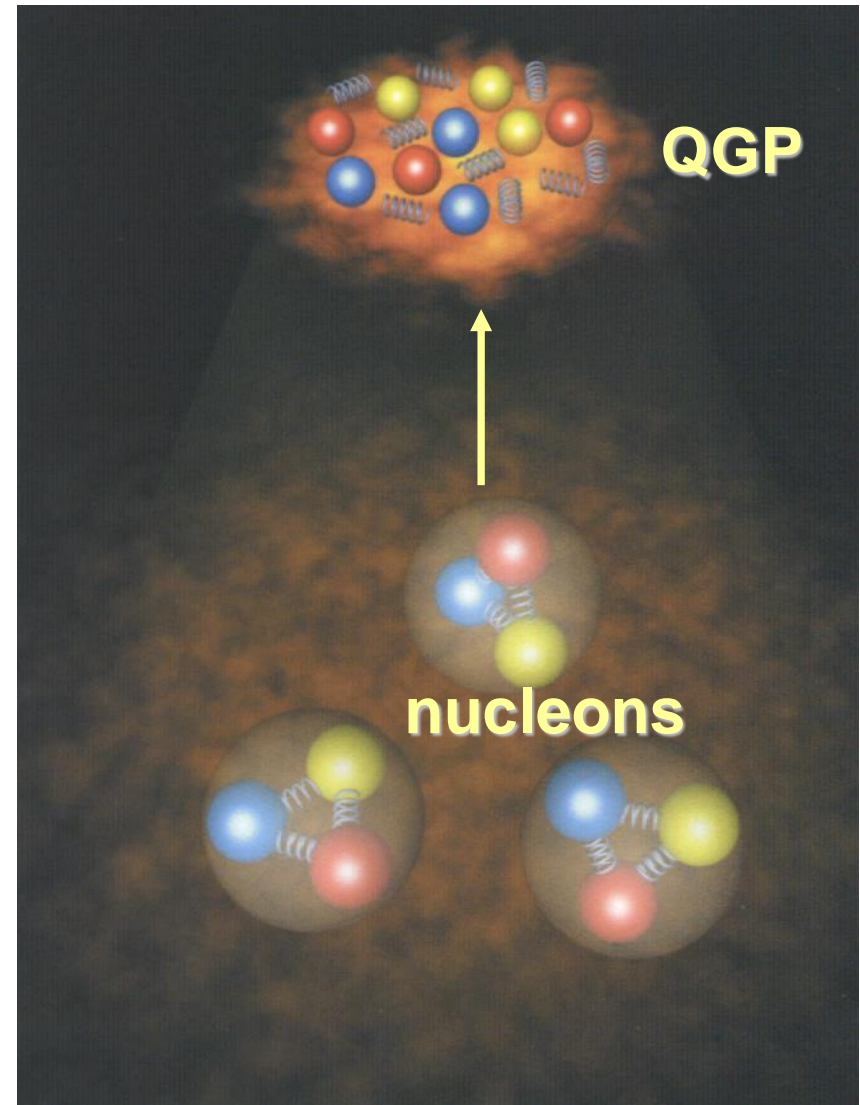
such that

nucleons/mesons decouple to quarks and gluons --

**Quark-Gluon-Plasma**

‚Little Bangs‘ in the **Laboratory :**

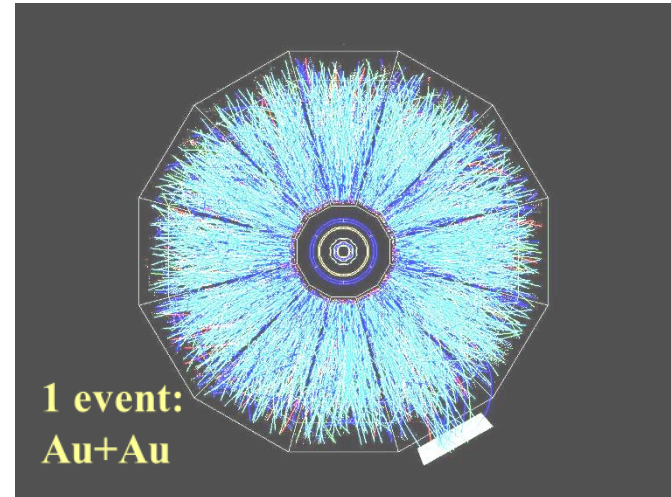
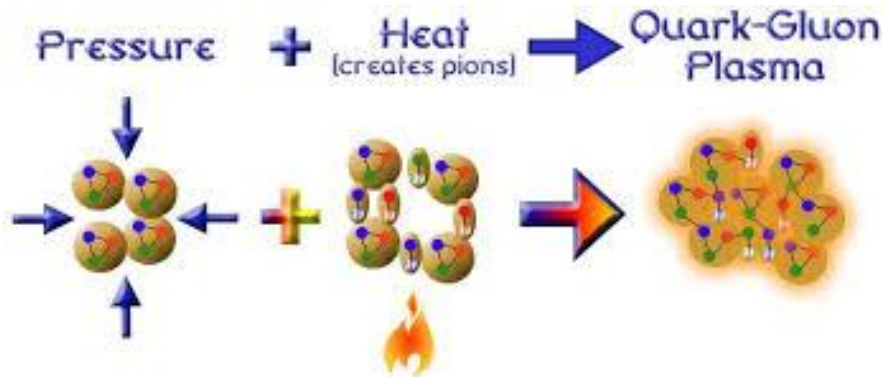
Heavy-ion collisions at ultrarelativistic energies



# Heavy-ion collisions

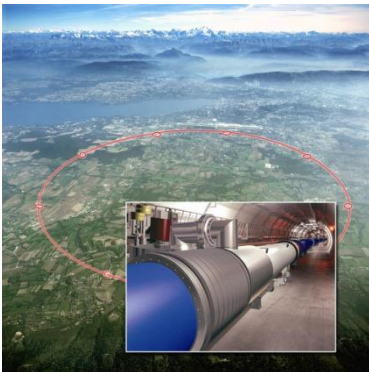
## □ Heavy-ion collision experiment

→ ,re-creation‘ of the Big Bang conditions in laboratory:  
matter at high **pressure** and **temperature**

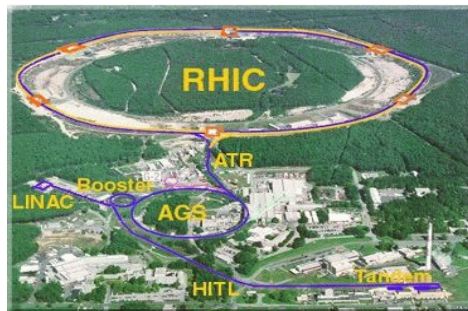


## □ Heavy-ion accelerators:

Large Hadron Collider -  
LHC (CERN):  
Pb+Pb up to 574 A TeV



Relativistic-Heavy-Ion-Collider -  
RHIC (Brookhaven):  
Au+Au up to 21.3 A TeV



Facility for Antiproton and Ion  
Research – FAIR (Darmstadt)  
(Under construction)  
Au+Au up to 10 (30) A GeV



Nuclotron-based Ion Collider  
Facility – NICA (Dubna)  
(Under construction)  
Au+Au up to 70 A GeV

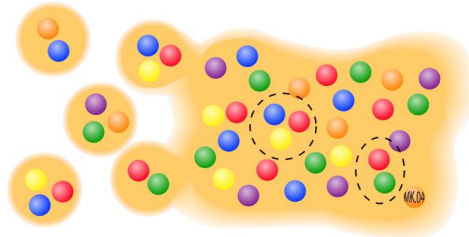


# The QGP in Lattice QCD

## Quantum Chromo Dynamics :

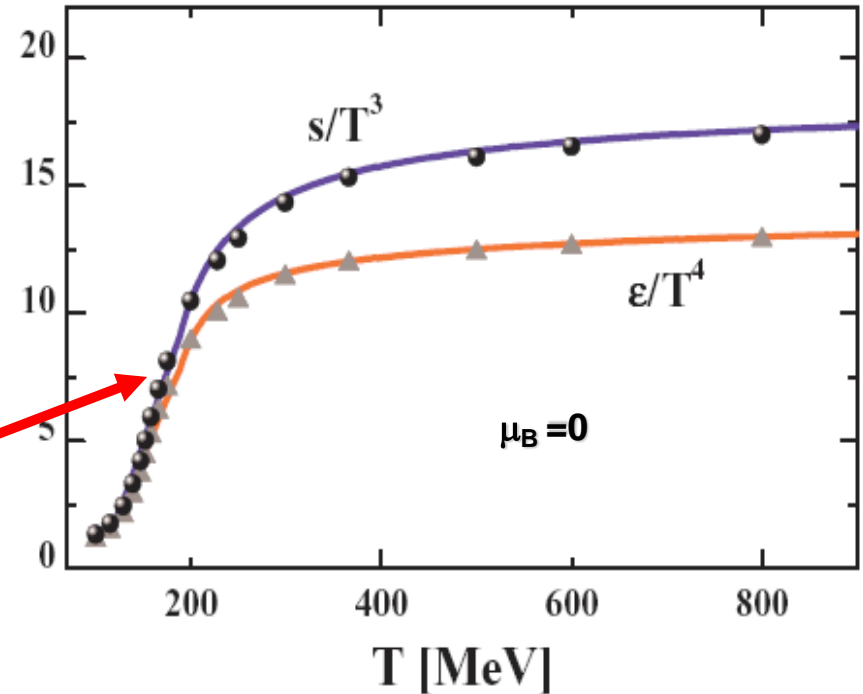
predicts strong increase of the **energy density  $e$**  at critical temperature  **$T_C \sim 160$  MeV**

$\Rightarrow$  Possible **phase transition** from hadronic to **partonic matter** (quarks, gluons) at critical energy density  **$\epsilon_C \sim 0.5$  GeV/fm<sup>3</sup>**

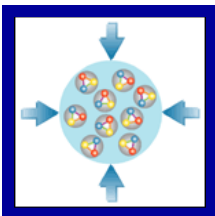


## Lattice QCD:

energy density versus temperature

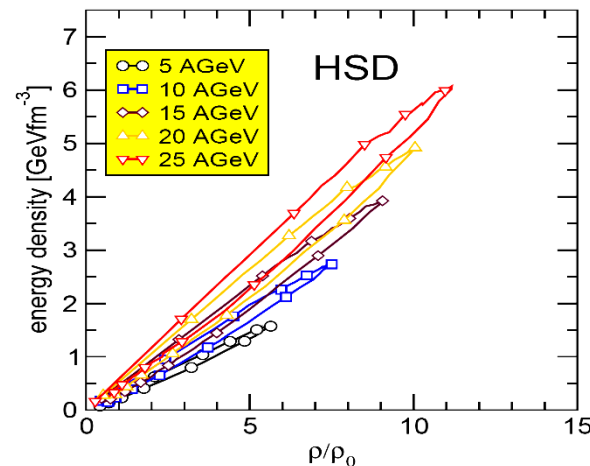
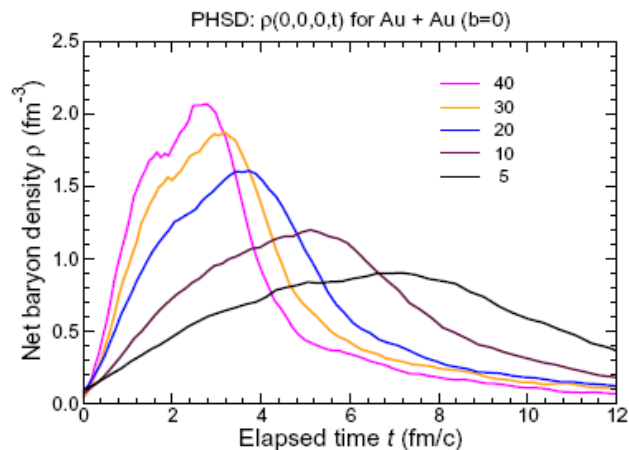
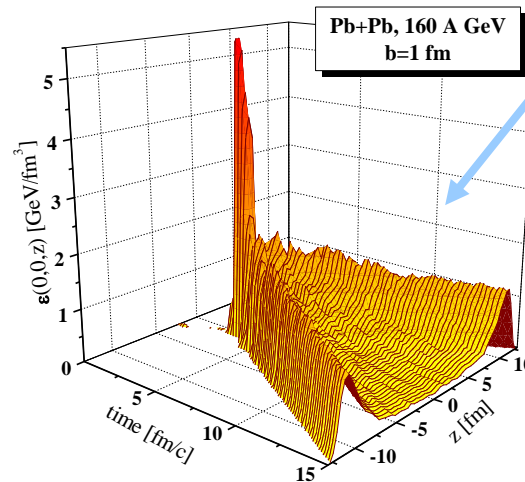
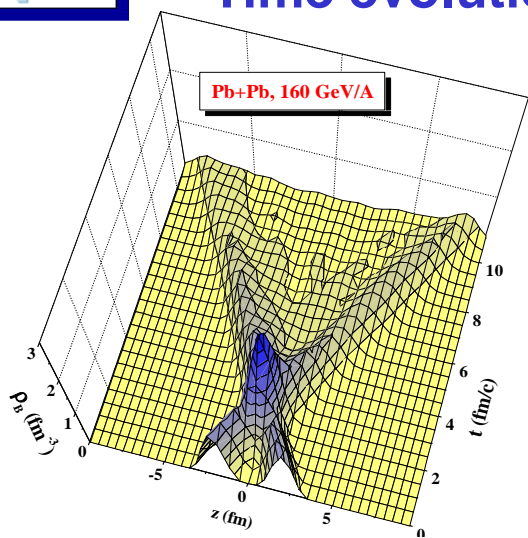


Critical conditions -  **$\epsilon_C \sim 0.5$  GeV/fm<sup>3</sup>** ,  **$T_C \sim 160$  MeV** - can be reached in **heavy-ion experiments** at bombarding energies  **$> 5$  GeV/A**



# Dense and hot matter – average quantities

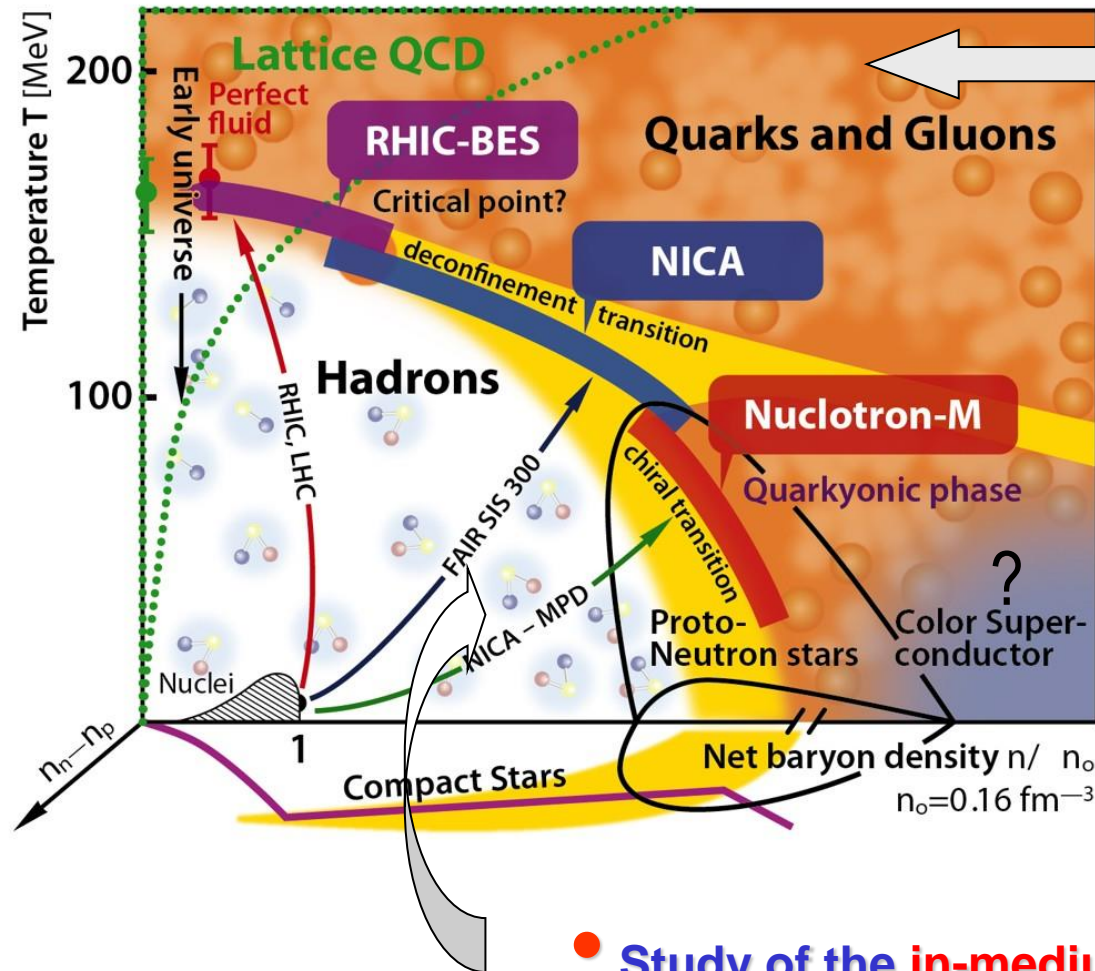
## Time evolution of the baryon density and energy density



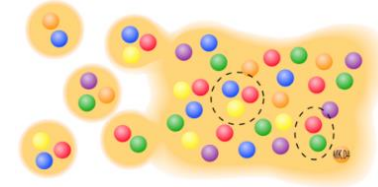
huge energy and baryon densities are reached ( $\epsilon > \epsilon_{\text{crit}}=0.5 \text{ GeV/fm}^3$ )  
at FAIR/NICA energies ( $> 5 \text{ A GeV}$ )

# The ,holy grail' of heavy-ion physics:

## The phase diagram of QCD



- Search for the **critical point**



- Study of the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma**

- Search for signatures of **chiral symmetry restoration**

- Search for the **critical point**

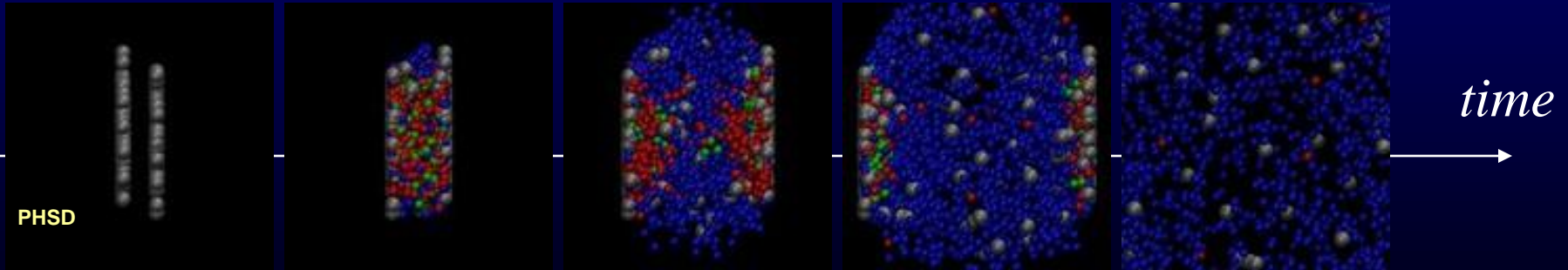
- Study of the **in-medium** properties of hadrons at high baryon density and temperature



# „Little Bangs‘ in the Laboratory

Initial State

Hadronization



Au+Au

Quark-Gluon-Plasma ?

hadron  
degrees  
of freedom



quarks and gluons



hadron  
degrees  
of freedom

How can we prove that an equilibrium QGP has been created in central heavy-ion collisions ?!

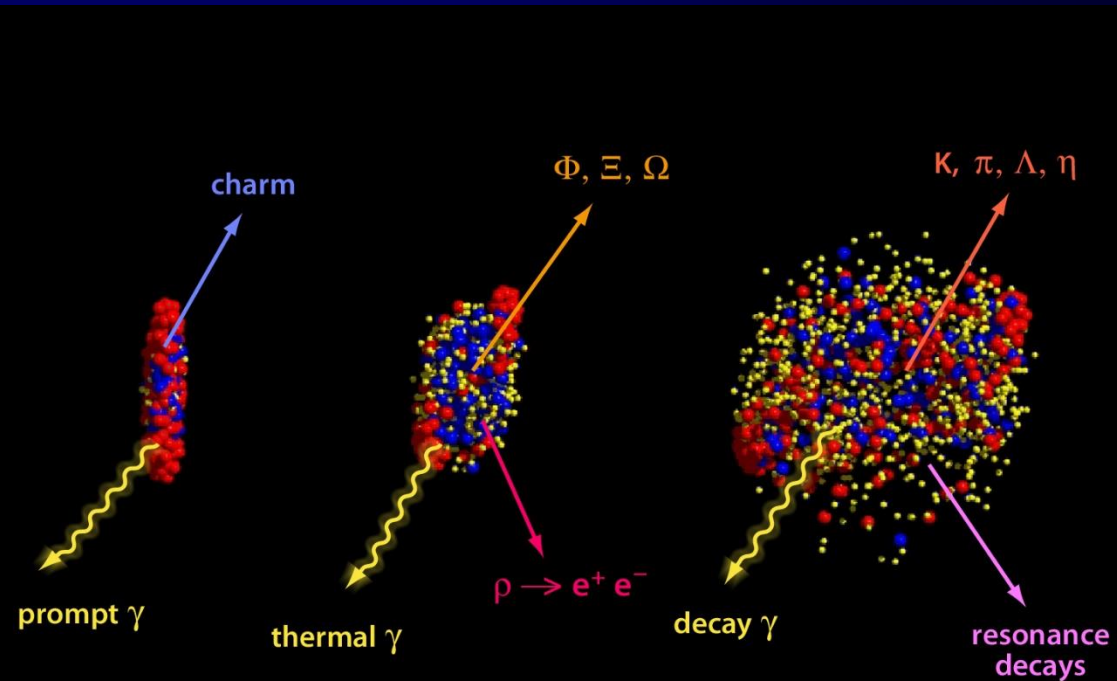
## Signals of the phase transition:

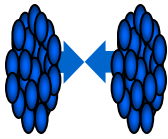
- Multi-strange particle enhancement in A+A
- Charm suppression
- Collective flow ( $v_1, v_2$ )
- Thermal dileptons
- Jet quenching and angular correlations
- High  $p_T$  suppression of hadrons
- Nonstatistical event by event fluctuations and correlations
- ...

**Experiment:** measures final hadrons and leptons

How to learn about physics from data?

Compare with theory!





# Basic models for heavy-ion collisions

- Statistical models:

**basic assumption:** system is described by a (grand) canonical ensemble of non-interacting fermions and bosons in **thermal and chemical equilibrium**  
= **thermal hadron gas at freeze-out** with common  $T$  and  $\mu_B$

[ - : no dynamical information]

- Hydrodynamical models:

**basic assumption:** conservation laws + equation of state (EoS);  
assumption of **local thermal and chemical equilibrium**

- Interactions are ,hidden' in properties of the **fluid** described by **transport coefficients** (shear and bulk viscosity  $\eta$ ,  $\zeta$ , ..), which is **'input'** for the hydro models

[ - : simplified dynamics]

- Microscopic transport models:

**based on transport theory of relativistic quantum many-body systems**

- **Explicitly account for the interactions of all degrees of freedom** (hadrons and partons)  
in terms of cross sections and potentials

- Provide a unique dynamical description of **strongly interaction matter**

**in- and out-of equilibrium:**

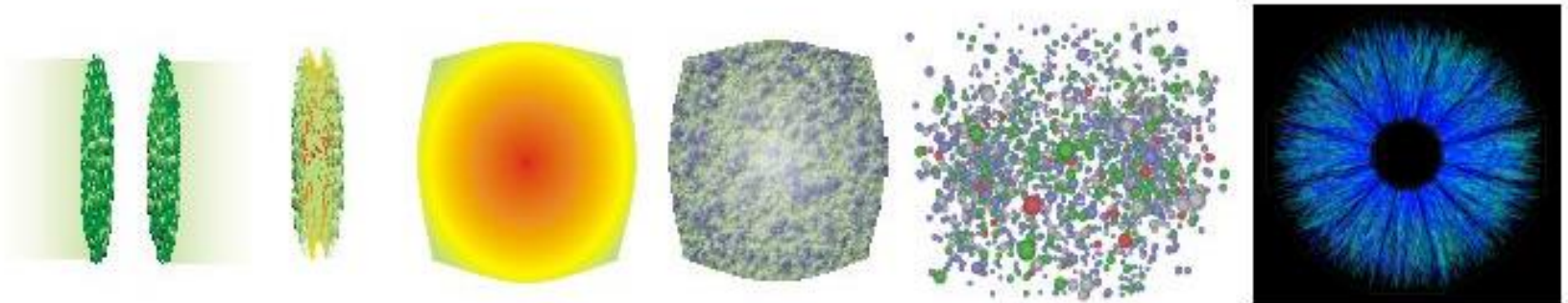
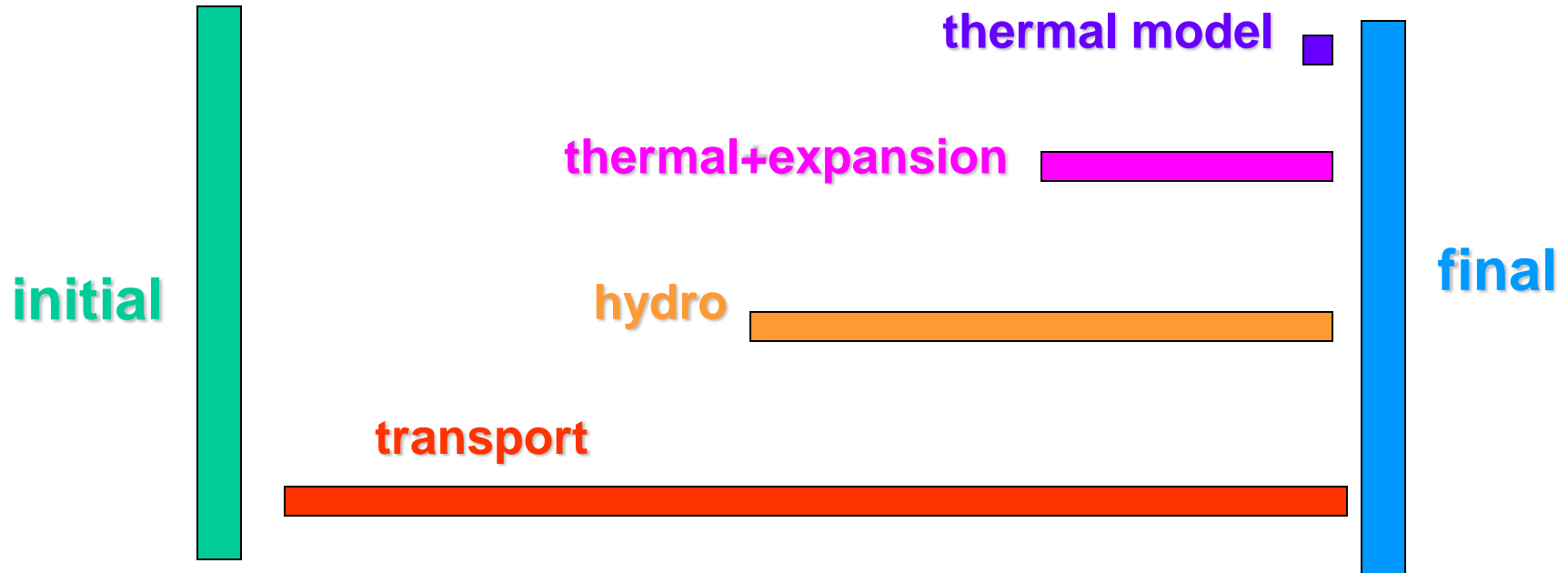
- **In-equilibrium:** transport coefficients are calculated in a box – controlled by IQCD

- **Nonequilibrium dynamics** – controlled by HIC

Actual solutions: Monte Carlo simulations

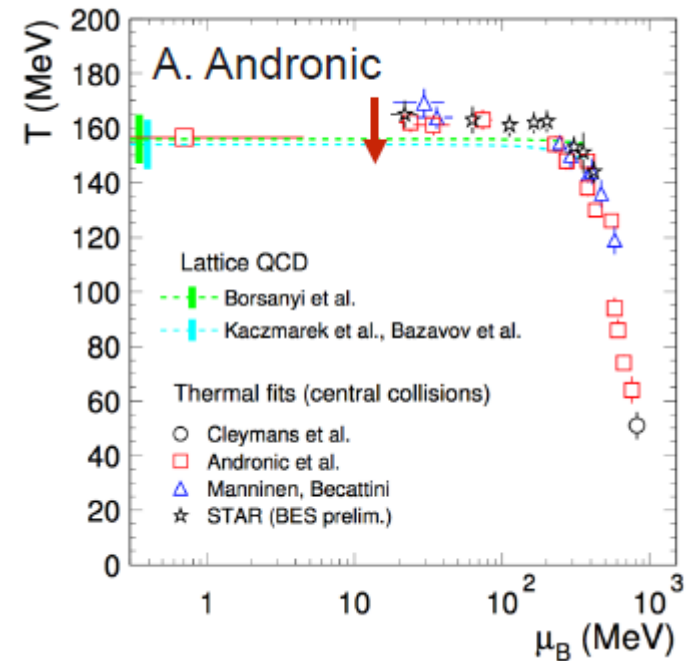
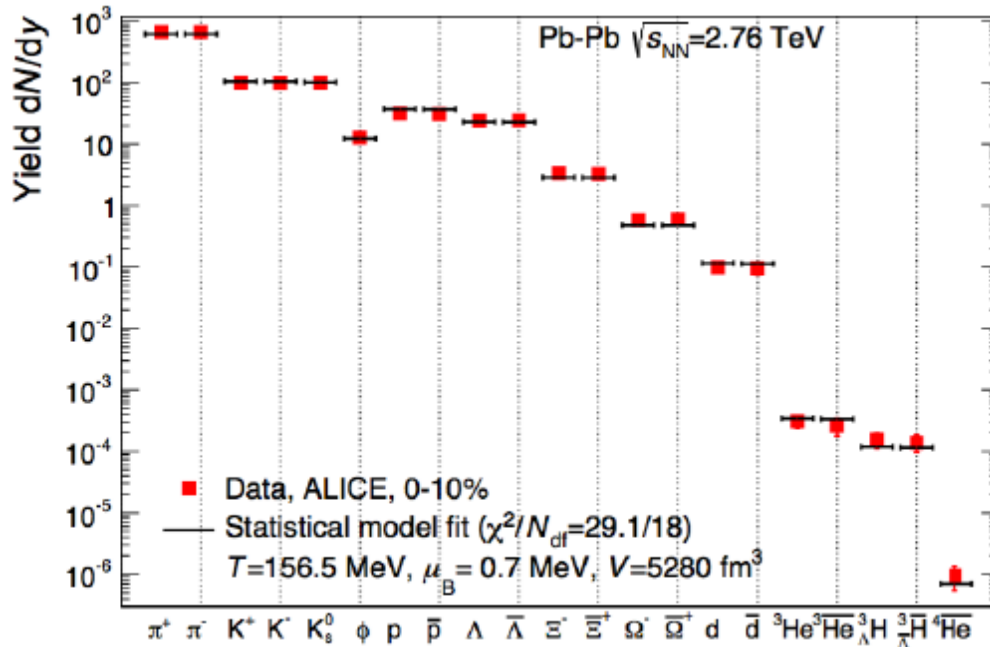
[+ : full dynamics | - : very complicated]

# Models of heavy-ion collisions



# Results from statistical models for HIC

J. Stachel et al., J.Phys. Conf. Ser. 509 (2014) 012019



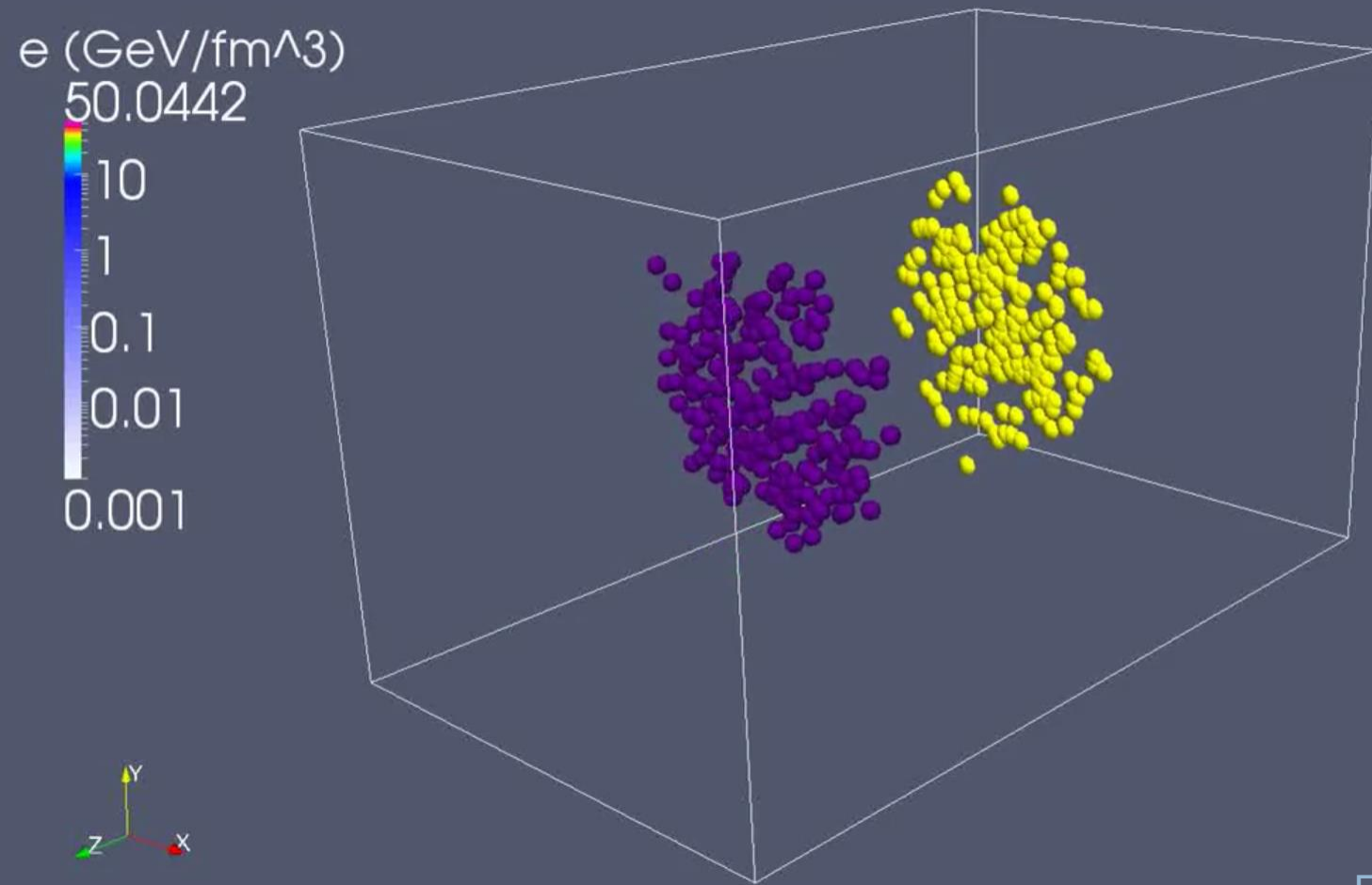
Good description of the hadron abundances by the **thermal hadron gas model** →  
 The hadron abundances are in rough agreement with a **thermally equilibrated system** !

→ **Partial thermal and chemical equilibration is approximately reached in central heavy-ion collisions at relativistic energies!**

! **Statistical models do not provide an answer to the origin of thermalization.**  
 HIC dynamics and the approach to thermal equilibrium is driven by the interactions !

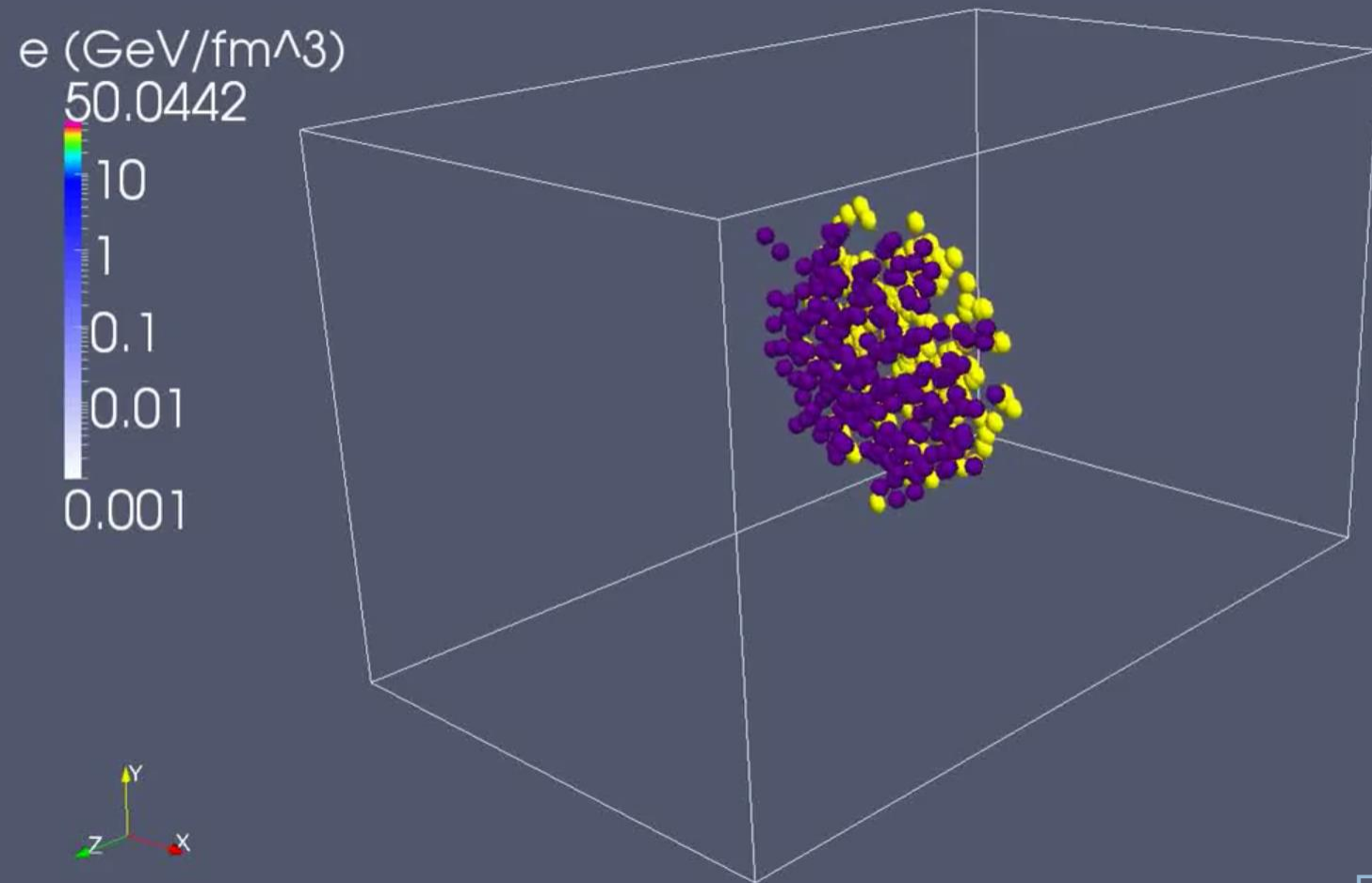
→ **dynamical models of HIC**

# Stages of a collision in VISHNU



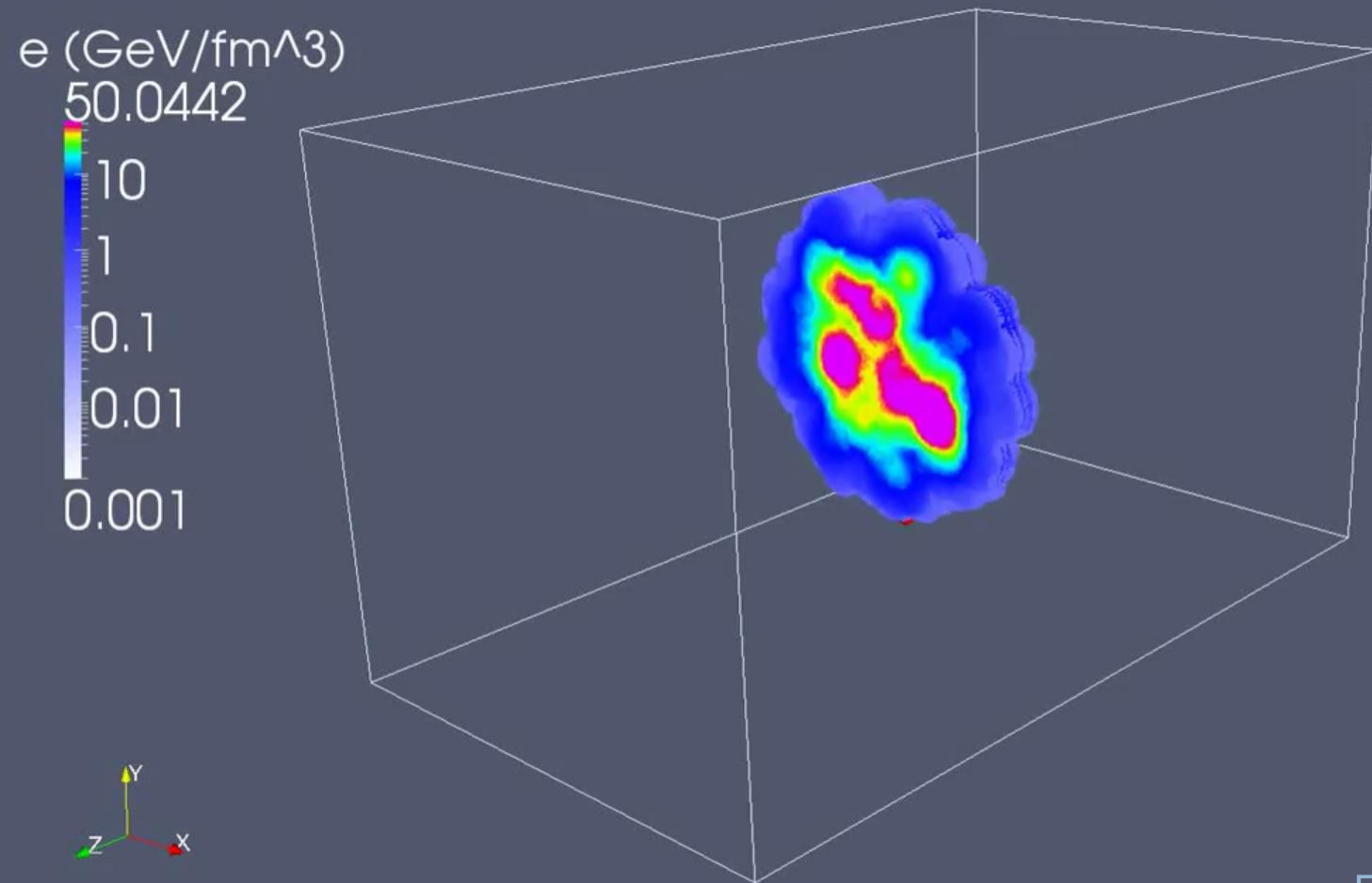
From [u.osu.edu/vishnu/](http://u.osu.edu/vishnu/)

# Stages of a collision in VISHNU



From [u.osu.edu/vishnu/](http://u.osu.edu/vishnu/)

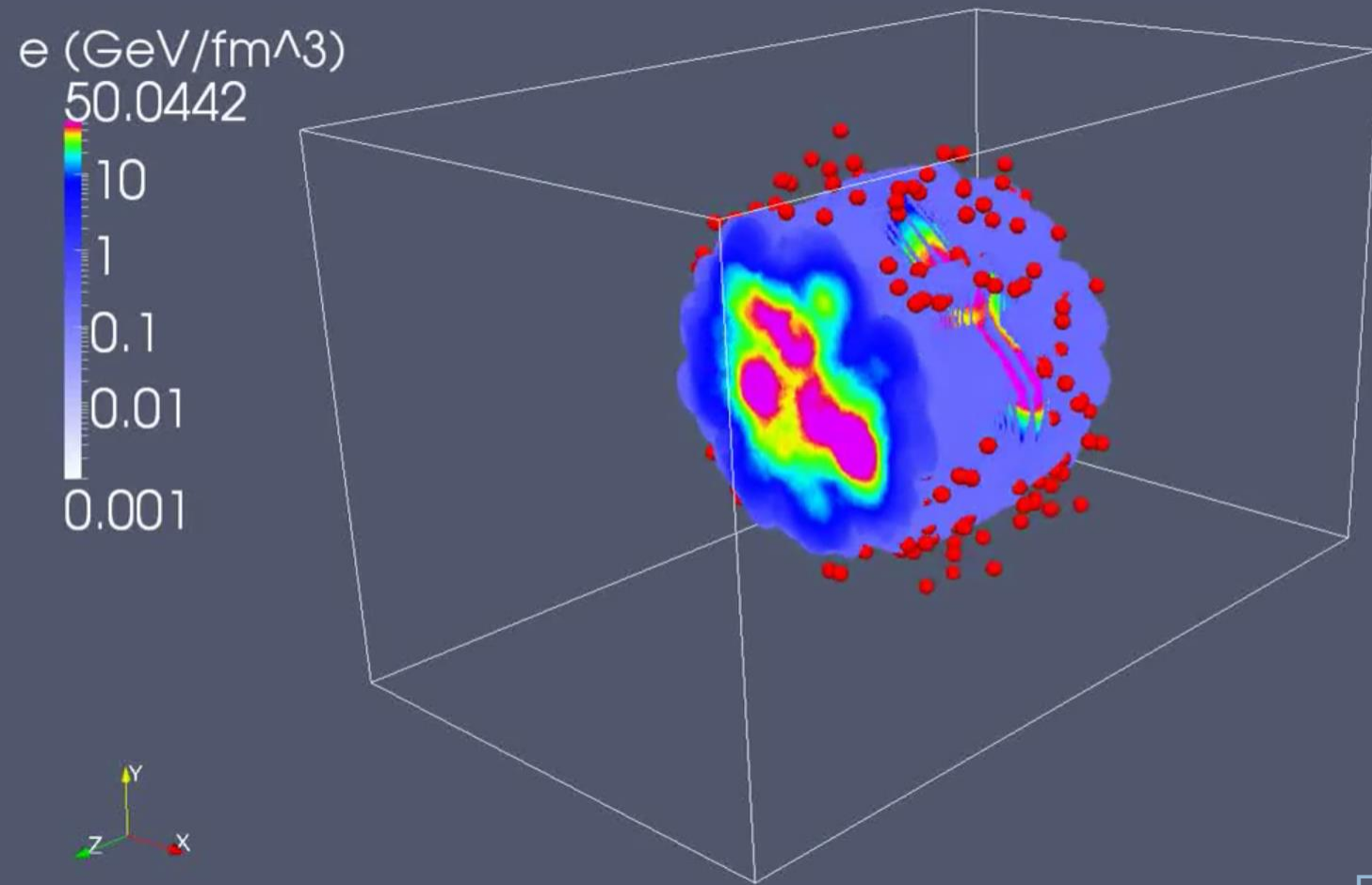
# Stages of a collision in VISHNU



From [u.osu.edu/vishnu/](http://u.osu.edu/vishnu/)

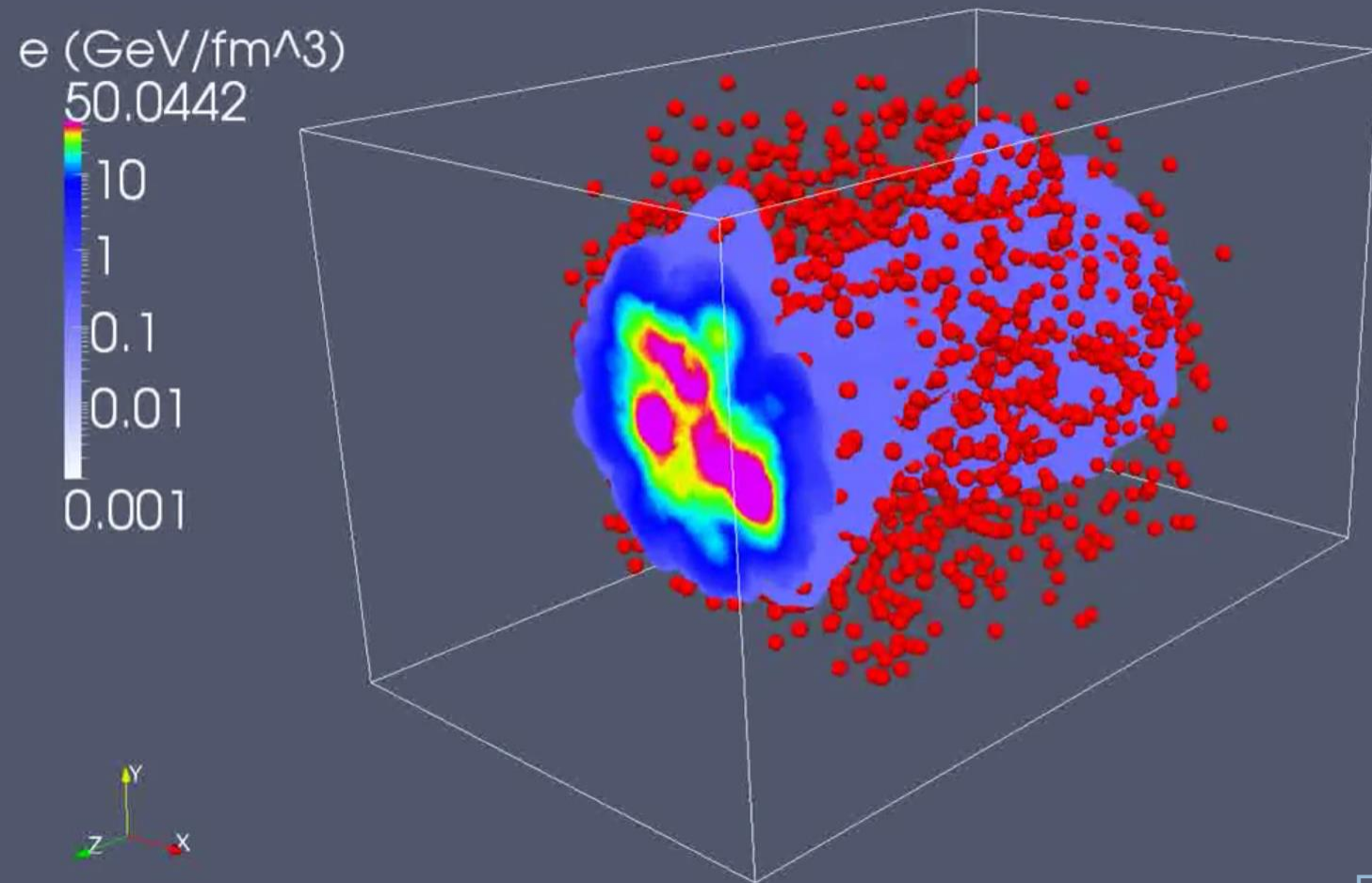


# Stages of a collision in VISHNU



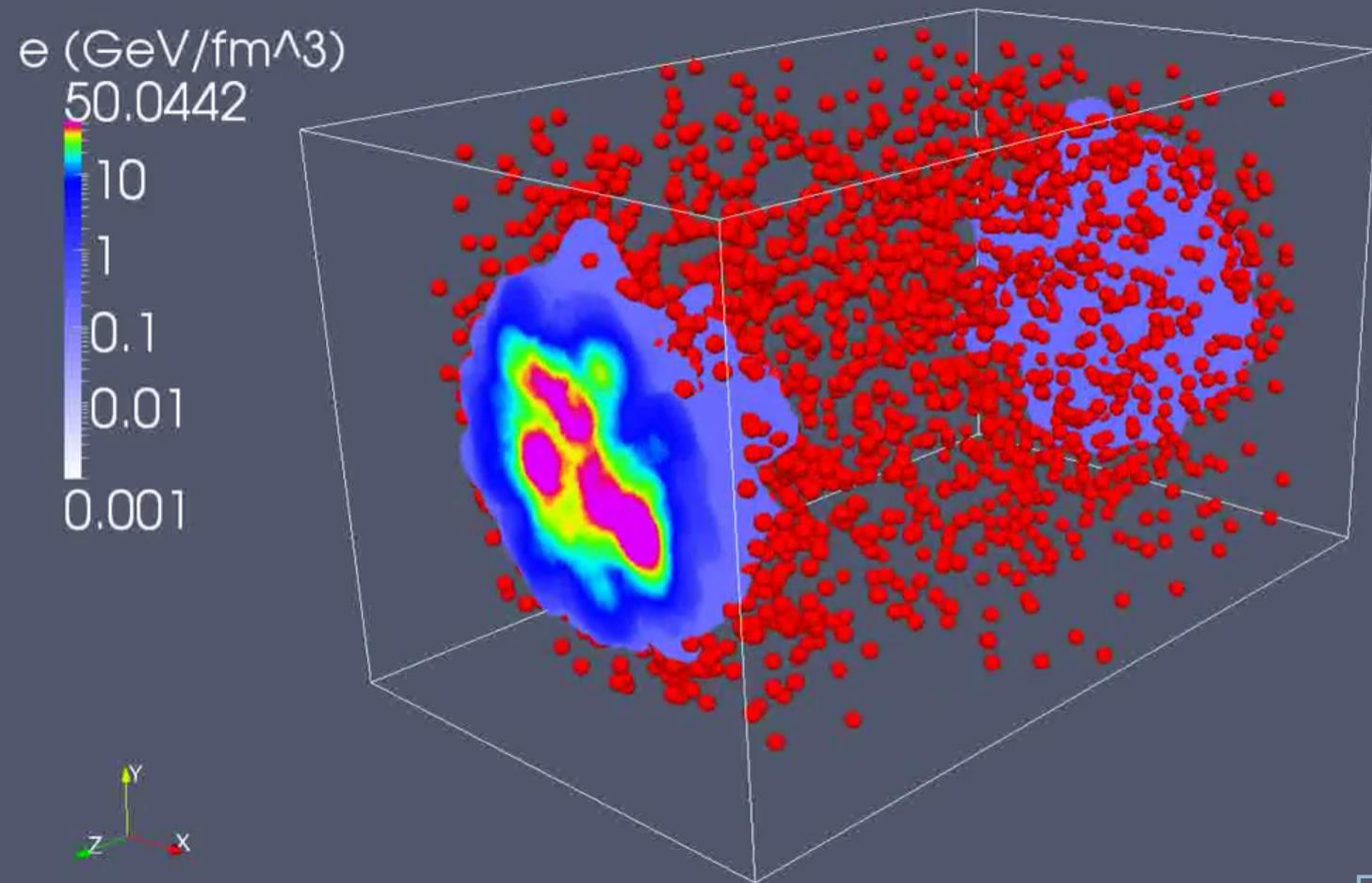
From [u.osu.edu/vishnu/](http://u.osu.edu/vishnu/)

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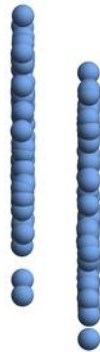
From [u.osu.edu/vishnu/](http://u.osu.edu/vishnu/)






# Au+Au at 200 A GeV, $b=2.2$ fm

$t = 0.1$  fm/c



**Au + Au  $\sqrt{s_{NN}} = 200$  GeV**  
 **$b = 2.2$  fm – Section view**



-  Baryons (394)
-  Antibaryons ( 0)
-  Mesons ( 0)
-  Quarks ( 0)
-  Gluons ( 0)



# Au+Au at 200 A GeV, $b=2.2$ fm

$t = 1.63549$  fm/c



**Au + Au  $\sqrt{s_{NN}} = 200$  GeV**  
 **$b = 2.2$  fm – Section view**



-  Baryons (394)
-  Antibaryons ( 0)
-  Mesons (1598)
-  Quarks (4383)
-  Gluons (344)

# Au+Au at 200 A GeV, $b=2.2$ fm

$t = 2.06543$  fm/c



**Au + Au  $\sqrt{s_{NN}} = 200$  GeV**  
 **$b = 2.2$  fm – Section view**



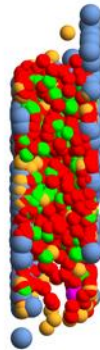
-  Baryons (396)
-  Antibaryons ( 2)
-  Mesons (1136)
-  Quarks (5066)
-  Gluons (516)

# Au+Au at 200 A GeV, b=2.2 fm

t = 3.20258 fm/c



**Au + Au  $\sqrt{s_{NN}} = 200$  GeV**  
**b = 2.2 fm – Section view**



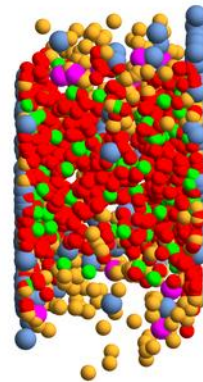
- Baryons (413)
- Antibaryons ( 13)
- Mesons (1080)
- Quarks (4708)
- Gluons (761)


# Au+Au at 200 A GeV, b=2.2 fm

t = 5.56921 fm/c



**Au + Au  $\sqrt{s_{NN}} = 200$  GeV**  
**b = 2.2 fm – Section view**



-  Baryons (472)
-  Antibaryons ( 70)
-  Mesons (1724)
-  Quarks (3843)
-  Gluons (652)

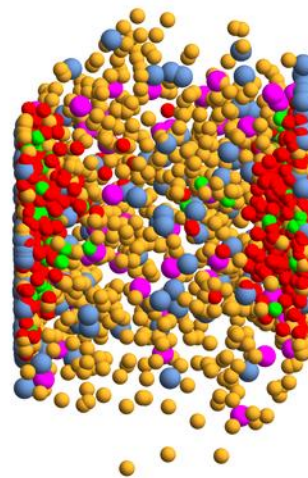


# Au+Au at 200 A GeV, $b=2.2$ fm

$t = 8.06922$  fm/c



**Au + Au  $\sqrt{s_{NN}} = 200$  GeV**  
 **$b = 2.2$  fm – Section view**



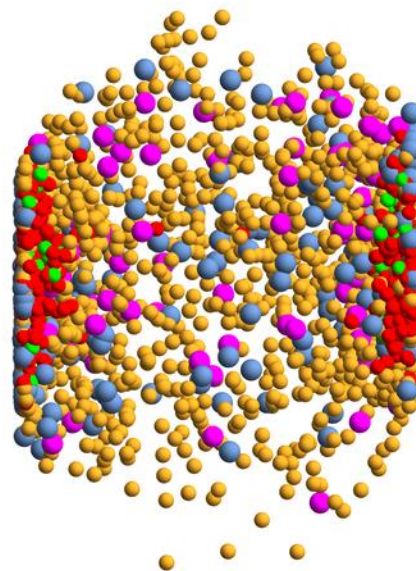
-  Baryons (559)
-  Antibaryons (139)
-  Mesons (2686)
-  Quarks (2628)
-  Gluons (442)

# Au+Au at 200 A GeV, $b=2.2$ fm

$t = 10.5692$  fm/c



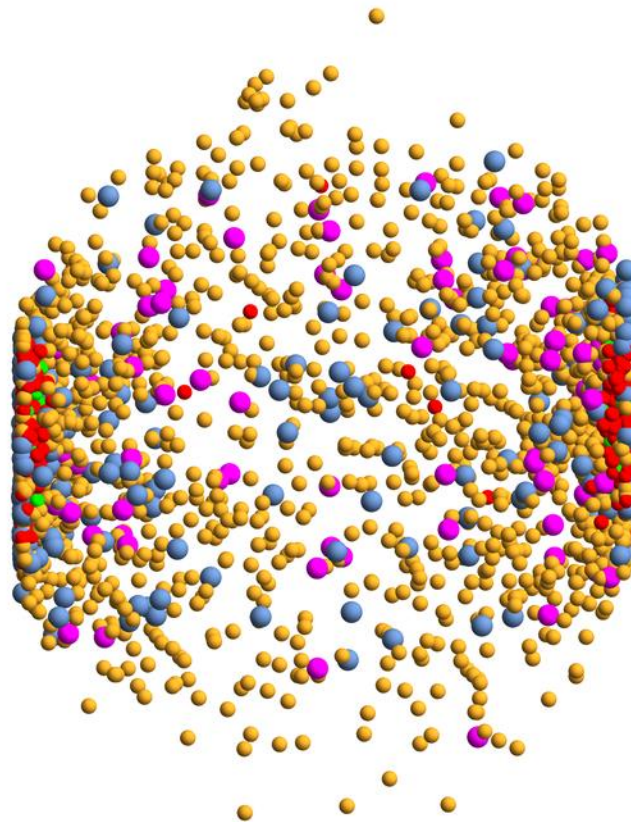
**Au + Au  $\sqrt{s_{NN}} = 200$  GeV**  
 **$b = 2.2$  fm – Section view**



-  Baryons (604)
-  Antibaryons (187)
-  Mesons (3169)
-  Quarks (2076)
-  Gluons (319)

# Au+Au at 200 A GeV, $b=2.2$ fm

$t = 15.5692$  fm/c

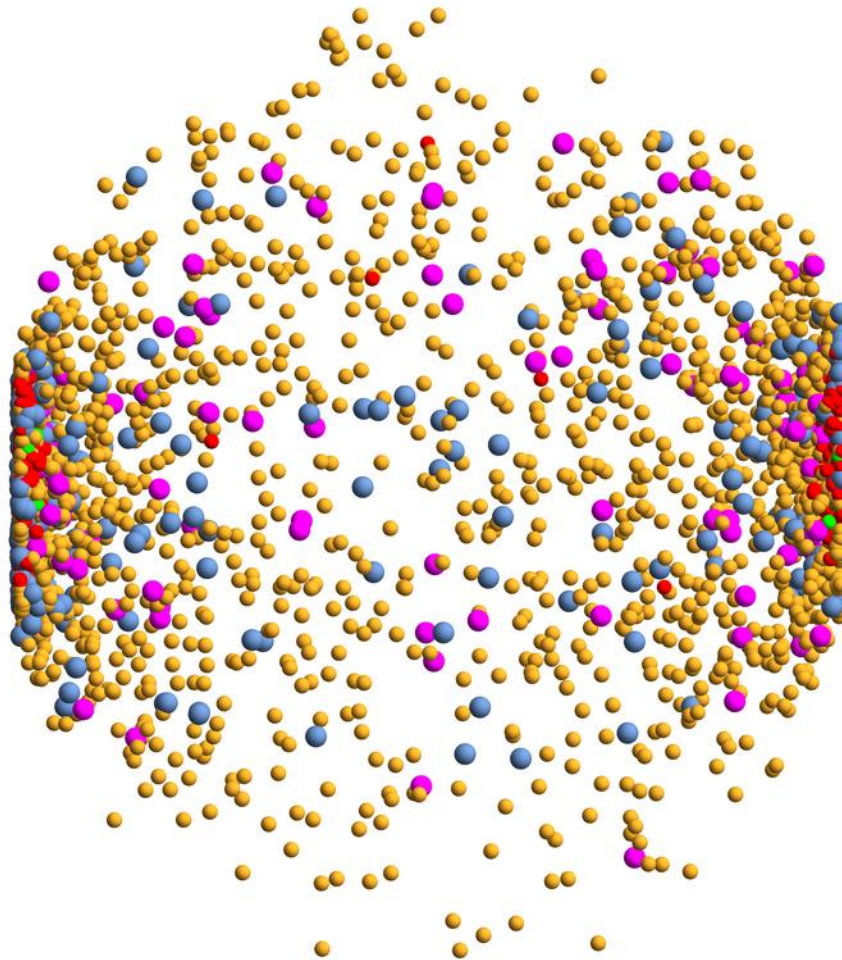


**Au + Au  $\sqrt{s_{NN}} = 200$  GeV**  
 **$b = 2.2$  fm – Section view**


-  Baryons (662)
-  Antibaryons (229)
-  Mesons (3661)
-  Quarks (1499)
-  Gluons (175)

# Au+Au at 200 A GeV, $b=2.2$ fm

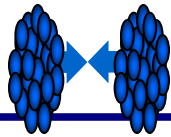
$t = 20.5692$  fm/c



**Au + Au  $\sqrt{s_{NN}} = 200$  GeV**  
 **$b = 2.2$  fm – Section view**

-  Baryons (692)
-  Antibaryons (266)
-  Mesons (4022)
-  Quarks (1184)
-  Gluons ( 90)

# Dynamical models for HIC



## Macroscopic

## Microscopic

### hydro-models:

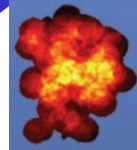
- description of QGP and hadronic phase by hydrodynamical equations for fluid
- **assumption of local equilibrium**
- EoS with phase transition from QGP to HG
- initial conditions (e-b-e, fluctuating)

### ideal

(Jyväskylä, SHASTA, TAMU, ...)

### viscous

(Romachkka, (2+1)D VISH2+1, (3+1)D MUSIC, ...)



### fireball models:

- no explicit dynamics: parametrized time evolution (TAMU)

### ,Hybrid'

- QGP phase: hydro with QGP EoS
- hadronic freeze-out: after burner - hadron-string transport model
- (,hybrid'-UrQMD, EPOS, ...)

Non-equilibrium microscopic transport models – based on many-body theory

### Hadron-string models

(UrQMD, IQMD, HSD, QGSM, SMASH ...)

### Partonic cascades pQCD based

(Duke, BAMPS, ...)

### Parton-hadron models:

- QGP: pQCD based cascade
- massless q, g
- hadronization: coalescence (AMPT, HIJING)

- QGP: IQCD EoS
- massive quasi-particles (q and g with spectral functions) in self-generated mean-field
- dynamical hadronization
- HG: off-shell dynamics (applicable for strongly interacting systems)



# References

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**Eds: B. L. Friman, C. Höhne, J. E. Knoll, S. K. K. Leupold, J. Randrup, R. Rapp, and P. Senger;**

**Springer, Series: 'Lecture Notes in Physics', Vol. 815 (2010), 960 p.;**  
**ISBN: 978-3-642-13292-6**