

Lecture

Introduction:

„Dynamical models for relativistic heavy-ion collisions“

Lectures:

Thursday, 11:15-12:45

Lecturers: Elena Bratkovskaya, Igor Mishustin

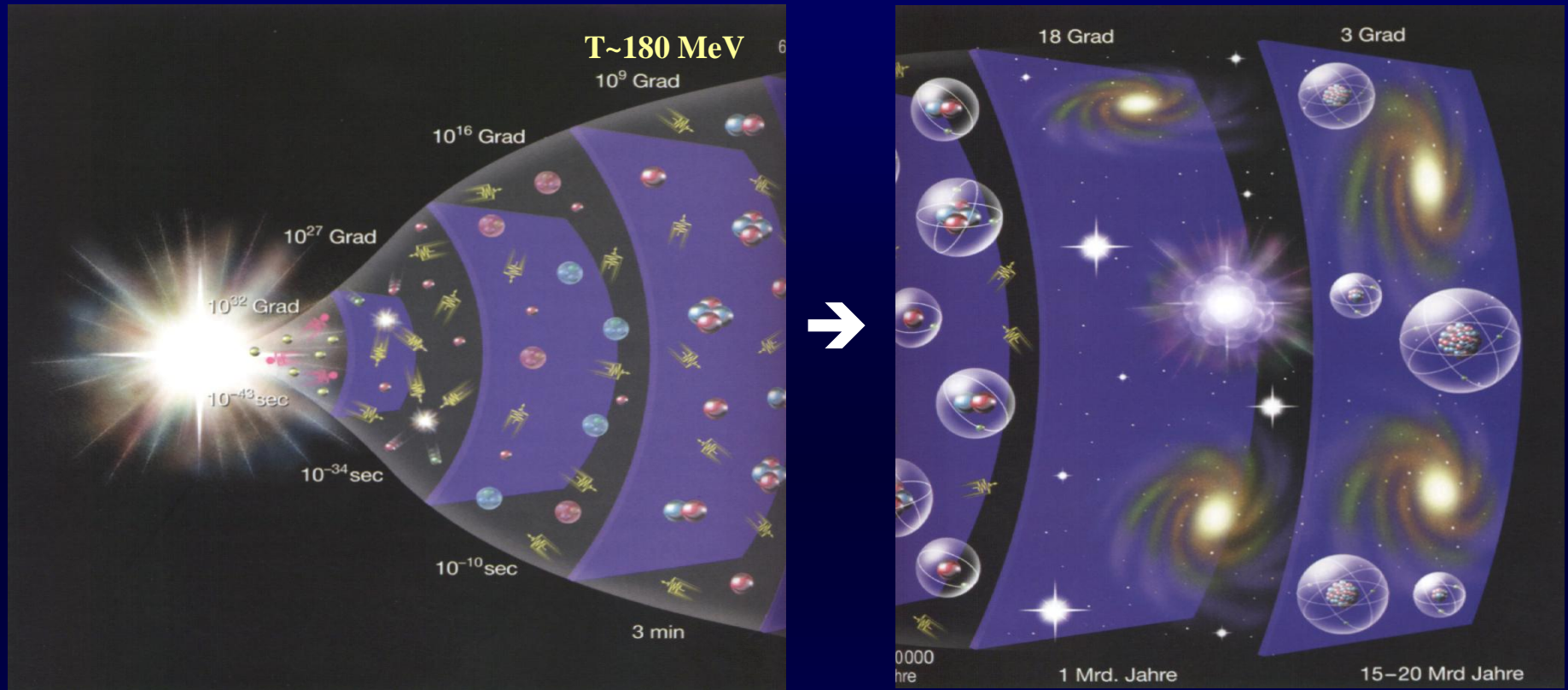
e-mail: Elena.Bratkovskaya@itp.uni-frankfurt.de

or E.Bratkovskaya@gsi.de

e-mail: mishustin@fias.uni-frankfurt.de

http://theory.gsi.de/~ebratkov/LecturesSS2025/Lec_SS2025.html

From Big Bang to Formation of the Universe



time

10^{-3} sec

quarks
gluons
photons

3 min

nucleons
deuterons
 α -particles

300000 years

atoms

15 Mrd years

our Universe

← Can we go back in time?



... back in time

‘Re-create’ the **Big Bang**
conditions:

matter at high temperature
and pressure

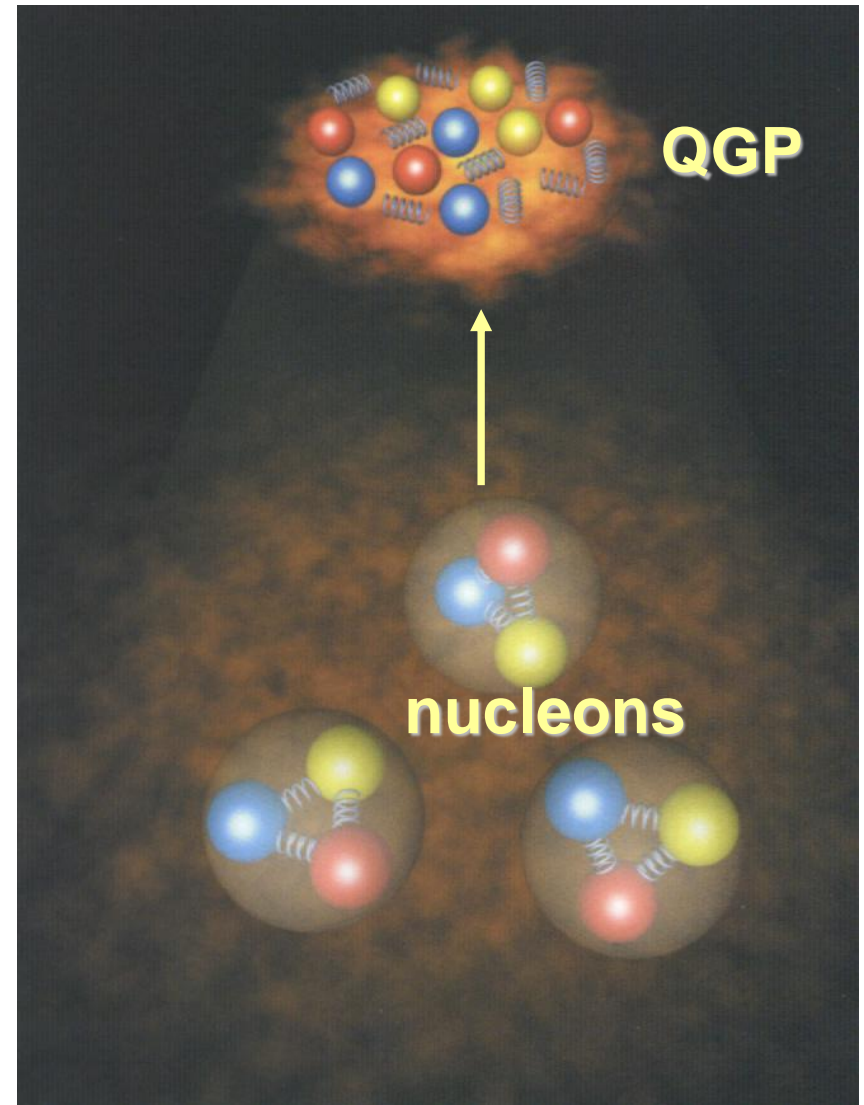
such that

nucleons/mesons decouple
to quarks and gluons --

Quark-Gluon-Plasma

‘Little Bangs’ in the
Laboratory :

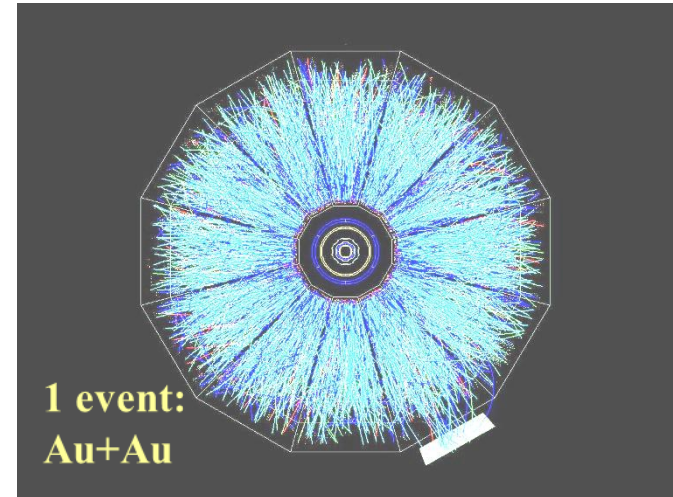
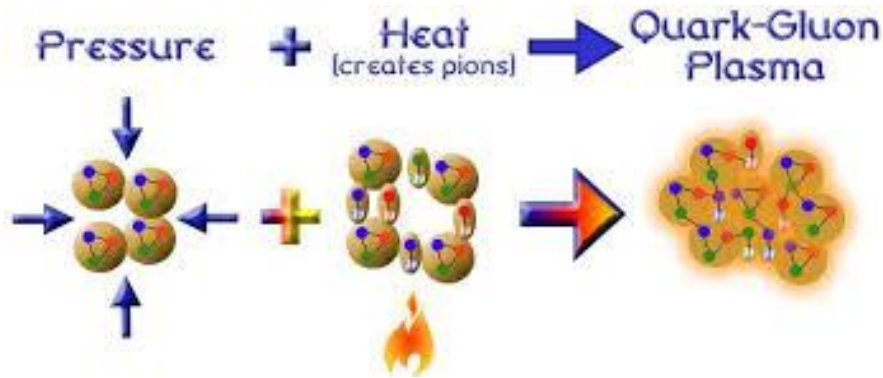
Heavy-ion collisions at
ultrarelativistic energies



Heavy-ion collisions

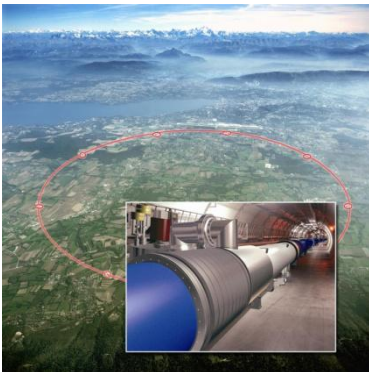
Heavy-ion collision experiment

→ ,re-creation' of the Big Bang conditions in laboratory:
matter at high **pressure** and **temperature**

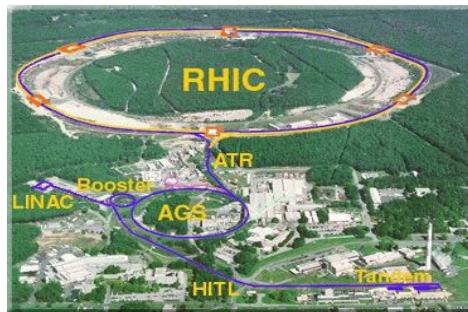


Heavy-ion accelerators:

Large Hadron Collider -
LHC (CERN):
Pb+Pb up to 574 A TeV



Relativistic-Heavy-Ion-Collider -
RHIC (Brookhaven):
Au+Au up to 21.3 A TeV



Facility for Antiproton and Ion
Research – FAIR (Darmstadt)
(Under construction)
Au+Au up to 10 (30) A GeV



Nuclotron-based Ion Collider
fAcility – NICA (Dubna)
(Under construction)
Au+Au up to 70 A GeV

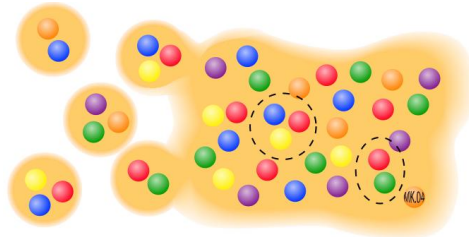


The QGP in Lattice QCD

Quantum Chromo Dynamics :

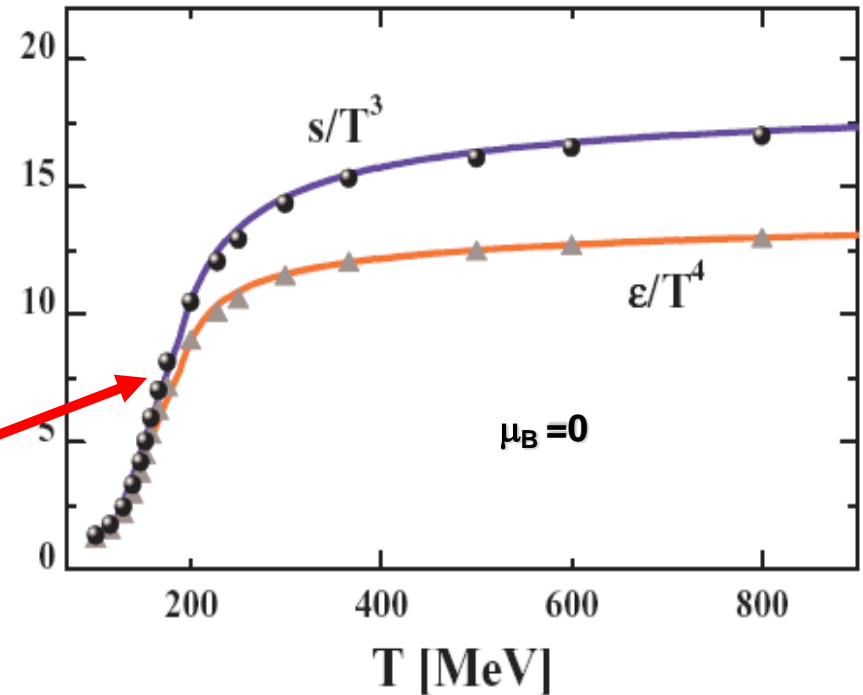
predicts strong increase of the **energy density e** at critical temperature **$T_c \sim 160$ MeV**

\Rightarrow Possible **phase transition** from hadronic to **partonic matter** (quarks, gluons) at critical energy density **$\epsilon_c \sim 0.5$ GeV/fm³**

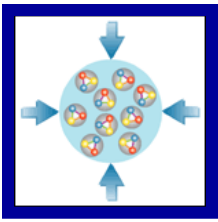


Lattice QCD:

energy density versus temperature

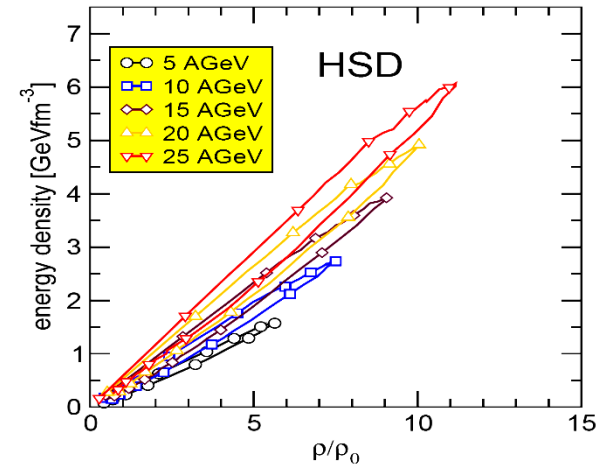
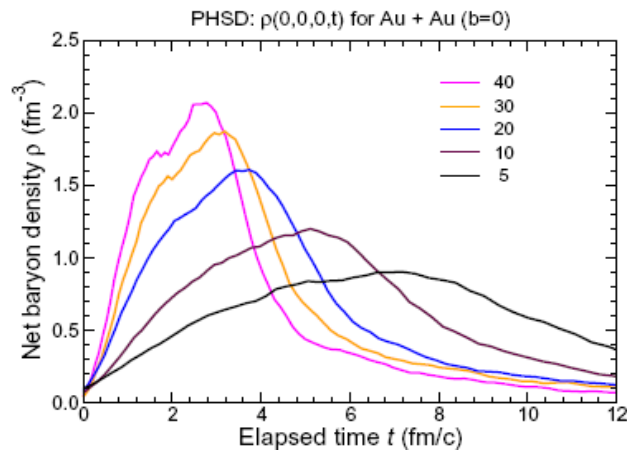
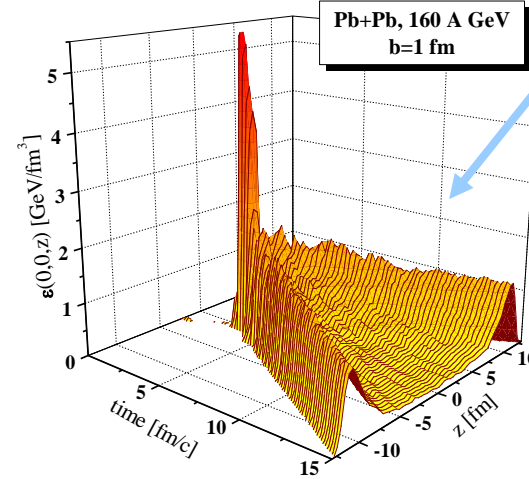
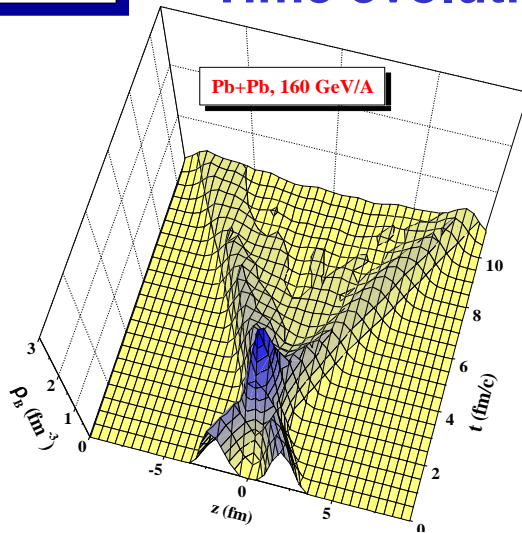


Critical conditions - **$\epsilon_c \sim 0.5$ GeV/fm³** , **$T_c \sim 160$ MeV** - can be reached in **heavy-ion experiments** at bombarding energies **> 5 GeV/A**



Dense and hot matter – average quantities

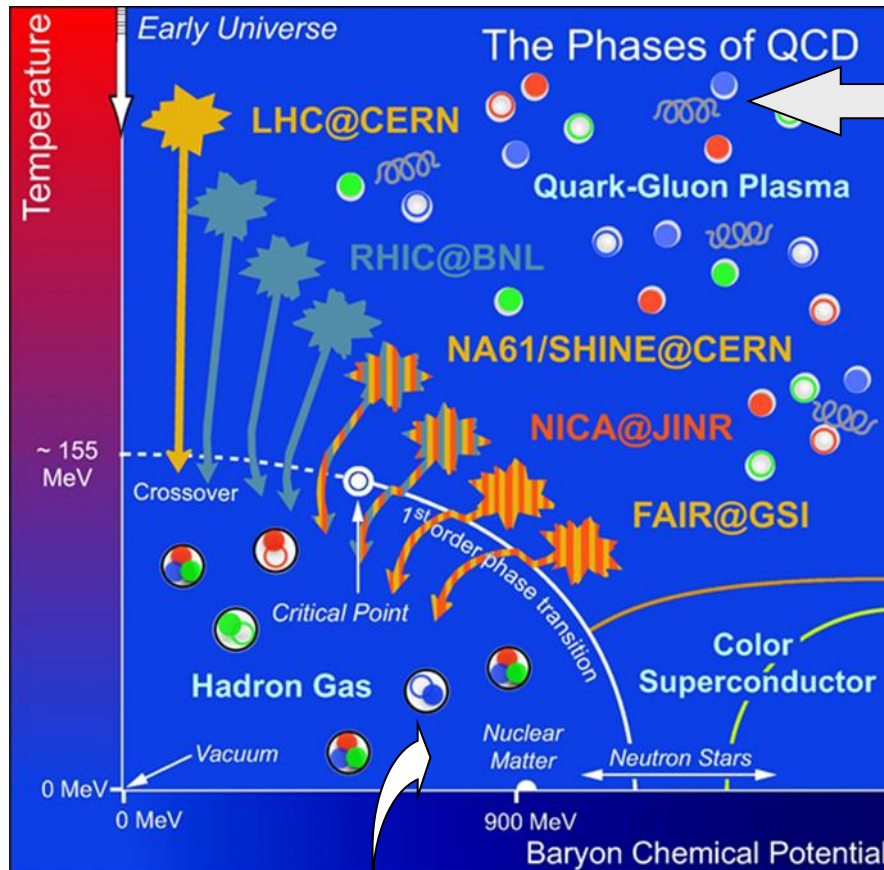
Time evolution of the baryon density and energy density



huge energy and baryon densities are reached ($\epsilon > \epsilon_{\text{crit}} = 0.5 \text{ GeV/fm}^3$)
at FAIR/NICA energies ($> 5 \text{ A GeV}$)

The ,holy grail' of heavy-ion physics:

The phase diagram of QCD



- Search for the **critical point**



- Study of the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma**

- Search for signatures of **chiral symmetry restoration**

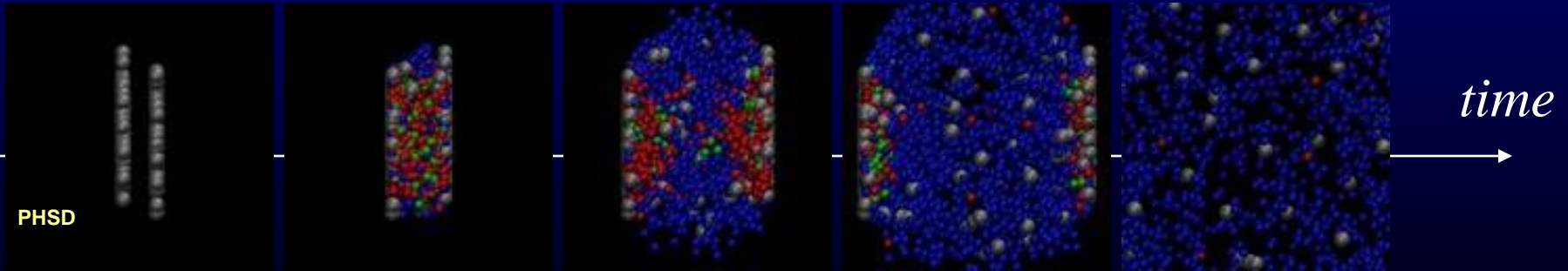
- Search for the **critical point**

- Study of the **in-medium** properties of hadrons at high baryon density and temperature

,Little Bangs' in the Laboratory

Initial State

Hadronization



Au+Au

Quark-Gluon-Plasma ?

hadron
degrees
of freedom



quarks and gluons



hadron
degrees
of freedom

How can we prove that an equilibrium QGP has been created in central heavy-ion collisions ?!

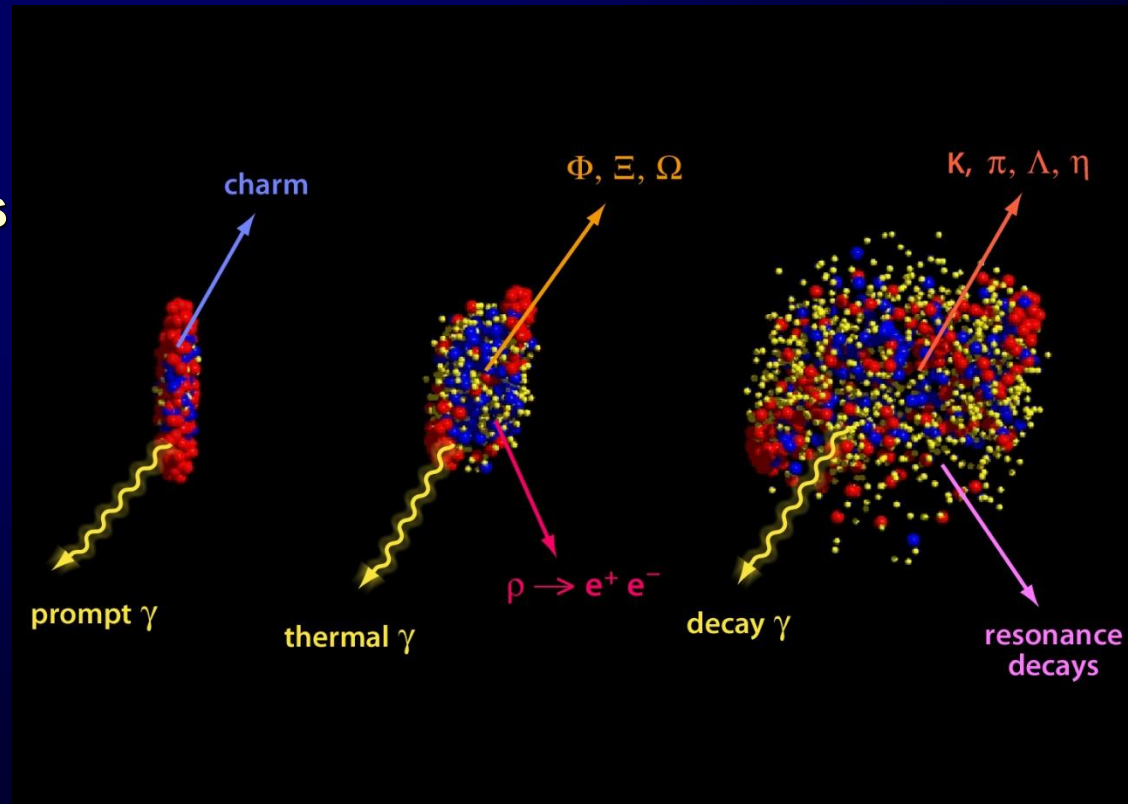
Signals of the phase transition:

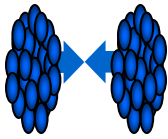
- Multi-strange particle enhancement in A+A
- Charm suppression
- Collective flow (v_1, v_2)
- Thermal dileptons
- Jet quenching and angular correlations
- High p_T suppression of hadrons
- Nonstatistical event by event fluctuations and correlations
- ...

Experiment: measures
final hadrons and leptons

How to learn about
physics from data?

Compare with theory!





Basic models for heavy-ion collisions

- Statistical models:

basic assumption: system is described by a (grand) canonical ensemble of non-interacting fermions and bosons in **thermal and chemical equilibrium**
= **thermal hadron gas at freeze-out** with common T and μ_B

[- : no dynamical information]

- Hydrodynamical models:

basic assumption: conservation laws + equation of state (EoS);
assumption of **local thermal and chemical equilibrium**

- Interactions are 'hidden' in properties of the **fluid** described by **transport coefficients** (shear and bulk viscosity η , ζ , ..), which is '**input**' for the hydro models

[- : simplified dynamics]

- Microscopic transport models:

based on transport theory of relativistic quantum many-body systems

- **Explicitly account for the interactions of all degrees of freedom** (hadrons and partons)
in terms of cross sections and potentials

- Provide a unique dynamical description of **strongly interaction matter**

in- and out-of equilibrium:

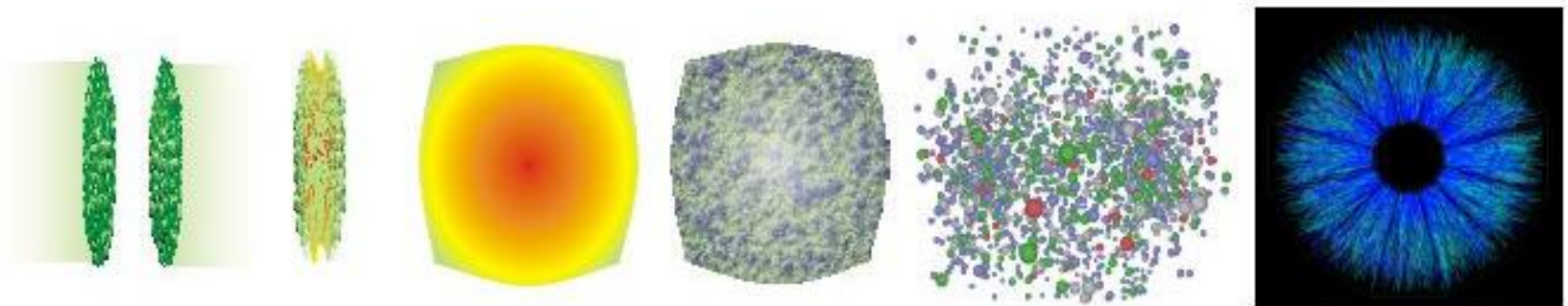
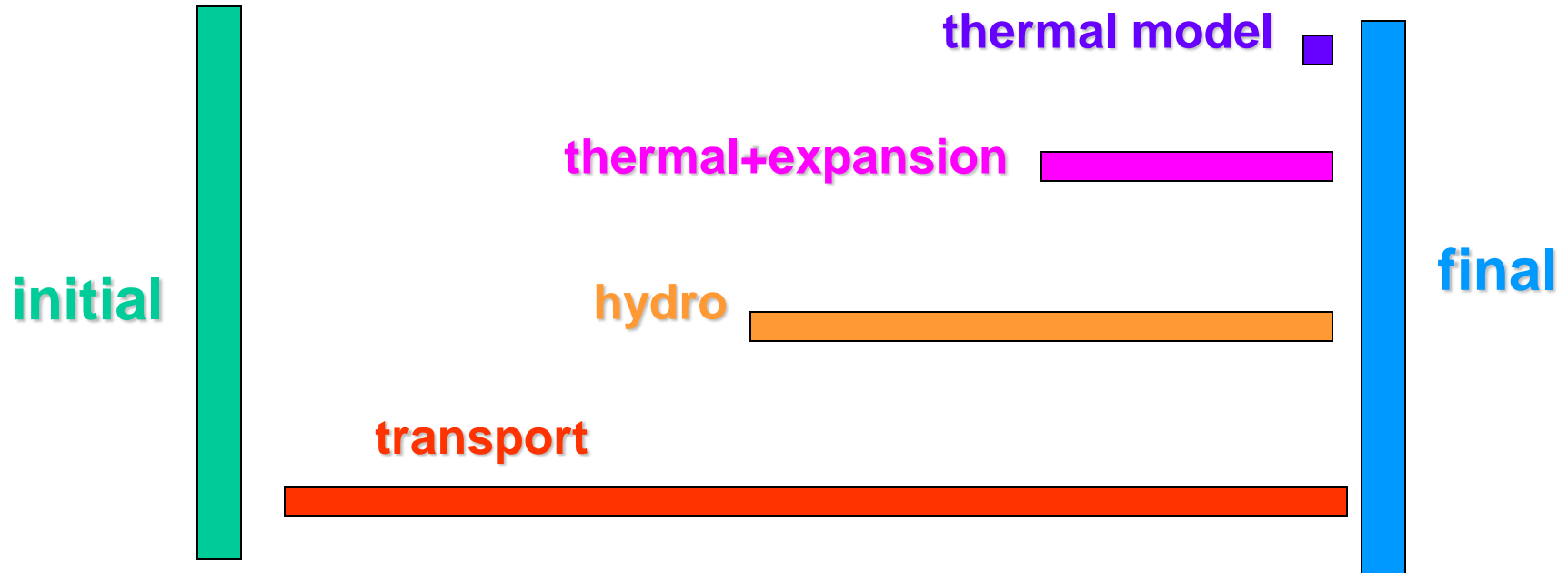
- **In-equilibrium:** transport coefficients are calculated in a box – controlled by IQCD

- **Nonequilibrium dynamics** – controlled by HIC

Actual solutions: Monte Carlo simulations

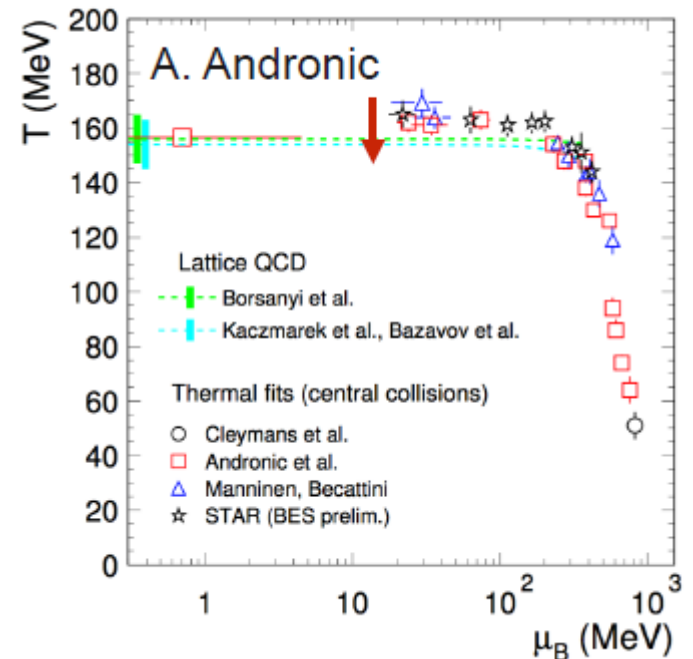
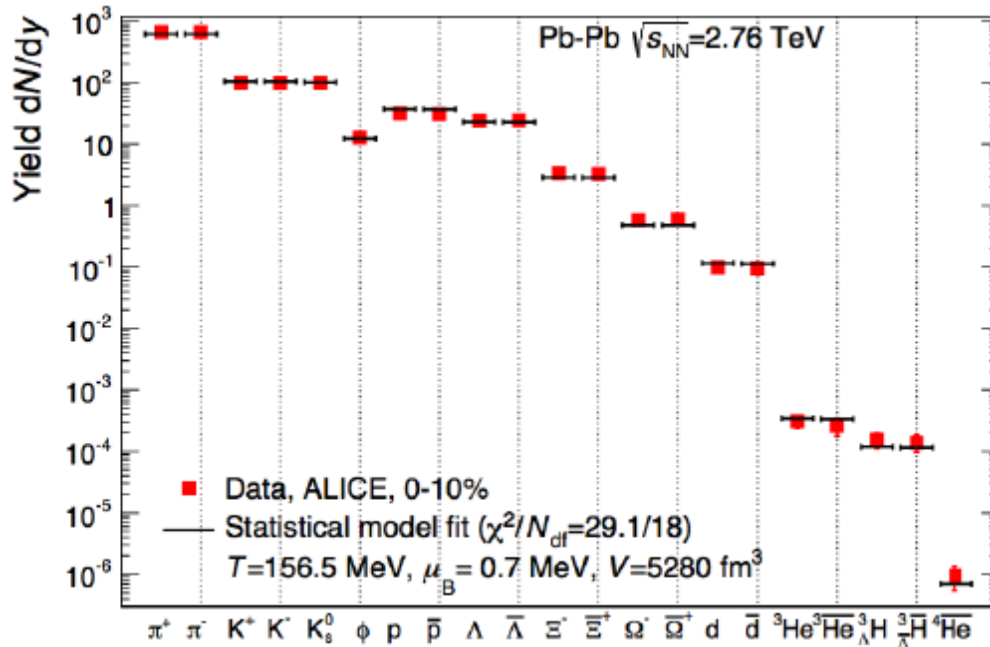
[+ : full dynamics | - : very complicated]

Models of heavy-ion collisions



Results from statistical models for HIC

J. Stachel et al., J.Phys. Conf. Ser. 509 (2014) 012019



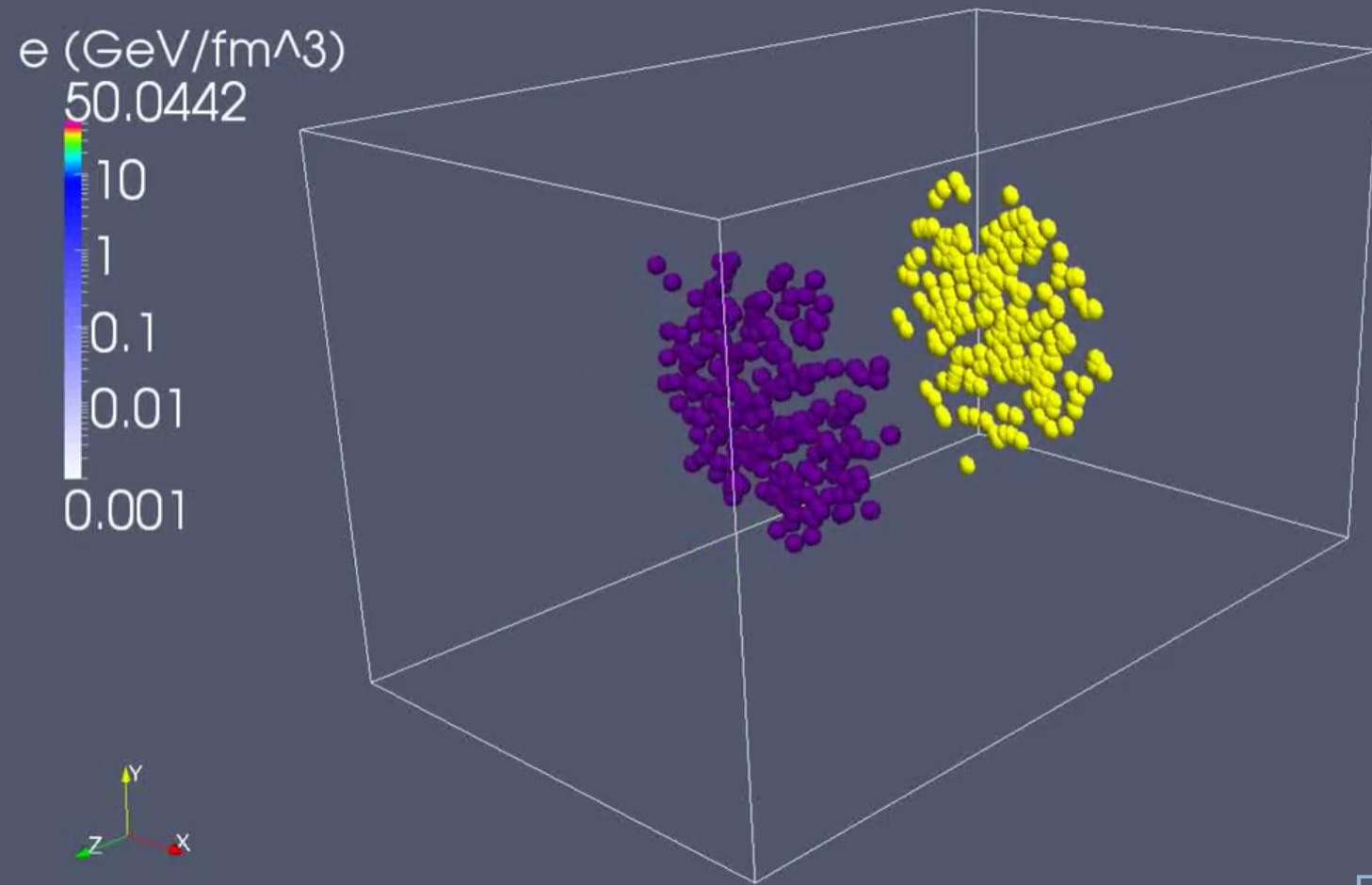
Good description of the hadron abundances by the **thermal hadron gas model** →
The hadron abundances are in rough agreement with a **thermally equilibrated system** !

→ **Partial thermal and chemical equilibration is approximately reached in central heavy-ion collisions at relativistic energies!**

! Statistical models do not provide an answer to the **origin of thermalization**.
HIC dynamics and the approach to thermal equilibrium is driven by the interactions !

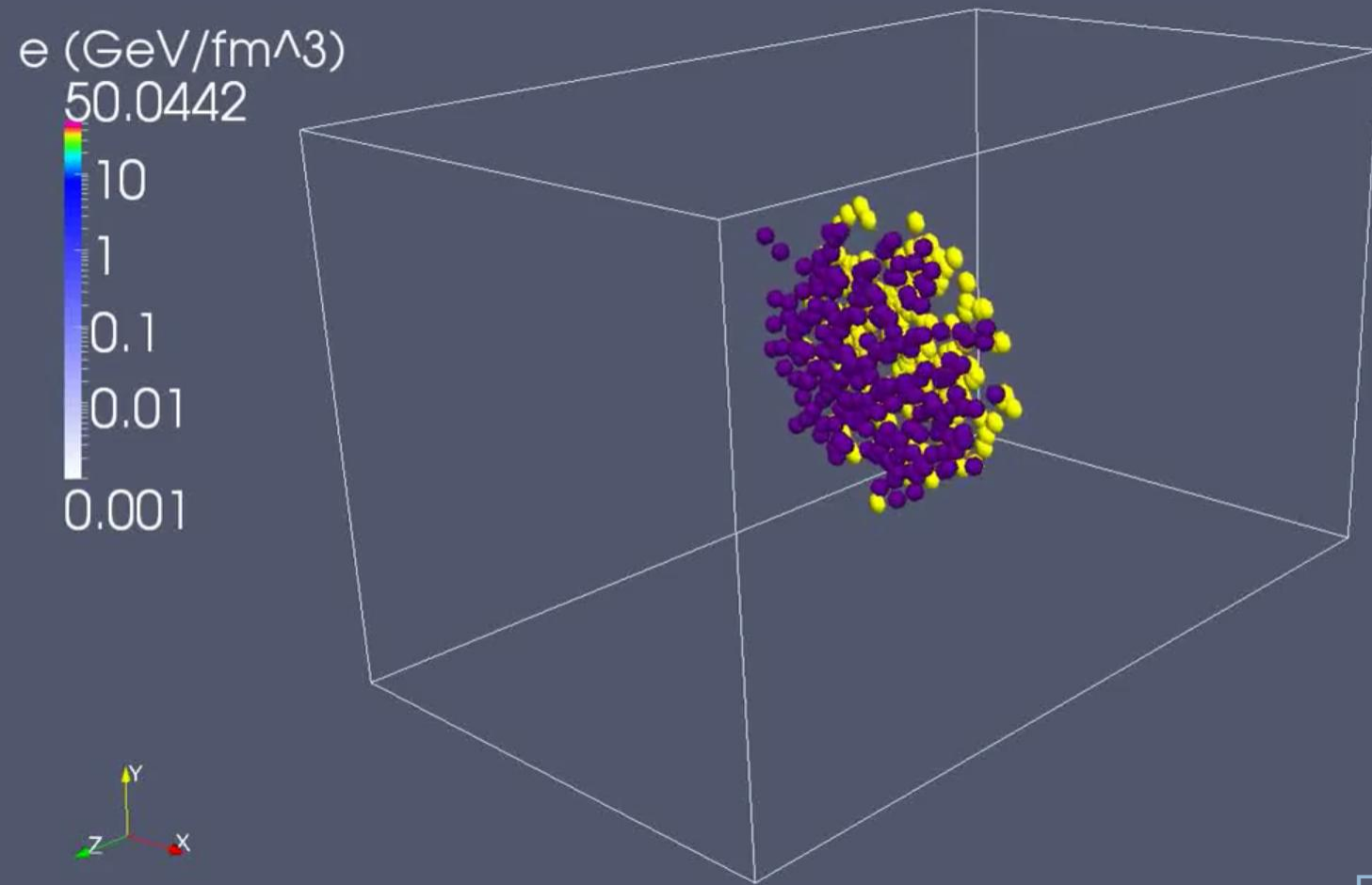
→ **dynamical models of HIC**

Stages of a collision in VISHNU



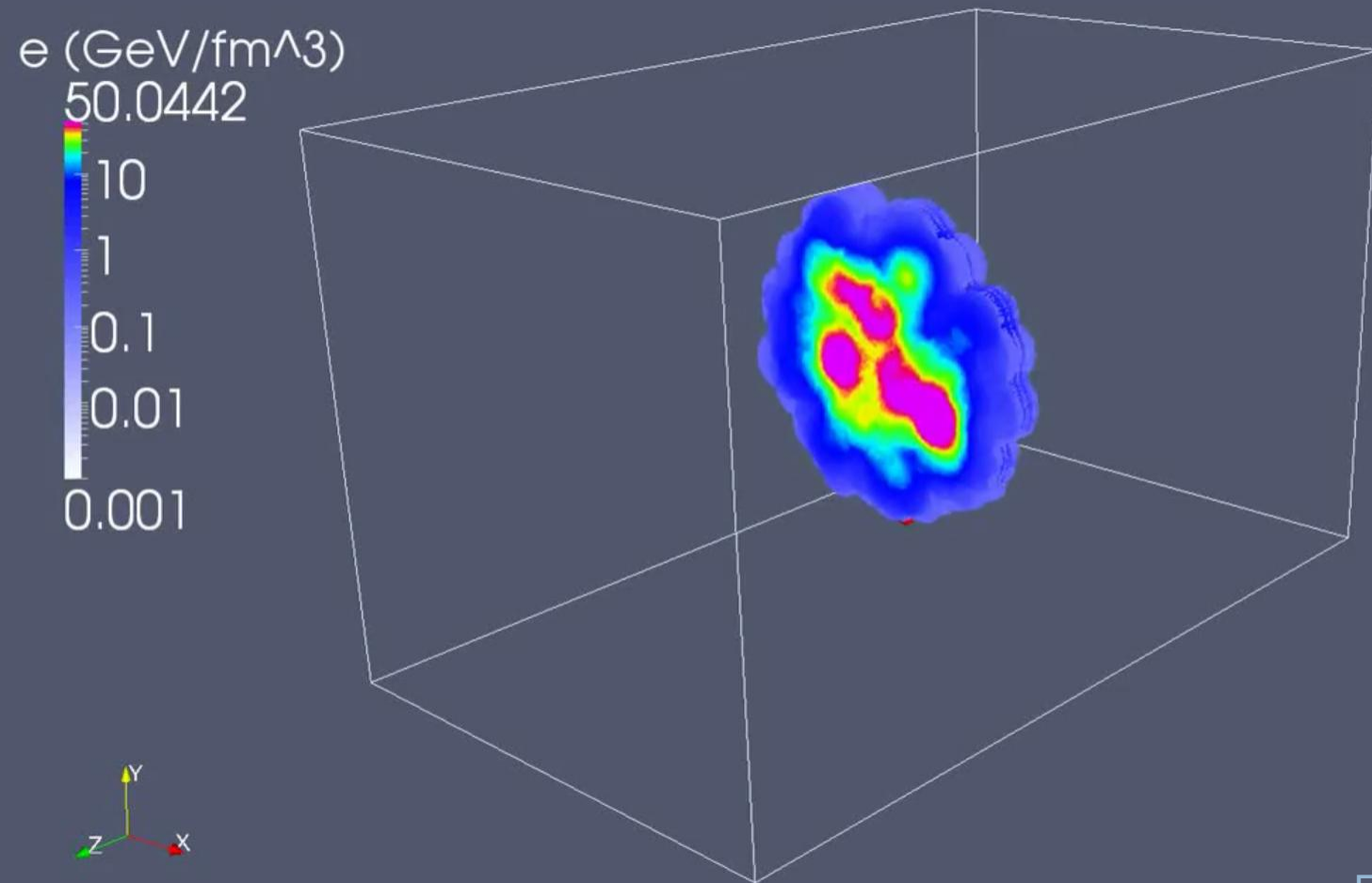
From u.osu.edu/vishnu/

Stages of a collision in VISHNU



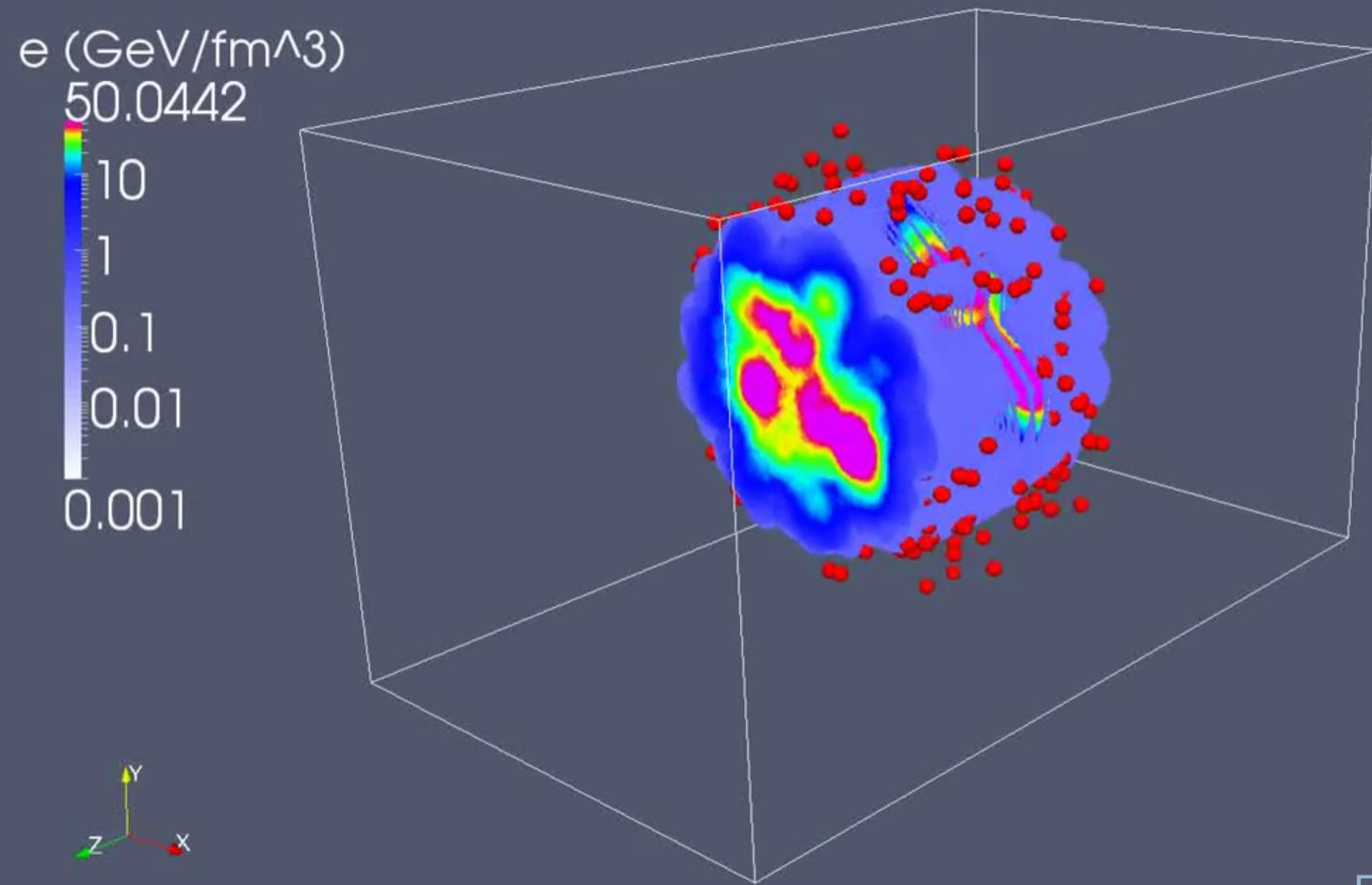
From u.osu.edu/vishnu/

Stages of a collision in VISHNU



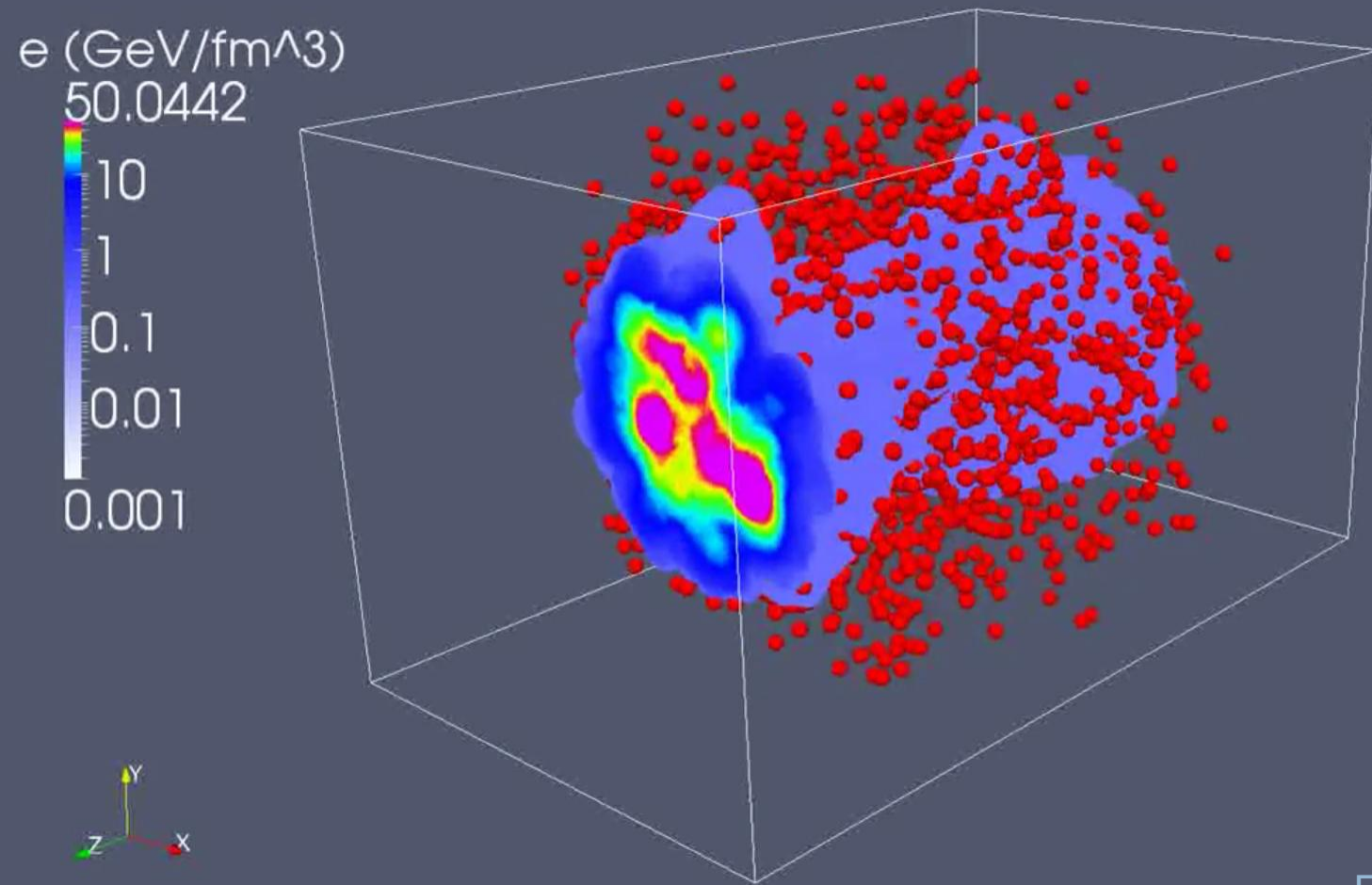
From u.osu.edu/vishnu/

Stages of a collision in VISHNU



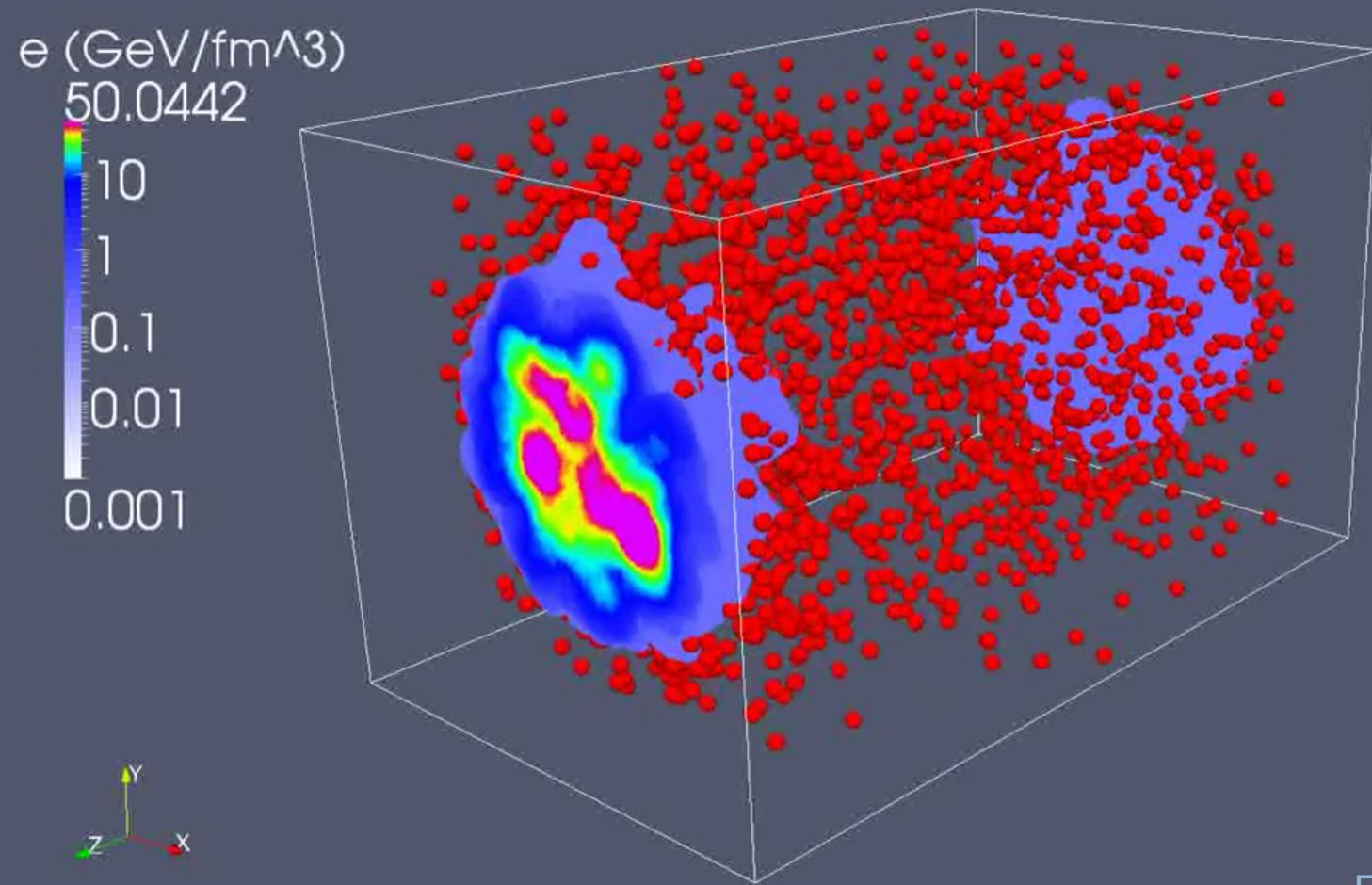
From u.osu.edu/vishnu/

Stages of a collision in VISHNU



From u.osu.edu/vishnu/

Stages of a collision in VISHNU



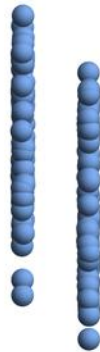
From u.osu.edu/vishnu/






Au+Au at 200 A GeV, $b=2.2$ fm

$t = 0.1$ fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV
 $b = 2.2$ fm – Section view



-  Baryons (394)
-  Antibaryons (0)
-  Mesons (0)
-  Quarks (0)
-  Gluons (0)






Au+Au at 200 A GeV, $b=2.2$ fm

$t = 1.63549$ fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV
 $b = 2.2$ fm – Section view



-  Baryons (394)
-  Antibaryons (0)
-  Mesons (1598)
-  Quarks (4383)
-  Gluons (344)


Au+Au at 200 A GeV, $b=2.2$ fm

$t = 2.06543$ fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV
 $b = 2.2$ fm – Section view



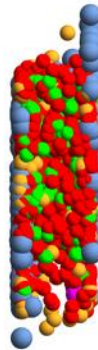
-  Baryons (396)
-  Antibaryons (2)
-  Mesons (1136)
-  Quarks (5066)
-  Gluons (516)

Au+Au at 200 A GeV, $b=2.2$ fm

$t = 3.20258$ fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV
 $b = 2.2$ fm – Section view



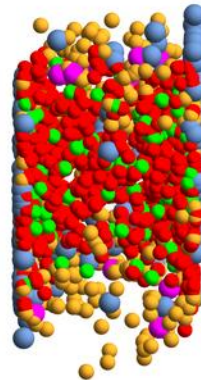
-  Baryons (413)
-  Antibaryons (13)
-  Mesons (1080)
-  Quarks (4708)
-  Gluons (761)


Au+Au at 200 A GeV, $b=2.2$ fm

$t = 5.56921$ fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV
 $b = 2.2$ fm – Section view



-  Baryons (472)
-  Antibaryons (70)
-  Mesons (1724)
-  Quarks (3843)
-  Gluons (652)

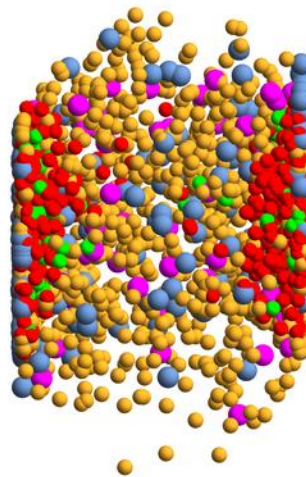
Au+Au at 200 A GeV, $b=2.2$ fm

$t = 8.06922$ fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV

$b = 2.2$ fm – Section view



-  Baryons (559)
-  Antibaryons (139)
-  Mesons (2686)
-  Quarks (2628)
-  Gluons (442)

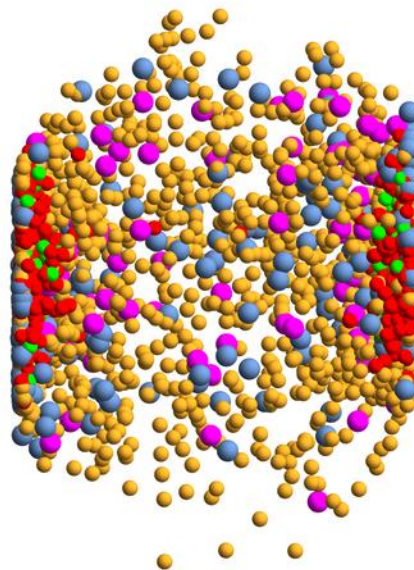
Au+Au at 200 A GeV, $b=2.2$ fm

$t = 10.5692$ fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV

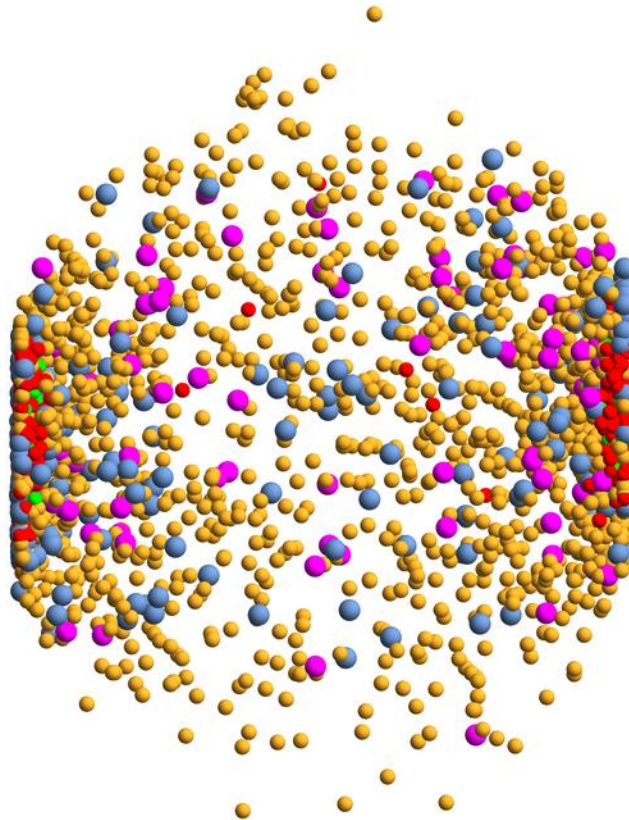
$b = 2.2$ fm – Section view



-  Baryons (604)
-  Antibaryons (187)
-  Mesons (3169)
-  Quarks (2076)
-  Gluons (319)

Au+Au at 200 A GeV, $b=2.2$ fm

$t = 15.5692$ fm/c



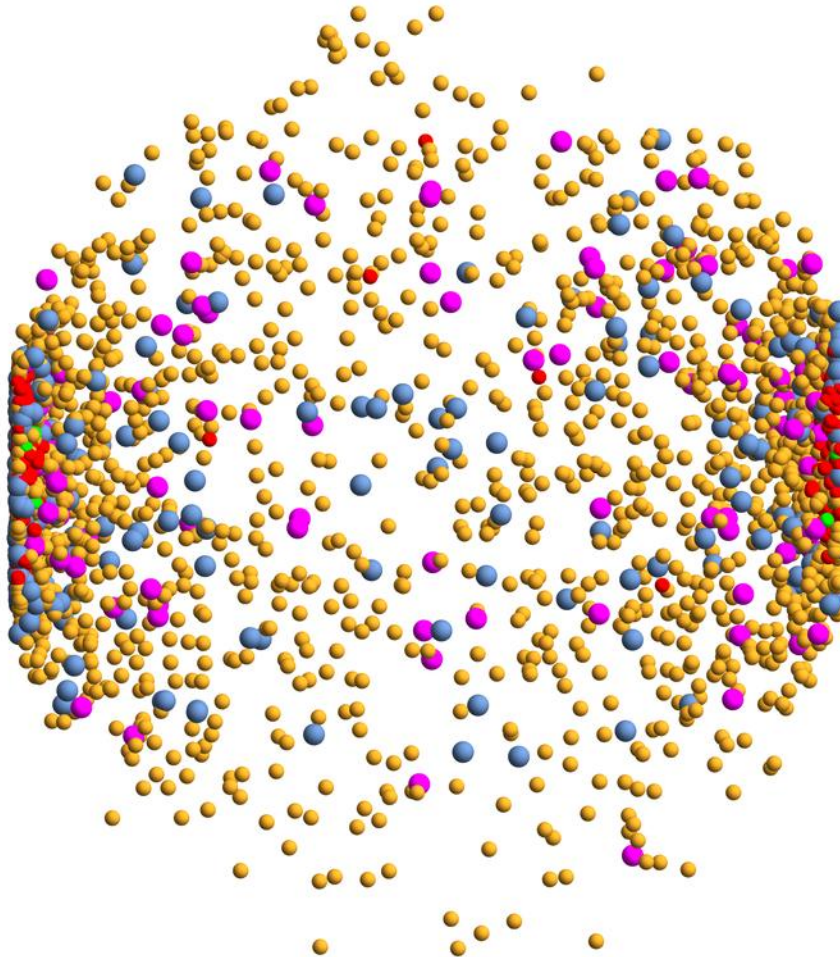
Au + Au $\sqrt{s_{NN}} = 200$ GeV

$b = 2.2$ fm – Section view

-  Baryons (662)
-  Antibaryons (229)
-  Mesons (3661)
-  Quarks (1499)
-  Gluons (175)


Au+Au at 200 A GeV, $b=2.2$ fm

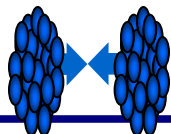
$t = 20.5692$ fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV

$b = 2.2$ fm – Section view

-  Baryons (692)
-  Antibaryons (266)
-  Mesons (4022)
-  Quarks (1184)
-  Gluons (90)



Dynamical models for HIC

Macroscopic

hydro-models:

- description of QGP and hadronic phase by hydrodynamical equations for fluid
- **assumption of local equilibrium**
- EoS with phase transition from QGP to HG
- initial conditions (e-b-e, fluctuating)

ideal

(Jyväskylä, SHASTA, TAMU, ...)

viscous

(Romachkko, (2+1)D VISH2+1, (3+1)D MUSIC, ...)

fireball models:

- no explicit dynamics: parametrized time evolution (TAMU)

Hybrid'

QGP phase: hydro with QGP EoS

- hadronic freeze-out: after burner - hadron-string transport model

(,hybrid'-UrQMD, EPOS, ...)

Microscopic

Non-equilibrium microscopic transport models – based on many-body theory

Hadron-string models

(UrQMD, IQMD, HSD, QGSM, SMASH ...)

Partonic cascades pQCD based

(Duke, BAMPS, ...)

Parton-hadron models:

- QGP: **pQCD** based cascade
- massless q, g
- hadronization: coalescence (AMPT, HIJING)

- QGP: **IQCD** EoS
- **massive quasi-particles** (q and g with spectral functions) in self-generated mean-field
- dynamical hadronization
- HG: off-shell dynamics (applicable for strongly interacting systems)



References

Eds: B. L. Friman, C. Höhne, J. E. Knoll, S. K. K. Leupold, J. Randrup, R. Rapp, and P. Senger;

Springer, Series: ‘Lecture Notes in Physics’, Vol. 815 (2010), 960 p.;
ISBN: 978-3-642-13292-6