

# Lecture

# The Quark model

# Quark model

The **quark model** is a classification scheme for hadrons in terms of their **valence quarks** — the quarks and antiquarks which give rise to the quantum numbers of the hadrons.

The quark model in its modern form was developed by **Murray Gell-Mann** - american physicist who received the **1969 Nobel Prize** in physics for his work on the theory of elementary particles.

\* QM - independently proposed by **George Zweig**

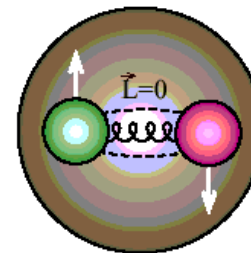


Murray Gell-Mann  
1929-2019

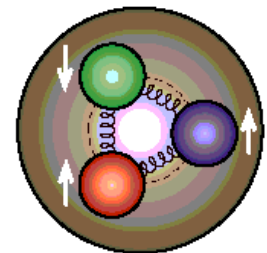
■ **Hadrons are not ,fundamental‘**, but they are built from **,valence quarks‘**, i.e. quarks and antiquarks, which give the quantum numbers of the hadrons

$$| \text{Baryon} \rangle = | qqq \rangle \quad | \text{Meson} \rangle = | q\bar{q} \rangle$$

q= quarks,  $\bar{q}$  – antiquarks



Meson ( $q\bar{q}$ )



Baryon ( $qqq$ )

# Quark quantum numbers

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## The quark quantum numbers:

- **flavor (6):** **u** (up-), **d** (down-), **s** (strange-), **c** (charm-), **t** (top-), **b**(bottom-) quarks  
anti-flavor for anti-quarks  $\bar{q}$ :  $\bar{u}$ ,  $\bar{d}$ ,  $\bar{s}$ ,  $\bar{c}$ ,  $\bar{t}$ ,  $\bar{b}$
- **charge:**  $Q = -1/3, +2/3$  (u: 2/3, d: -1/3, s: -1/3, c: 2/3, t: 2/3, b: -1/3 )
- **baryon number:**  $B=1/3$  - as baryons are made out of three quarks
- **spin:**  $s=1/2$  - quarks are the fermions!
- **strangeness:**  $S_s = -1$ ,  $S_{\bar{s}} = 1$ ,  $S_q = 0$  for  $q = u, d, c, t, b$  (and  $\bar{q}$ )
- **charm:**  $C_c = 1$ ,  $C_{\bar{c}} = -1$ ,  $C_q = 0$  for  $q = u, d, s, t, b$  (and  $\bar{q}$ )
- **bottomness:**  $B_b = -1$ ,  $B_{\bar{b}} = 1$ ,  $B_q = 0$  for  $q = u, d, s, c, t$  (and  $\bar{q}$ )
- **topness:**  $T_t = 1$ ,  $T_{\bar{t}} = -1$ ,  $T_q = 0$  for  $q = u, d, s, c, b$  (and  $\bar{q}$ )

# Quark quantum numbers

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## The quark quantum numbers:

hypercharge:  $Y = B + S + C + B + T$  (1)

(= baryon charge + strangeness + charm + bottomness + topness)

■  $I_3$  (or  $I_z$  or  $T_3$ ) - 3<sup>d</sup> component of isospin

charge (Gell-Mann–Nishijima formula):

$$Q = I_3 + Y/2$$
 (2)

(= 3<sup>d</sup> component of isospin + hypercharge/2)

# Quark quantum numbers

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Property \ Quark	<i>d</i>	<i>u</i>	<i>s</i>	<i>c</i>	<i>b</i>	<i>t</i>
Q – electric charge	$-\frac{1}{3}$	$+\frac{2}{3}$	$-\frac{1}{3}$	$+\frac{2}{3}$	$-\frac{1}{3}$	$+\frac{2}{3}$
I – isospin	$\frac{1}{2}$	$\frac{1}{2}$	0	0	0	0
$I_z$ – isospin <i>z</i> -component	$-\frac{1}{2}$	$+\frac{1}{2}$	0	0	0	0
S – strangeness	0	0	-1	0	0	0
C – charm	0	0	0	+1	0	0
B – bottomness	0	0	0	0	-1	0
T – topness	0	0	0	0	0	+1

# Quark quantum numbers

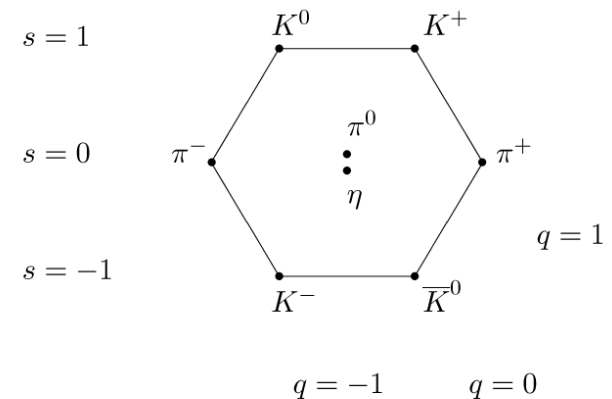
The quark model is the follow-up to the **Eightfold Way** classification scheme (proposed by Murray Gell-Mann and Yuval Ne'eman, 1961 )

The **Eightfold Way** may be understood as a consequence of **flavor symmetries** between various kinds of quarks. Since the strong nuclear force affects quarks the same way regardless of their flavor, replacing one flavor of a quark with another in a hadron should not change its mass very much. Mathematically, this replacement may be described by **elements of the SU(3) group**.

Consider **u, d, s quarks** :

→ then the quarks lie in the fundamental representation, **3** (called the **triplet**) of the flavour group **SU(3) : [3]**

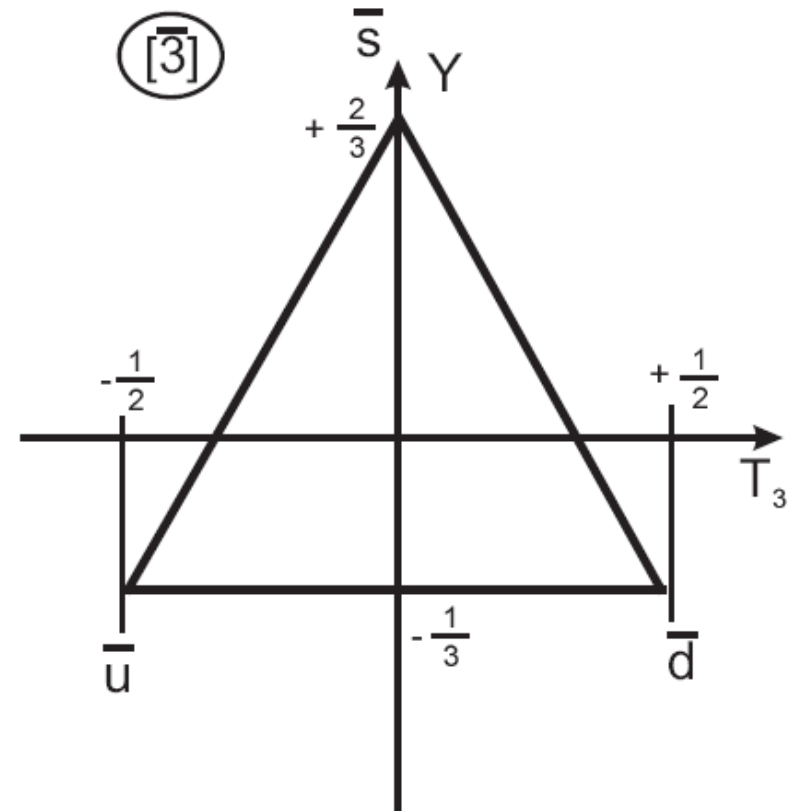
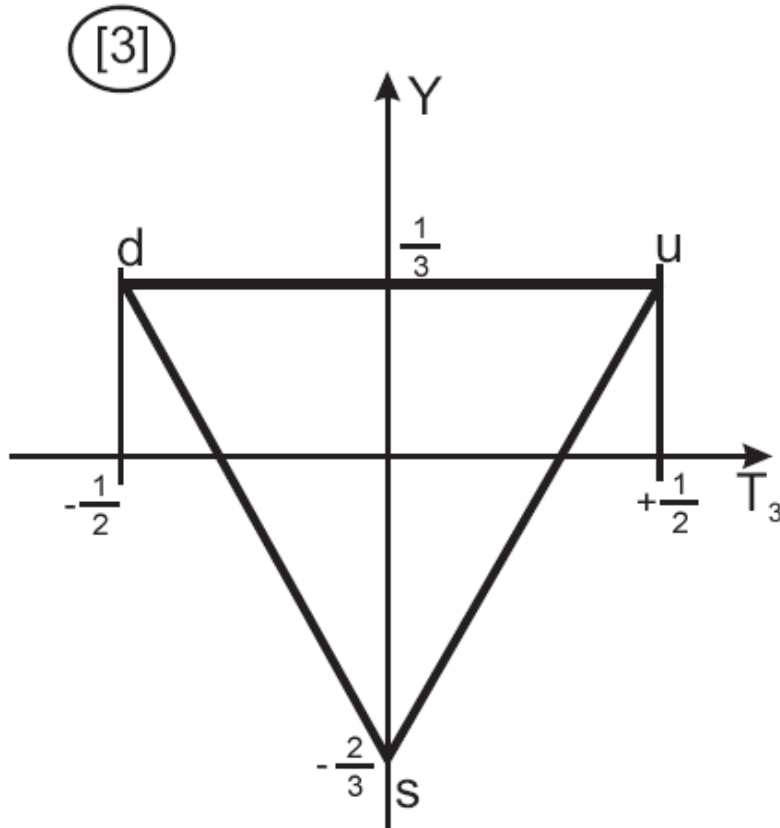
The **antiquarks** lie in the complex conjugate representation **3 - anti-triplet: [ $\bar{3}$ ]**



# Quark quantum numbers

triplet in  $SU(3)_{\text{flavor}}$  group:  $[3]$

anti-triplet in  $SU(3)_{\text{flavor}}$  group:  $[\bar{3}]$



$$Y=2(Q-T_3)$$

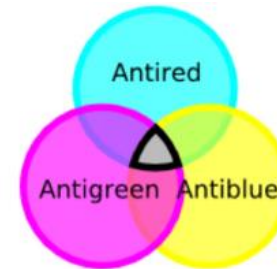
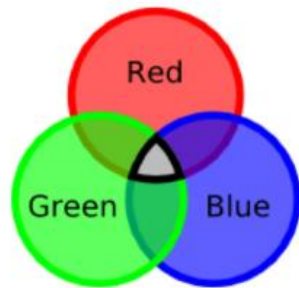
E.g. u-quark:  $Q=+2/3$ ,  $T_3=+1/2 \rightarrow Y=1/3$

# Quark quantum numbers

## The quark quantum numbers:

■ **Collor 3:** red, green and blue → **triplet** in  $SU(3)_{\text{collor}}$  group: [3]

**Anticollor 3:** antired, antigreen and antiblue → **anti-triplet** in  $SU(3)_{\text{collor}}$  group  $[\bar{3}]$



- The quark colors (red, green, blue) combine to be **colorless**
  - The quark anticolors (antired, antigreen, antiblue) also combine to be **colorless**
- All hadrons → color neutral = color singlet in the  $SU(3)_{\text{collor}}$  group**

**History:** The quantum number ,color‘ has been introduced (idea from Greenberg, 1964) to describe the state  $\Delta^{++}(uuu)$  ( $Q=+2, J=3/2$ ), discovered by Fermi in 1951 as  $\pi^+p$  resonance:  $\Delta^{++}(uuu) \rightarrow p( uud ) + \pi^+(\bar{d}u)$   
The state  $\Delta^{++}(u \uparrow u \uparrow u \uparrow)$  with all parallel spins (to achieve  $J=3/2$ ) is forbidden according to the Fermi statistics (without color) !

# Quark quantum numbers

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## The current quark masses:

The **current quark mass** is also called as the mass of the 'naked' (,bare') quark defined as the constituent quark cores (constituent quarks with no covering) of a valence quark

### ■ **current masses** of the quarks

$$m_u = 1.8 - 2.8 \text{ MeV}/c^2$$

$$m_d = 4.3 - 5.2 \text{ MeV}/c^2$$

$$m_s = 92 - 104 \text{ MeV}/c^2$$

$$m_c = 1.3 - 1.5 \text{ GeV}/c^2$$

$$m_b = 4.2 - 4.7 \text{ GeV}/c^2$$

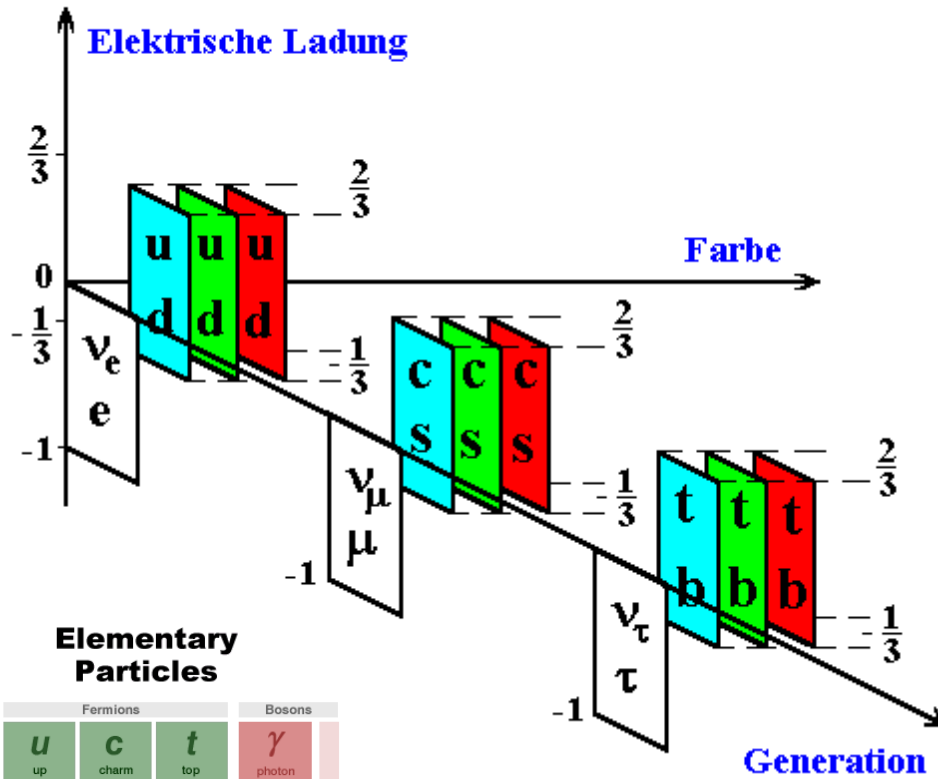
$$m_t = 156 - 176 \text{ GeV}/c^2$$

**Note:** the **constituent quark mass** is the mass of a '**dressed**' current quark, i.e. for quarks surrounded by a cloud of virtual quarks and gluons:

$$M_{u(d)}^* \sim 350 \text{ MeV}/c^2$$

# Building Blocks of Matter

## Fermionen

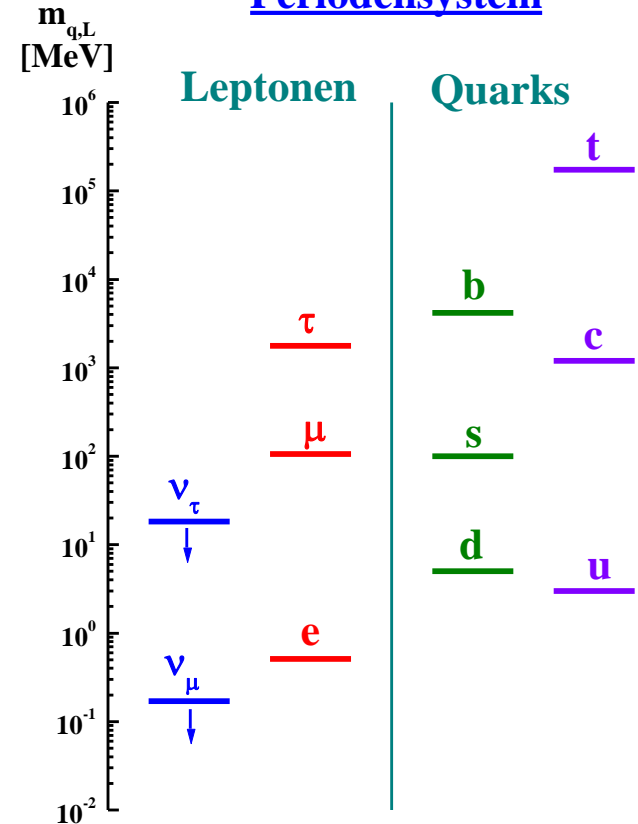


Elementary Particles

	Fermions			Bosons	
Quarks	$u$ up	$c$ charm	$t$ top	$\gamma$ photon	Force carriers
	$d$ down	$s$ strange	$b$ bottom	$Z$ Z boson	
Leptons	$\nu_e$ electron neutrino	$\nu_\mu$ muon neutrino	$\nu_\tau$ tau neutrino	$W$ W boson	
	$e$ electron	$\mu$ muon	$\tau$ tau	$g$ gluon	

I II III  
Three Families of Matter

## Periodensystem



# Hadrons in the Quark model

Gell-Mann (1964): **Hadrons are not ,fundamental‘, but they are built from ,valence quarks‘,**

$$| \text{Baryon} \rangle = | qqq \rangle \quad | \text{Meson} \rangle = | q\bar{q} \rangle \quad (3)$$

Baryon charge:  $B_B = 1$   $B_m = 0$

**Constraints** to build hadrons from quarks:

- strong color interaction (red, green, blue)
- confinement
- quarks must form color-neutral hadrons

■ **State function for baryons (fermions) – antisymmetric** under interchange of two quarks

$$\Psi_A \equiv |qqq\rangle_A = [|color\rangle \otimes |space\rangle \otimes |spin\rangle \otimes |flavor\rangle]_A \quad (4)$$

Since all baryons are color neutral, the color part of  $\Psi_A$  must be antisymmetric, i.e. a  $SU(3)_{\text{color}}$  singlet (c.f.  $\Delta^{++}(u \uparrow u \uparrow u \uparrow)$  state  $J=S=3/2, L=0: [|space\rangle_s \otimes |spin\rangle_s \otimes |flavor\rangle_s]_s$  )

$$\Psi_A \equiv |qqq\rangle_A = \underbrace{|color\rangle_A}_{\text{antisymmetric}} \otimes \underbrace{[|space\rangle \otimes |spin\rangle \otimes |flavor\rangle]_s}_{\text{symmetric}} \quad (5)$$

# Hadrons in Quark model

→ Possible states  $\Psi_A$ :

$$\Psi_A = |\text{color}\rangle_A \otimes [|\text{space}\rangle_S \otimes |\text{spin}\rangle_A \otimes |\text{flavor}\rangle_A]_S \quad (6)$$

$$[|\text{space}\rangle_S \otimes |\text{spin}\rangle_S \otimes |\text{flavor}\rangle_S]_S \quad (7)$$

or a linear combination of (6) and (7):

$$\begin{aligned} \Psi_A = & \alpha |\text{color}\rangle_A \otimes [|\text{space}\rangle_S \otimes |\text{spin}\rangle_A \otimes |\text{flavor}\rangle_A]_S \\ & + \beta |\text{color}\rangle_A \otimes [|\text{space}\rangle_S \otimes |\text{spin}\rangle_S \otimes |\text{flavor}\rangle_S]_S \end{aligned} \quad (8)$$

where  $\alpha^2 + \beta^2 = 1$

■ Consider **flavor space (u,d,s quarks)** → **SU(3)<sub>flavor</sub> group**

Possible states: **|flavor>** : (6) – antisymmetric  
for baryons (7) – symmetric  
(8) – mixed symmetry

# Mesons in the Quark model

$$| \text{Meson} \rangle = | q \bar{q} \rangle$$

**Quark**

triplet in  $SU(3)_{\text{flavor}}$  group:  $[3]$

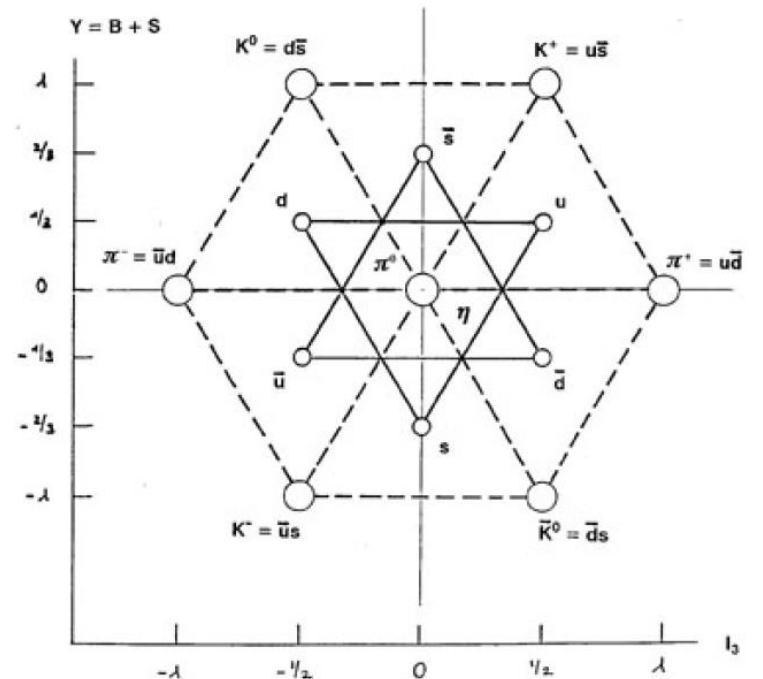
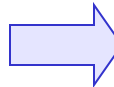
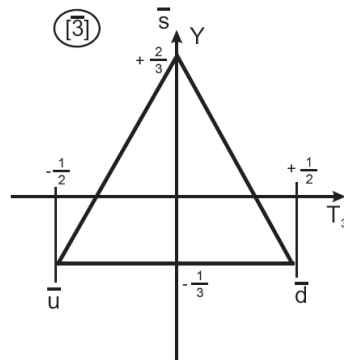
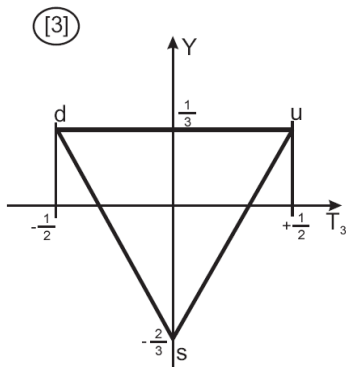
**Anti-quark**

anti-triplet in  $SU(3)_{\text{flavor}}$  group:  $[\bar{3}]$

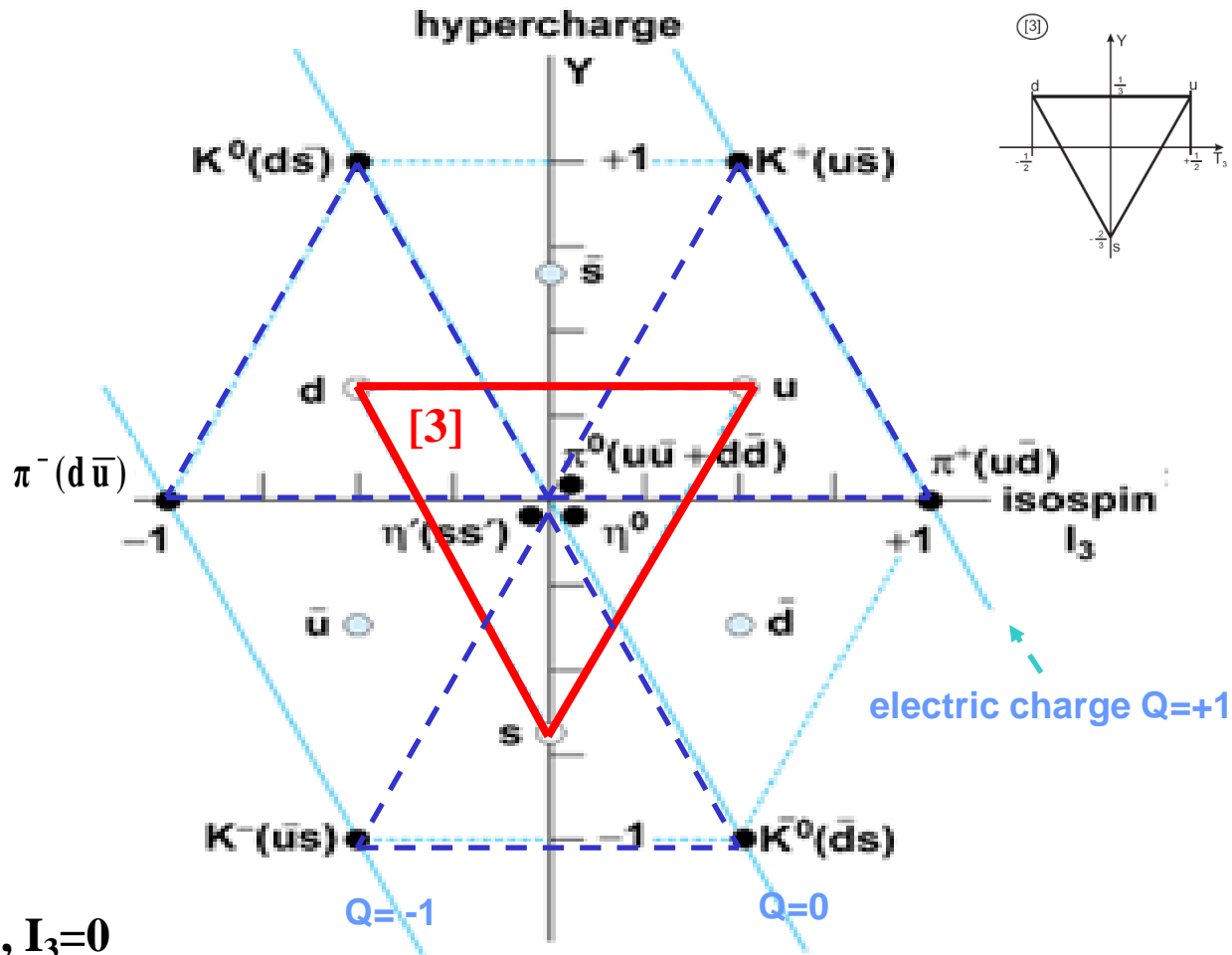
From group theory: the nine states (nonet) made out of a pair can be decomposed into the trivial representation, 1 (called the **singlet**), and the adjoint representation, 8 (called the **octet**).

$$[3] \otimes [\bar{3}] = [8] \oplus [1]$$

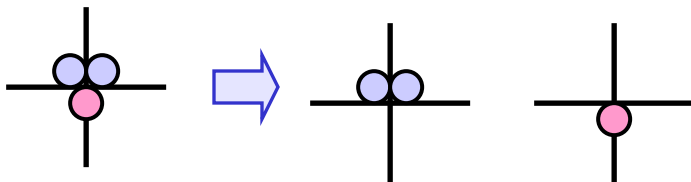
octet + singlet



# Mesons in the Quark model



3 states:  $Y=0, I_3=0$



A,B,C: in octet: A,B singlet state C

linear combination of  $u\bar{u}, d\bar{d}, s\bar{s}$

$$A = \sqrt{\frac{1}{2}}(u\bar{u} - d\bar{d}) \Rightarrow \pi^0, \quad B = \sqrt{\frac{1}{6}}(u\bar{u} + d\bar{d} - 2s\bar{s}) \Rightarrow \eta$$

$$C = \sqrt{\frac{1}{3}}(u\bar{u} + d\bar{d} + s\bar{s}) \Rightarrow \eta'$$

# Mesons in the Quark model

## Classification of mesons:

### ❖ Quantum numbers:

- spin  $S$
- orbital angular momentum  $L$
- total angular momentum  $\vec{J} = \vec{L} + \vec{S}$

### ❖ Properties with respect to Poincare transformation:

1) **continuous transformation**  $\rightarrow$  Lorentz boost (3 parameters:  $\beta$ )

$$U_B \sim e^{i\vec{\beta}\vec{a}} \quad \text{Casimir operator (invariant under transformation): } M^2 = p_\mu p^\mu$$

2) **rotations** (3 parameters: Euler angle  $\varphi$ ) :

$$U_R \sim e^{i\vec{\varphi}\vec{J}} \quad \text{Casimir operator: } J^2$$

3) **space-time shifts** (4 parameters:  $a_\mu$ )

$$U_{st} \sim e^{i\alpha_\mu x^\mu} \quad x'_\mu \rightarrow x_\mu + a_\mu$$



**10 parameters  
of Poincare group**

# Mesons in the Quark model

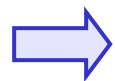
## Classification of mesons:

### ❖ Discrete operators:

4) **parity transformation:** flip in sign of the spacial coordinate  $\vec{r} = -\vec{r}$   
eigenvalue  $P = \underline{\pm 1}$   
 $P = (-1)^{L+1}$

5) **time reversal:**  $t \rightarrow -t$   
eigenvalue  $T = \underline{\pm 1}$

6) **charge conjugation:**  $C = -C$  ( $C$ -parity applies only to neutral systems)  
 $C$  - parity: eigenvalue  $C = \underline{\pm 1}$   
 $C = (-1)^{L+S}$



**General PCT –theorem:**

$$P \cdot C \cdot T = 1$$

due to the fact that discrete transformations correspond to the U(1) group they are multiplicative

**Properties of the distinguishable (not continuum!) particles are defined by**

$$M^2 (\text{or } M), \quad J^2 (\text{or } J), \quad P, \quad C$$

# Mesons in the Quark model

## Classification of mesons:

the mesons are classified in  $J^{PC}$  multiplets

1)  **$L=0$  states:**  $J=0$  or  $1$ , i.e.  $J=S$

$$P = (-1)^{L+1} = -1 \qquad C = (-1)^{L+S} = (-1)^S = \begin{cases} +1 & \text{for } S=0 \\ -1 & \text{for } S=1 \end{cases}$$

$$J^{PC} = \begin{cases} 0^{-+} & \text{- pseudoscalar states} \\ 1^{-+} & \text{- vector states} \end{cases}$$

2)  **$L=1$  states** - orbital excitations;  $P = (-1)^{L+1} = +1$

$$\vec{J} = \vec{L} + \vec{S} \quad \left\{ \begin{array}{ll} S = -1 \ J = 0 & J^{PC} = 0^{++} \text{ - scalar states} \\ S = 0 \ J = 1 & 1^{++} \text{ - axial vectors} \\ & 1^{+-} \text{ - axial vectors} \\ S = 1 \ J = 2 & 2^{++} \text{ - tensor} \end{array} \right.$$

$$|L - S| \leq J \leq L + S$$

# Mesons in the Quark model

## Classification used in PDG (Particle Data Group)

C-parity applies only to neutral systems

$$I^G (J^{PC}) \text{ or } I^G (J^P) \text{ multiplets}$$

**G-parity** is a multiplicative quantum number that results from the generalization of C-parity to multiplets of particles, i.e to all charged states (since strong interaction doesn't depend on electric charge!)

$$G = C (-1)^I$$

$I$  – isospin of particles

Since  $C = (-1)^{L+S}$

$$G = C (-1)^{L+S+I}$$

Citation: P.A. Zyla et al. (Particle Data Group), Prog. Theor. Exp. Phys. 2020, 083C01 (2020)

$$\pi^0$$

$$I^G (J^{PC}) = 1^-(0^-+)$$

$$\pi^\pm$$

$$I^G (J^P) = 1^-(0^-)$$

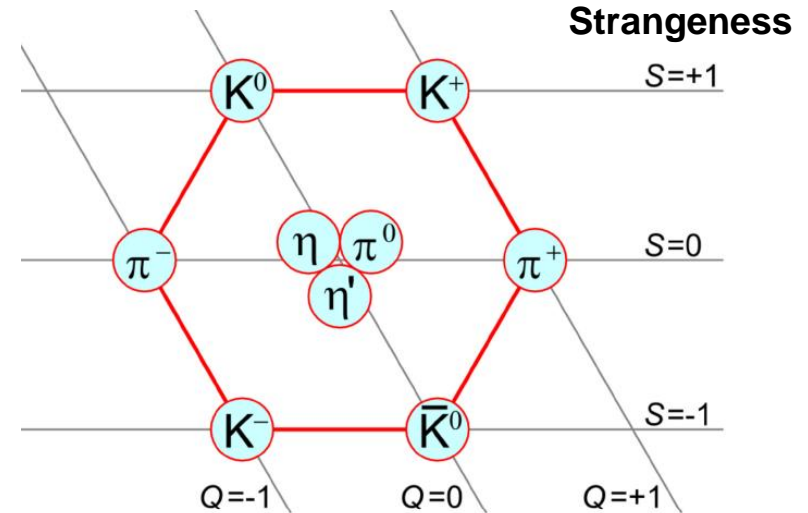
# Mesons in the Quark model

$L$	$S$	$J^{PC}$	isospin			$m$ [MeV]
			$I = 1$	$I = 1/2$	$I = 0$	
$L = 0$	$S = 0$	$0^{-+}$	$\pi$	$K$	$\eta, \eta'$	140 ( $m_\pi$ ) – 500
	$S = 1$	$1^{--}$	$\rho$	$K^*$	$\omega, \phi$	$\sim 800$
$L = 1$	$S = 0$	$1^{+-}$	$B$	$Q_2$	$H$	1250
	$S = 1$	$2^{++}$	$A_2$	$K'^*$	$f, f'$	1400
		$1^{++}$	$A_1$	$Q_1$	$D$	1300
		$0^{++}$	$\delta$	$\kappa$	$\epsilon, S^*$	1150

# Mesons in the Quark model

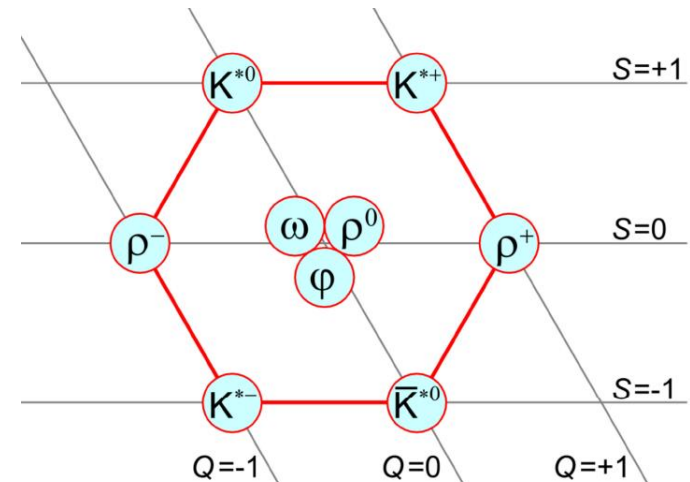
$J^{PC} = 0^{-+}$  - pseudoscalar nonet (L=0, S=0)

particle	symbol	Mass(MeV)	Isospin, I	$I_z$
$\pi^+$	$u\bar{d}$	140	1	1
$\pi^-$	$d\bar{u}$		1	-1
$\pi^0$	$(u\bar{u}-d\bar{d})/\sqrt{2}$	135	1	0
$K^+$	$u\bar{s}$	494	1/2	1/2
$K^-$	$s\bar{u}$	494	1/2	-1/2
$K^0$	$d\bar{s}$	"	1/2	-1/2
$\bar{K}^0$	$s\bar{d}$	"	1/2	1/2
$\eta$	$(u\bar{u}+d\bar{d}-2s\bar{s})/\sqrt{6}$	548	0	0
$\eta'$	$(u\bar{u}+d\bar{d}+s\bar{s})/\sqrt{3}$	958	0	0



$J^{PC} = 1^{--}$  - vector nonet (L=0, S=1)

particle	symbol	Mass(MeV)	Isospin, I	$I_z$
$\rho^+$	$u\bar{d}$	770	1	1
$\rho^-$	$d\bar{u}$	"	1	-1
$\rho^0$	$(u\bar{u}-d\bar{d})/\sqrt{2}$	"	1	0
$K^{*+}$	$u\bar{s}$	892	1/2	1/2
$K^{*-}$	$s\bar{u}$	"	1/2	-1/2
$K^{*0}$	$d\bar{s}$	"	1/2	-1/2
$\bar{K}^{*0}$	$s\bar{d}$	"	1/2	1/2
$\omega$	$(u\bar{u}+d\bar{d}-2s\bar{s})/\sqrt{6}$	782	0	0
$\phi$	$(u\bar{u}+d\bar{d}+s\bar{s})/\sqrt{3}$	1020	0	0



# Baryons in the Quark model

$$| \text{Baryon} \rangle = | qqq \rangle$$

Quark  
triplet in  $SU(3)_{\text{flavor}}$  group: [3]

Eqs. (4-8): **state function for baryons** – **antisymmetric** under interchange of two quarks:

$$\Psi_A \equiv | qqq \rangle_A = [ | \text{color} \rangle \otimes | \text{space} \rangle \otimes | \text{spin} \rangle \otimes | \text{flavor} \rangle ]_A$$

where  $| \text{flavor} \rangle$  state can be symmetric (S), antisymmetric (A) or mixed symmetry (M)

**From group theory:** with three flavours, the decomposition in flavour is

$$\begin{aligned} [3] \otimes [3] \otimes [3] &= ([6]_S \oplus [\bar{3}]_A) \otimes [3] = \\ &= ([6]_S \otimes [3]) \oplus ([\bar{3}] \otimes [3]) = \\ &= [10]_S \oplus [8]_M \oplus [8]_M \oplus [1]_A \end{aligned}$$

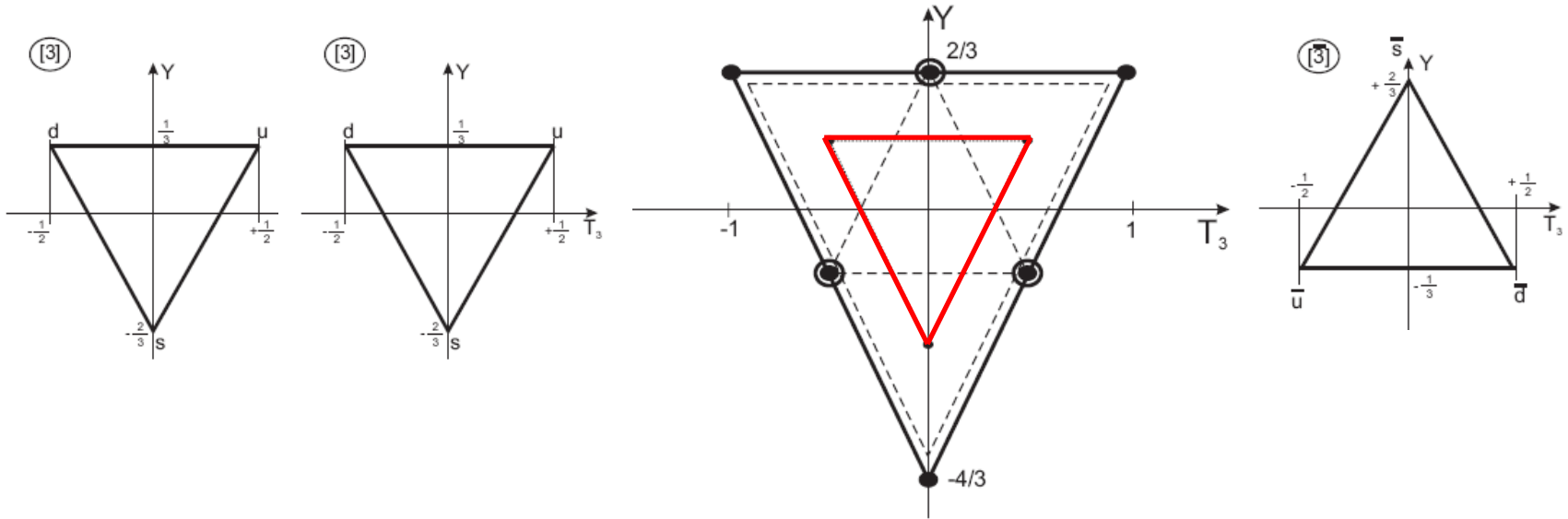
The **decuplet** is **symmetric in flavour**, the **singlet antisymmetric** and the **two octets** have **mixed symmetry** (they are connected by a unitary transformation and thus describe the same states).

The **space and spin parts of the states** are then fixed once the orbital angular momentum is given.

# Baryons in the Quark model

1) Combine first 2 quark triplets:

$$[3] \otimes [3] = [6]_S \oplus [\bar{3}]_A$$

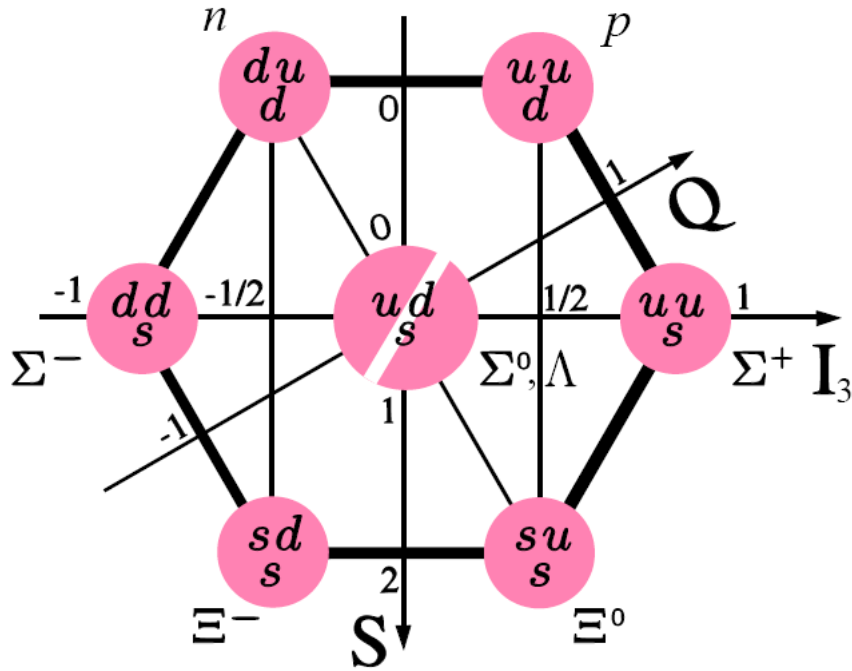


2) Add a 3<sup>d</sup> quark:

$$\begin{aligned}
 [3] \otimes [3] \otimes [3] &= ([6]_S \oplus [\bar{3}]_A) \otimes [3] = \\
 &= [10]_S \oplus [8]_M \oplus [8]_M \oplus [1]_A
 \end{aligned}$$

# Baryons in the Quark model

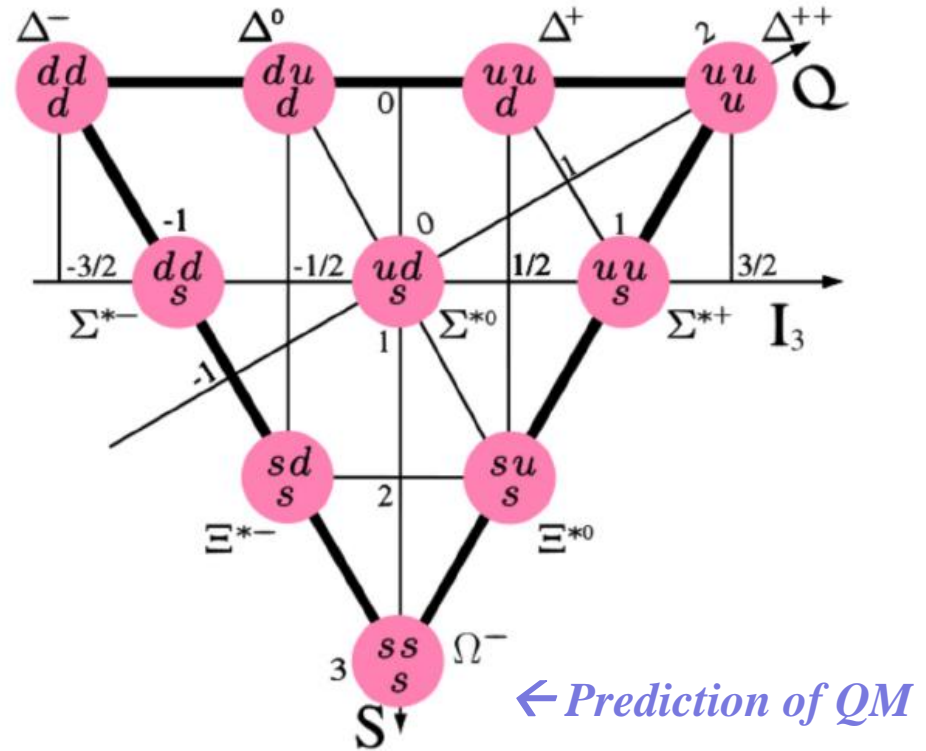
Octet [8]



Spin:  
 $J=S$   
 $L=0$

$$J^P = \frac{1}{2}^+$$

Decuplet [10]

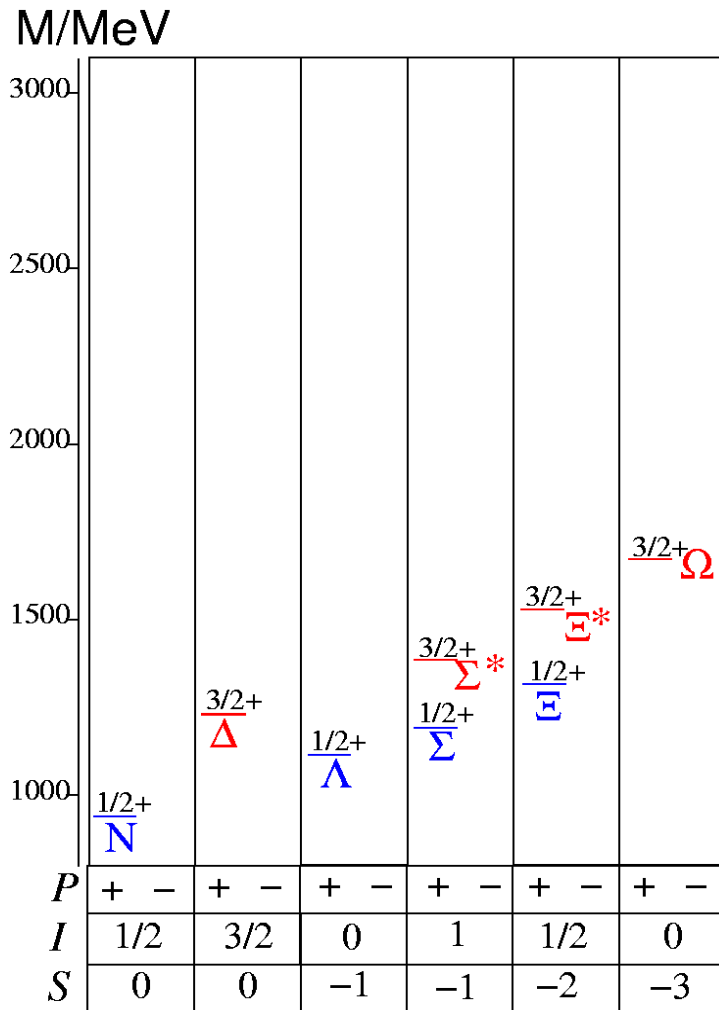


$J=S+L$   
 $L=1$

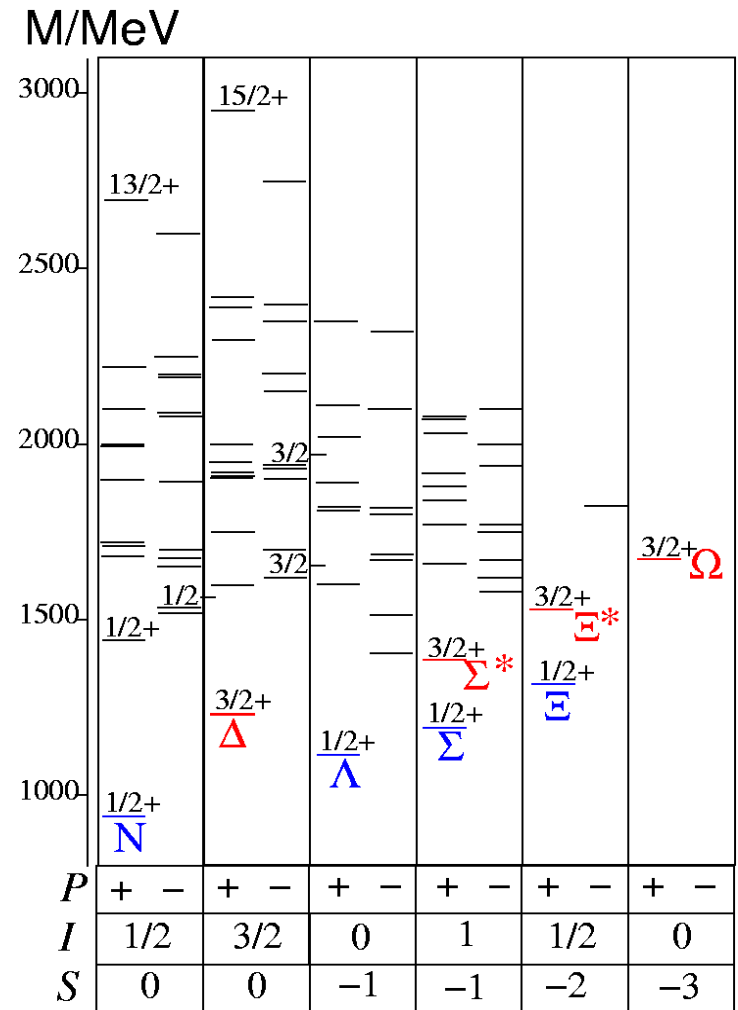
$$J^P = \frac{3}{2}^+$$

# Structure of known baryons

## Ground states of Baryons



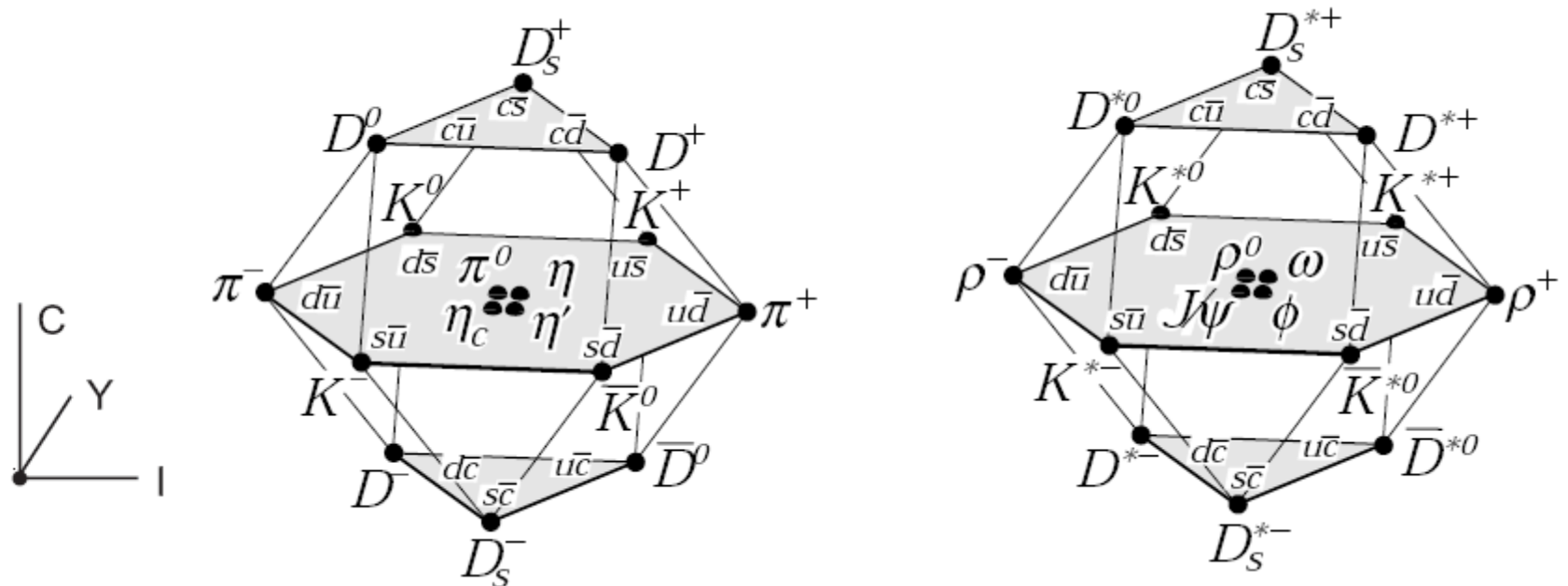
## + excitation spectra



# Mesons in the SU(4) flavor Quark model

Now consider the basis states of **mesons** in **4 flavour**  $SU(4)_{\text{flavor}}$ : **u, d, s, c** quarks

$$[4] \otimes [\bar{4}] = [15] \oplus [1]$$



**SU(4) weight diagram** showing the **16-plets for the pseudoscalar and vector mesons** as a function of isospin I, charm C and hypercharge Y. The nonets of light mesons occupy the central planes to which the ccbar states have been added.



# Exotic states

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## A SCHEMATIC MODEL OF BARYONS AND MESONS \*

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If we assume that the strong interactions of baryons and mesons are correctly described in terms of the broken "eightfold way"  $1-3$ , we are tempted to look for some fundamental explanation of the situation. A highly promised approach is the purely dynamical "bootstrap" model for all the strongly interacting particles within which one may try to derive isotopic spin and strangeness conservation and broken eightfold symmetry from self-consistency alone  $4$ ). Of course, with only strong interactions, the orientation of the asymmetry in the unitary space cannot be specified; one hopes that in some way the selection of specific components of the F-spin by electromagnetism and the weak interactions determines the choice of isotopic spin and hypercharge directions.

Even if we consider the scattering amplitudes of strongly interacting particles on the mass shell only and treat the matrix elements of the weak, electromagnetic, and gravitational interactions by means

ber  $n_t - n_{\bar{t}}$  would be zero for all known baryons and mesons. The most interesting example of such a model is one in which the triplet has spin  $\frac{1}{2}$  and  $z = -1$ , so that the four particles  $d^-$ ,  $s^-$ ,  $u^0$  and  $b^0$  exhibit a parallel with the leptons.

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon  $b$  if we assign to the triplet  $t$  the following properties: spin  $\frac{1}{2}$ ,  $z = -\frac{1}{3}$ , and baryon number  $\frac{1}{3}$ . We then refer to the members  $u^{\frac{2}{3}}$ ,  $d^{-\frac{1}{3}}$ , and  $s^{-\frac{1}{3}}$  of the triplet as "quarks"  $6$ )  $q$  and the members of the anti-triplet as anti-quarks  $\bar{q}$ . Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqq\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(qq\bar{q}\bar{q})$ , etc. It is assuming that the lowest baryon configuration  $(qqq)$  gives just the representations **1**, **8**, and **10** that have been observed, while the lowest meson configuration  $(q\bar{q})$  similarly gives just **1** and **8**.

# Exotic states

$$|\text{Meson}\rangle = |q\bar{q}\rangle + |qqq\bar{q}\rangle + |qqg\rangle + \dots$$

$$|\text{Baryon}\rangle = |qqq\rangle + |qqq\bar{q}\rangle + |qqqg\rangle + \dots$$

$$|\text{Hybrid}\rangle = |qq\bar{g}\rangle + \dots$$

$$|\text{Baryonium}\rangle = |qqq\bar{q}\rangle + \dots$$

$$|\text{Glueball}\rangle = |gg\rangle + \dots$$

Experimental evidence:

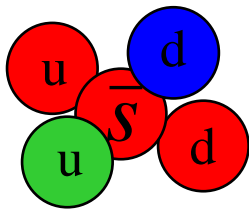
$\pi(1400)$

$\sigma(600)$

$f_0(1500)$

||

very broad width  
(200-300 MeV) => short  
lifetime < 1 fm/c



$$|\text{Pentaquark}\rangle = |qqqq\bar{q}\rangle + \dots$$

# Pentaquarks

„Flavour“-exotic state, e.g.

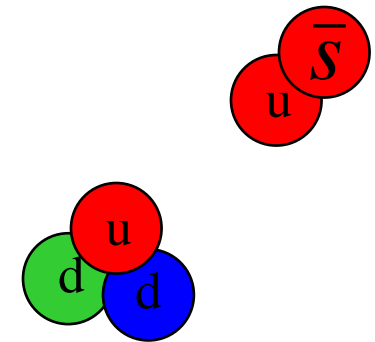
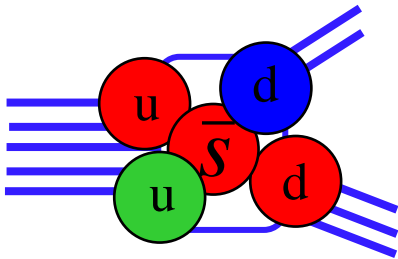
$$|\Theta^+\rangle = |uudd\bar{s}\rangle$$

**Decay:**  $|uudd\bar{s}\rangle \rightarrow |udd\rangle + |u\bar{s}\rangle$

$$|\Theta^+\rangle \rightarrow |n\rangle + |K^+\rangle$$

$$|uudd\bar{s}\rangle \rightarrow |uud\rangle + |d\bar{s}\rangle$$

$$|\Theta^+\rangle \rightarrow |p\rangle + |K^0\rangle$$



**Very small life time (big width)?**

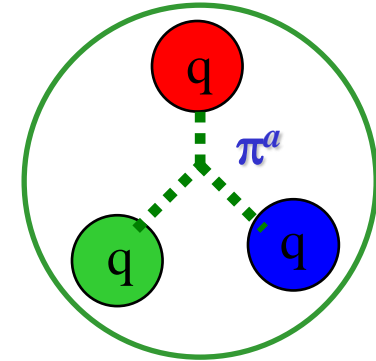
# (Quark)-Soliton-Model

Diakonov, Petrov, Polyakov ('97)

Chiral Lagrangean:  
invariant under SU(3)-flavor Rotation

$$L_{\text{eff}} = \bar{q} \left[ i\partial - M \exp\left(i\gamma_5 \pi^a \lambda^a / f_\pi\right) \right] q$$

Pseudoscalar fields:  $\pi^a = \{\pi, K, \eta\}$

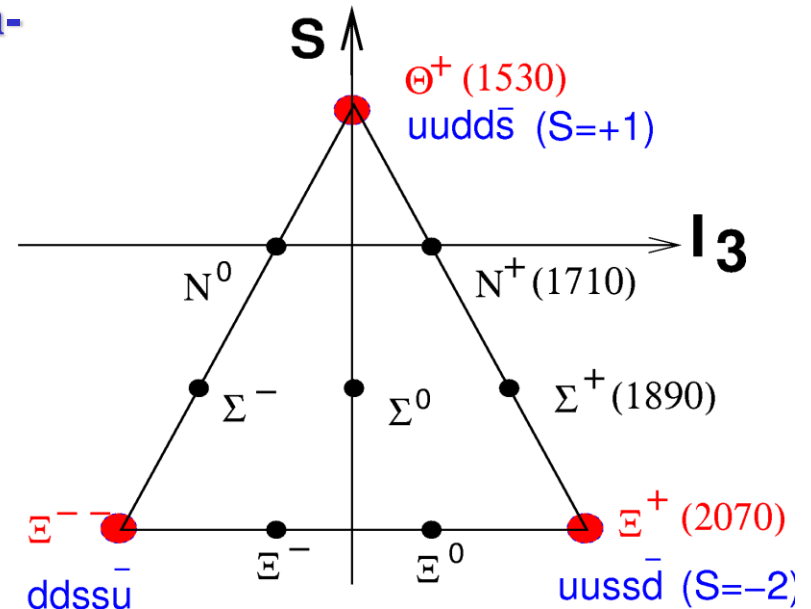


Chiral Quark-Soliton Model:

- solution of the Euler-Lagrange equation-of-motion => **Solitons**
- quantization of the soliton solutions under  $SU(3)_f$

Predictions for the pentaquark state:

- Spin  $J=1/2$ , Parity  $P$ =positive:  $J^P = 1/2^+$
- Width  $\Gamma < 30$  MeV
- $SU(3)_f$  - **Antidecuplet**

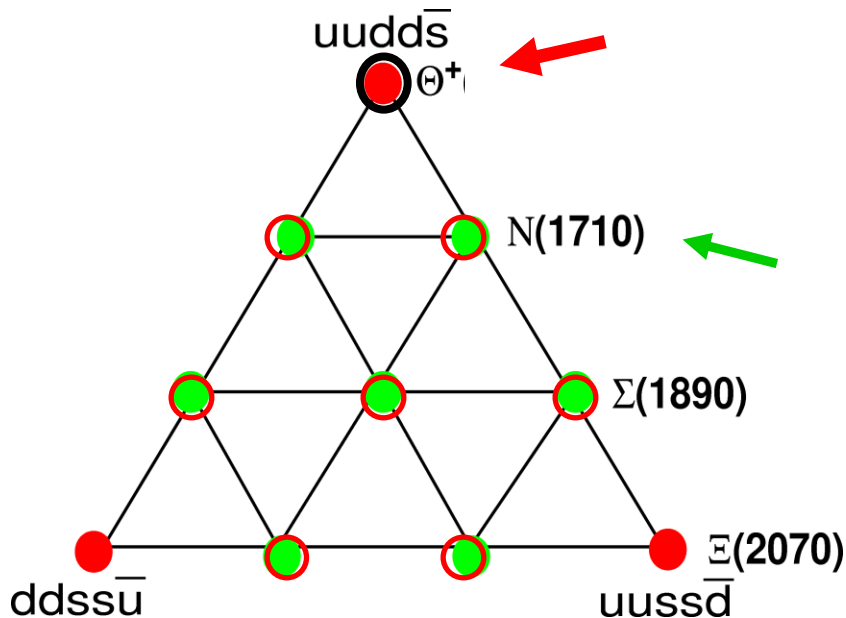
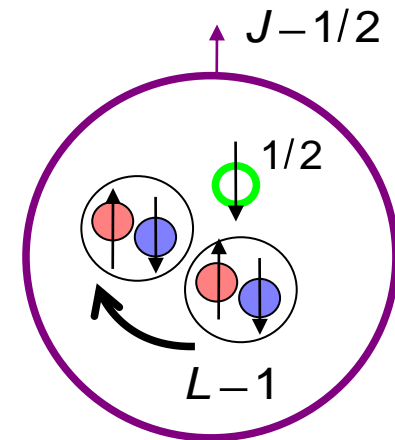


# Quark-Correlations (diquark) Model

Jaffe, Wilczek, Karliner, Lipkin ('03)

- [qq] correlations: antisymmetric in Color, Flavor und Spin state = **diquark**

- **Pentaquark:**  $\left[ [q_1 q_2]_{\bar{3}^c} \otimes [q_1 q_2]_{\bar{3}^c} \right]_{3^c} \otimes q_{\bar{3}^c}$



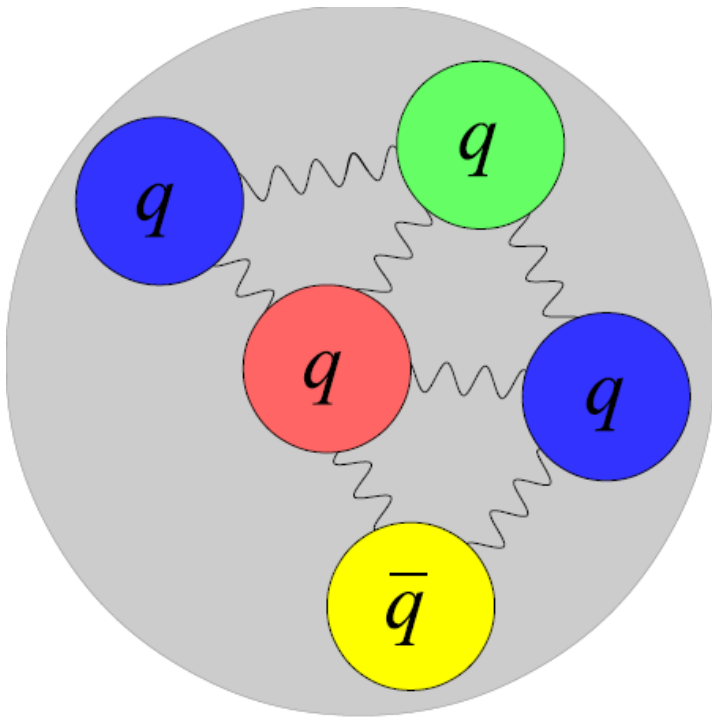
## Predictions for the pentaquarks:

- Spin  $J=1/2$ , Parity  $P=$ positiv:  $J^P = 1/2^+$
- Width  $\Gamma < 15$  MeV
- $SU(3)_f$  - Antidecuplet + Oktet  
Oktet: Partner with  $J^P = 3/2^+$

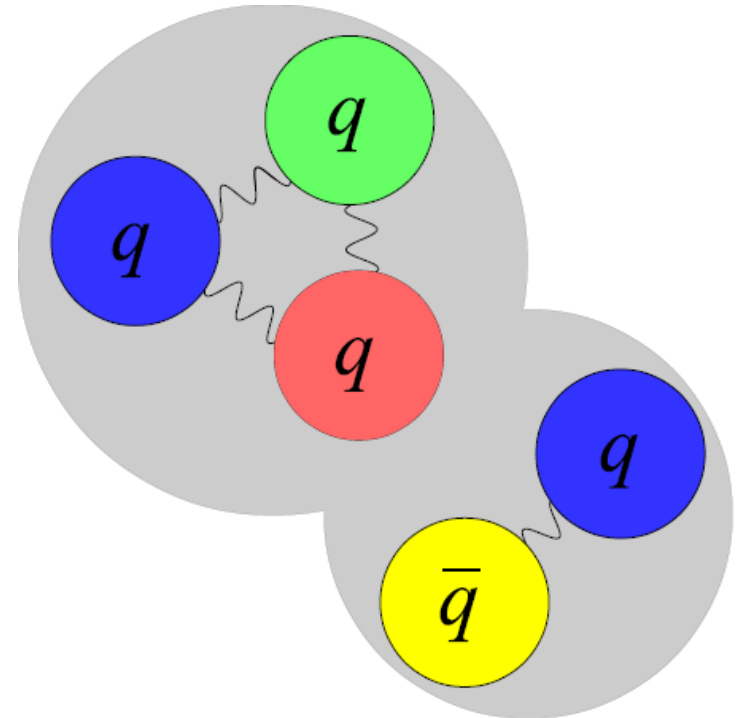
# Other models of pentaquarks

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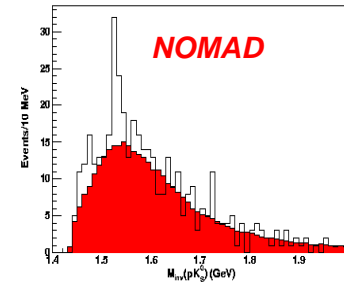
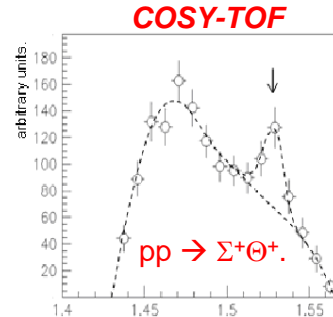
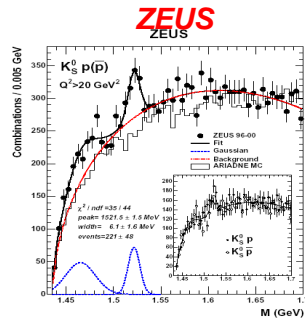
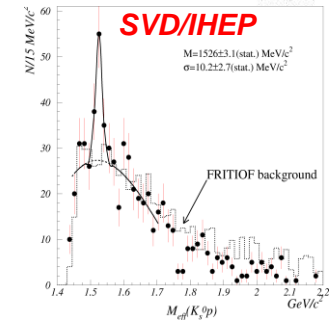
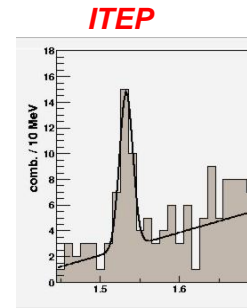
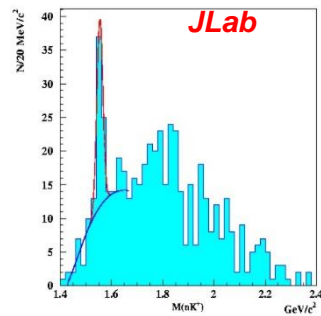
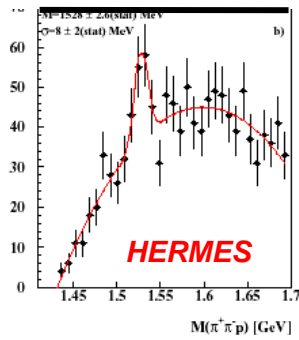
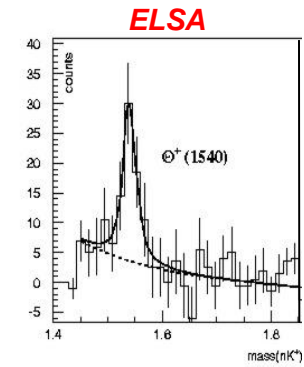
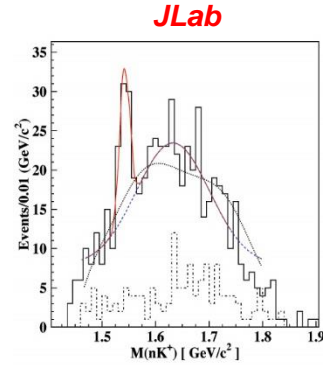
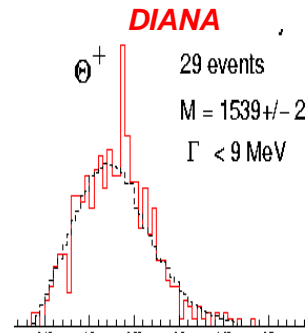
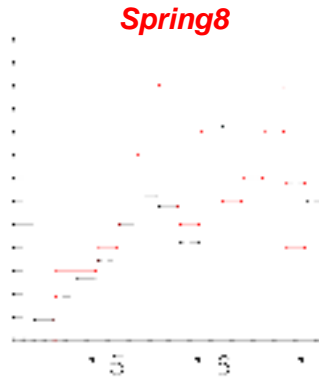
A five-quark "bag"



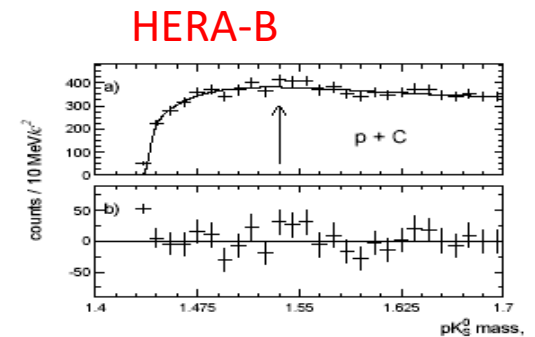
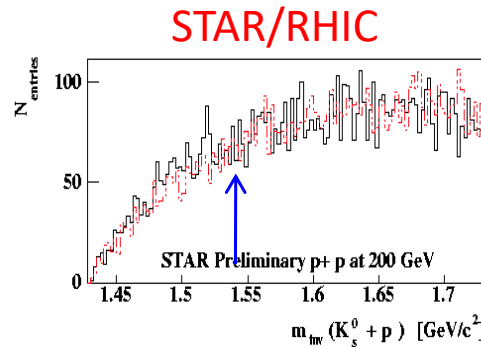
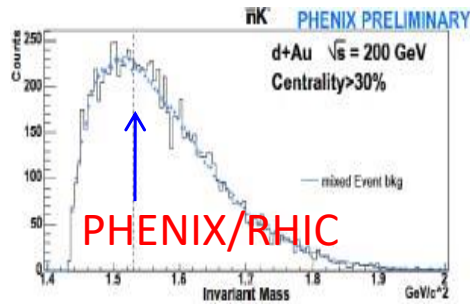
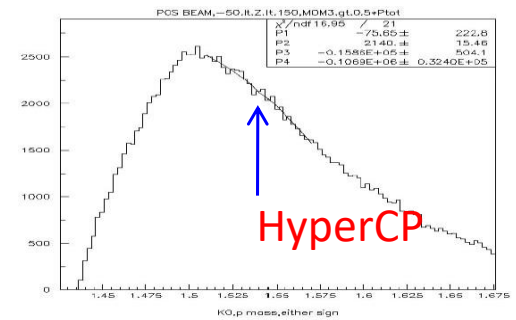
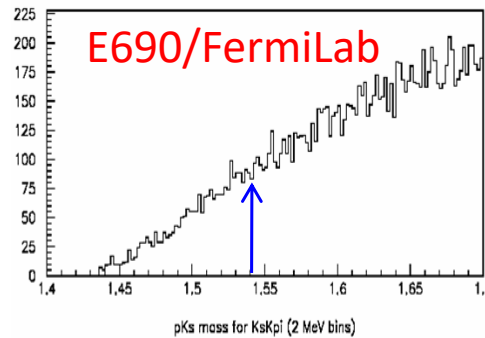
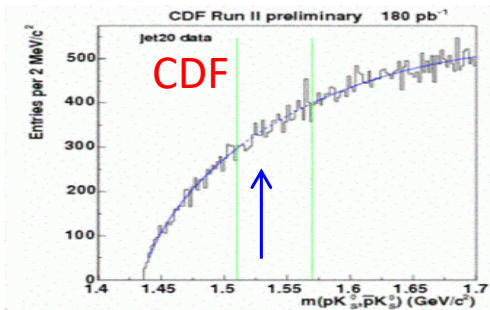
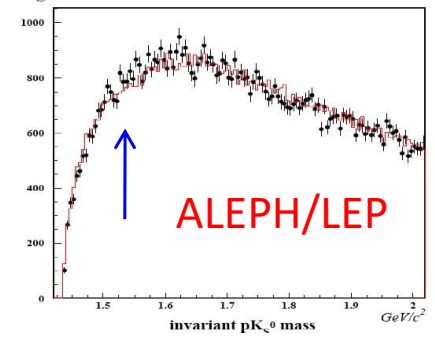
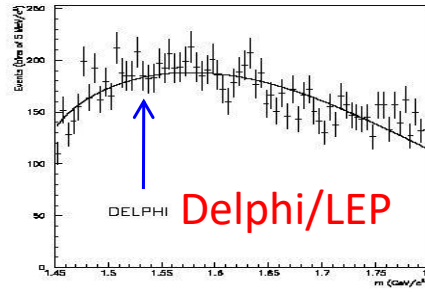
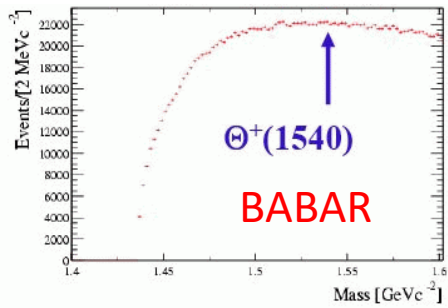
A "meson-baryon molecule"



# Positive experimental signals of $\Theta^+(1540)$



# ... but not seen by other experiments



# 2004: PDG entry for pentaquark – NOT any more in 2018!

Citation: S. Eidelman *et al.* (Particle Data Group), Phys. Lett. B 592, 1 (2004) (URL: <http://pdg.lbl.gov>)

## EXOTIC BARYONS

Minimum quark content:  $\Theta^+ = uud\bar{d}\bar{s}$ ,  $\Phi^{--} = ssdd\bar{u}$ ,  $\Phi^+ = ssuud\bar{d}$ .

$\Theta(1540)^+$

$$I(J^P) = 0(??)$$

It is difficult to deny a place in the Summary Tables for a state that six experiments claim to have seen. Nevertheless, we believe it reasonable to have some reservations about the existence of this state on the basis of the present evidence.

$$\text{Mass } m = 1539.2 \pm 1.6 \text{ MeV}$$

$$\text{Full width } \Gamma = 0.90 \pm 0.30 \text{ MeV}$$

$NK$  is the only strong decay mode allowed for a strangeness  $S=+1$  resonance of this mass.

$\Theta(1540)^+$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$KN$	100%	270

# 2015 LHCb results

In July 2015, the LHCb collaboration at CERN identified **pentaquarks** in the  $\Lambda_b^0 \rightarrow J/\psi K^- p$  channel

→ Two states, named  $P_c^+(4380)$  and  $P_c^+(4450)$

