

# Equation of state constraints from nuclear physics and observation

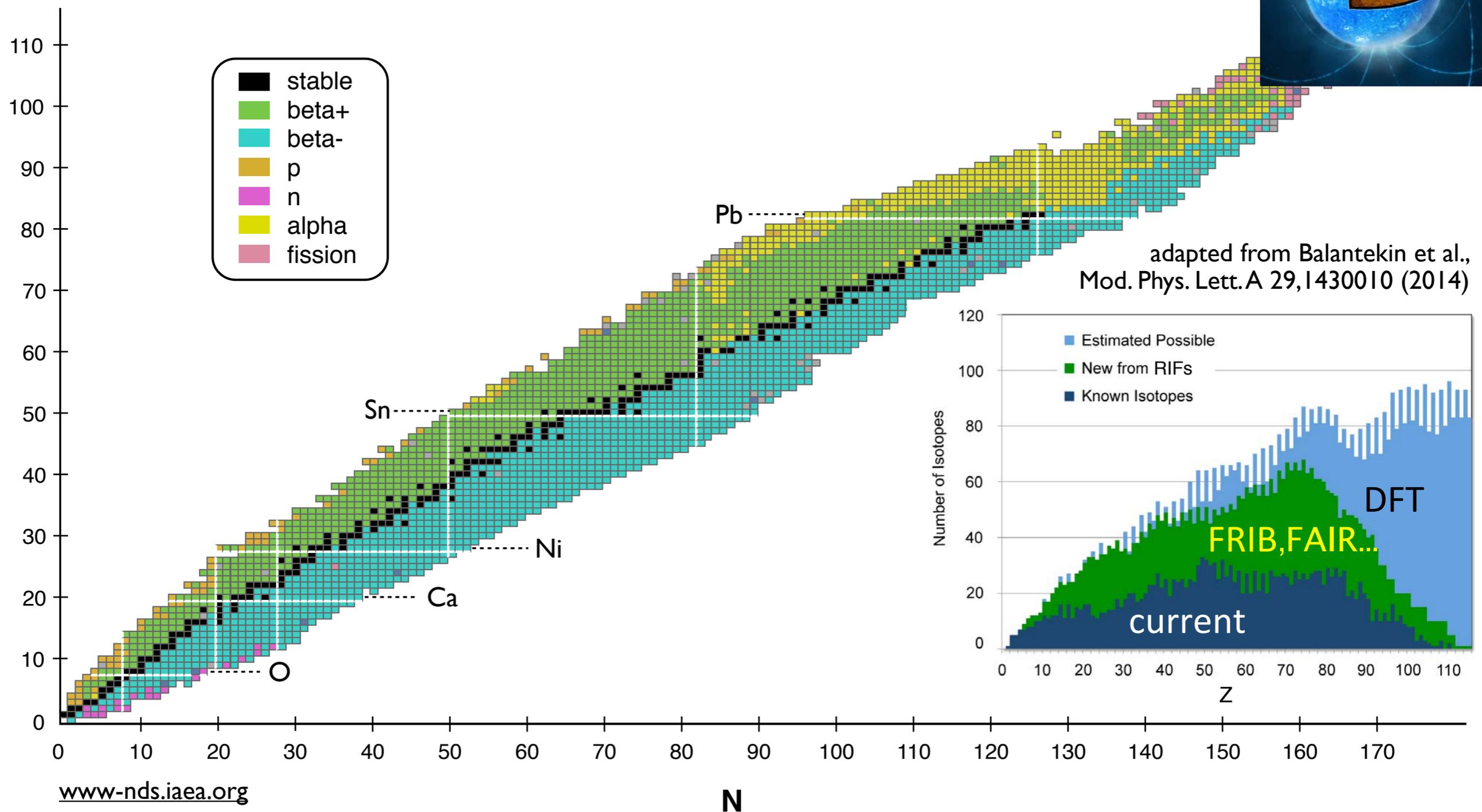
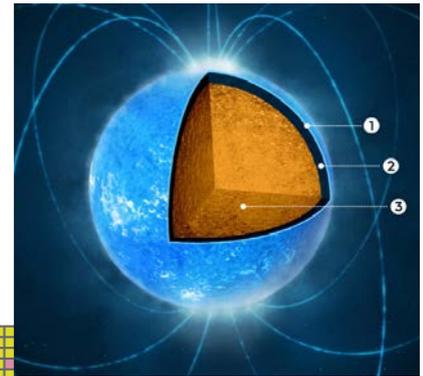
Kai Hebeler

Hirschegg, January 19, 2017

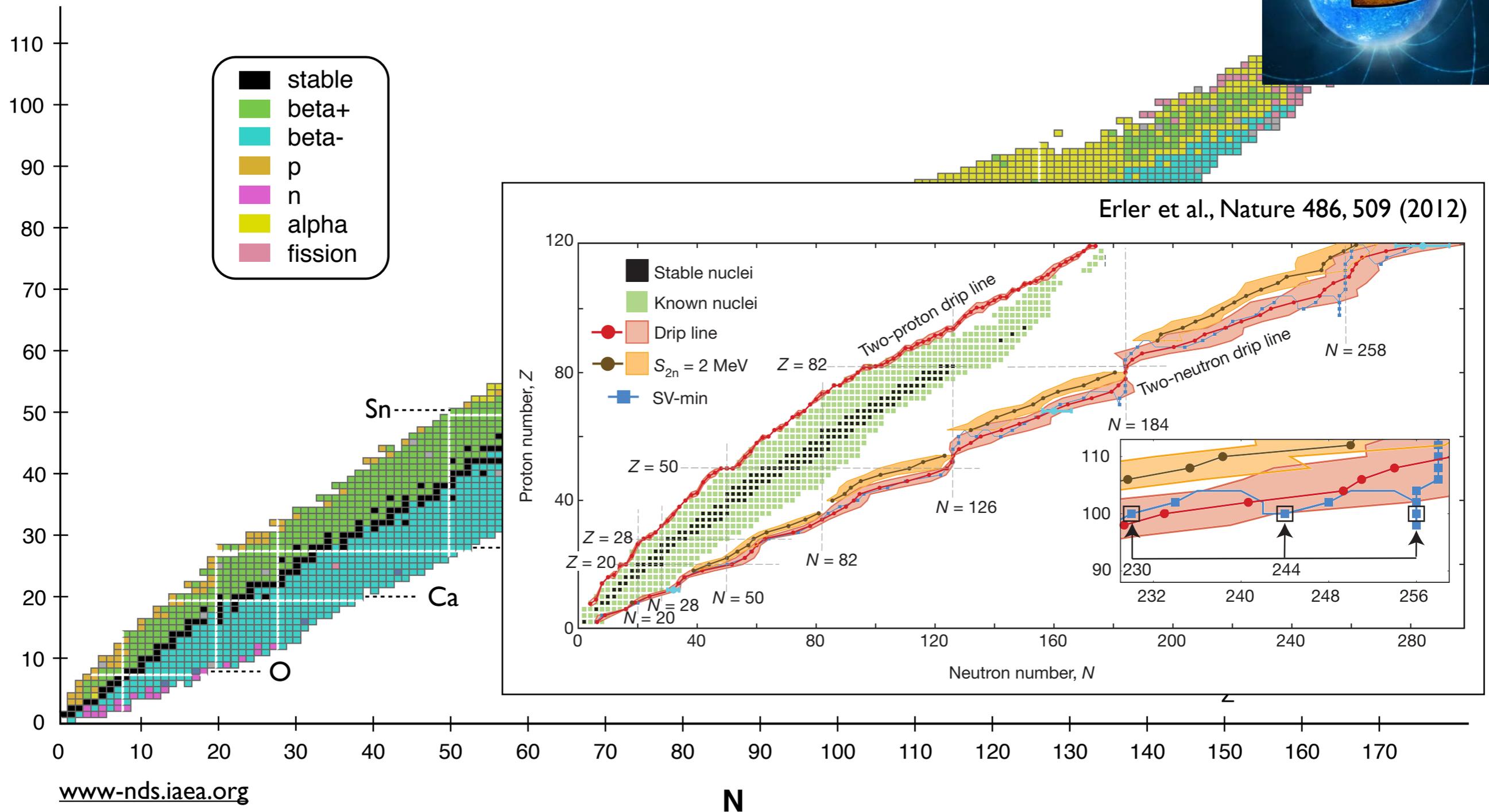
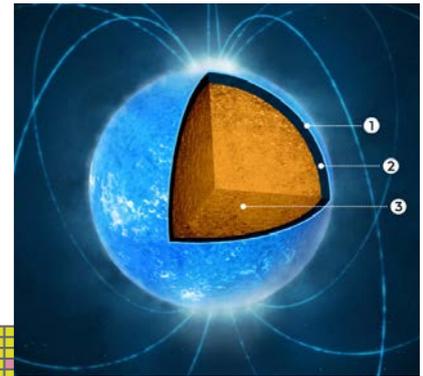
**Neutron star mergers:  
from gravitational waves to nucleosynthesis**



# The nuclear landscape: New frontiers from rare isotope facilities



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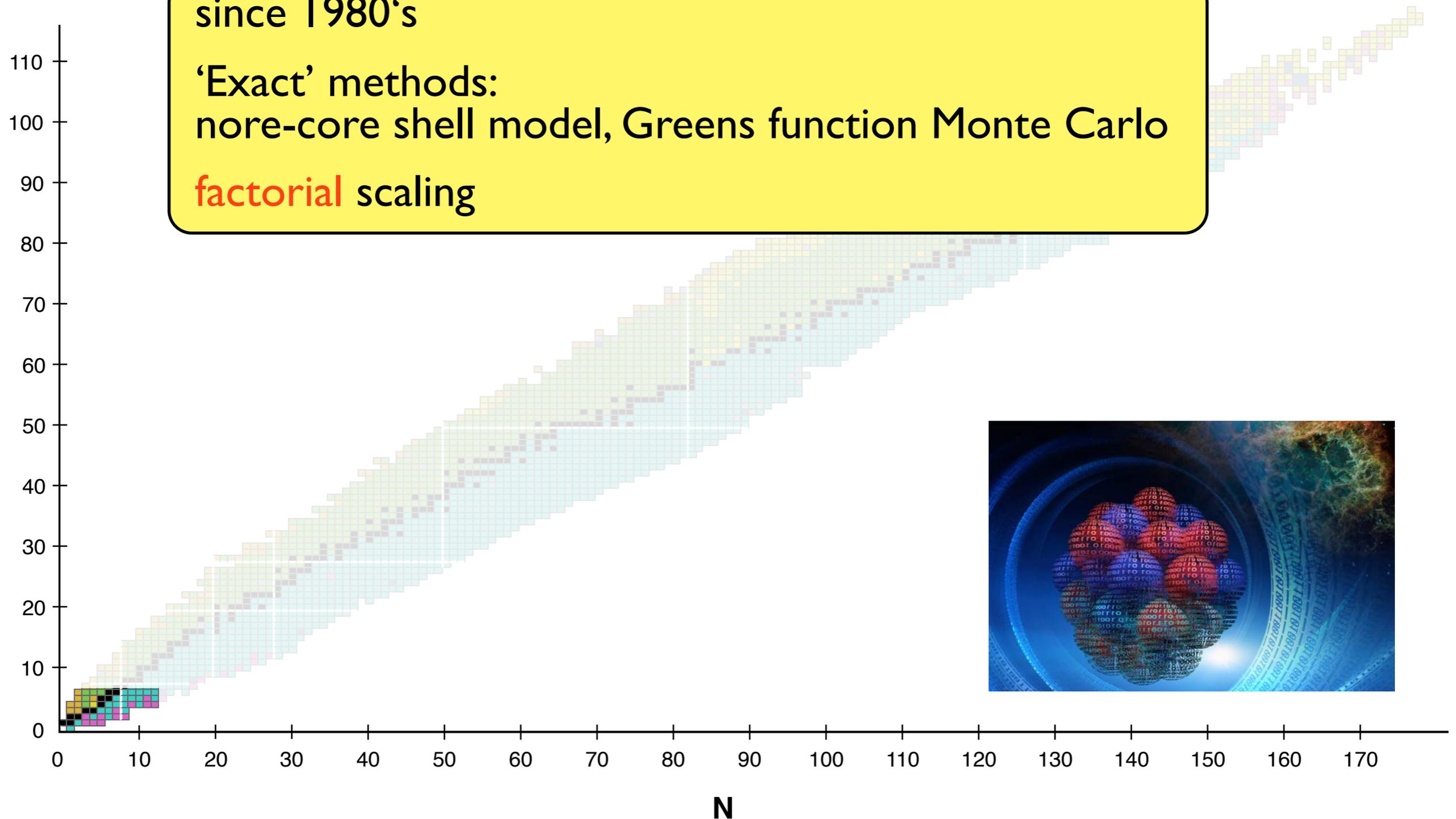


# The theoretical nuclear landscape: Scope of ab initio methods for atomic nuclei

since 1980's

'Exact' methods:  
no-core shell model, Greens function Monte Carlo

**factorial** scaling



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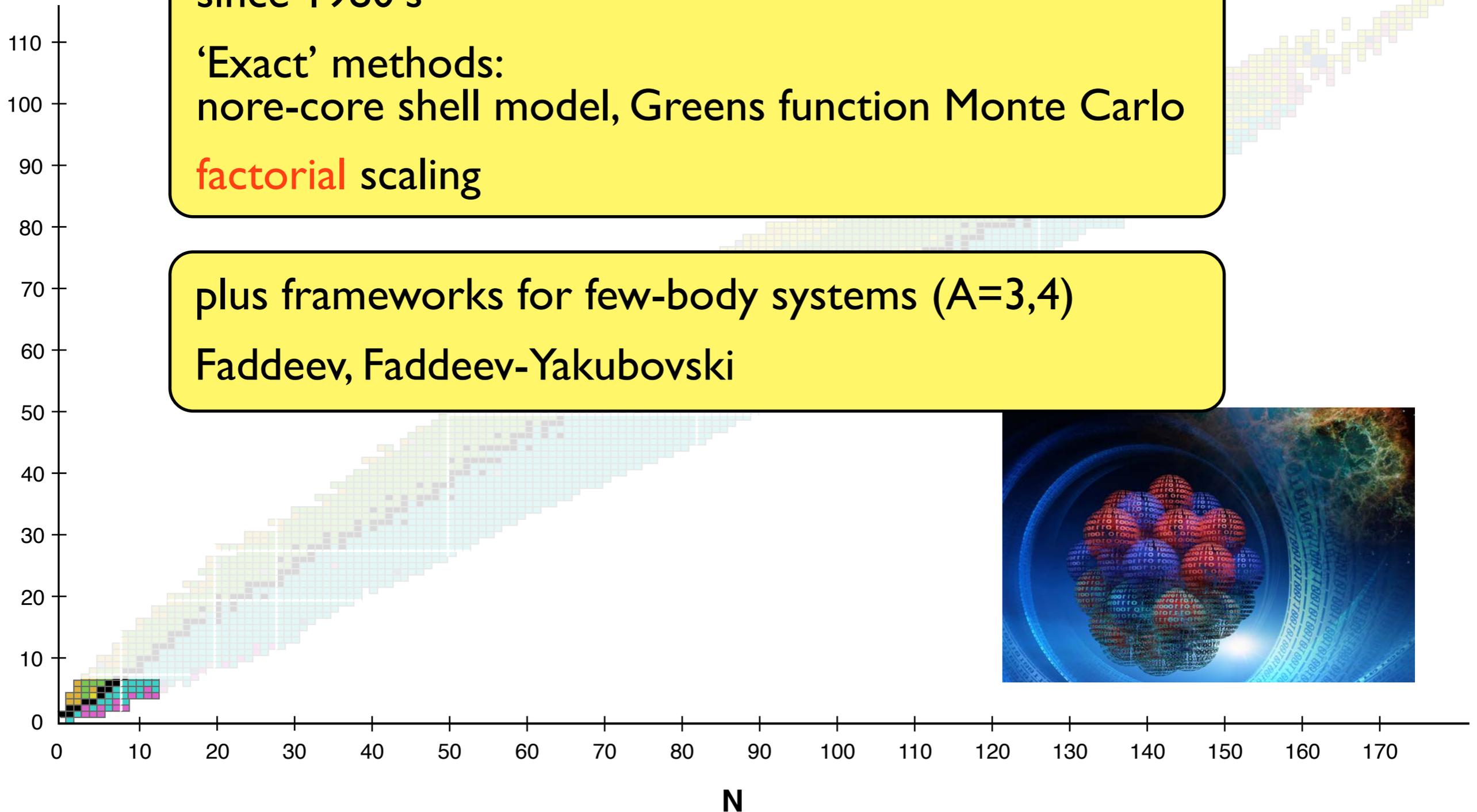
since 1980's

'Exact' methods:  
no-core shell model, Greens function Monte Carlo

**factorial** scaling

plus frameworks for few-body systems ( $A=3,4$ )

Faddeev, Faddeev-Yakubovski



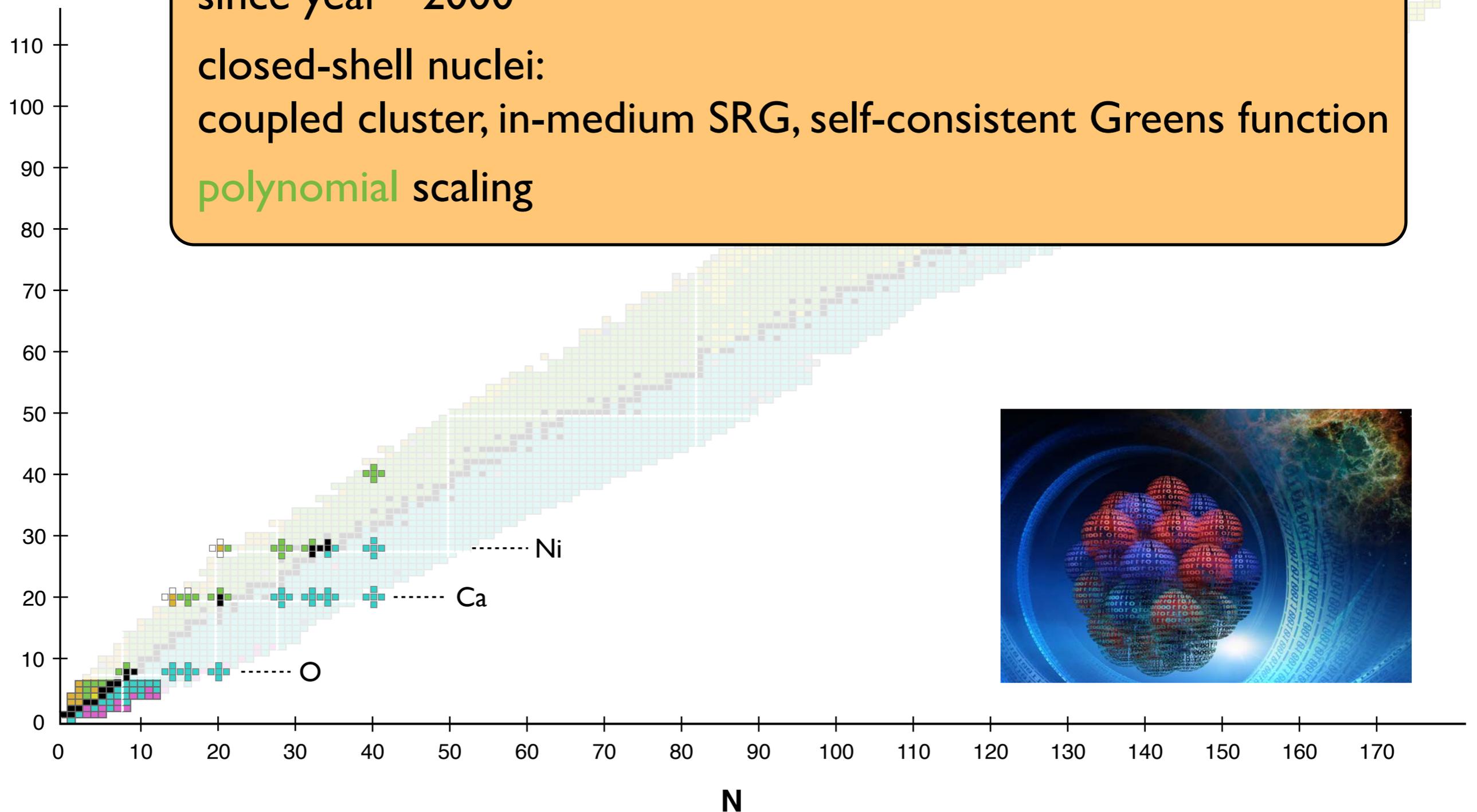
# The theoretical nuclear landscape: Scope of ab initio methods for atomic nuclei

since year ~2000

closed-shell nuclei:

coupled cluster, in-medium SRG, self-consistent Greens function

polynomial scaling



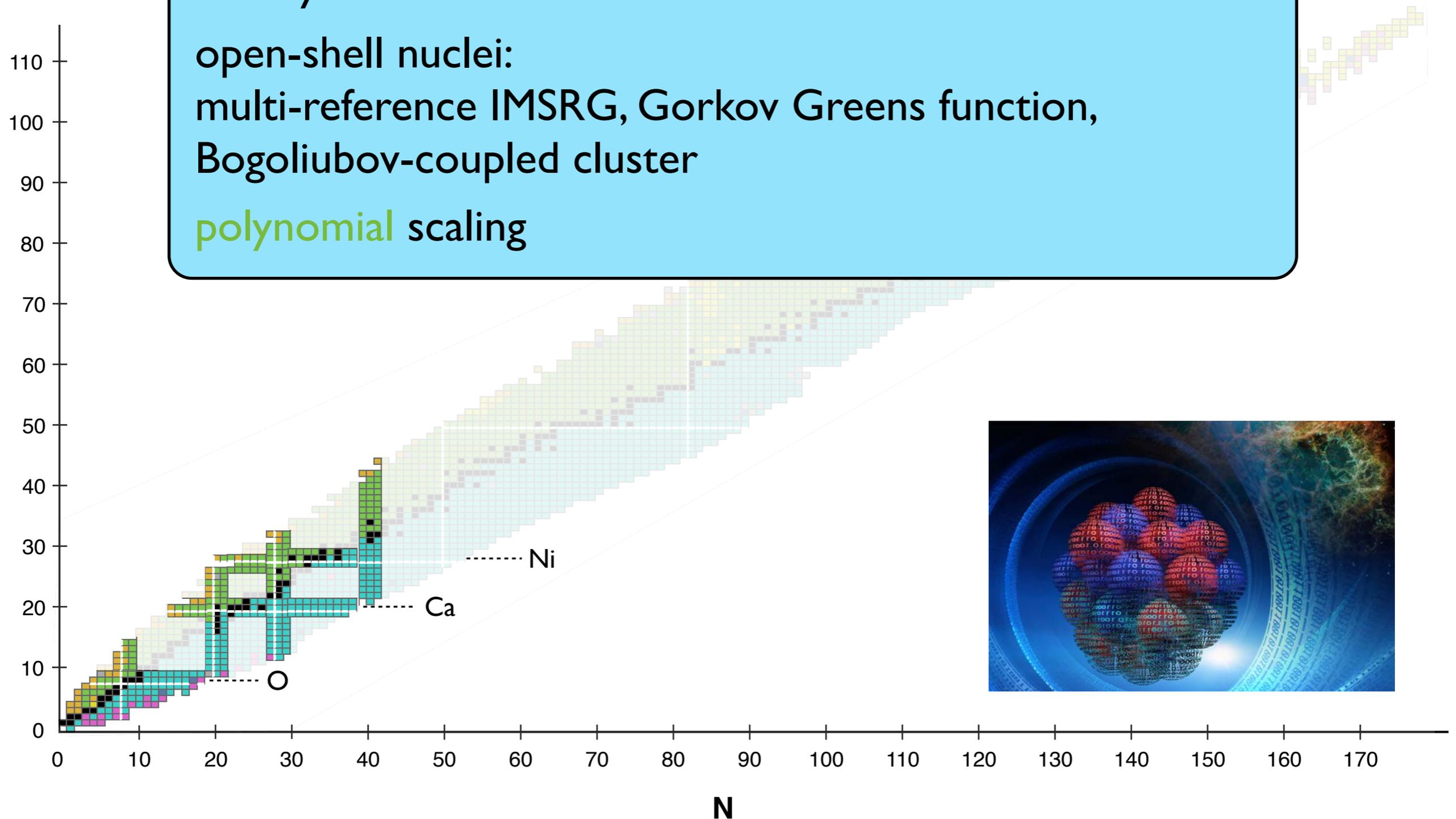
# The theoretical nuclear landscape: Scope of ab initio methods for atomic nuclei

since year ~2010

open-shell nuclei:

multi-reference IMSRG, Gorkov Greens function,  
Bogoliubov-coupled cluster

polynomial scaling

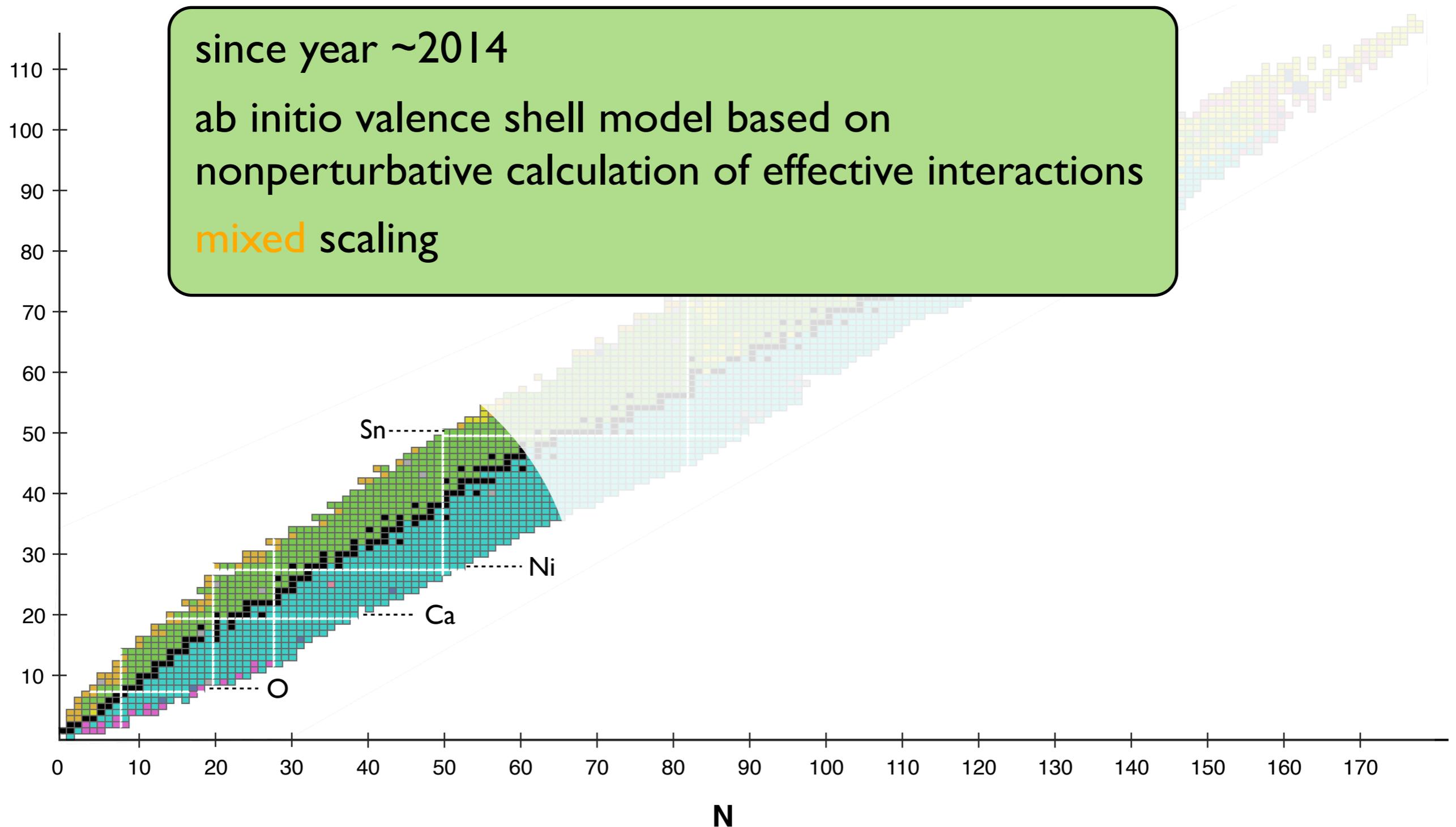


# The theoretical nuclear landscape: Scope of ab initio methods for atomic nuclei

since year ~2014

ab initio valence shell model based on  
nonperturbative calculation of effective interactions

mixed scaling

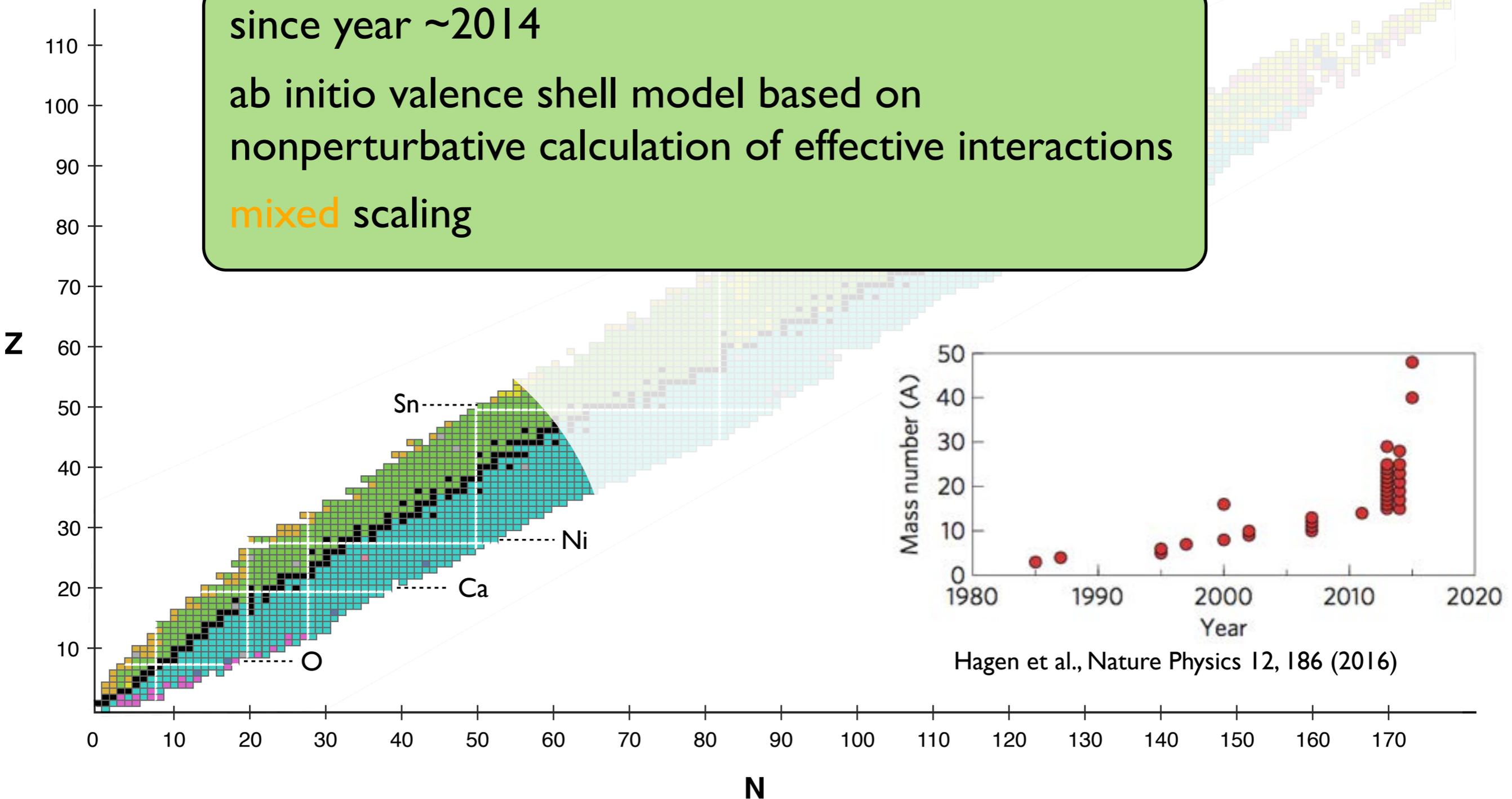


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# Ab initio nuclear structure and reaction theory

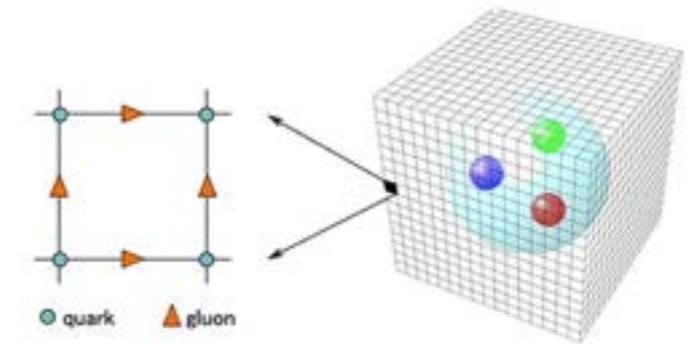
**nuclear structure and  
reaction observables**

**Quantum Chromodynamics**

# Ab initio nuclear structure and reaction theory

**nuclear structure and  
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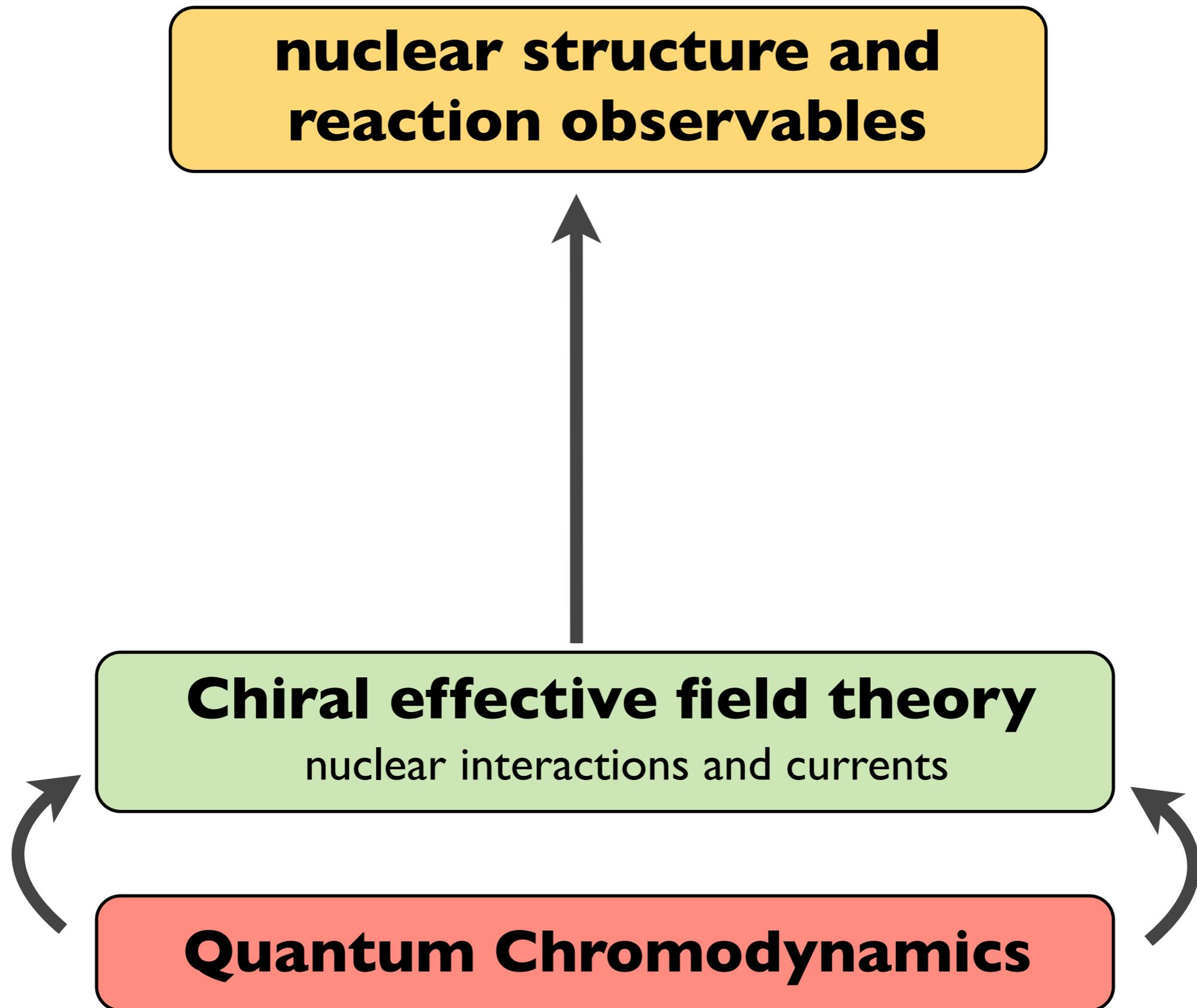
## Lattice QCD



- requires extreme amounts of computational resources
- currently limited to 1- or 2-nucleon systems
- current accuracy insufficient for precision nuclear structure

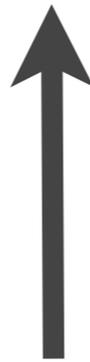
**Quantum Chromodynamics**

# Ab initio nuclear structure and reaction theory



# Ab initio nuclear structure and reaction theory

**nuclear structure and  
reaction observables**



**ab initio many-body frameworks**

Faddeev, Quantum Monte Carlo, no-core shell model, coupled cluster ...

**Chiral effective field theory**

nuclear interactions and currents

**Quantum Chromodynamics**



# Ab initio nuclear structure and reaction theory

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**Renormalization Group methods**

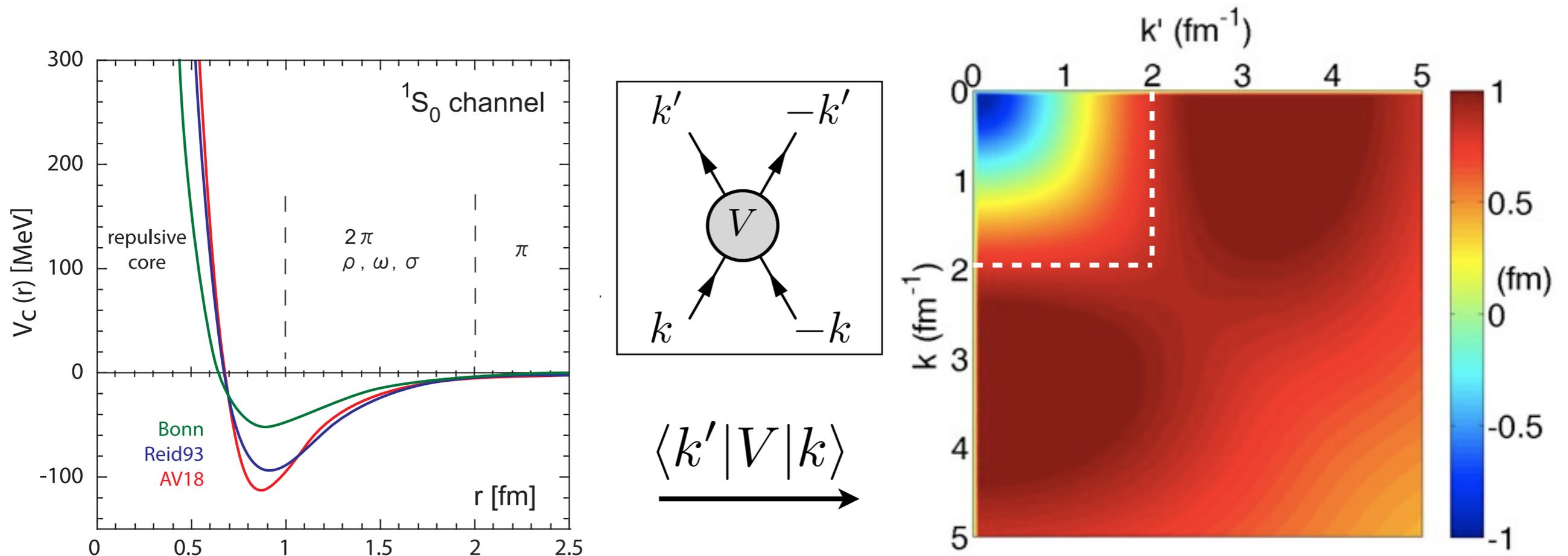
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# “Traditional” NN interactions



- constructed to fit NN scattering data (long-wavelength information)
- **long-range part** dominated by one pion exchange interaction
- short range part strongly **model dependent!**
- traditional NN interactions contain strongly repulsive core at small distance
  - ▶ many-body problem **hard to solve** using basis expansion!

# Systematic decoupling of high-momentum physics: The Similarity Renormalization Group

- generate unitary transformation which **decouples** low- and high momenta:

$$H_\lambda = U_\lambda H U_\lambda^\dagger \quad \text{with the resolution parameter } \lambda$$

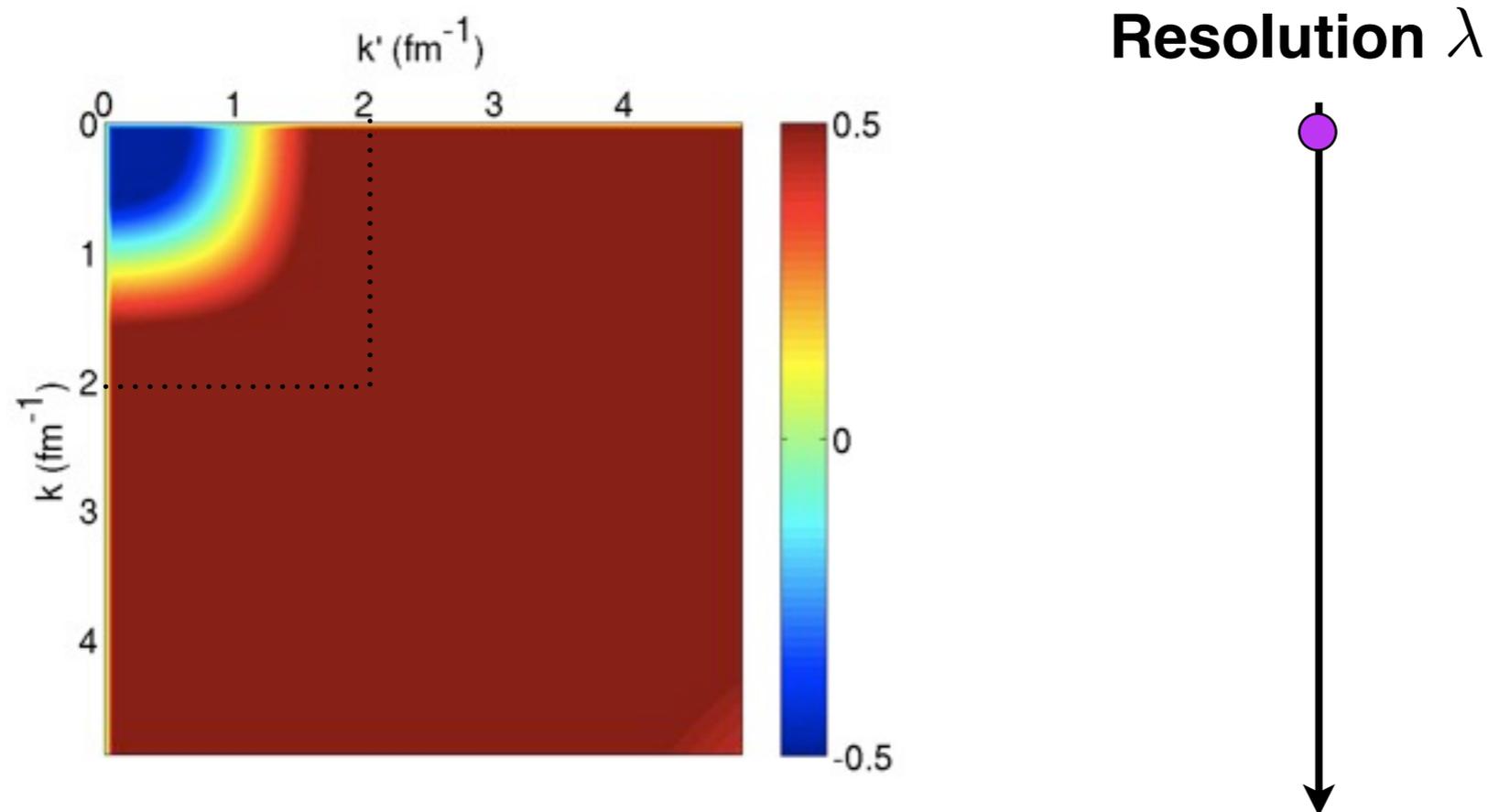
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  - generator  $\eta_\lambda$  can be chosen and **tailored** to different applications
  - observables are **preserved** due to unitarity of transformation
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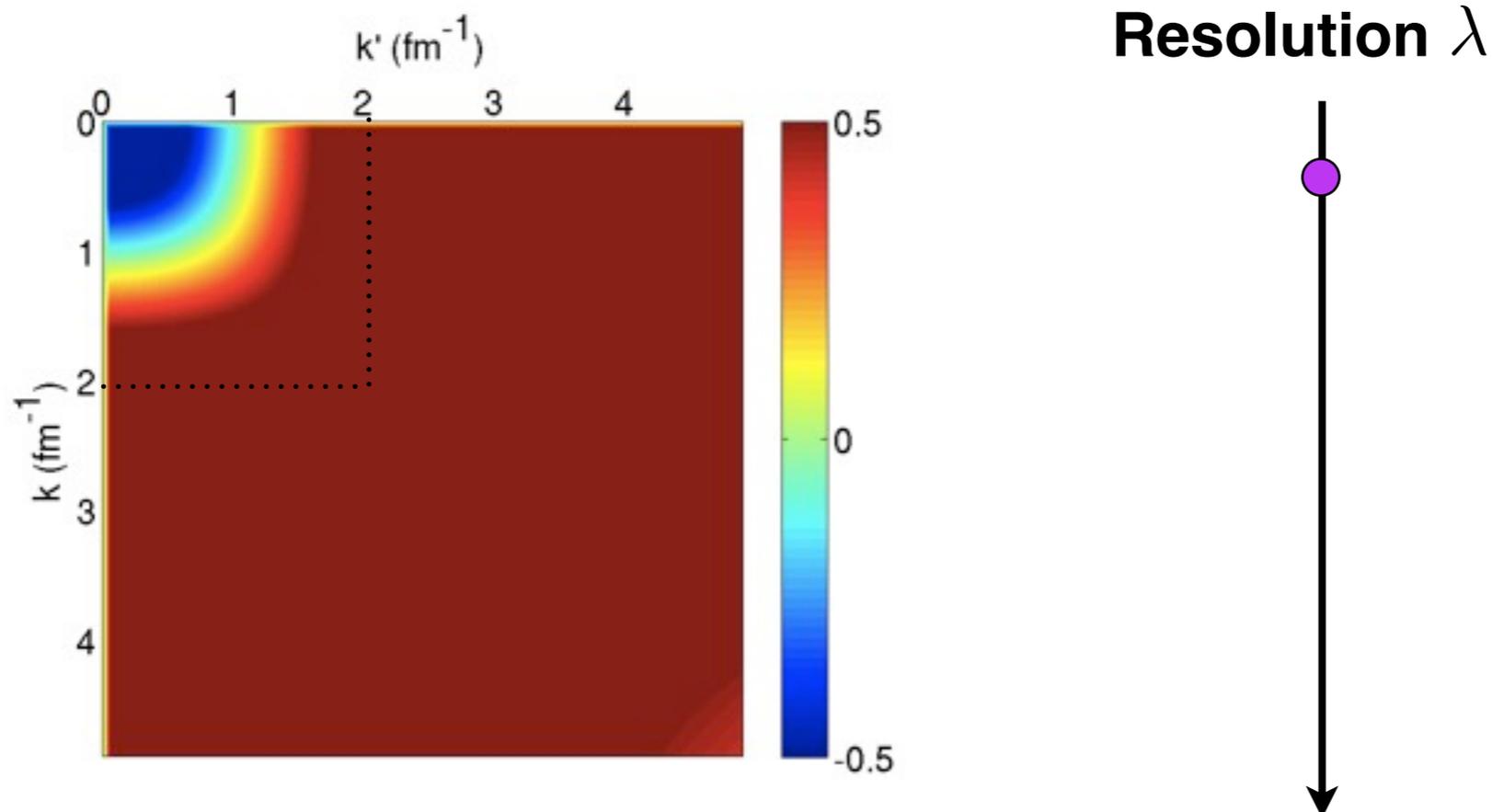


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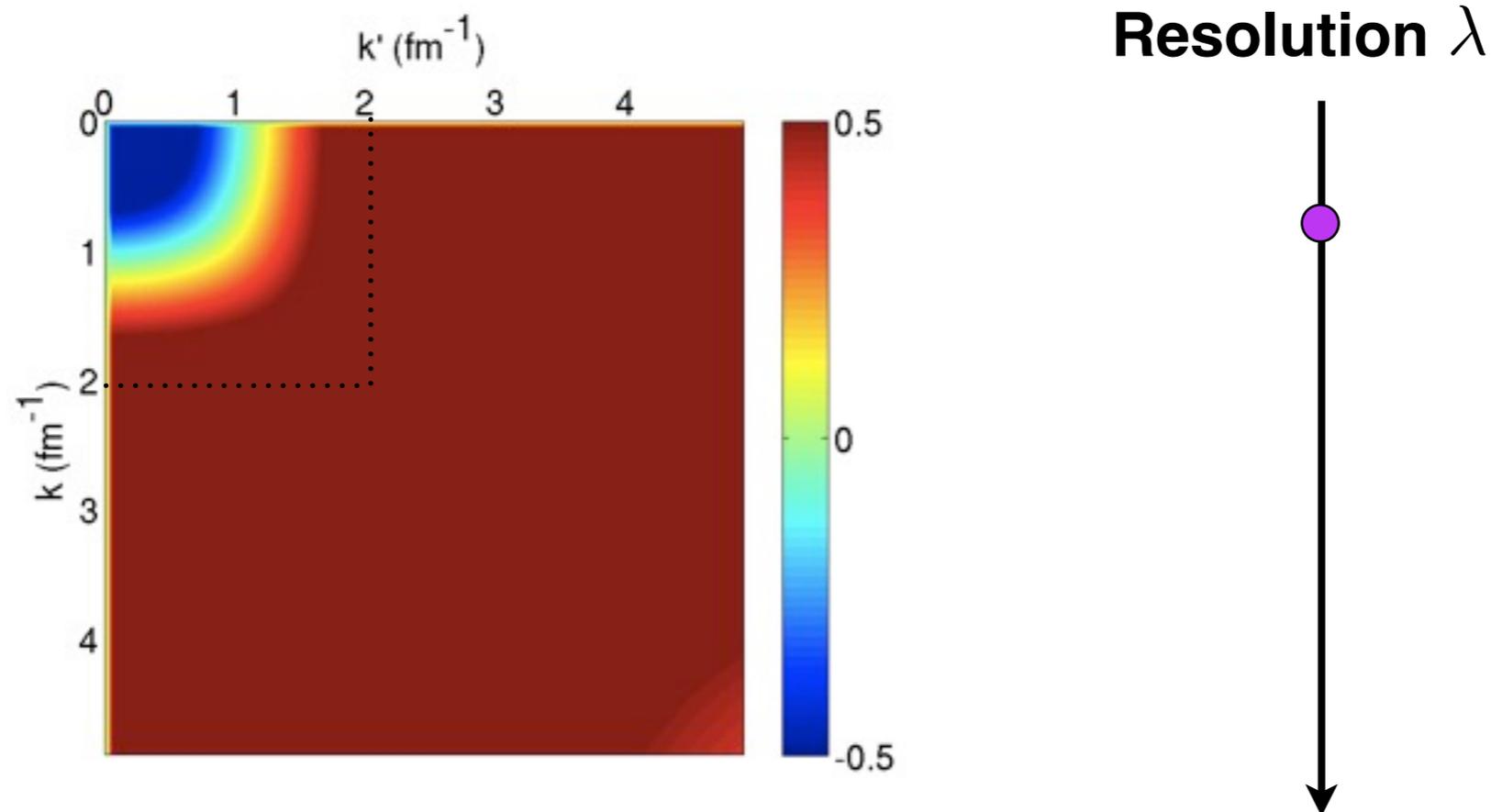


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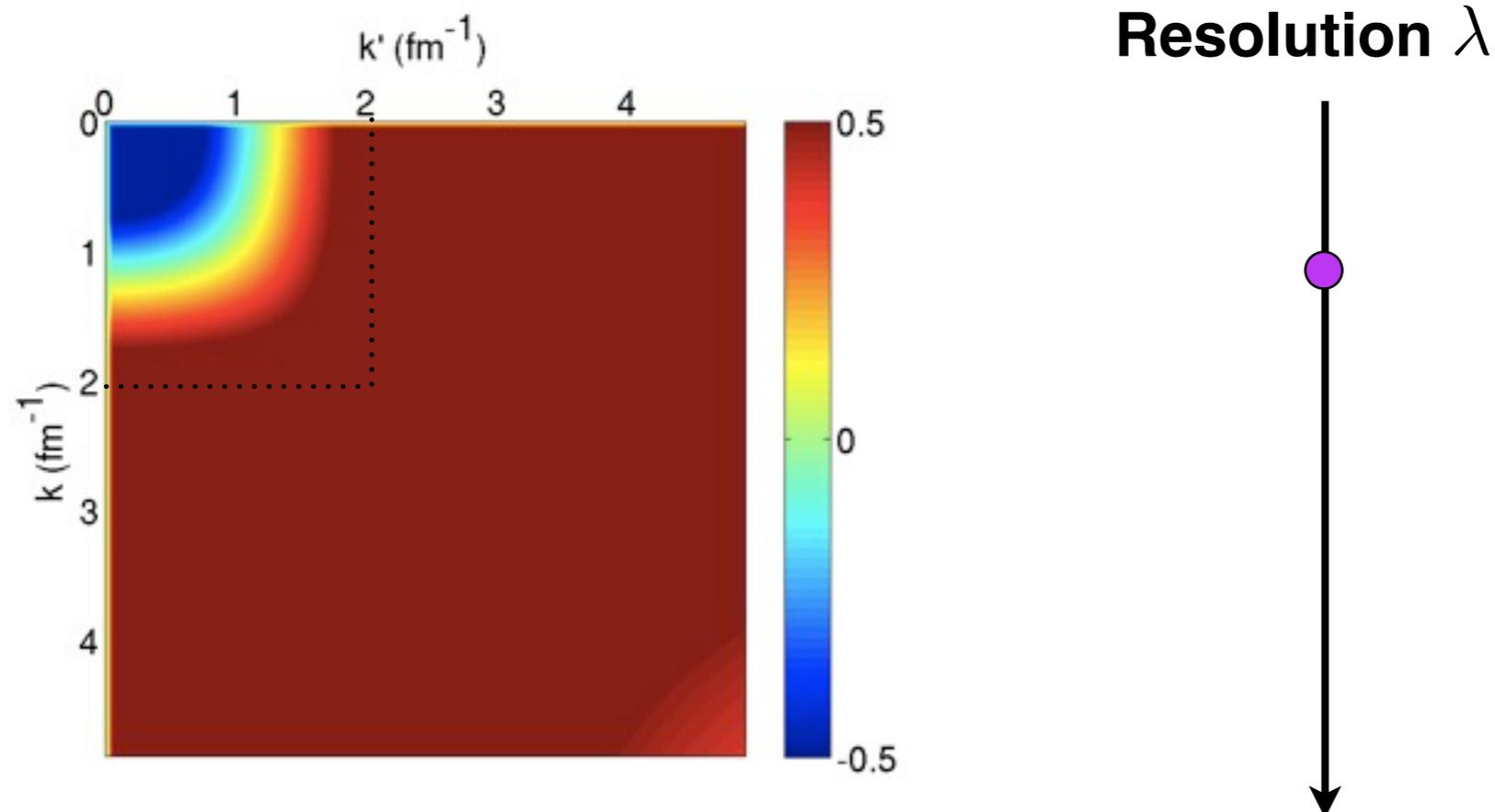


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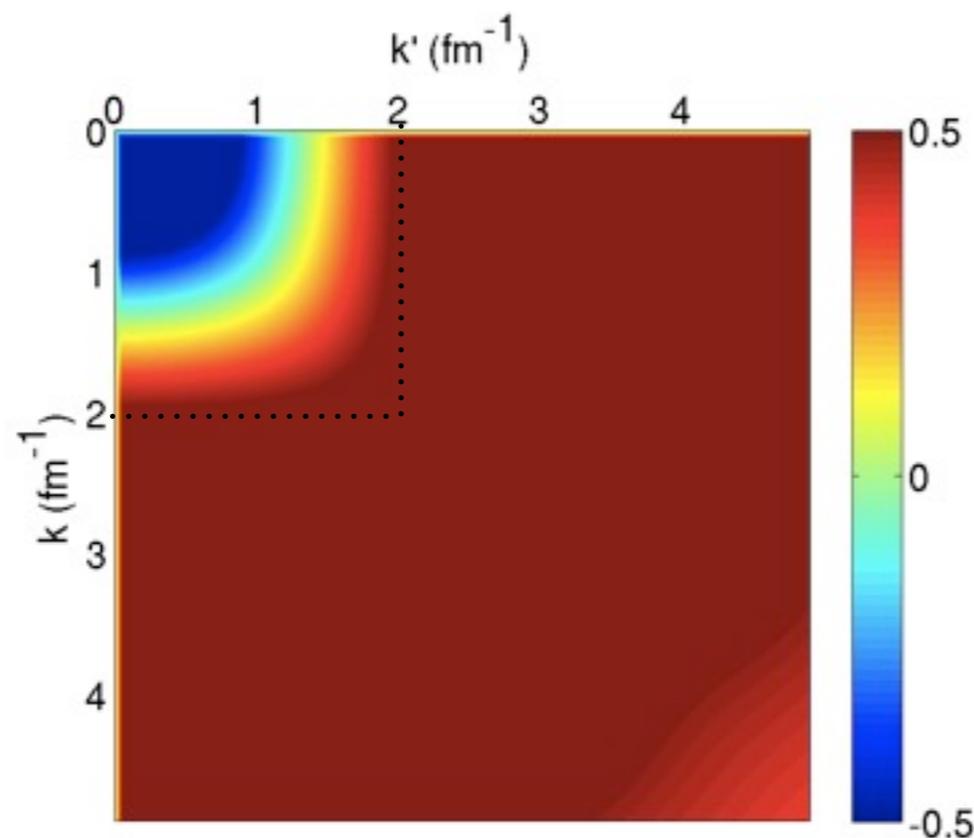


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Resolution  $\lambda$

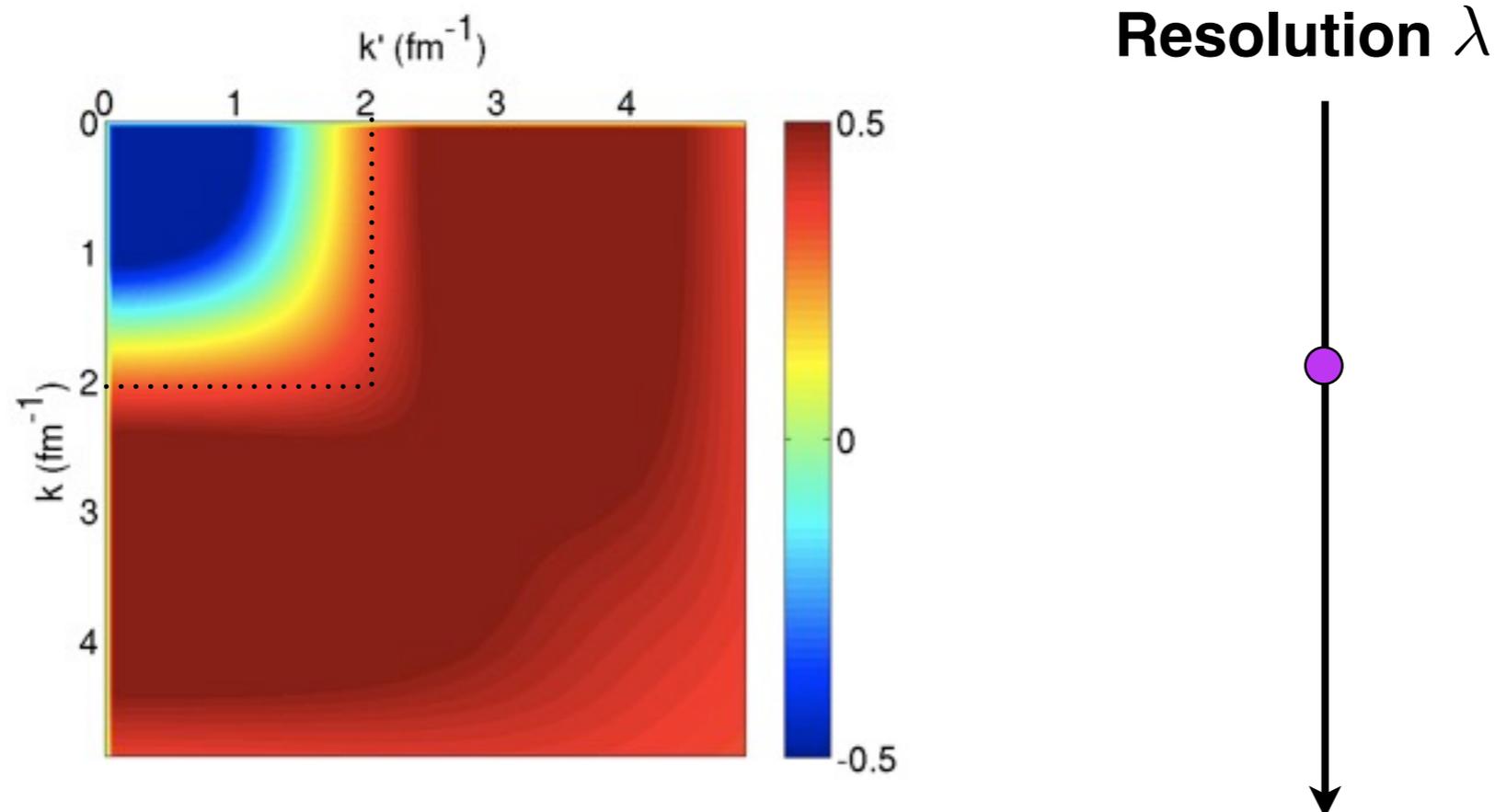


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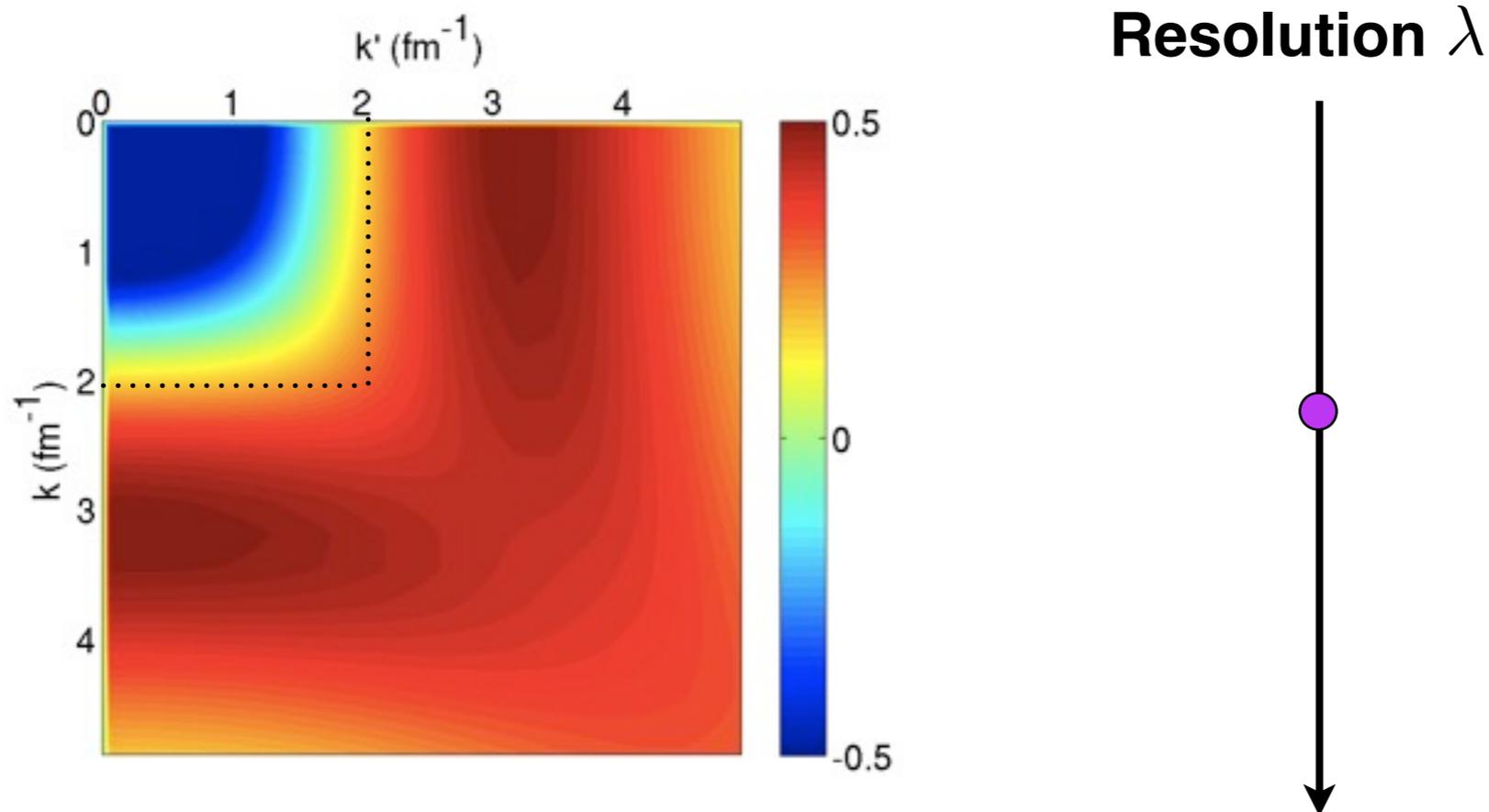


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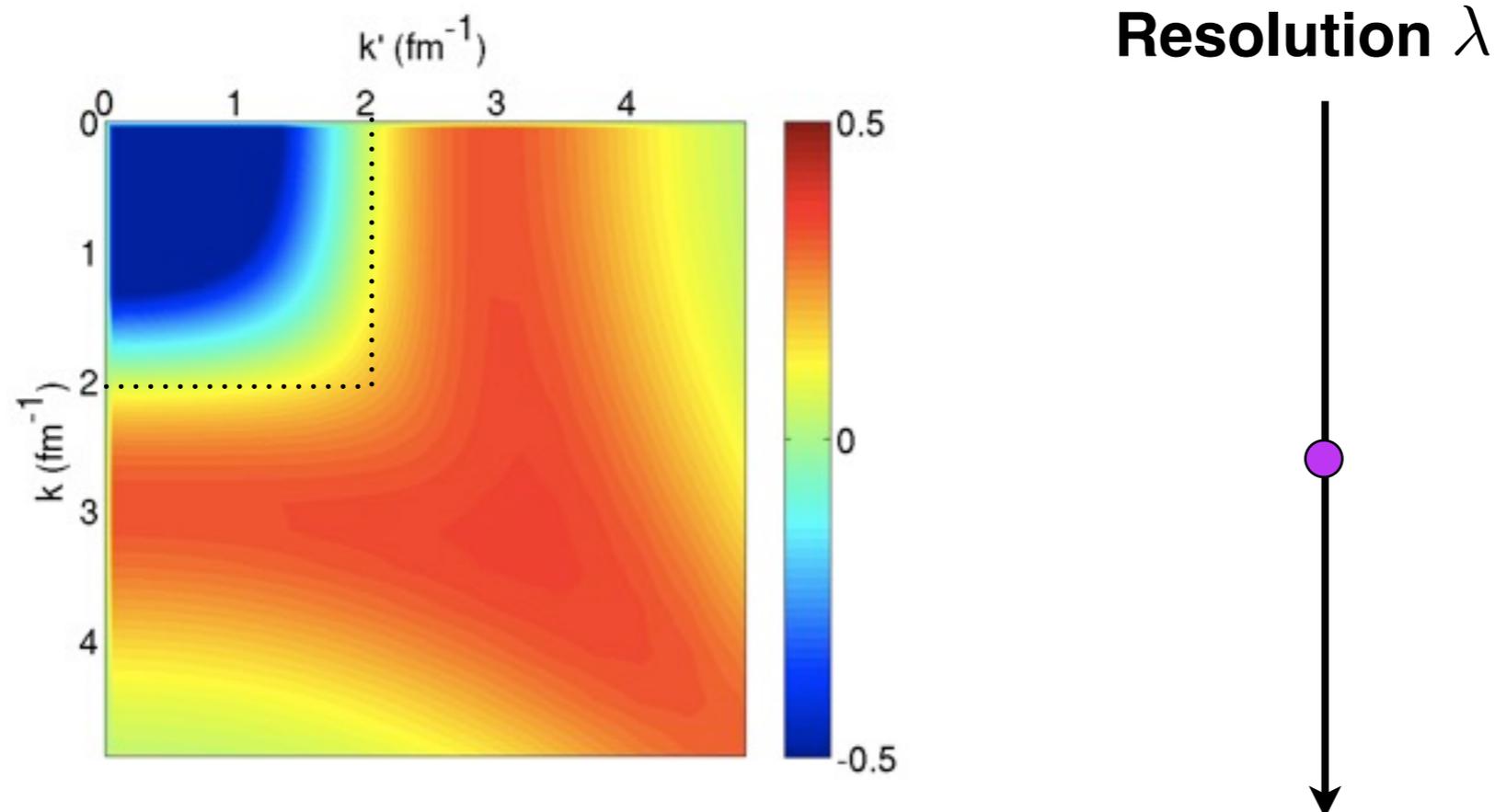


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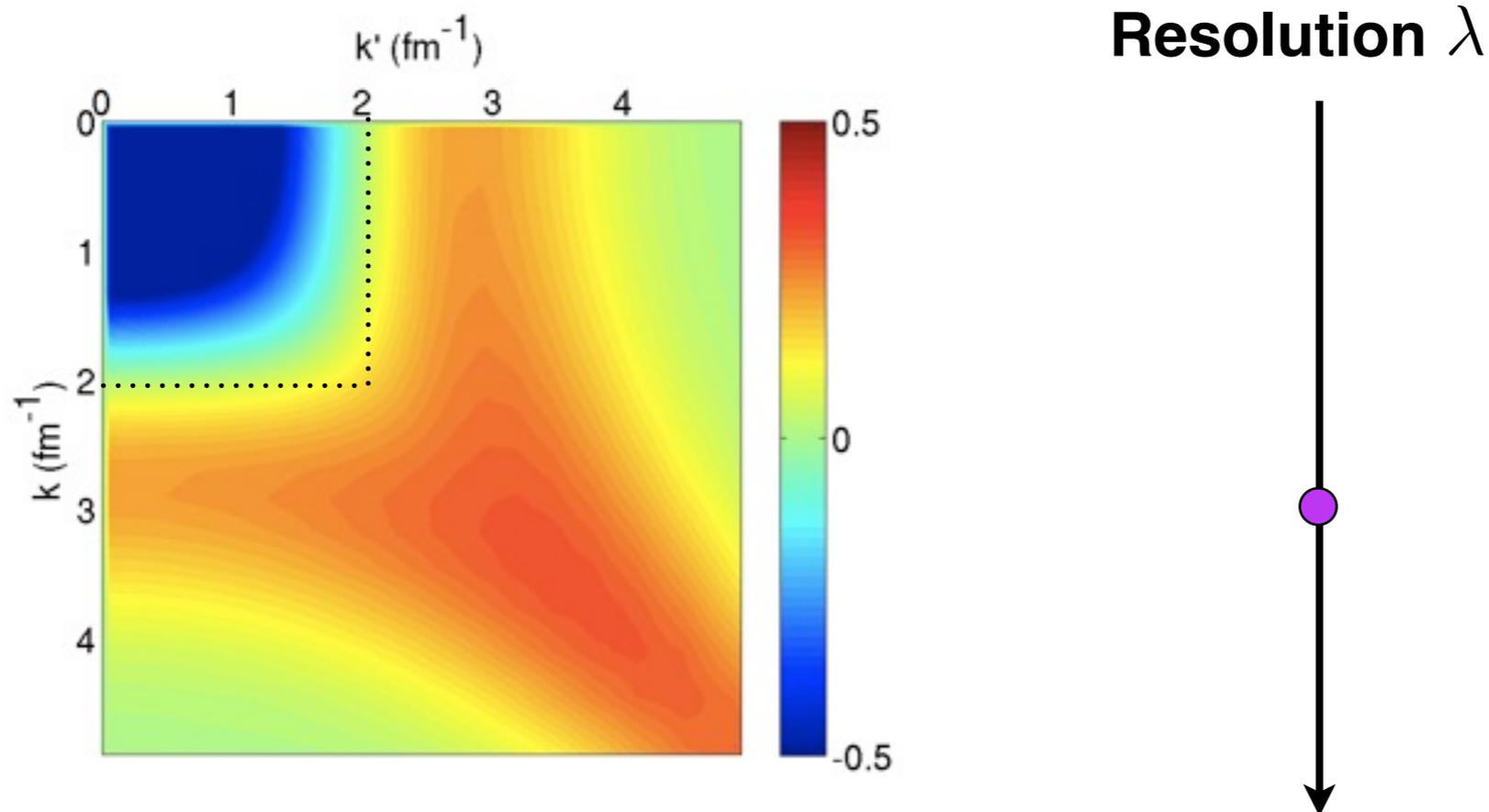


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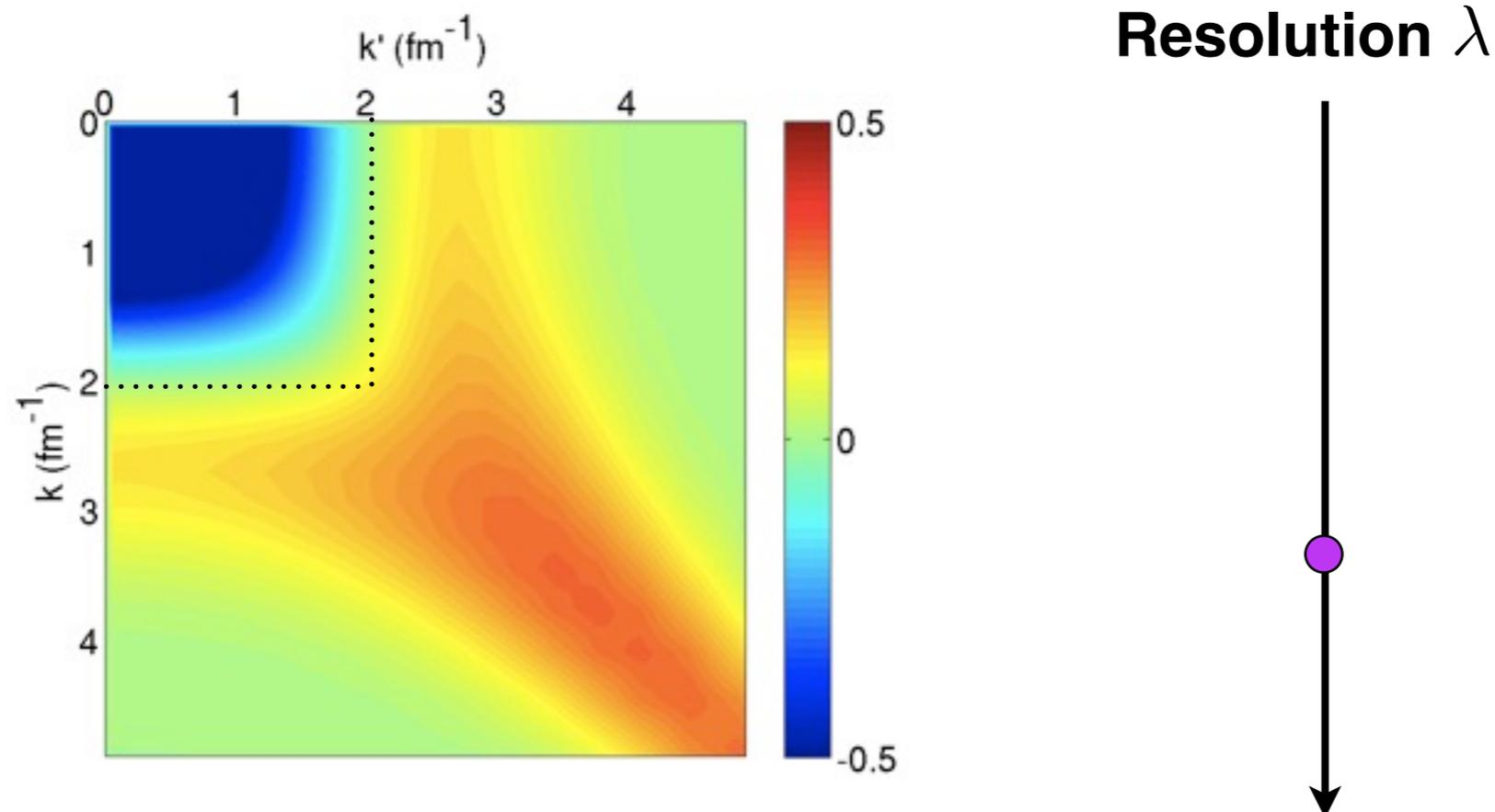


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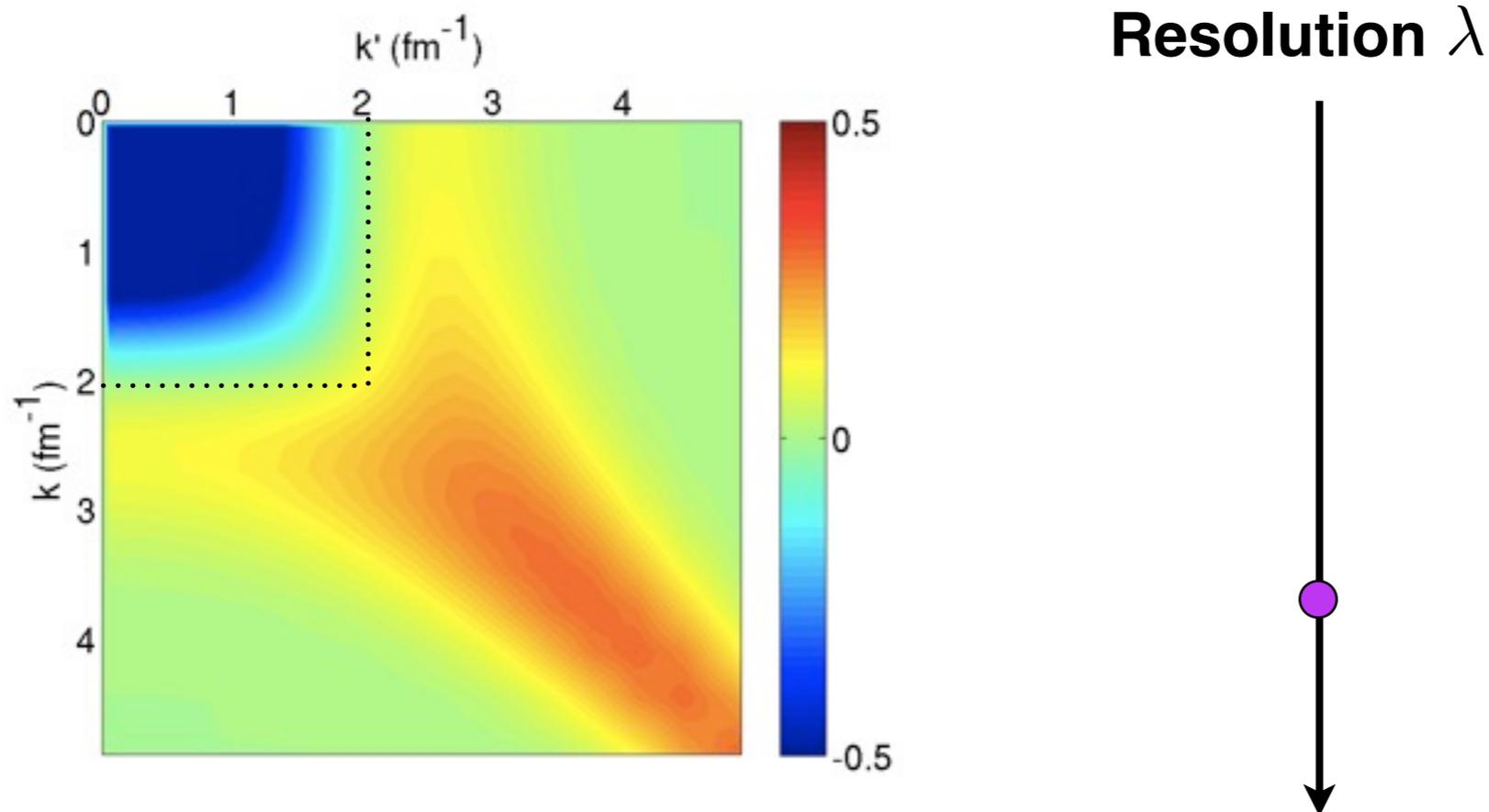


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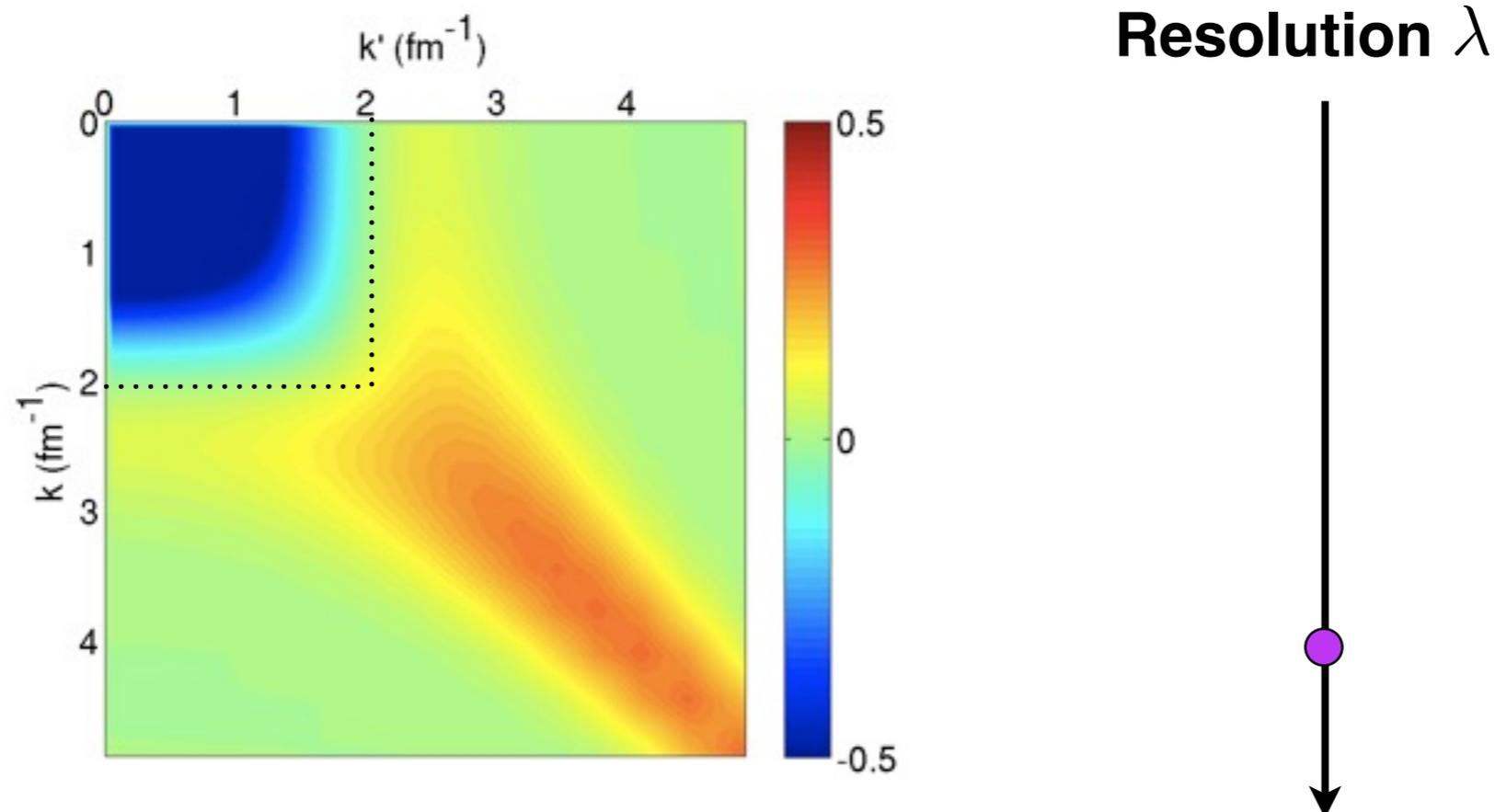


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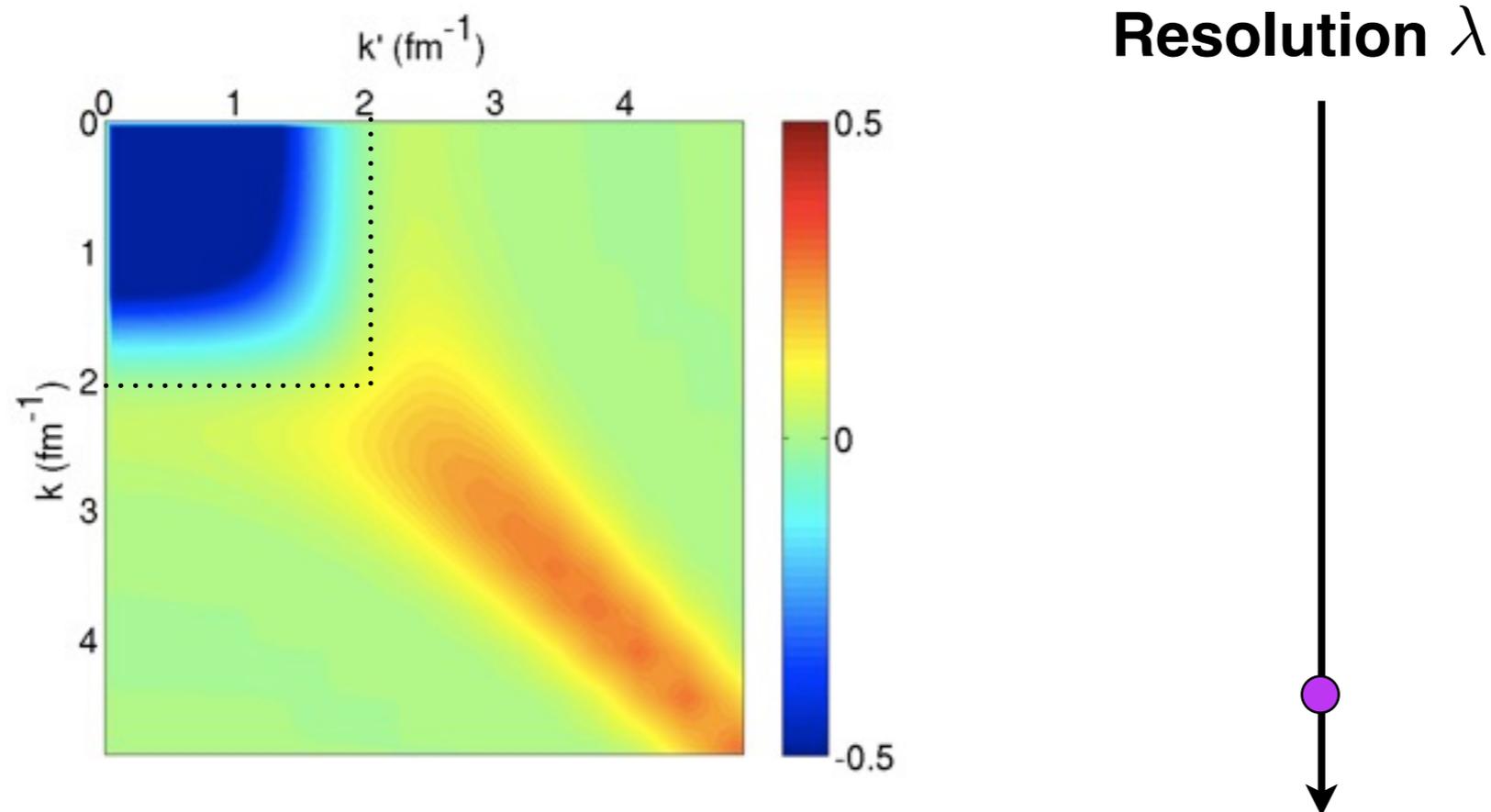


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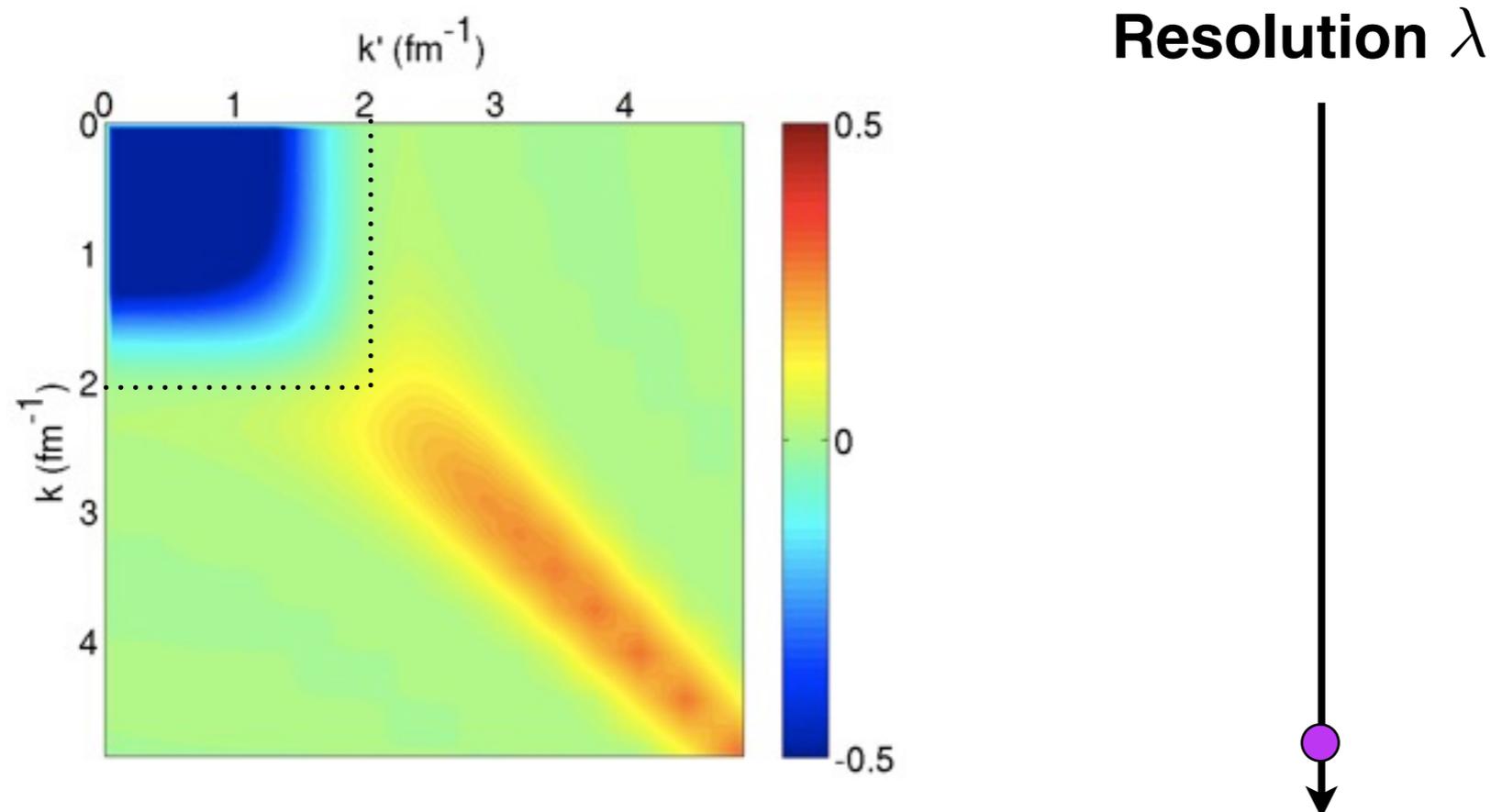


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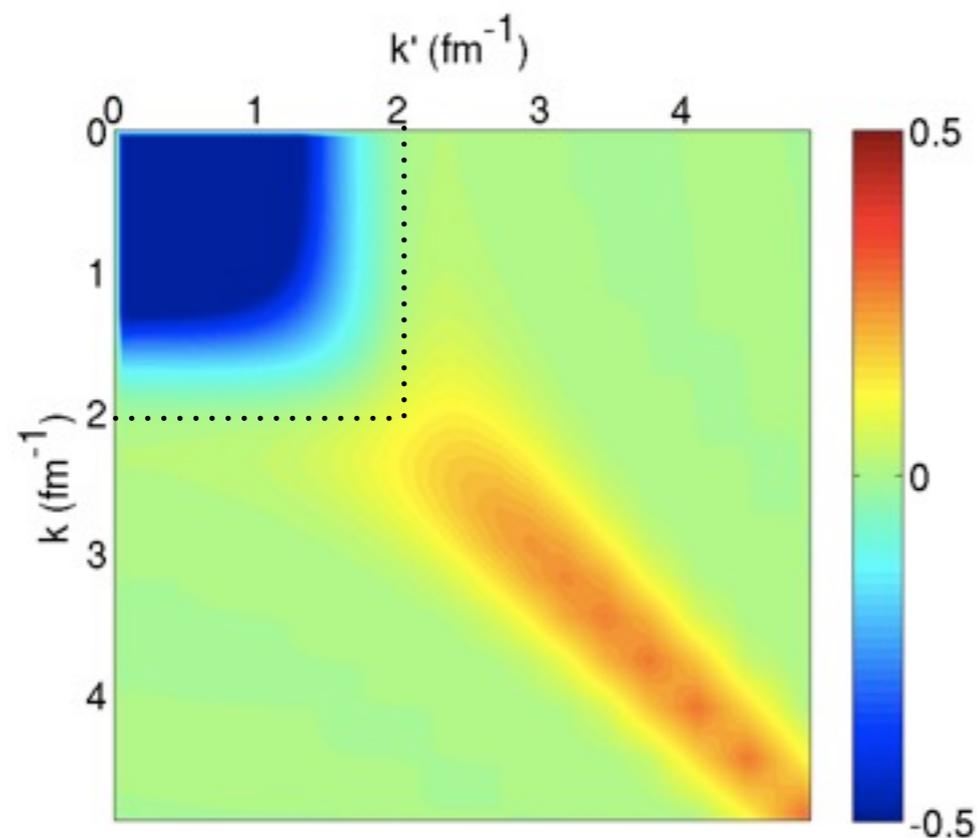
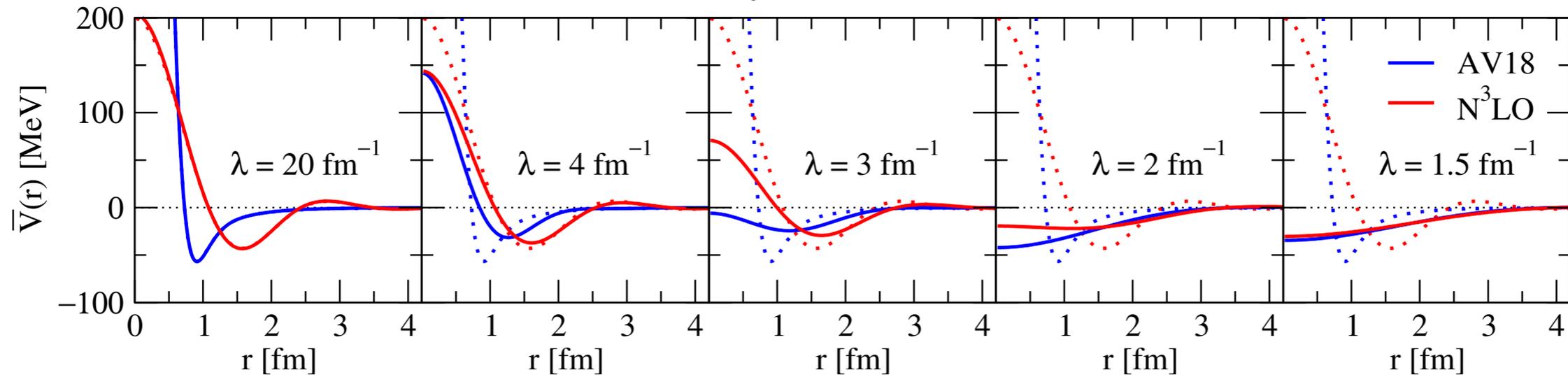
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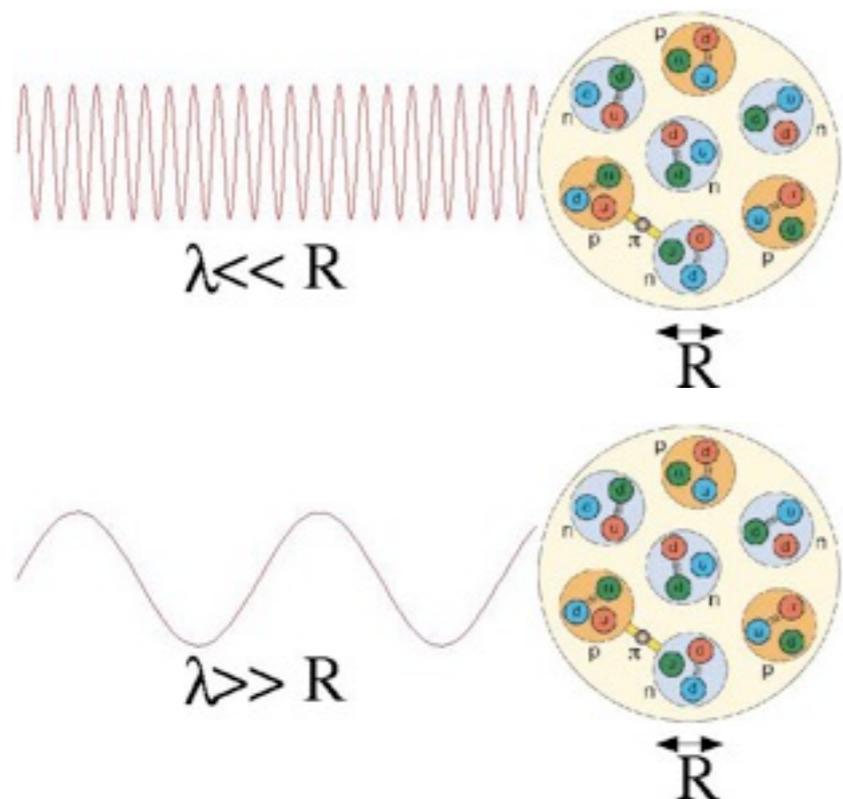
$$\bar{V}_\lambda(r) = \int dr' r'^2 V_\lambda(r, r')$$



**Resolution  $\lambda$**

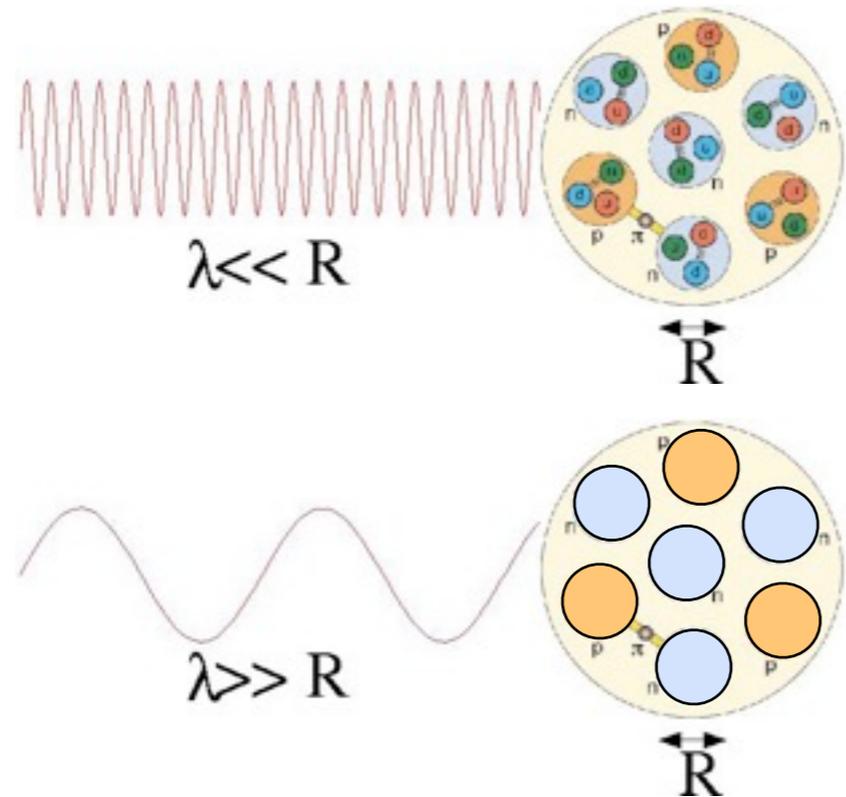


# Nuclear effective degrees of freedom



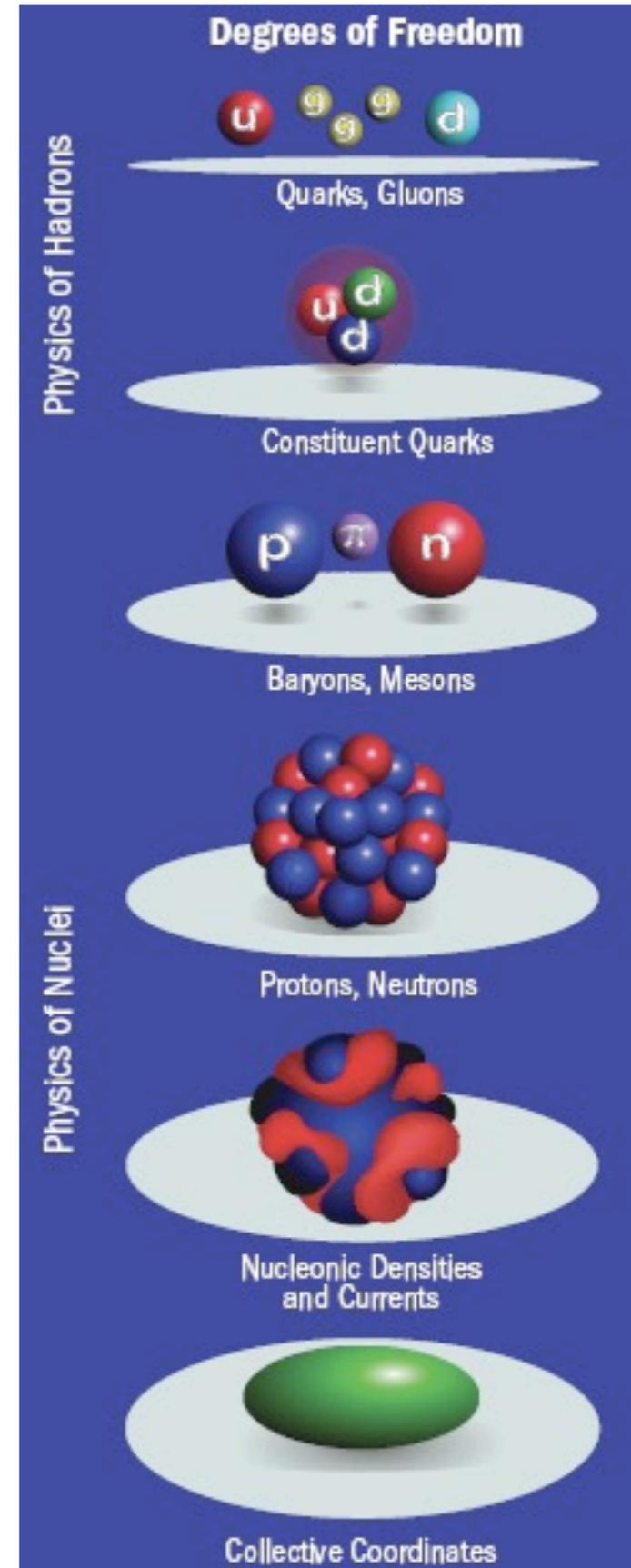
- if a nucleus is probed at high energies, nucleon substructure is resolved
- at low energies, details are not resolved

# Nuclear effective degrees of freedom



- if a nucleus is probed at high energies, nucleon substructure is resolved
- at low energies, details are not resolved
- replace fine structure by something simpler (compare multipole expansion)

→ effective field theory

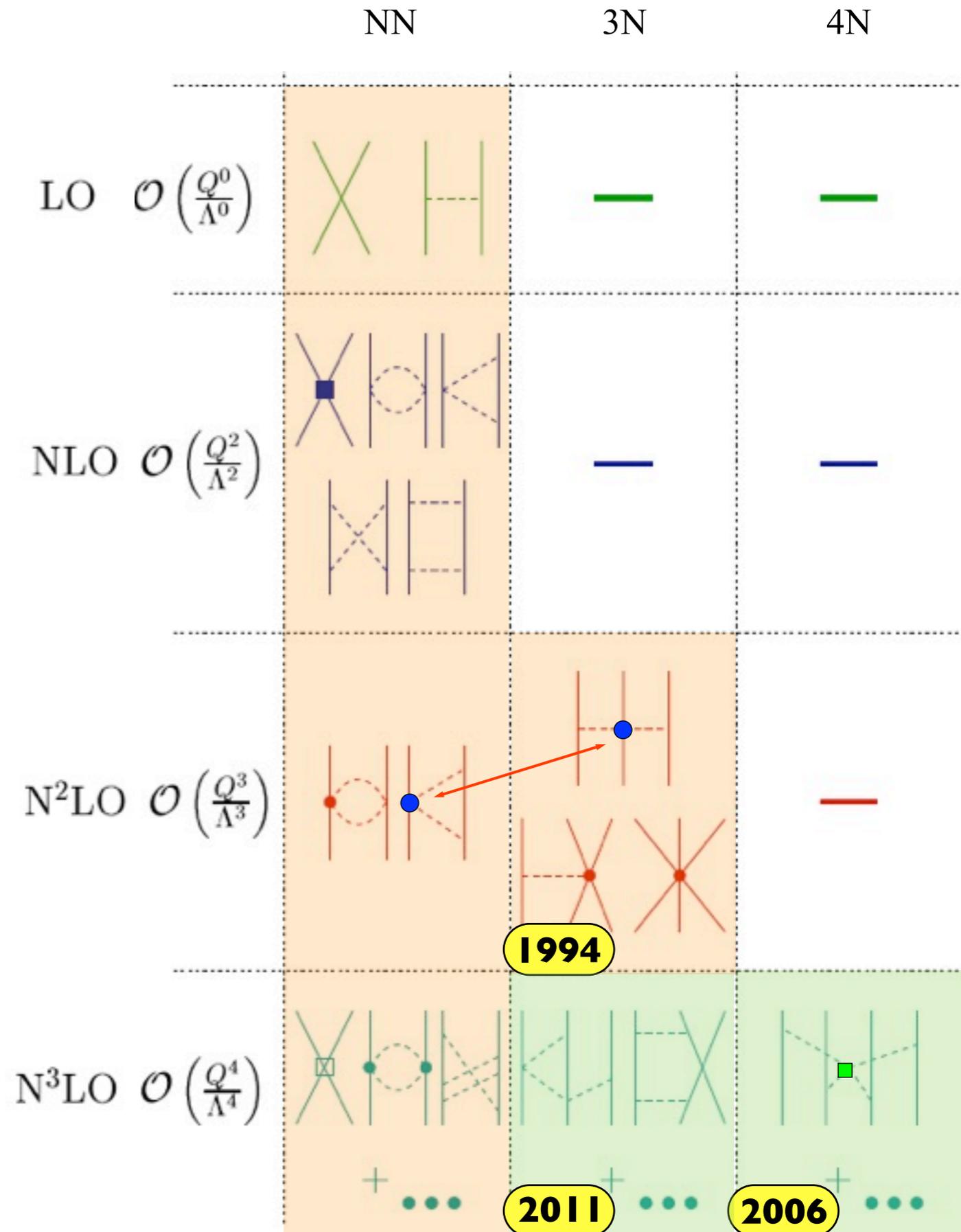


Resolution



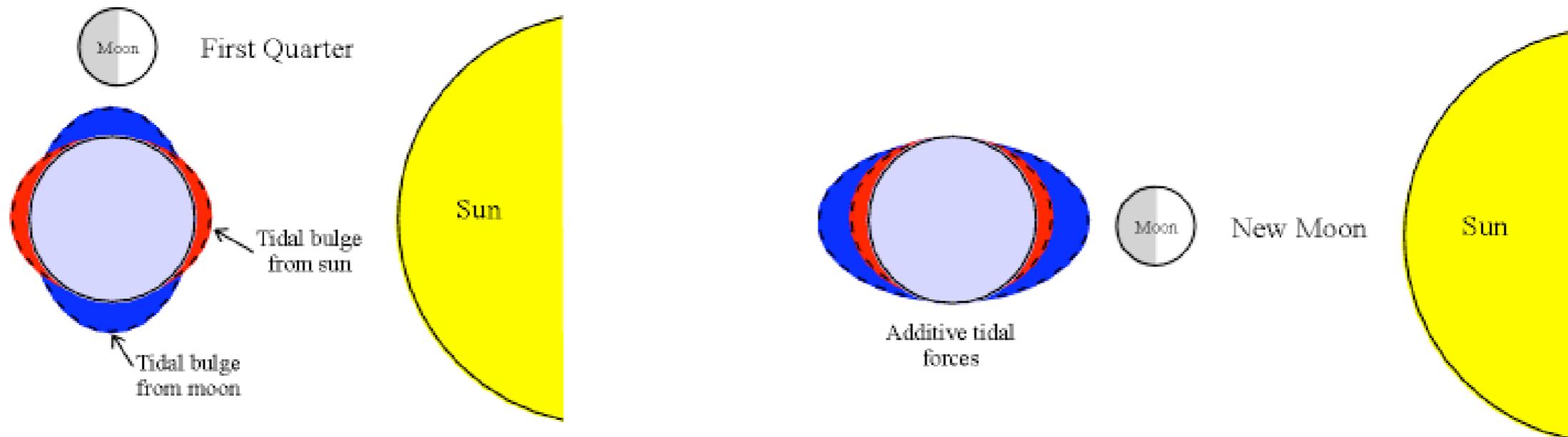
# Chiral effective field theory for nuclear forces

- choose relevant degrees of freedom: here nucleons and pions
- operators constrained by symmetries of QCD
- short-range physics captured in short-range couplings
- separation of scales:  $Q \ll \Lambda_b$ , breakdown scale  $\Lambda_b \sim 500$  MeV
- power-counting: expand in  $Q/\Lambda_b$
- systematic, obtain error estimates
- many-body forces appear naturally



# Aren't 3N forces unnatural? Do we really need them?

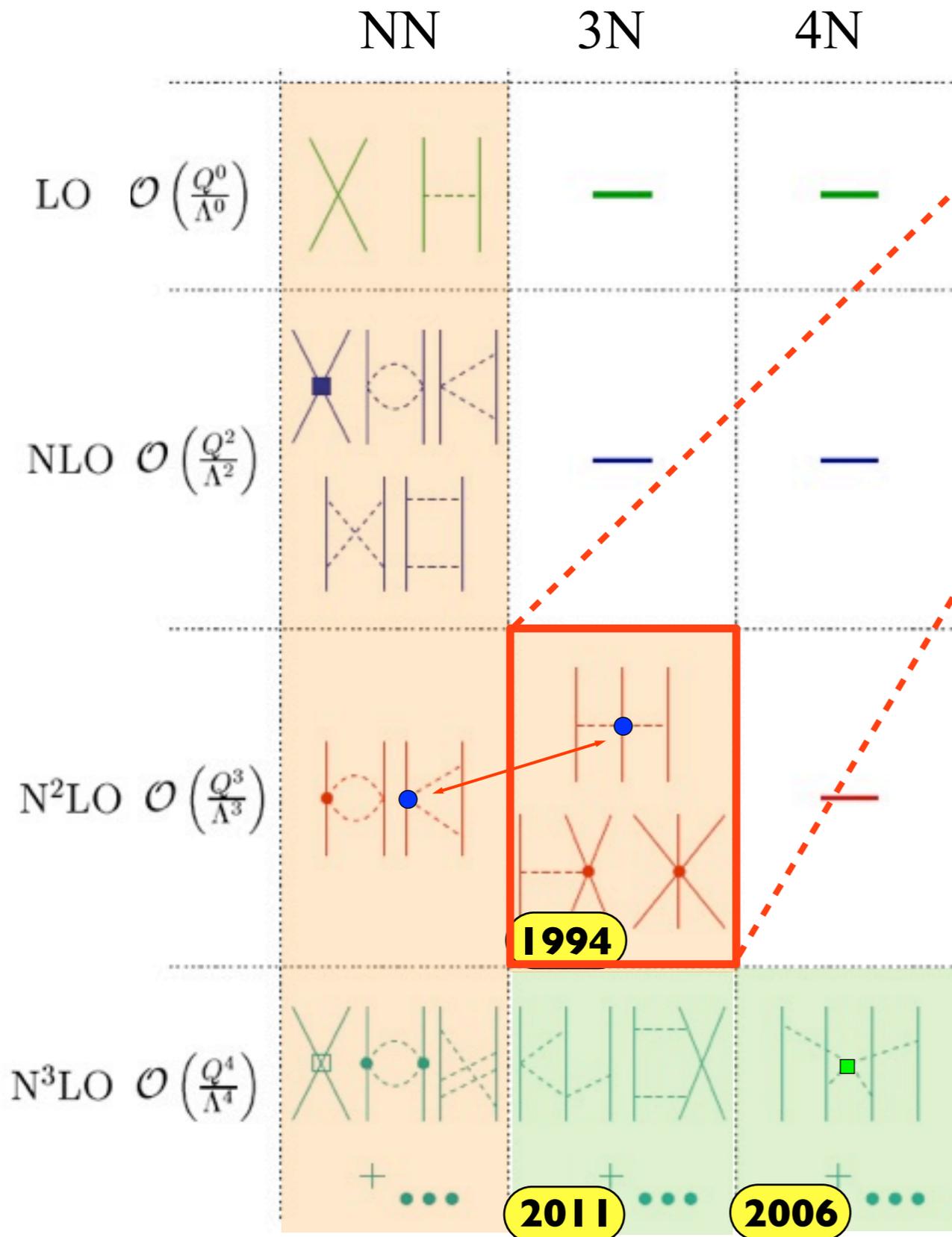
Consider classical analog: tidal effects in earth-sun-moon system



- force between earth and moon depends on the position of sun
- tidal deformations represent internal excitations
- describe system using point particles  $\longrightarrow$  3N forces inevitable!

- 
- nucleons are composite particles, can also be excited
  - change of resolution change excitations that can be described explicitly
    - ▶ existence of three-nucleon forces natural
    - ▶ crucial question: how important are their contributions?

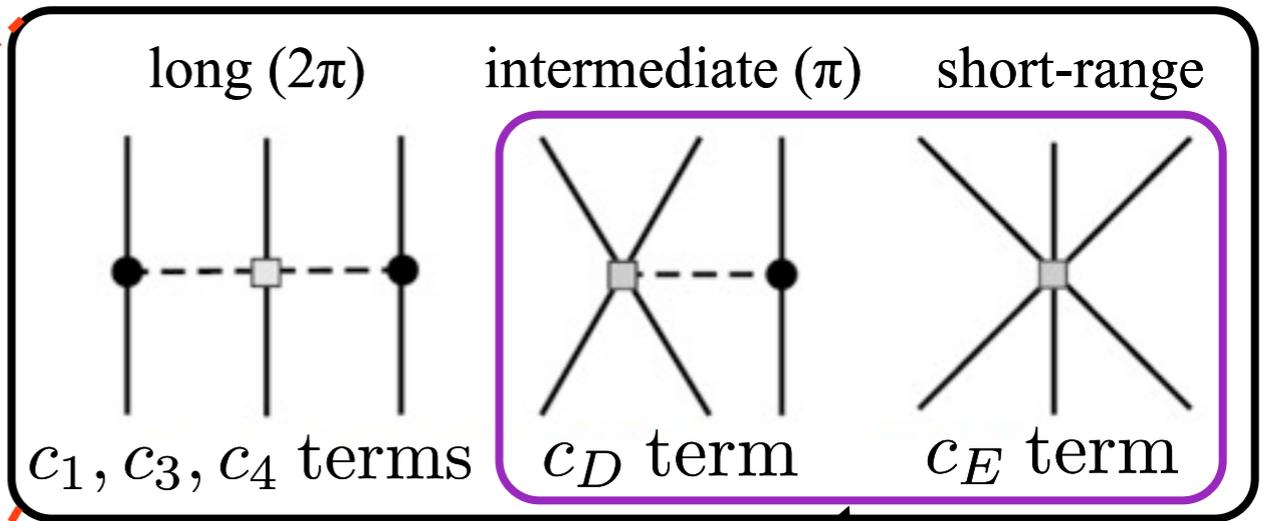
# Many-body forces in chiral EFT



1994

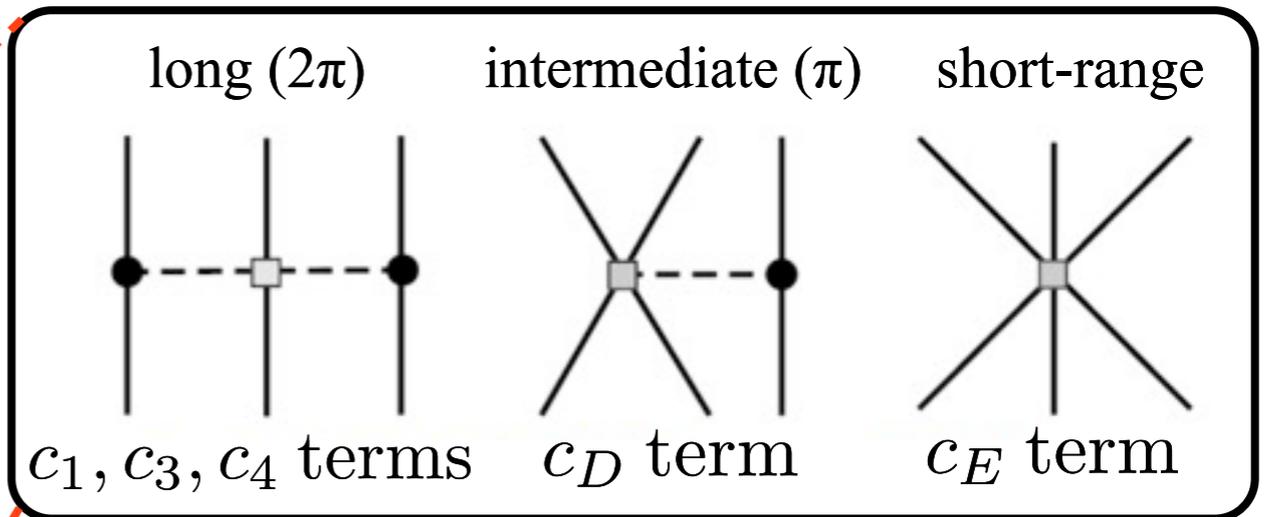
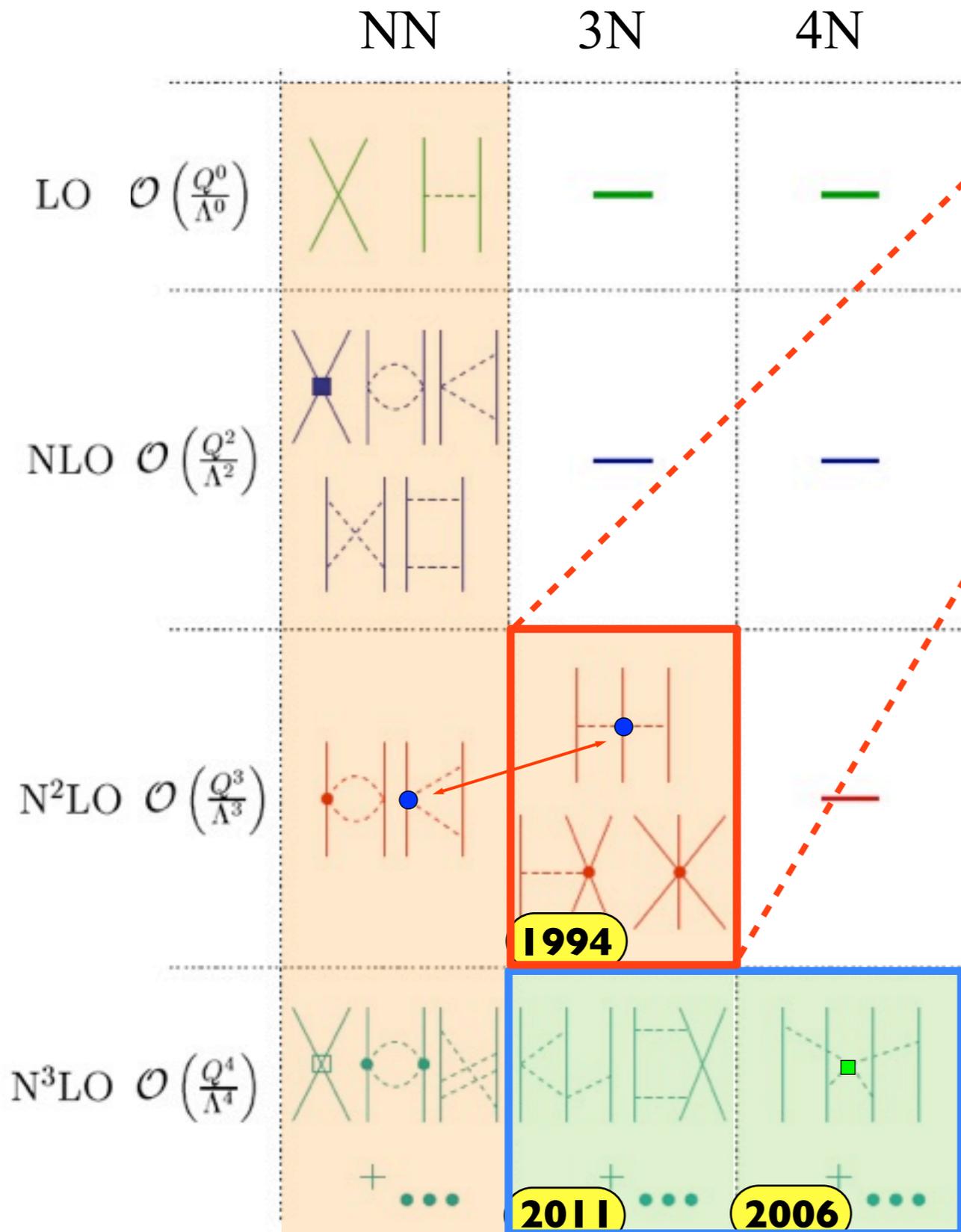
2011

2006



need to be fit to three-body and/or higher-body systems

# Many-body forces in chiral EFT



values of LECs  $c_1, c_3, c_4$  still contain large uncertainties!

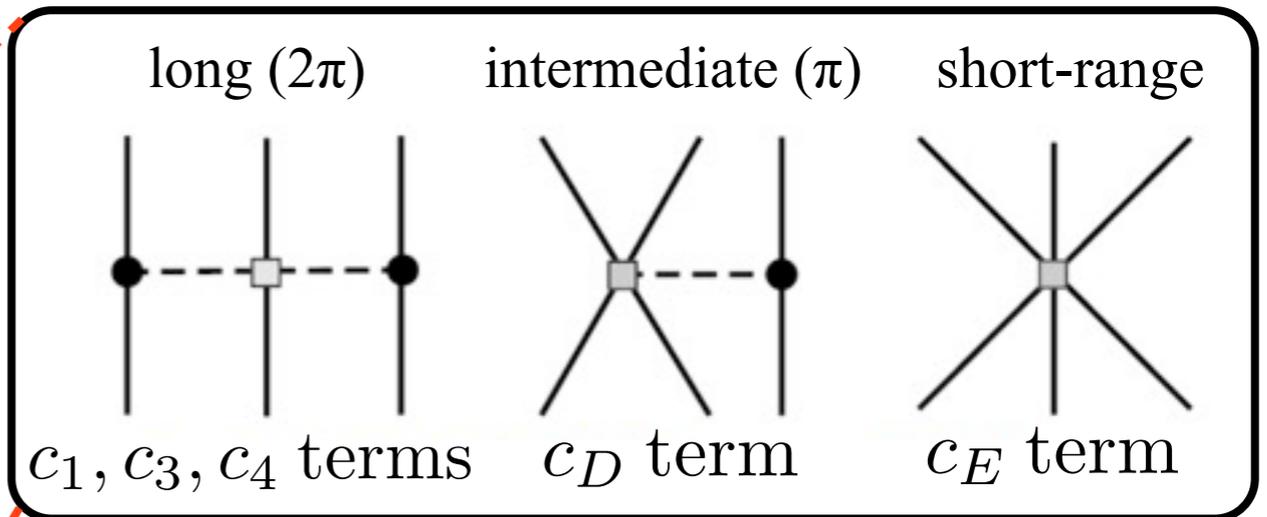
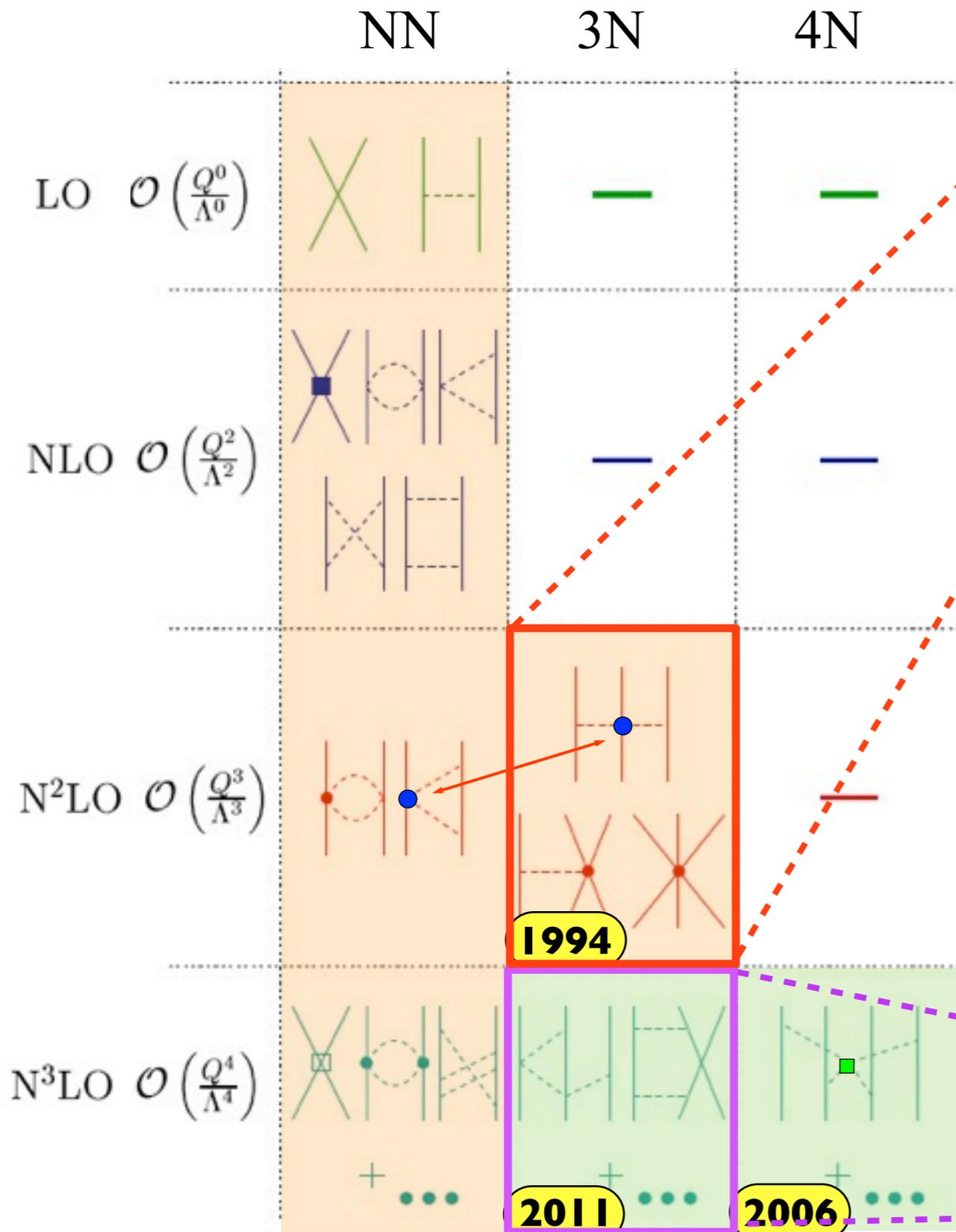
first incorporation in calculations of neutron and nuclear matter

Tews, Krüger, KH, Schwenk, PRL 110, 032504 (2013)

Krüger, Tews, KH, Schwenk, PRC 88, 025802 (2013)

**all terms predicted  
(no new low-energy couplings)**

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first calculation of matrix elements for ab initio studies of matter and nuclei

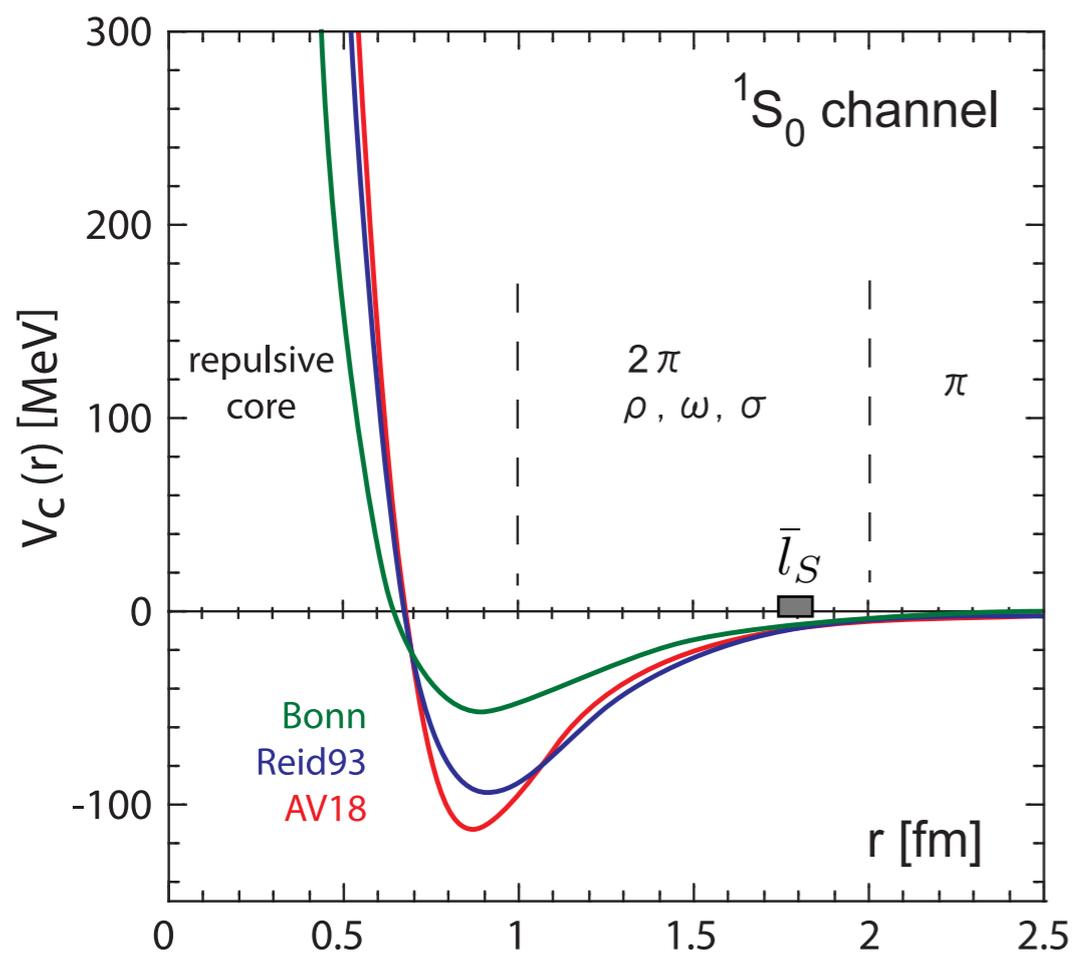
KH, Krebs, Epelbaum, Golak, Skibinski, PRC 91, 044001 (2015)

1994

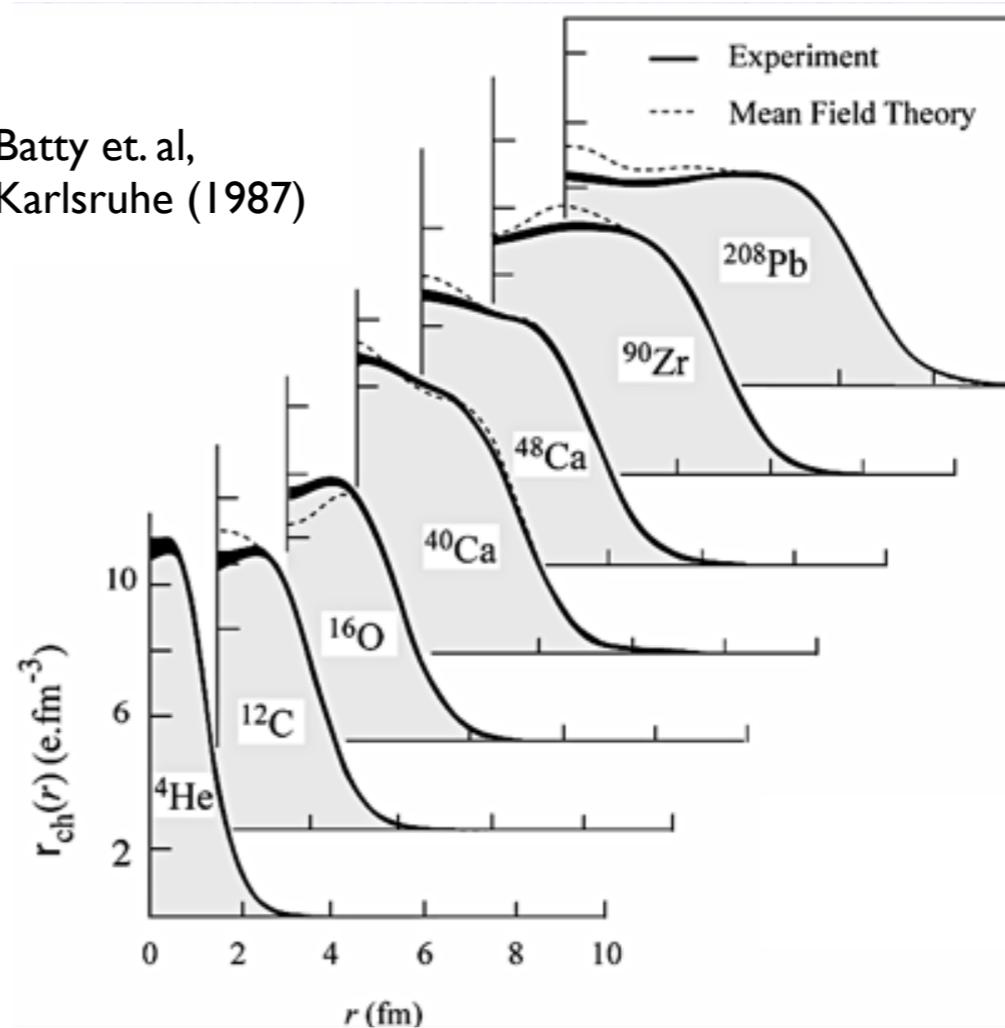
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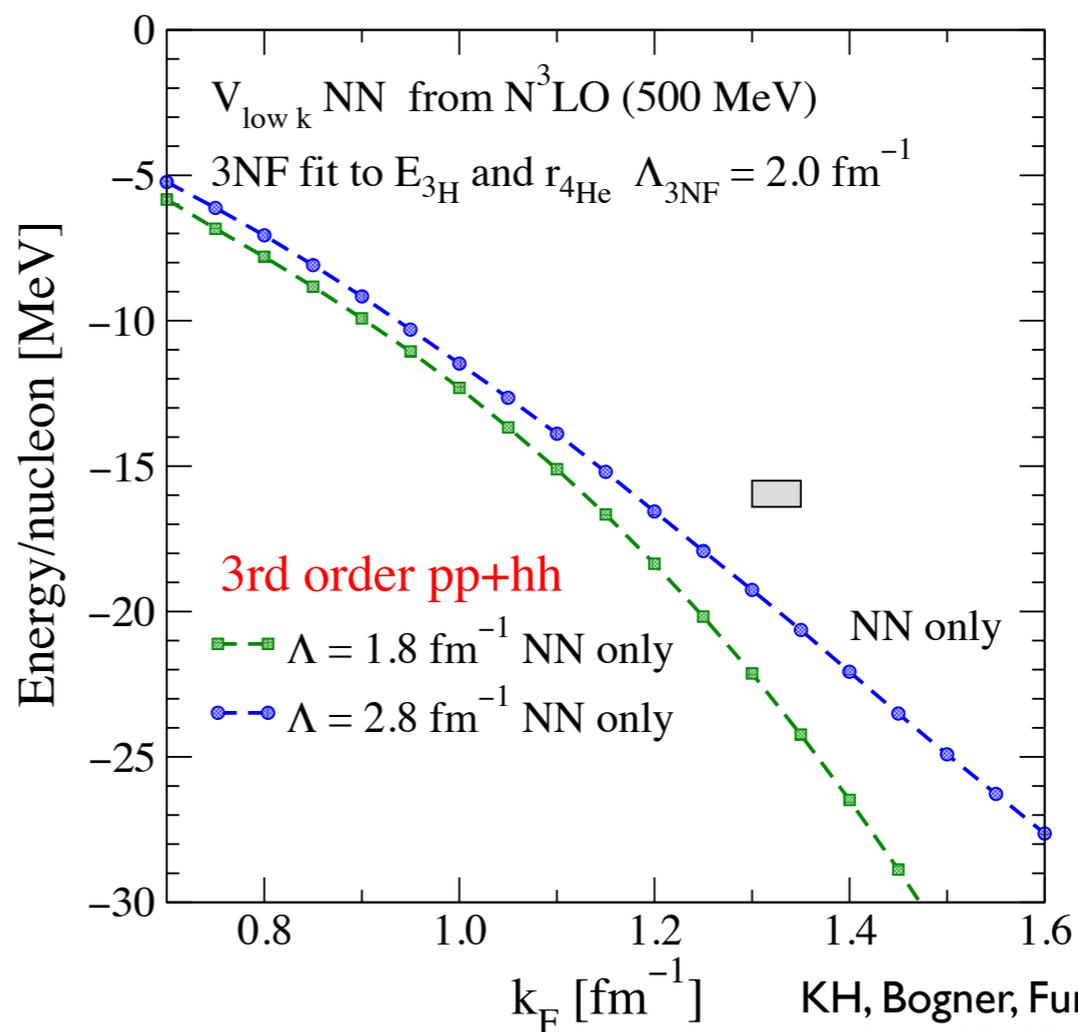
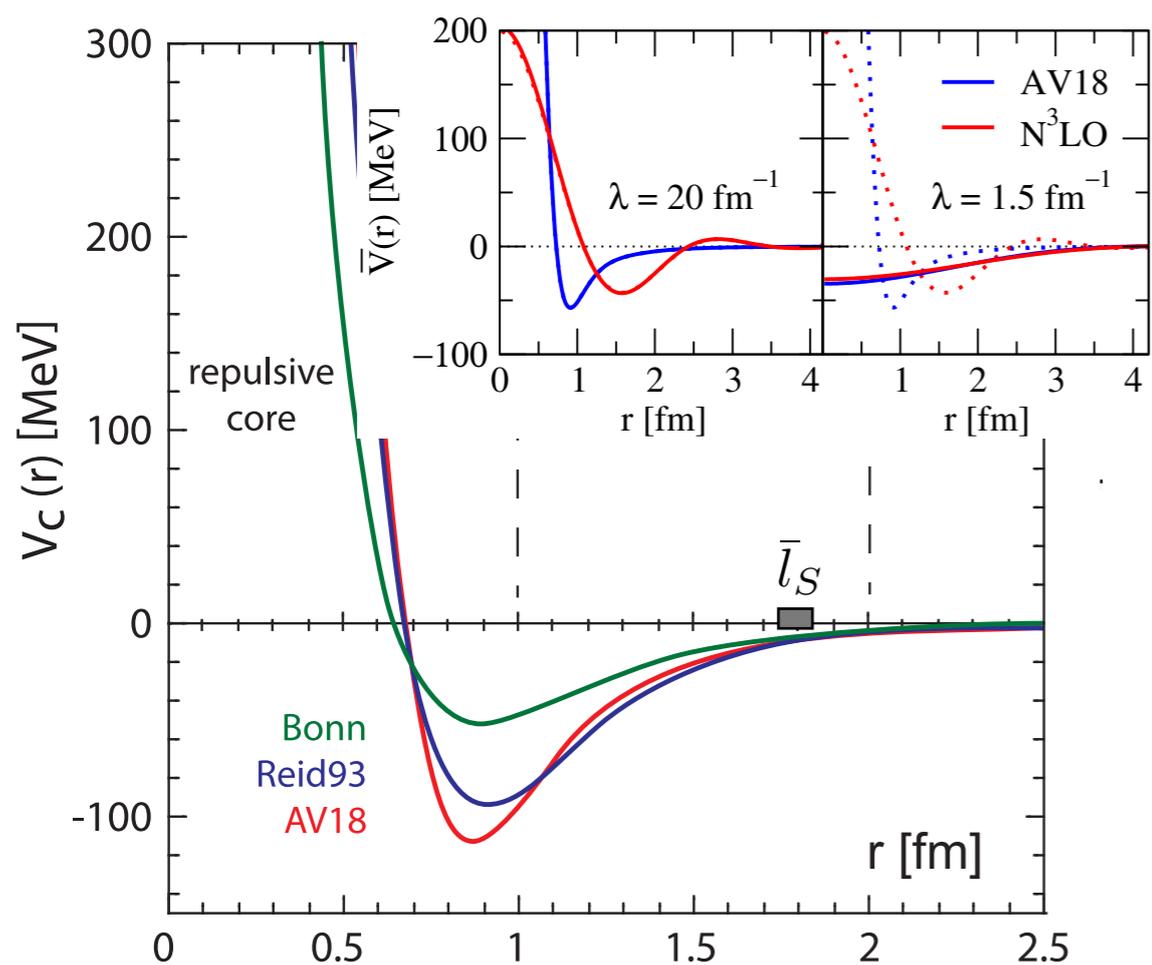
# Equation of state of symmetric nuclear matter: nuclear saturation



Batty et. al,  
Karlsruhe (1987)



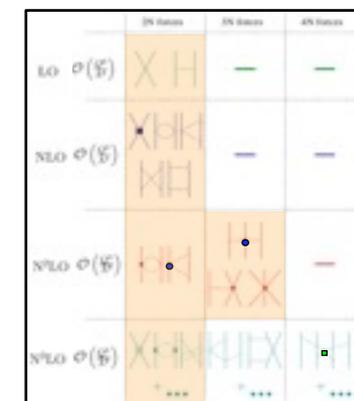
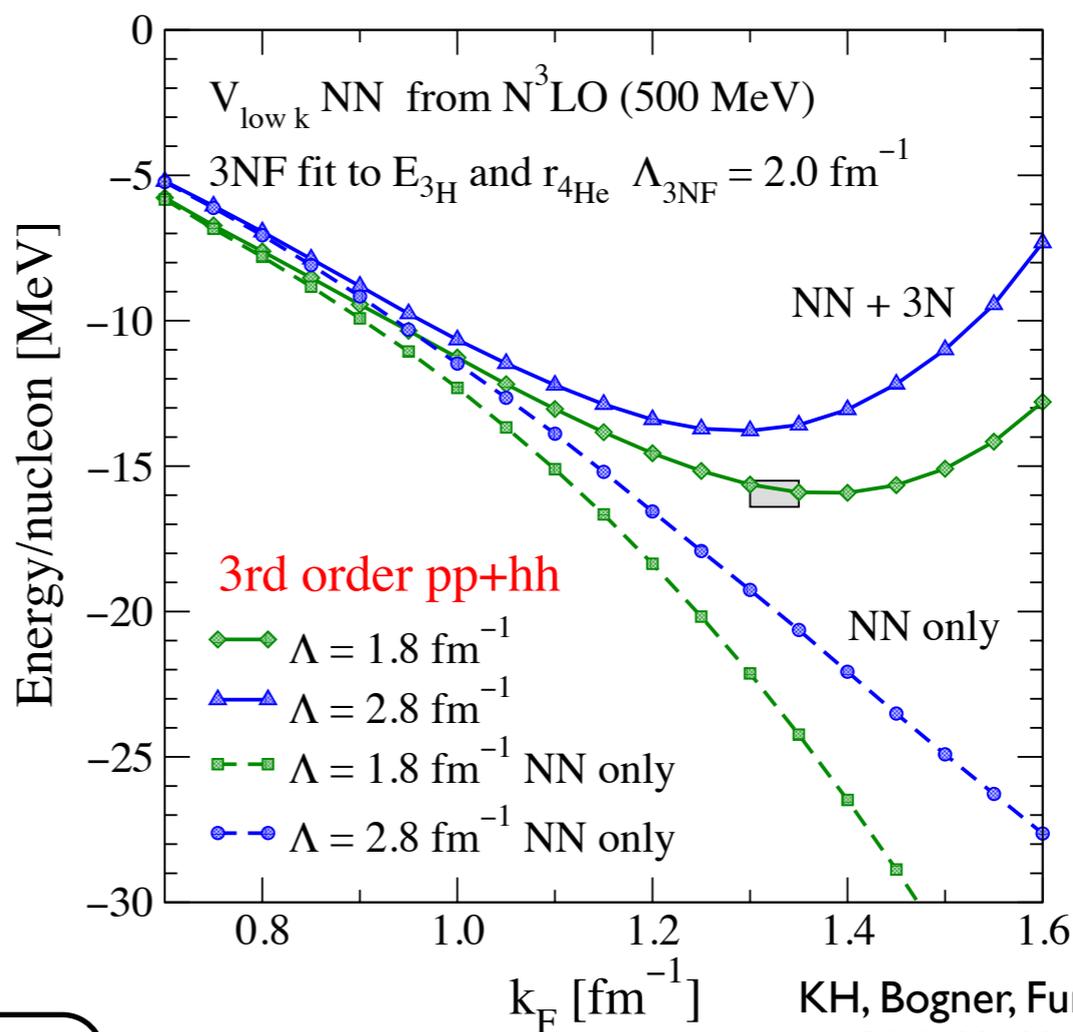
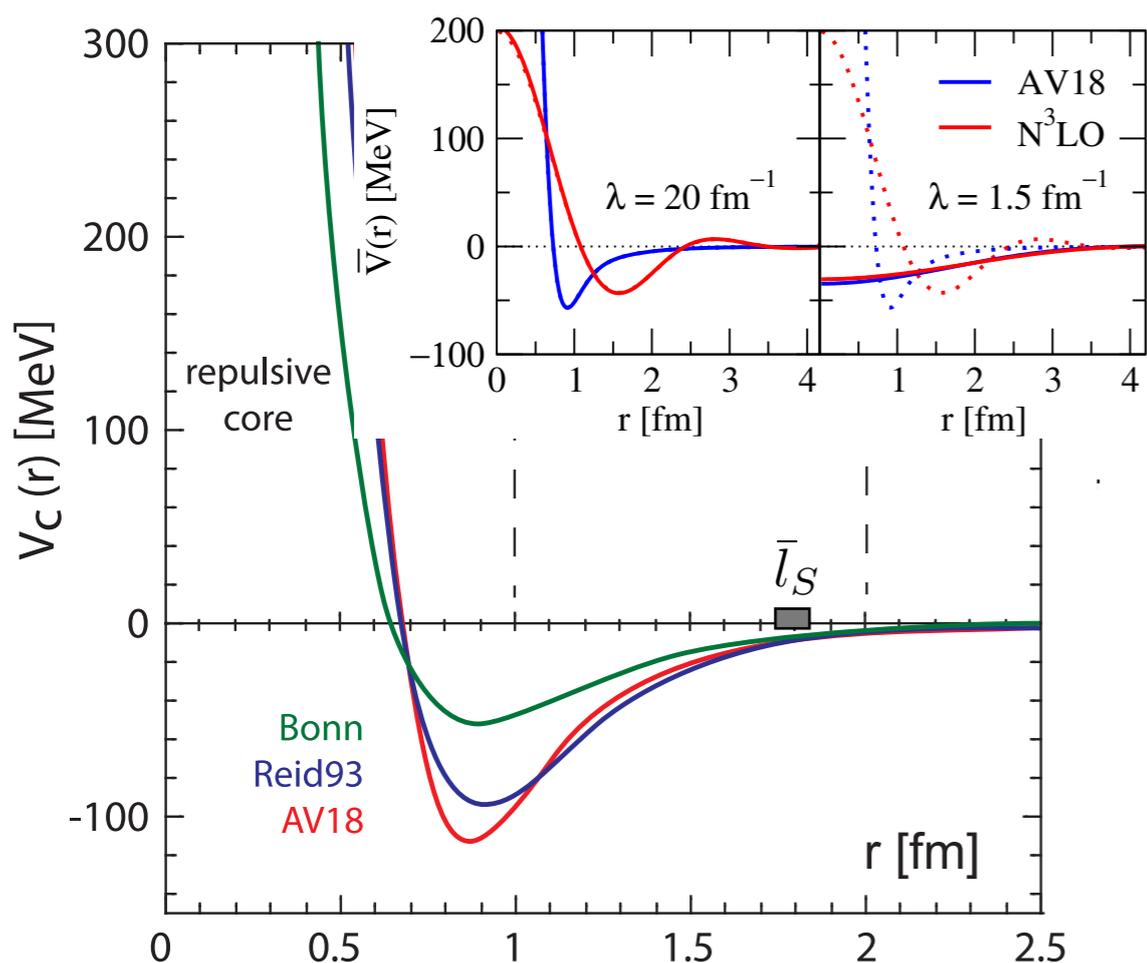
# Equation of state of symmetric nuclear matter: nucle



	2h terms	2h terms	2h terms
LO $\phi(\vec{p})$	X H	-	-
NLO $\phi(\vec{p})$	X H H	-	-
NLO $\phi(\vec{p})$	X H H	H	-
NLO $\phi(\vec{p})$	X H H	H H	H H

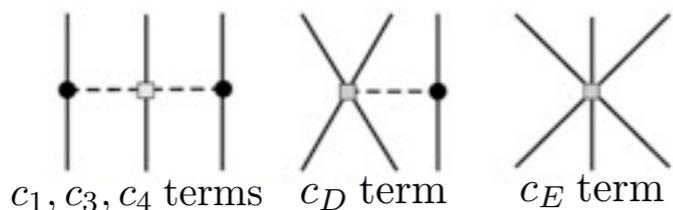
KH, Bogner, Furnstahl, Nogga,  
PRC(R) 83, 031301 (2011)

# Equation of state of symmetric nuclear matter: nuclear saturation



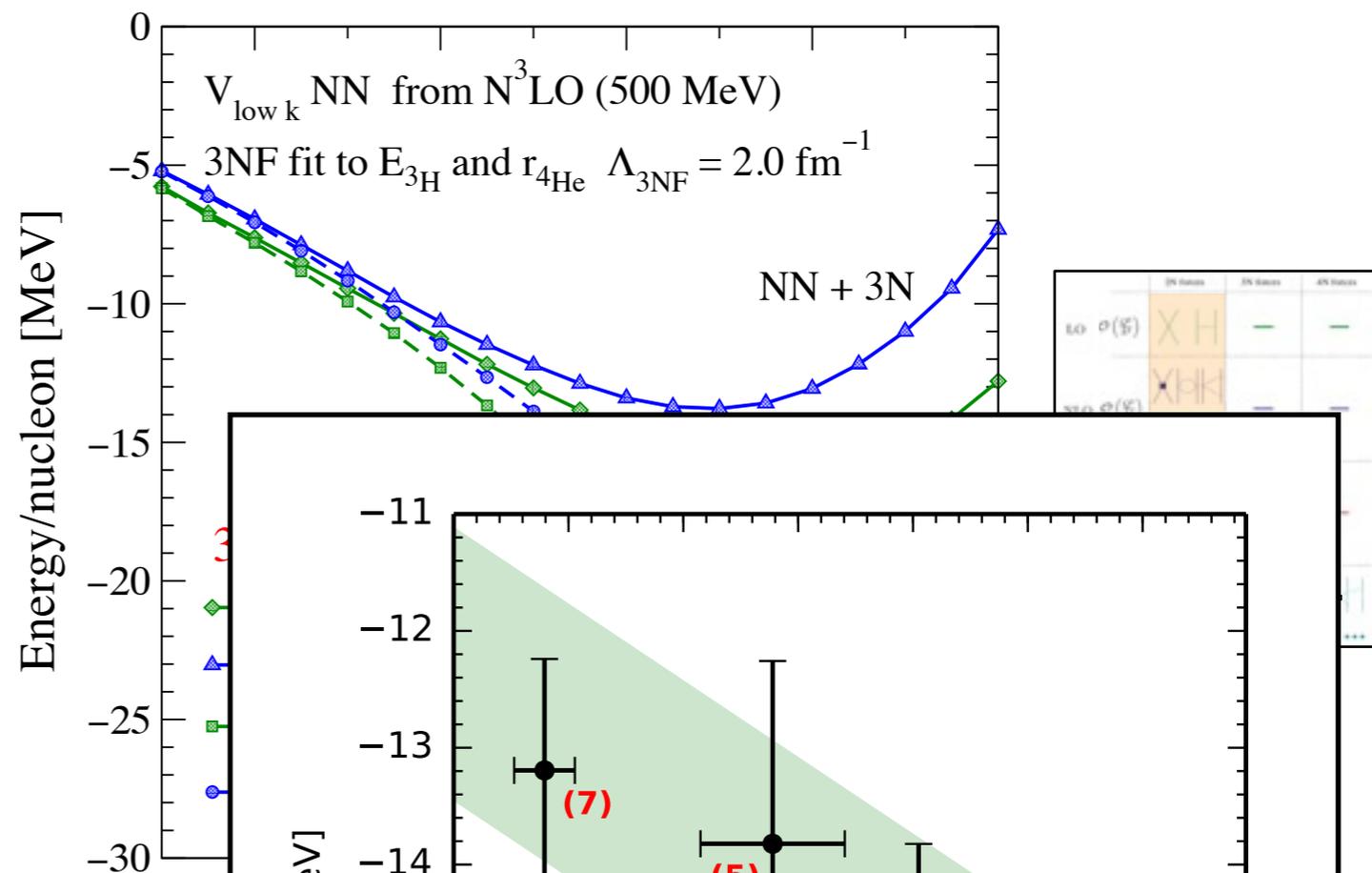
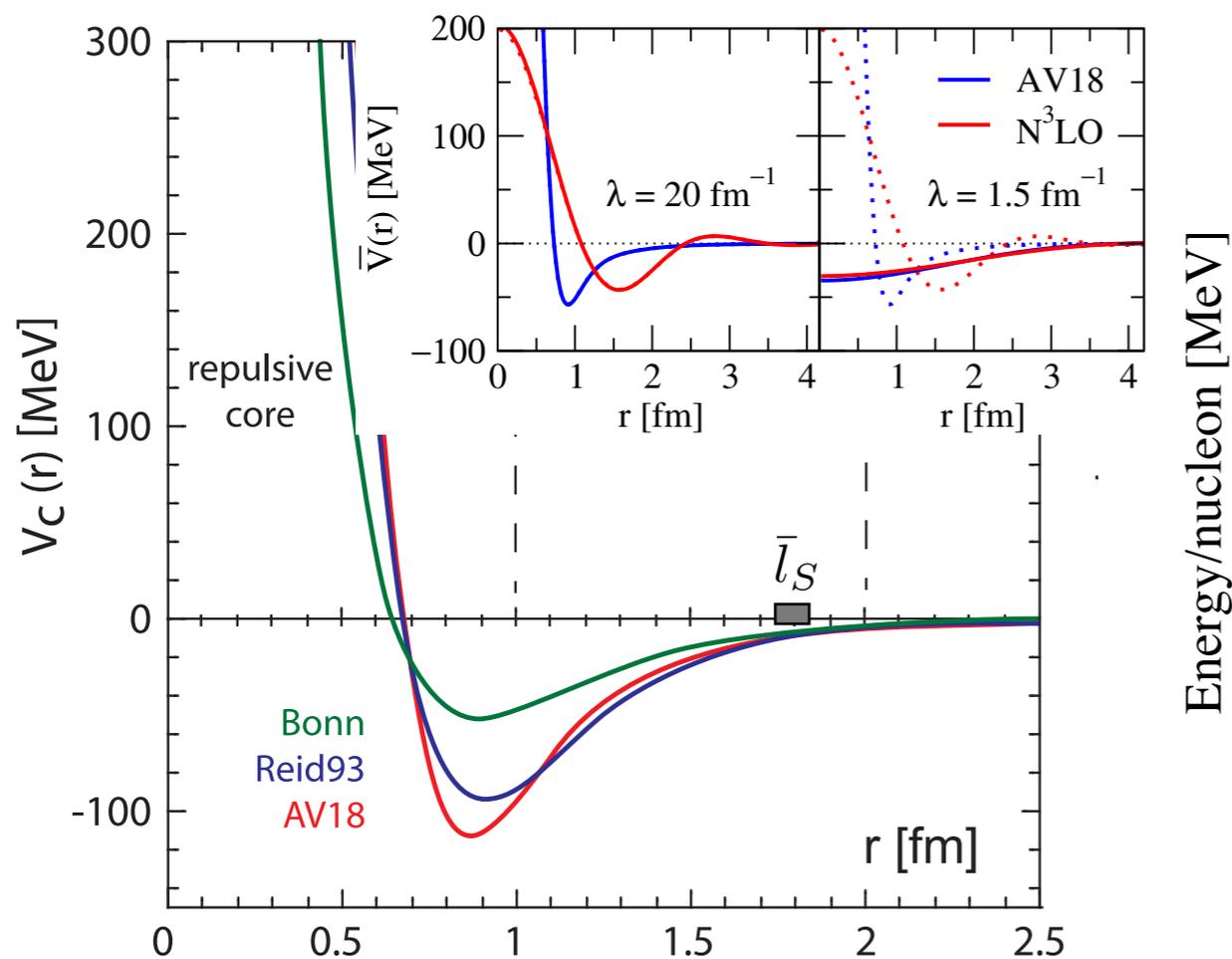
intermediate ( $c_D$ ) and short-range ( $c_E$ ) 3NF couplings fitted to few-body systems at different resolution scales:

$$E_{3H} = -8.482 \text{ MeV} \quad r_{4He} = 1.464 \text{ fm}$$



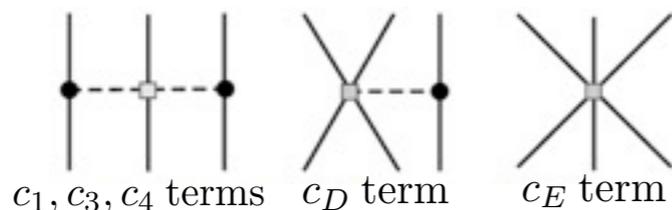
KH, Bogner, Furnstahl, Nogga,  
PRC(R) 83, 031301 (2011)

# Equation of state of symmetric nuclear matter: nuclear saturation



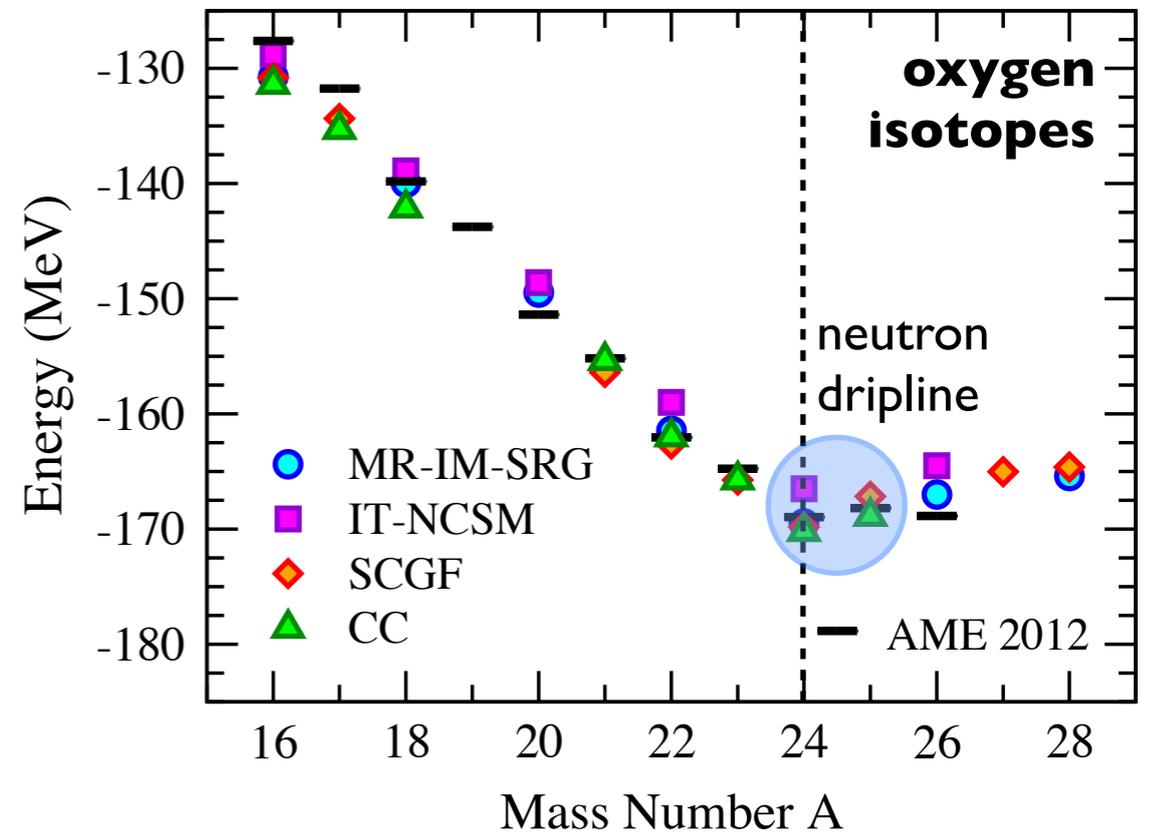
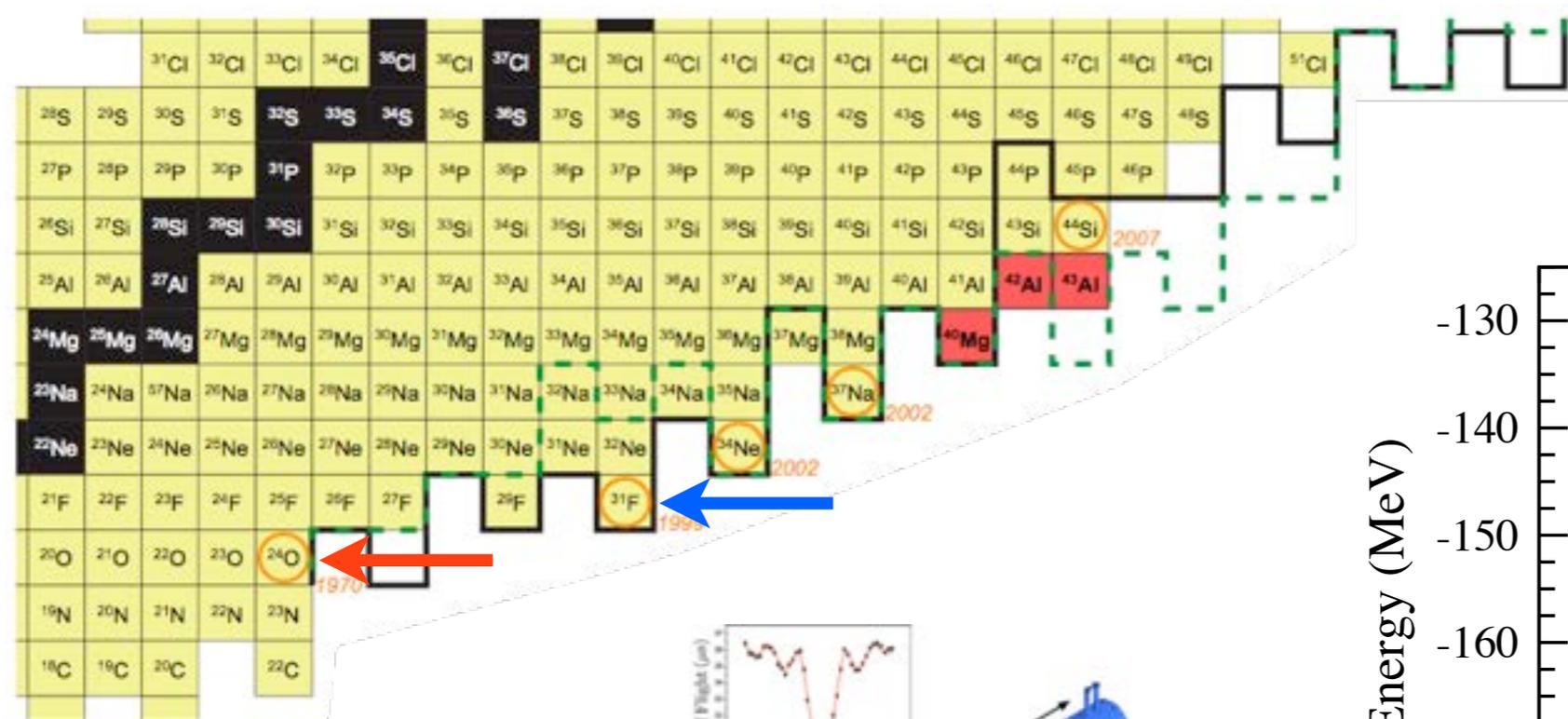
intermediate ( $c_D$ ) and short-range ( $c_E$ ) 3NF couplings fitted to few-body systems at different resolution scales:

$$E_{3\text{H}} = -8.482 \text{ MeV} \quad r_{4\text{He}} = 1.464 \text{ fm}$$



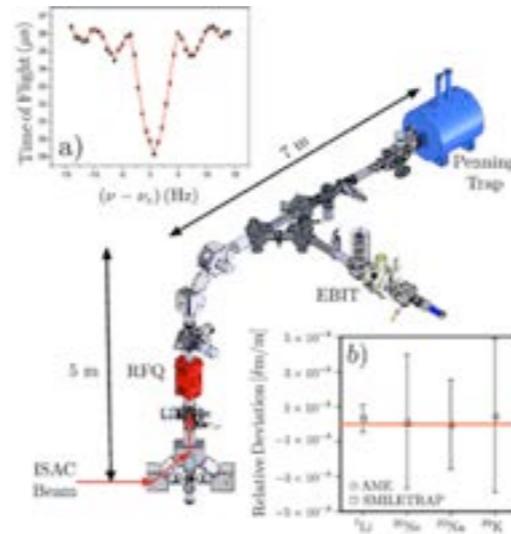
Drischler, KH, Schwenk, PRC93, 054314 (2016)

# Studies of neutron-rich nuclei: Neutron dripline and the oxygen anomaly



Gallant et al.  
PRL 109, 032506 (2012)

Wienholtz et al.  
Nature 498, 346 (2013)



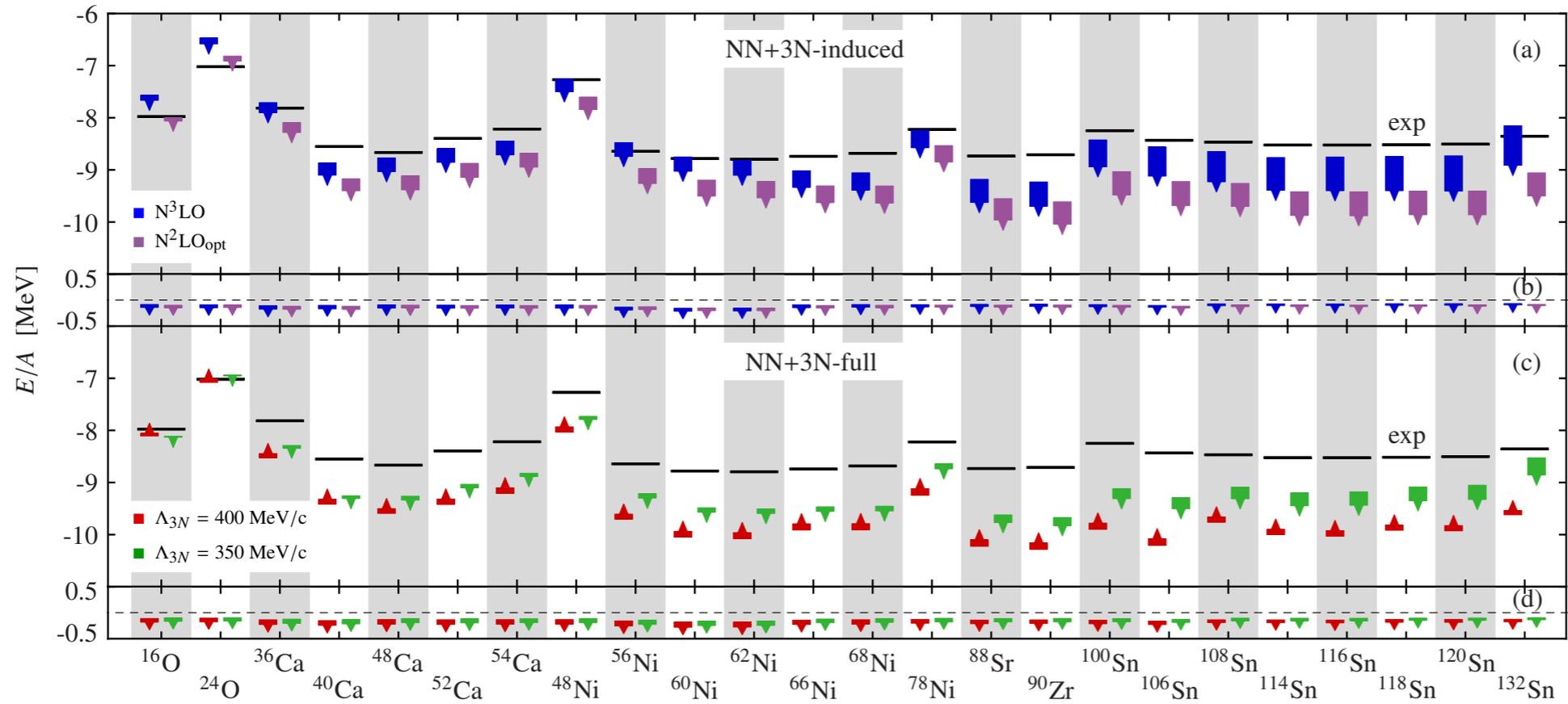
adapted from  
KH et al., Ann. Rev. Nucl. Part. Sci. 165, 457 (2015)

- remarkable agreement between different many-body frameworks
- very good agreement between theory and experiment for masses of oxygen and calcium isotopes based on specific chiral interactions
- contributions from 3N force play important role for drip line

# Ab initio calculations of heavier nuclei

	20 basis	25 basis	35 basis
LO $\sigma(\xi)$	X H	—	—
NLO $\sigma(\xi)$	X H H	—	—
N <sup>2</sup> LO $\sigma(\xi)$	X H H	X H	—
N <sup>3</sup> LO $\sigma(\xi)$	X H H H	X H H H	X H H H

## coupled cluster (CC) framework

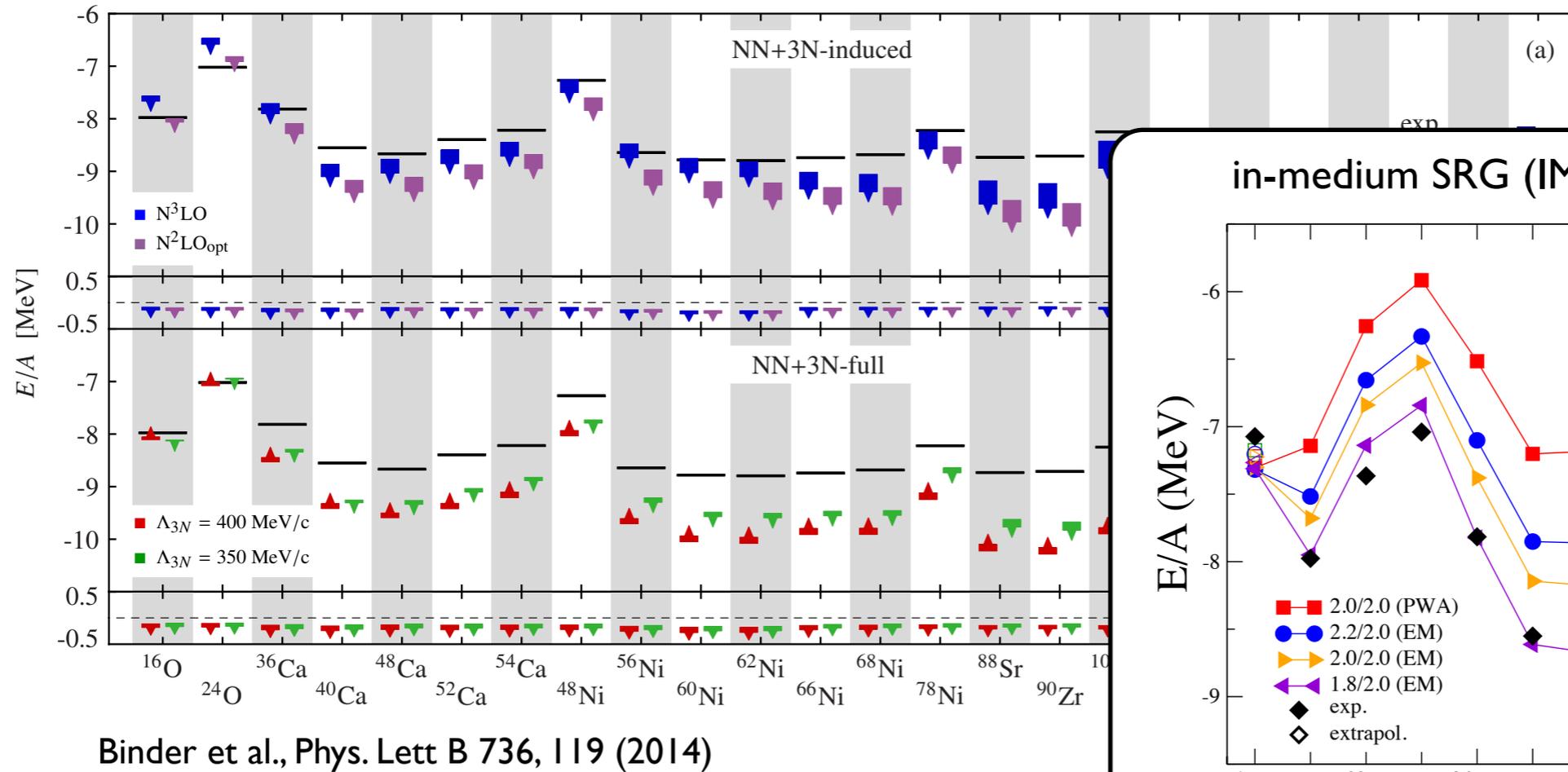


Binder et al., Phys. Lett B 736, 119 (2014)

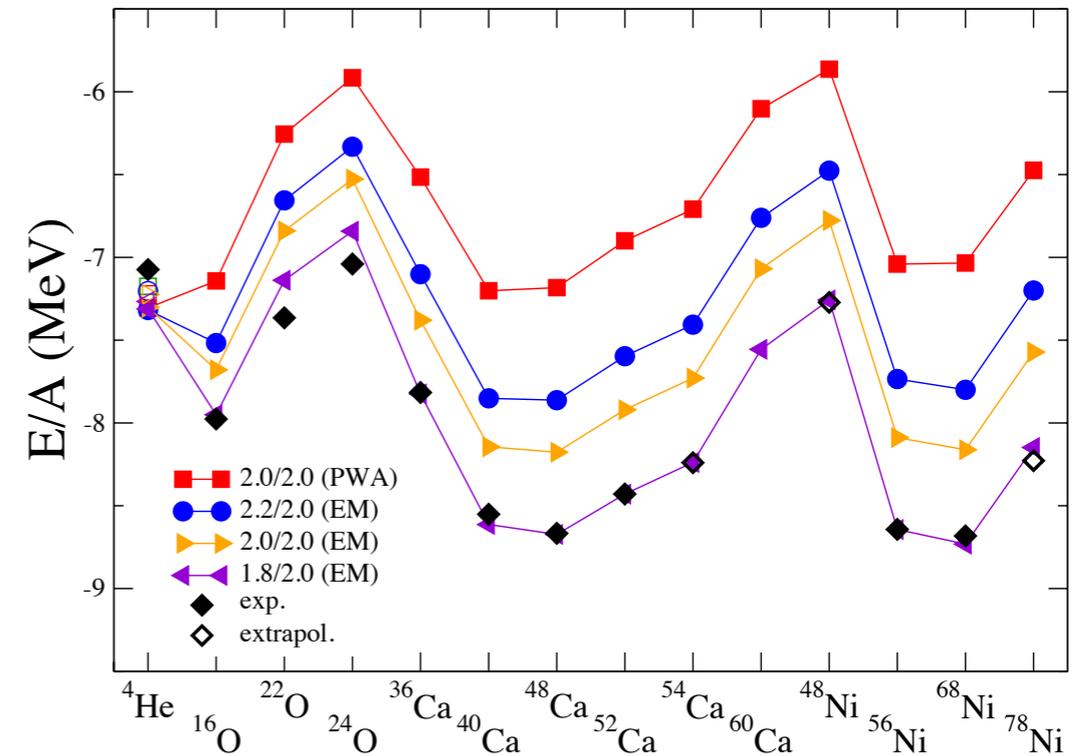
# Ab initio calculations of heavier nuclei

	2N basis	3N basis	4N basis
LO $\sigma(\xi)$	X H	—	—
NLO $\sigma(\xi)$	X H H	—	—
N <sup>2</sup> LO $\sigma(\xi)$	X H H	X H	—
N <sup>3</sup> LO $\sigma(\xi)$	X H H H	X H H	X H

## coupled cluster (CC) framework



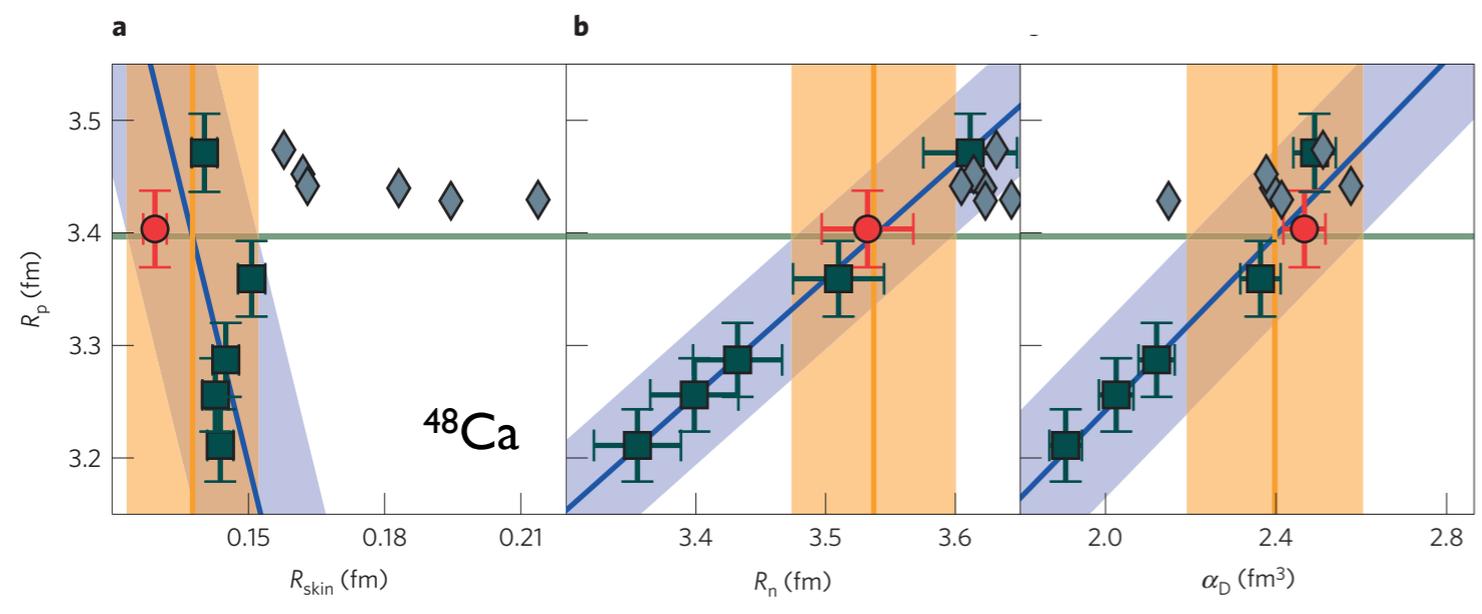
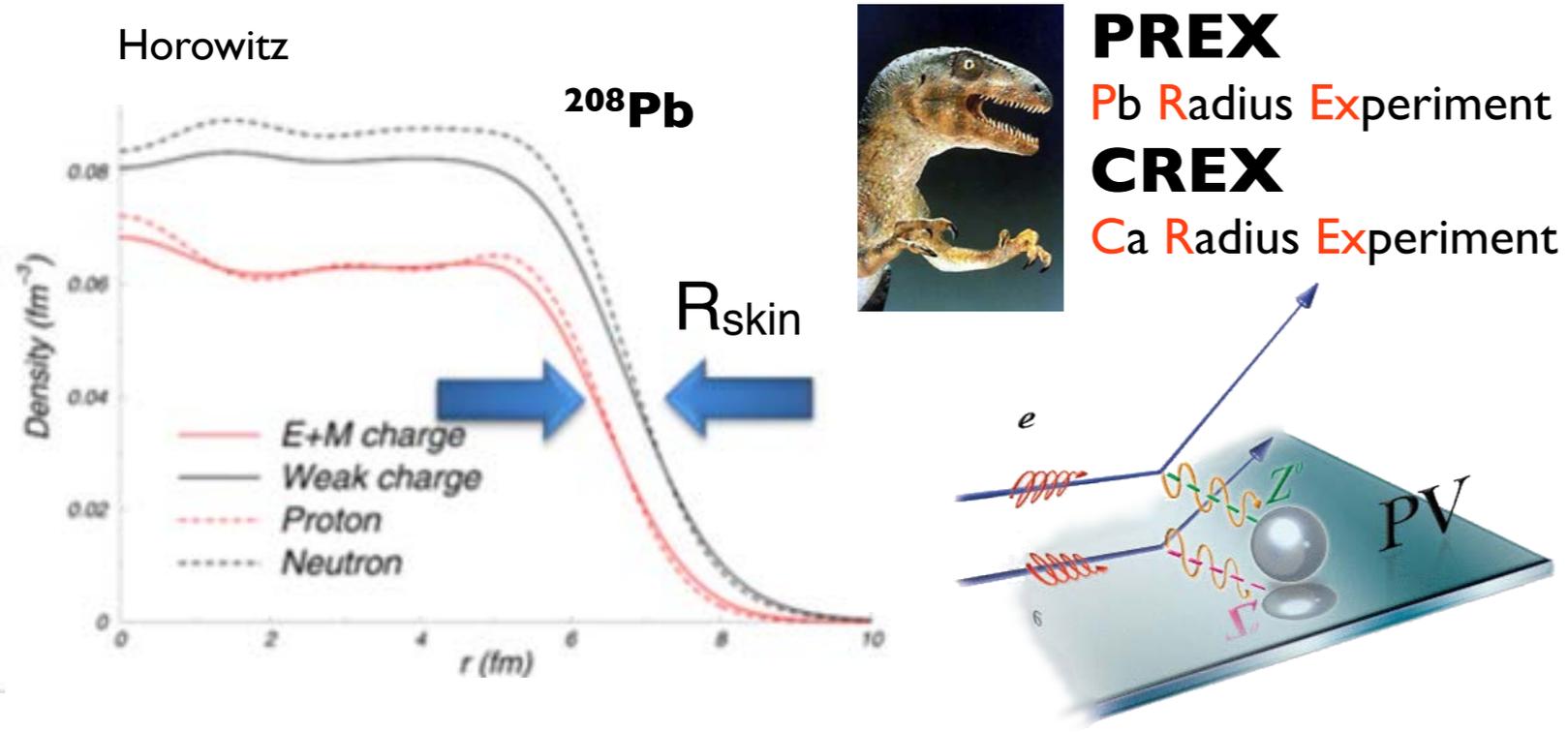
## in-medium SRG (IMSRG) framework



Simonis, Stroberg et al., in preparation

- **spectacular increase** in range of applicability of ab initio many body frameworks
- **significant discrepancies** to experimental data for heavy nuclei for (most of) presently used nuclear interactions
- need to **quantify theoretical uncertainties**

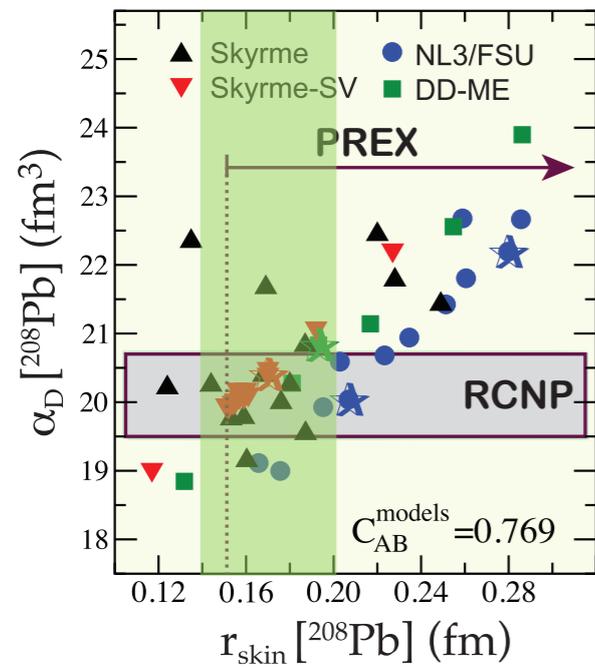
# The size of the atomic nucleus: challenges from novel high-precision measurements



Hagen. et al.. Nature Phys. 12, 186 (2015)

# The size of the atomic nucleus: challenges from novel high-precision measurements

Piekarewicz,  
PRC 85, 041302 (2012)

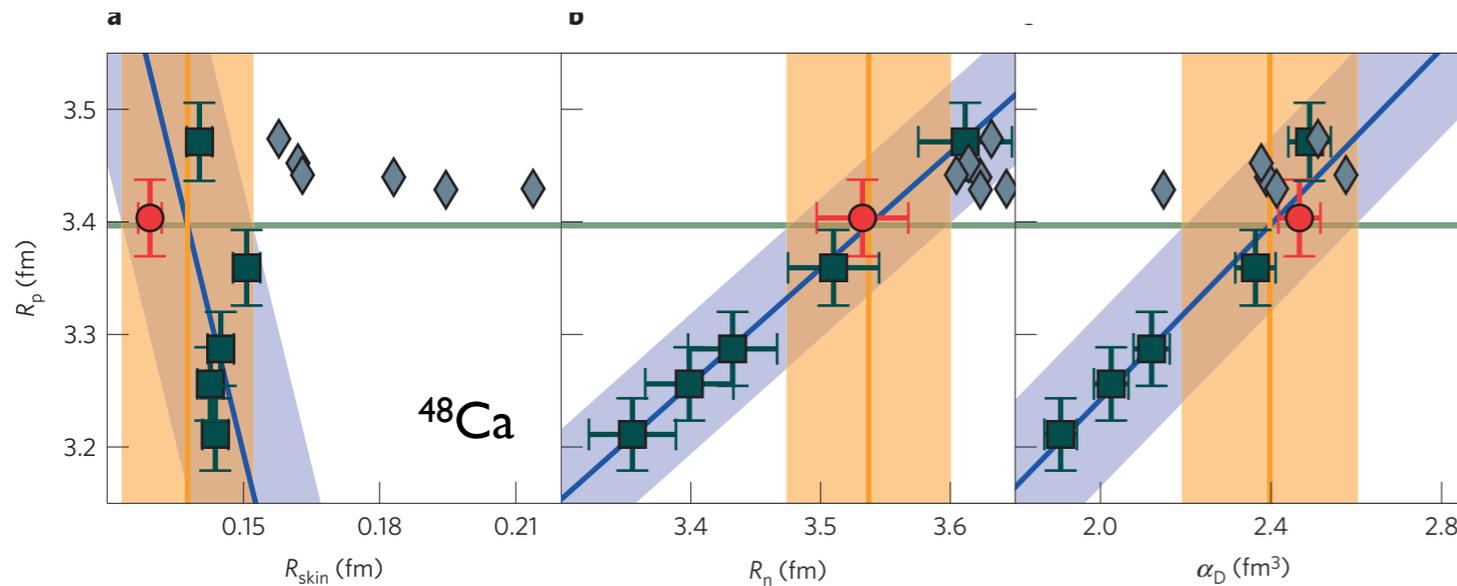
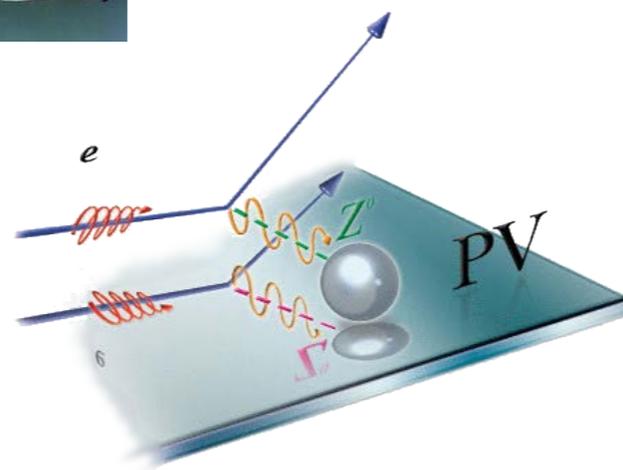


**PREX**

Pb Radius Experiment

**CREX**

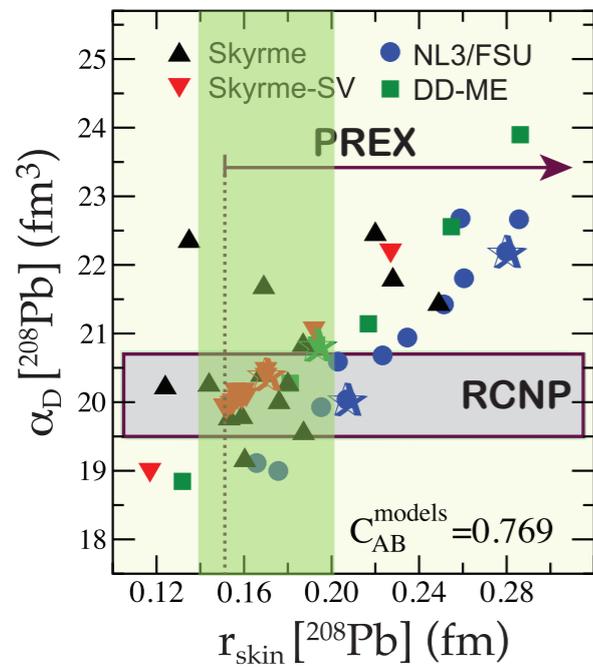
Ca Radius Experiment



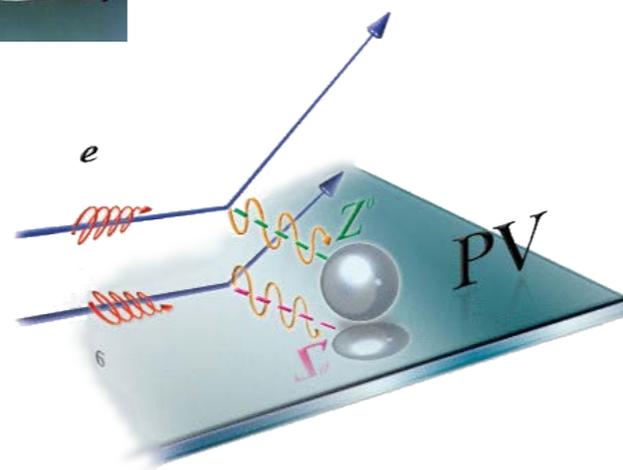
Hagen. et al.. Nature Phys. 12, 186 (2015)

# The size of the atomic nucleus: challenges from novel high-precision measurements

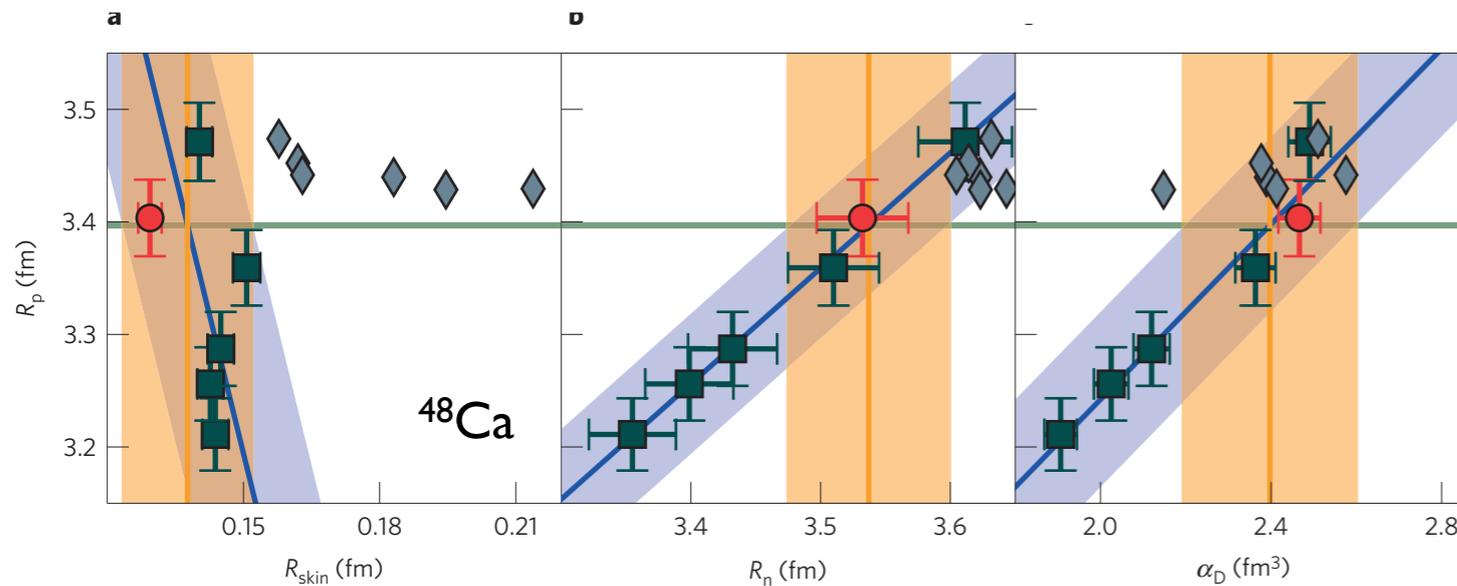
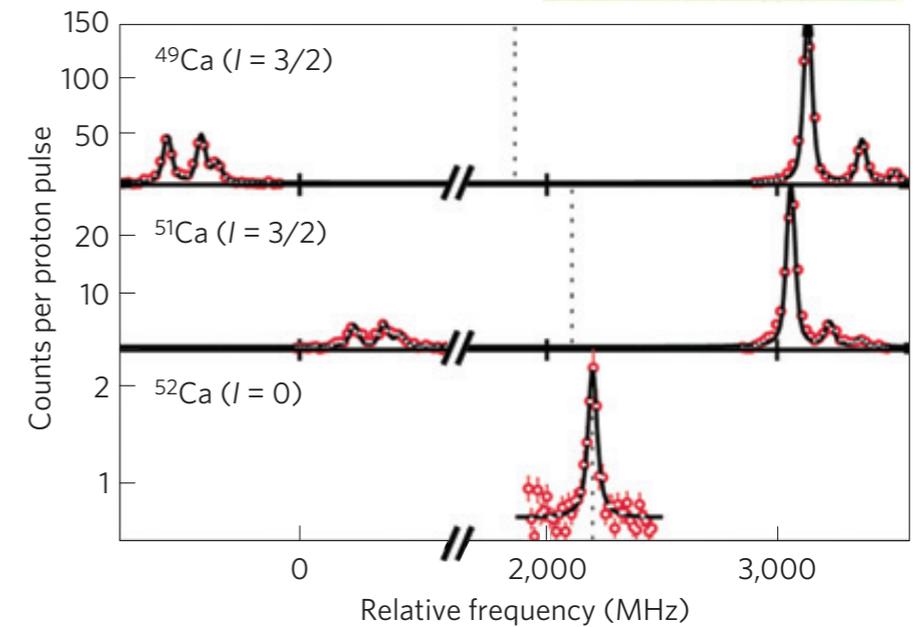
Piekarewicz,  
PRC 85, 041302 (2012)



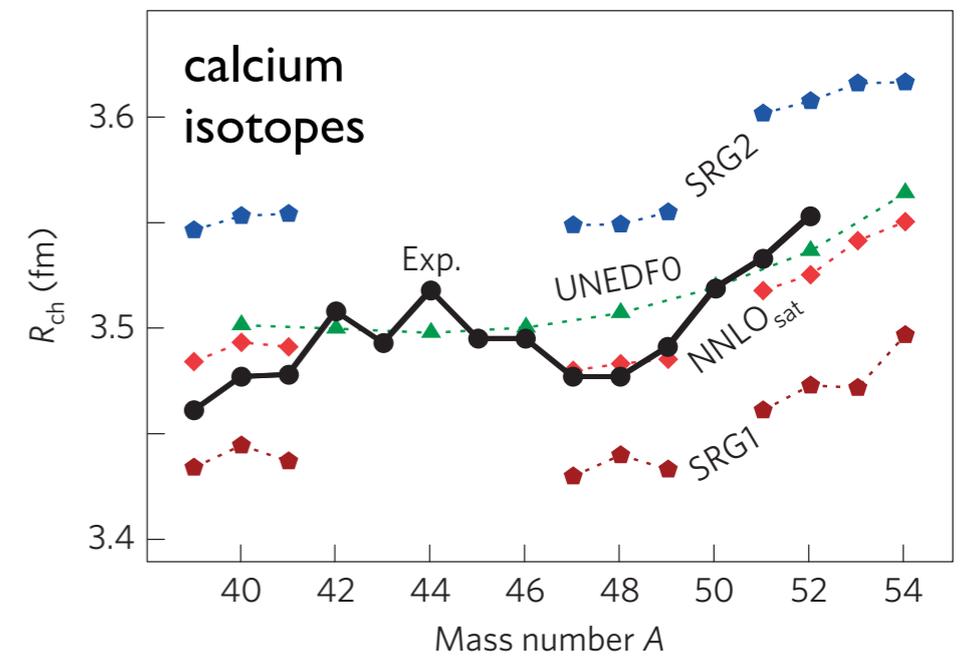
**PREX**  
Pb Radius Experiment  
**CREX**  
Ca Radius Experiment



ISOLDE



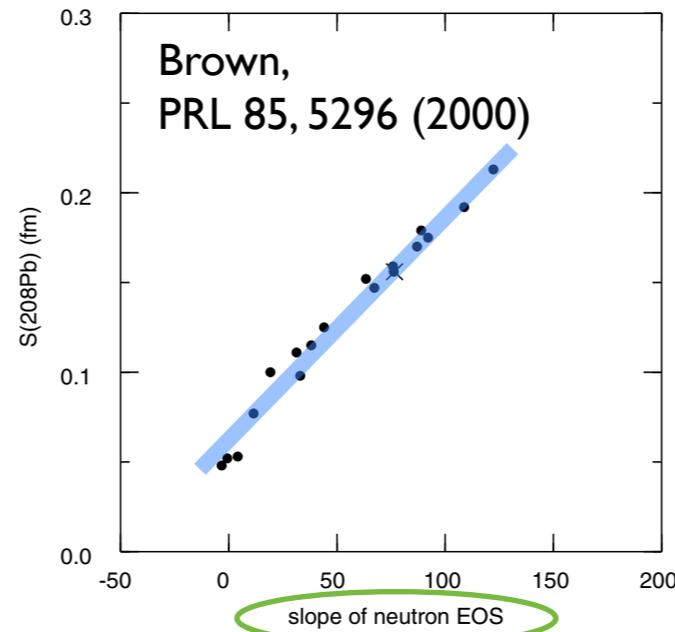
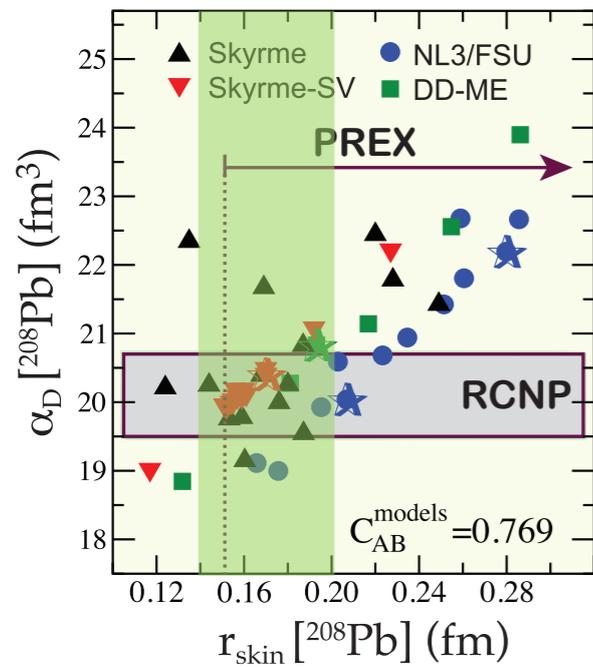
Hagen. et al.. Nature Phys. 12, 186 (2015)



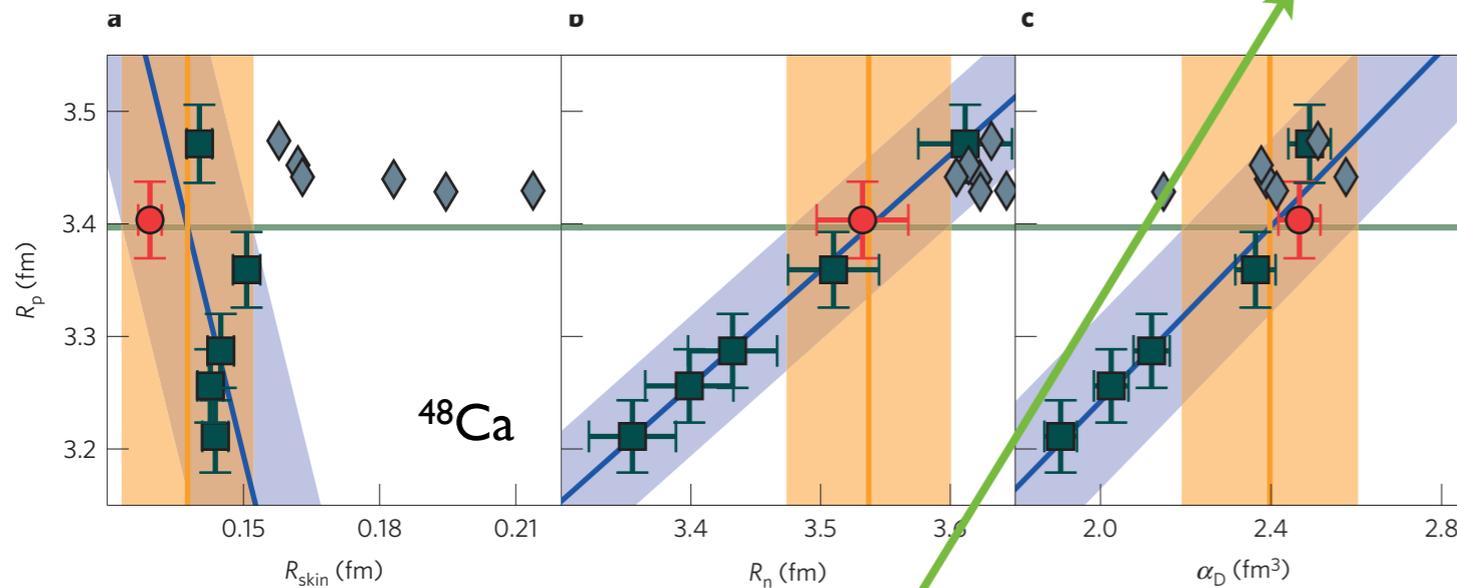
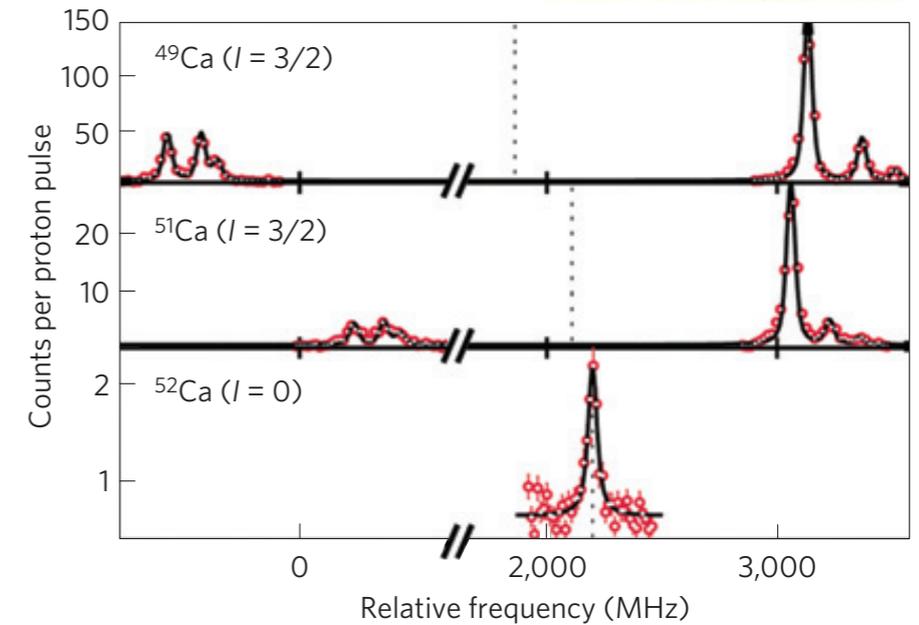
Garcia Ruiz. et al.,  
Nature Phys. 12, 594 (2016)

# The size of the atomic nucleus: challenges from novel high-precision measurements

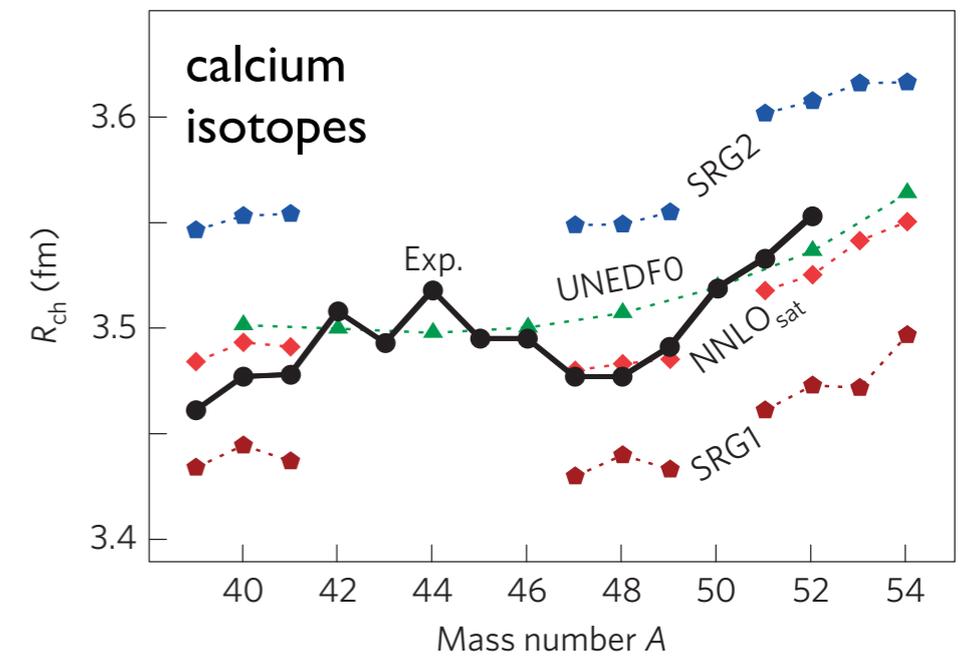
Piekarewicz,  
PRC 85, 041302 (2012)



ISOLDE



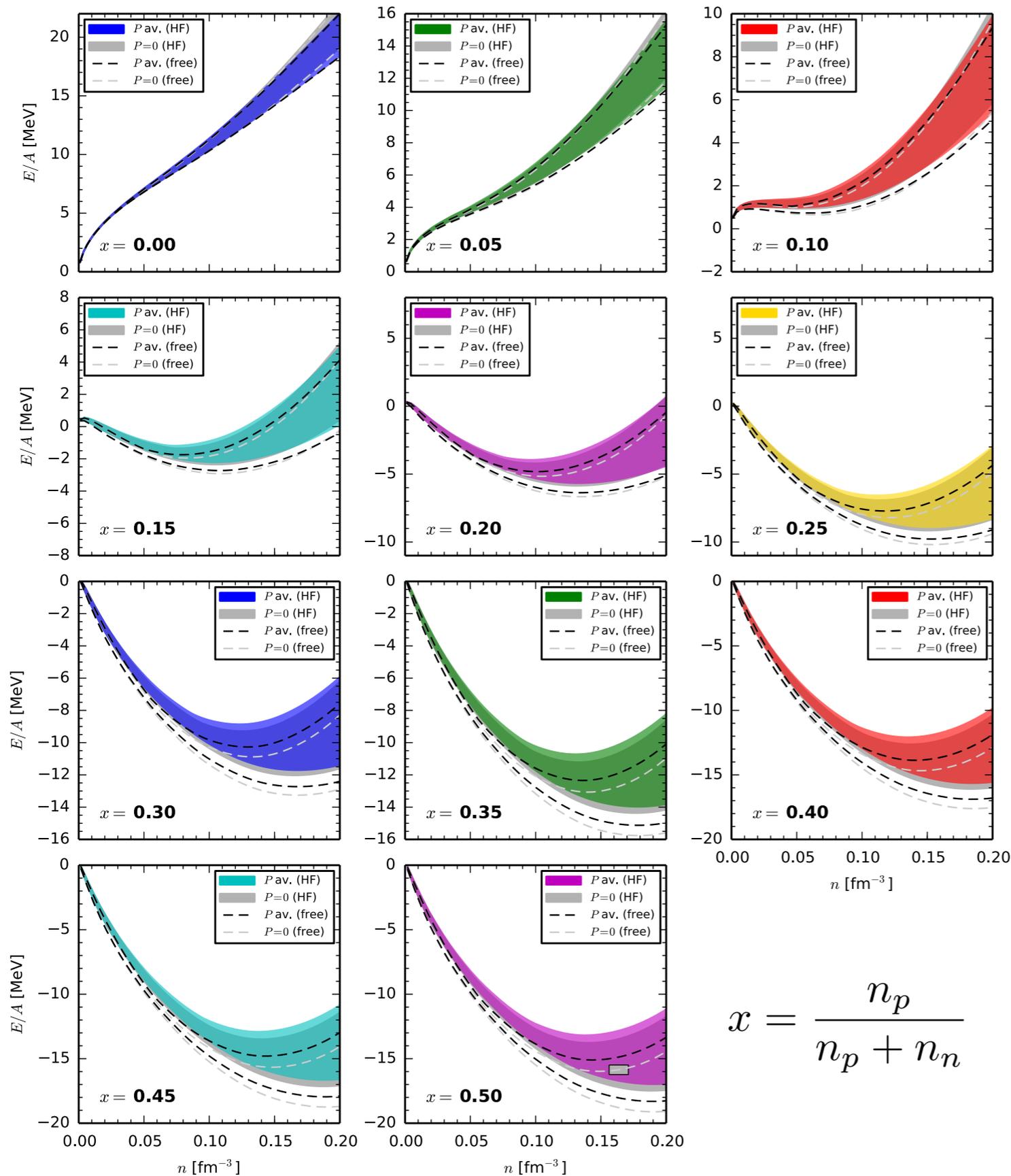
Hagen. et al.. Nature Phys. 12, 186 (2015)



Garcia Ruiz. et al.,  
Nature Phys. 12, 594 (2016)

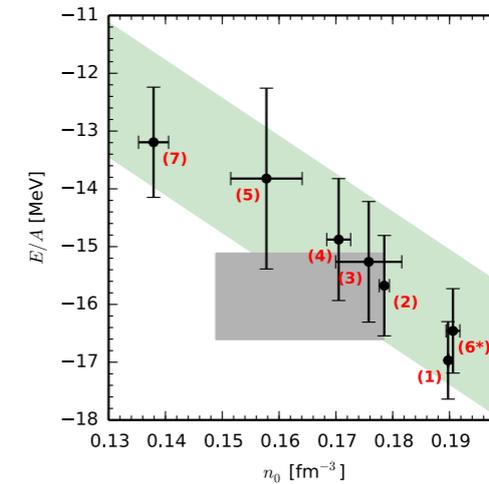
direct connections to astrophysics!

# Microscopic calculations of the equation of state



- microscopic framework to calculate equation of state for general proton fractions

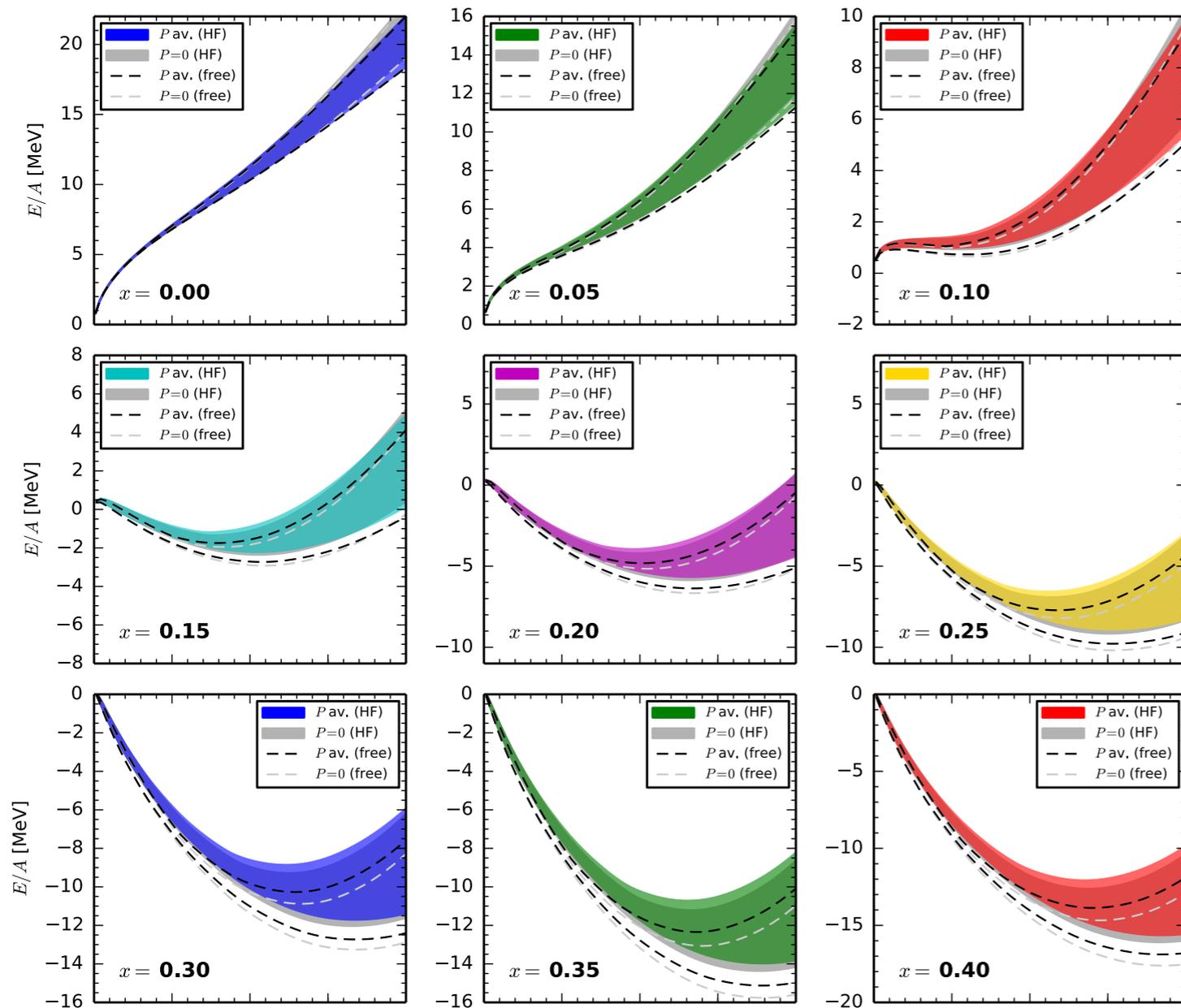
- uncertainty bands determined by set of 7 Hamiltonians



- many-body framework allows treatment of general 3N interaction

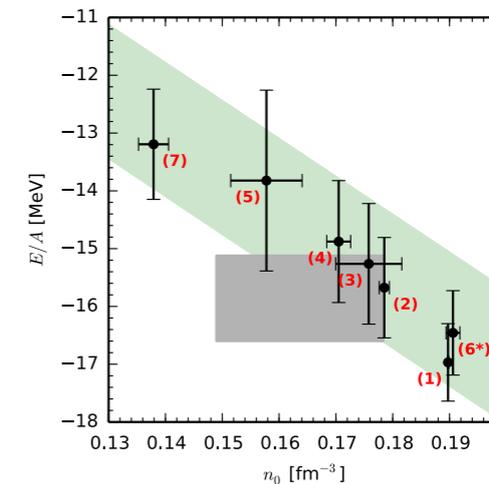
$$x = \frac{n_p}{n_p + n_n}$$

# Microscopic calculations of the equation of state



- microscopic framework to calculate equation of state for general proton fractions

- uncertainty bands determined by set of 7 Hamiltonians



- many body framework allows

**Problem:**

Calculation of neutron star properties require EOS up to high densities.

Reliable calculations only possible up to  $\sim 1-2 n_{sat}$ .

**Strategy:**

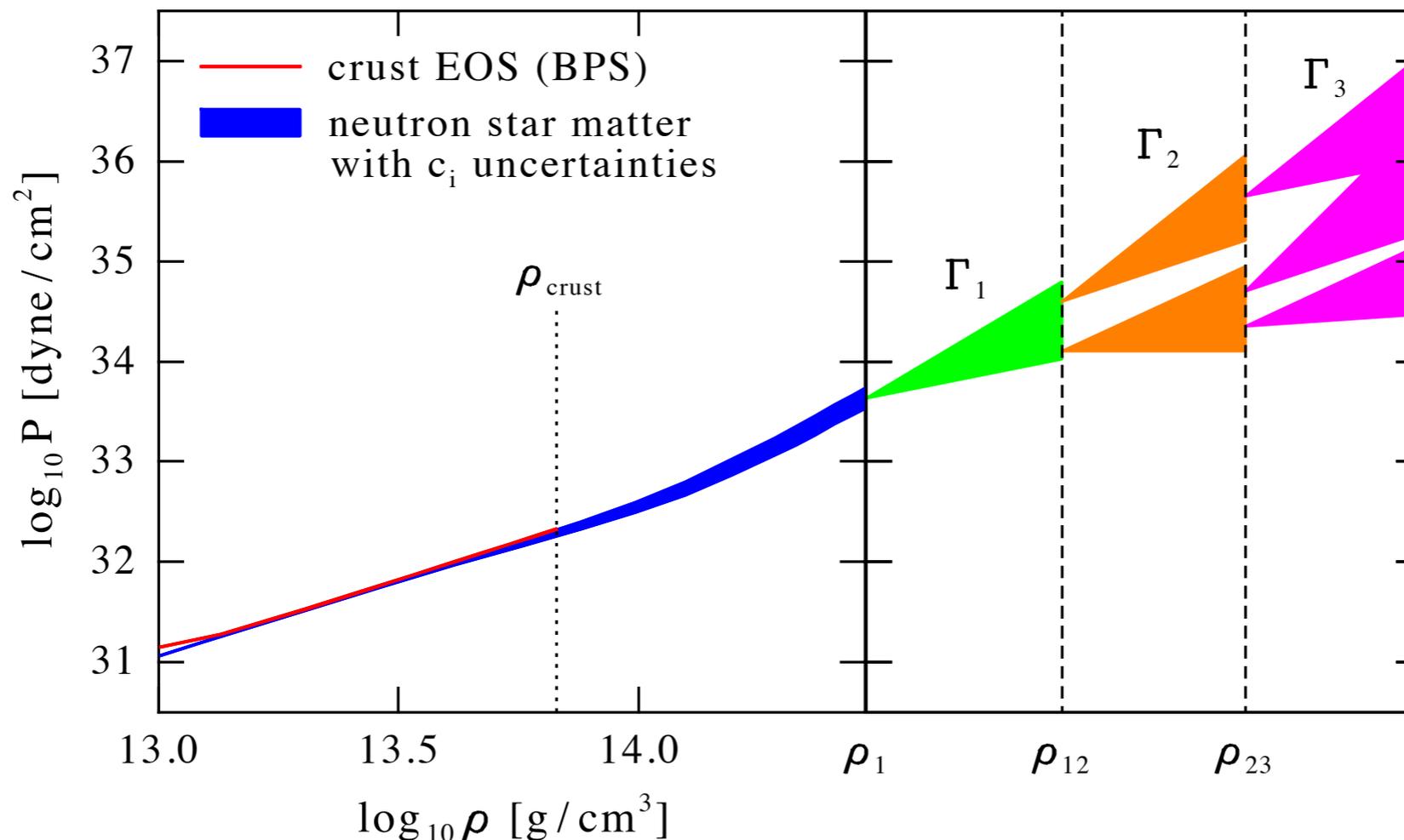
Use observations to constrain the high-density part of the nuclear EOS.

# Neutron star radius constraints

incorporation of beta-equilibrium: neutron matter  $\longrightarrow$  neutron star matter

parametrize our ignorance via piecewise high-density extensions of EOS:

- use polytropic ansatz  $p \sim \rho^\Gamma$  (results insensitive to particular form)
- range of parameters  $\Gamma_1, \rho_{12}, \Gamma_2, \rho_{23}, \Gamma_3$  limited by physics



# Constraints on the nuclear equation of state

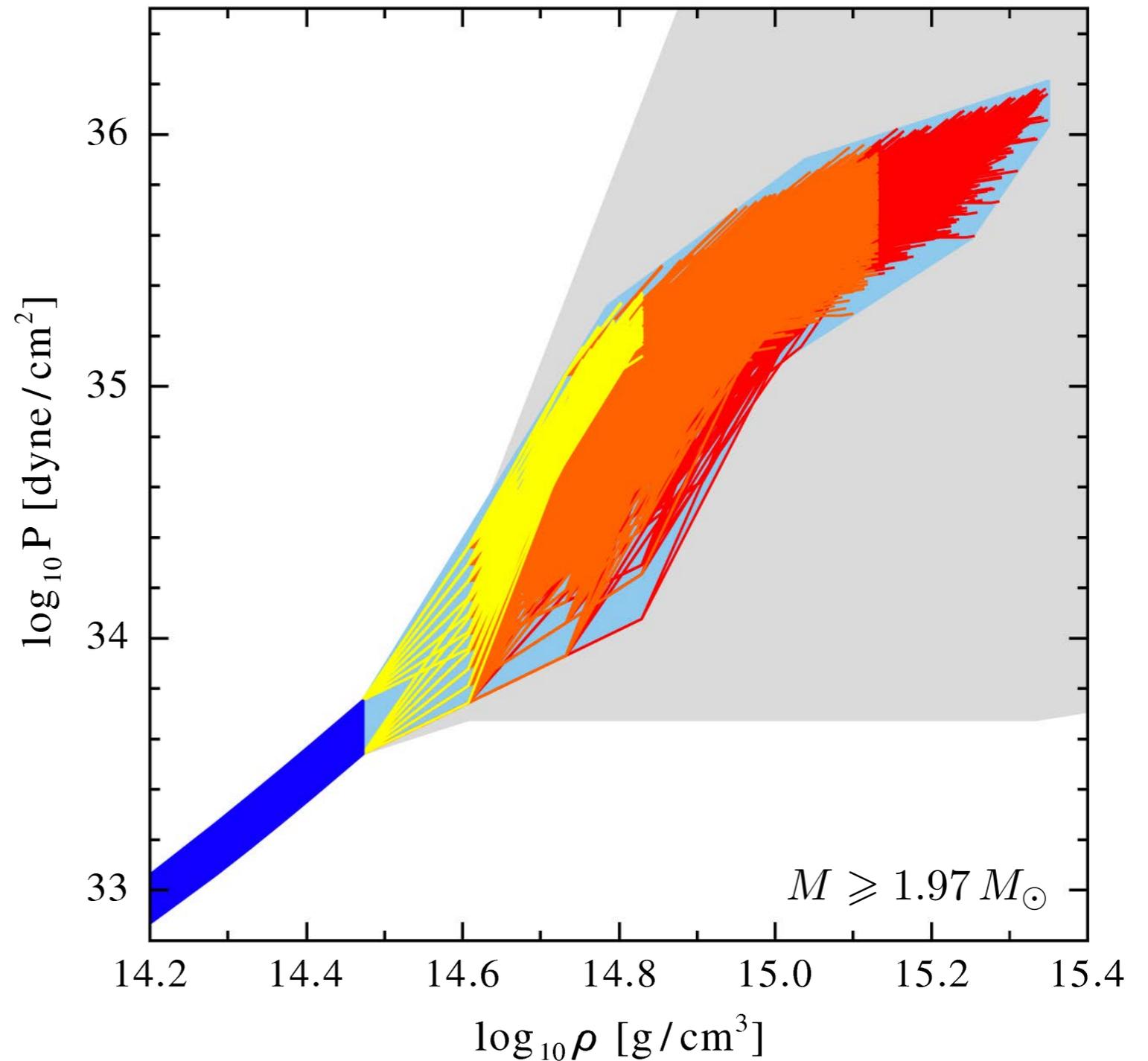
use the constraints:

recent NS observations

$$M_{\text{max}} > 1.97 M_{\odot}$$

causality

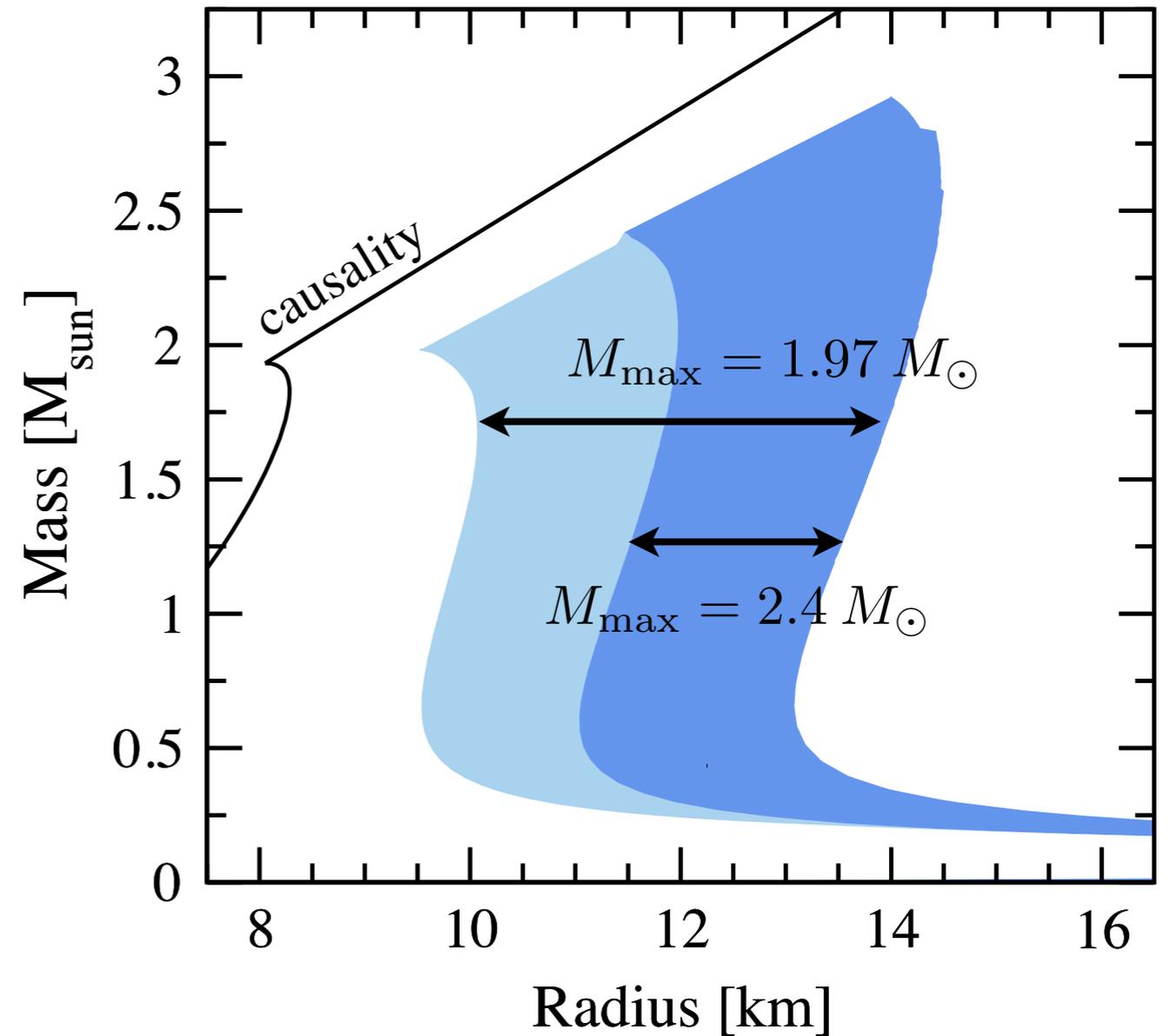
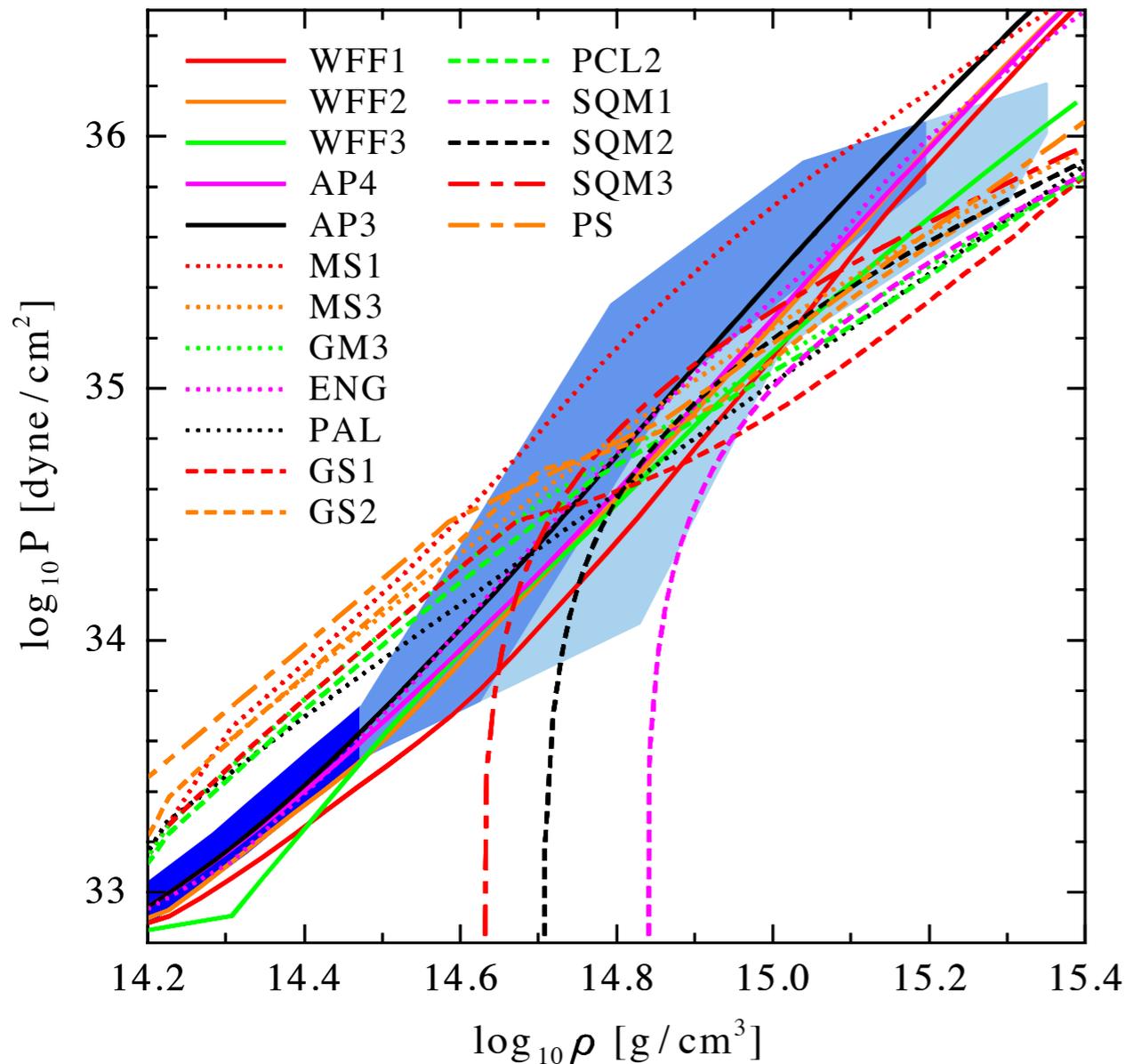
$$v_s(\rho) = \sqrt{dP/d\varepsilon} < c$$



KH, Lattimer, Pethick, Schwenk, ApJ 773, 11 (2013)

constraints lead to significant reduction of EOS uncertainty band

# Constraints on neutron star radii



KH, Lattimer, Pethick, Schwenk, ApJ 773, 11 (2013)

KH, Lattimer, Pethick, Schwenk, PRL 105, 161102 (2010)

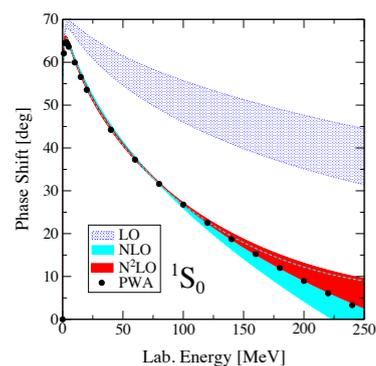
- low-density part of EOS sets scale for allowed high-density extensions

→ see talk by **Svenja Greif**

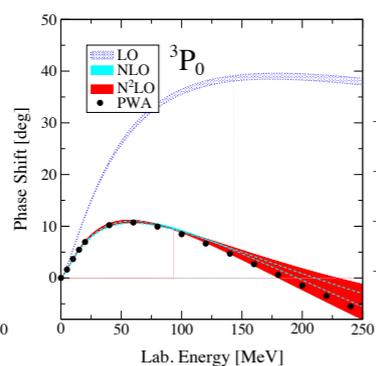
# Recent and current developments of novel nuclear interactions

## I. local EFT interactions, suitable for Quantum Monte Carlo calculations

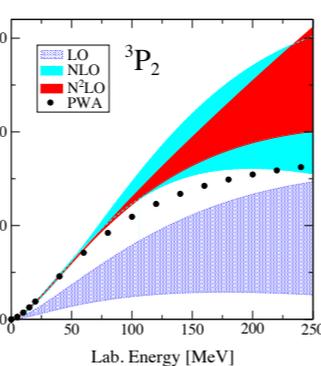
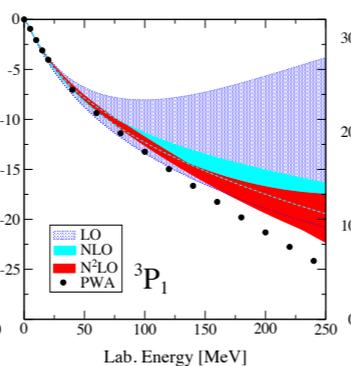
**status:** NN plus 3N up to N2LO, calculations of few-body systems and neutron matter



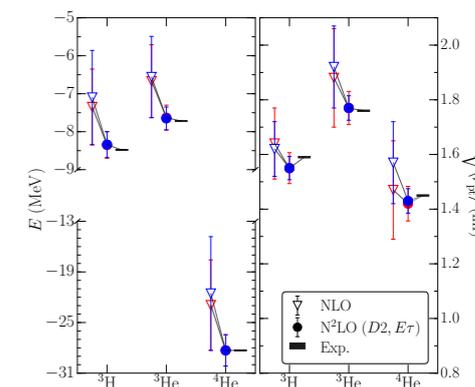
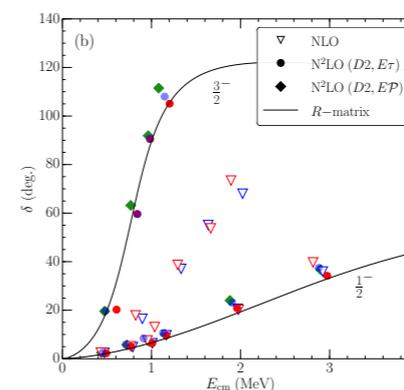
Gezerlis et al.,  
PRL 111, 032501 (2013)



Gezerlis et al.,  
PRC 90, 054323 (2014)



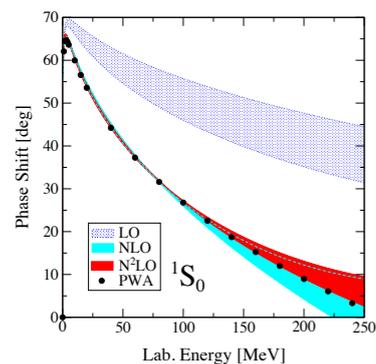
Lynn et al.,  
PRL 116, 062501 (2016)



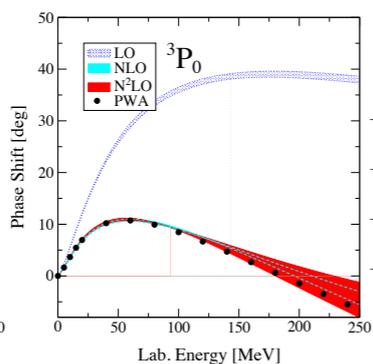
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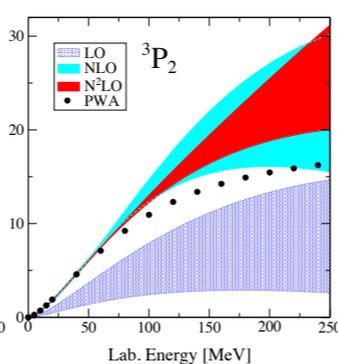
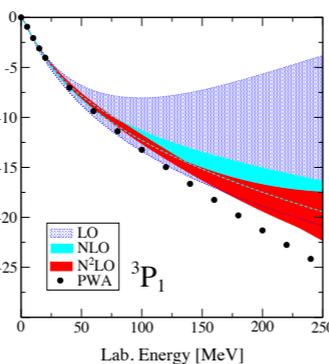
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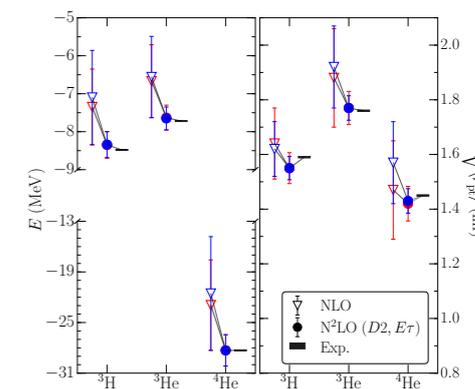
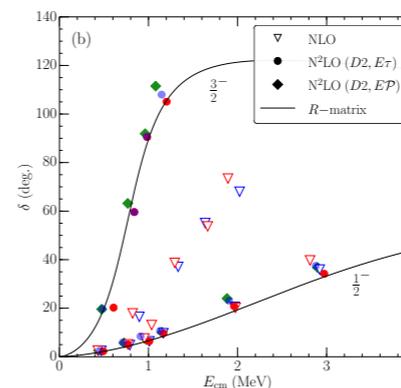
Gezerlis et al.,  
PRL 111, 032501 (2013)



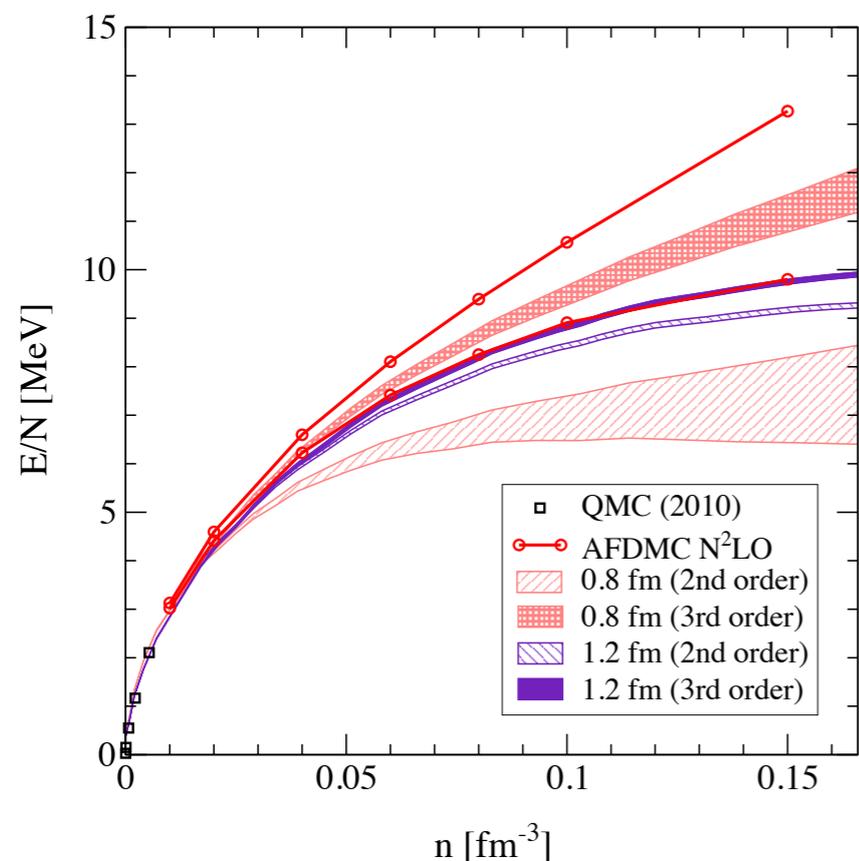
Gezerlis et al.,  
PRC 90, 054323 (2014)



Lynn et al.,  
PRL 116, 062501 (2016)



first Quantum Monte Carlo of neutron matter based on chiral EFT interactions



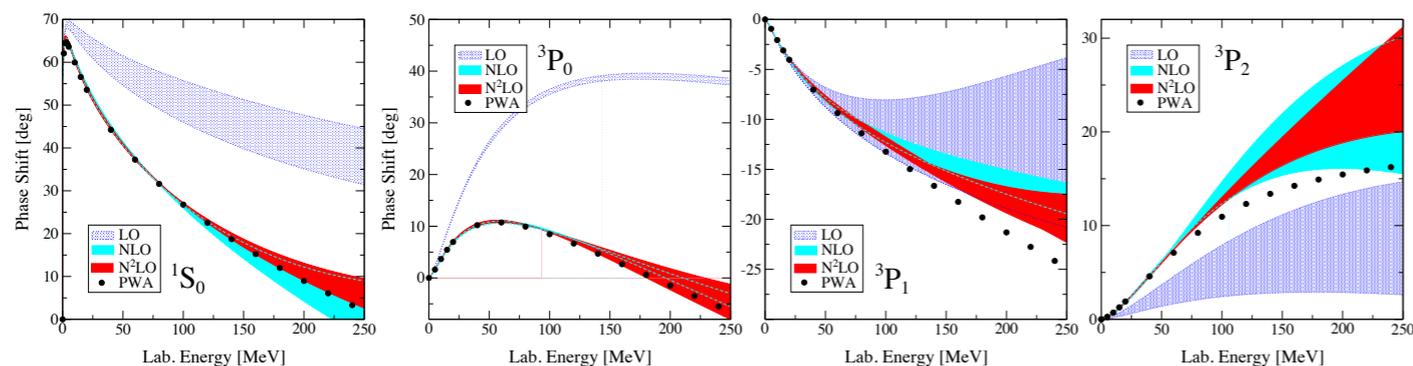
perfect agreement for soft interactions, first direct validation of calculations within many-body perturbation theory

Gezerlis et. al,  
PRL 111, 032501 (2013)

# Recent and current developments of novel nuclear interactions

## 1. local EFT interactions, suitable for Quantum Monte Carlo calculations

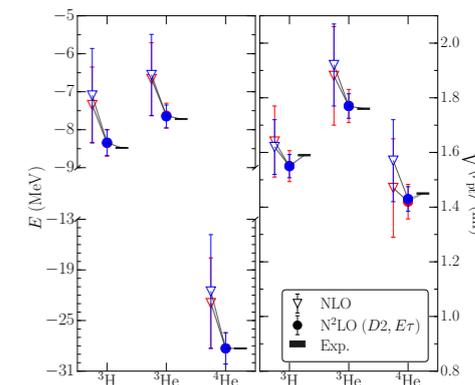
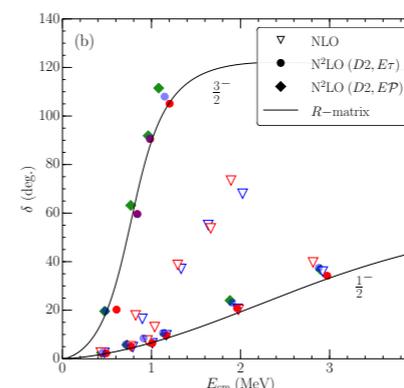
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Gezerlis et al.,  
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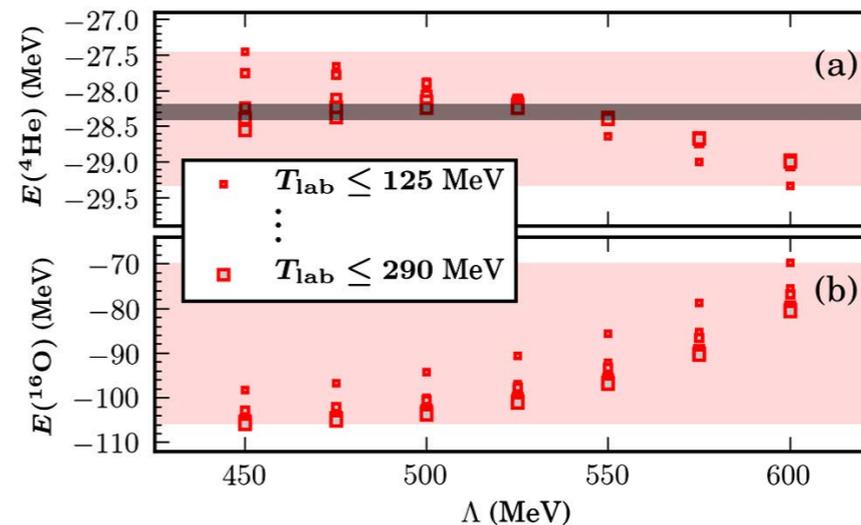
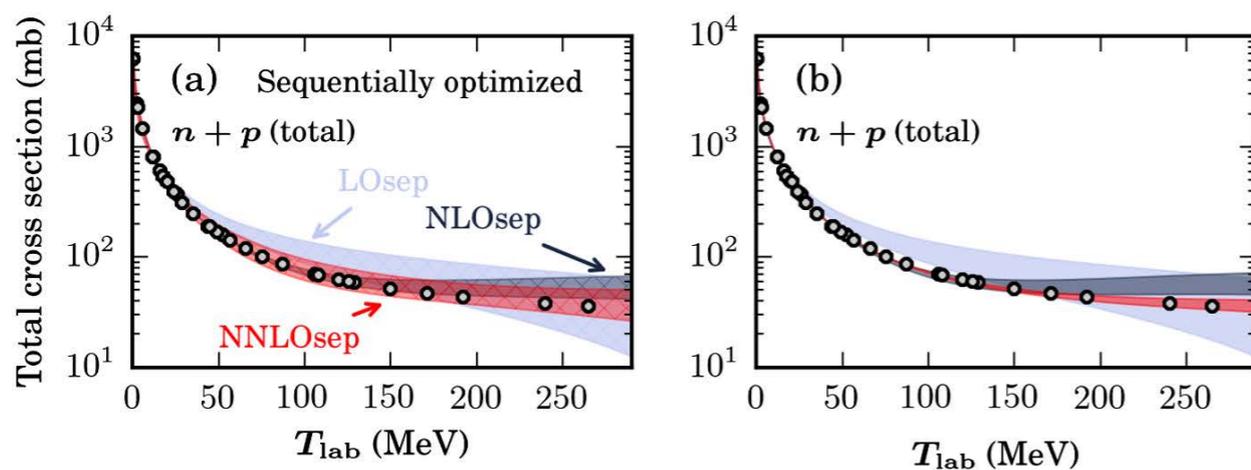
Gezerlis et al.,  
PRC 90, 054323 (2014)

Lynn et al.,  
PRL 116, 062501 (2016)



## 2. simultaneous fit of NN and 3N forces to two- and few-body observables

**status:** NN plus 3N up to N2LO, N3LO currently in development

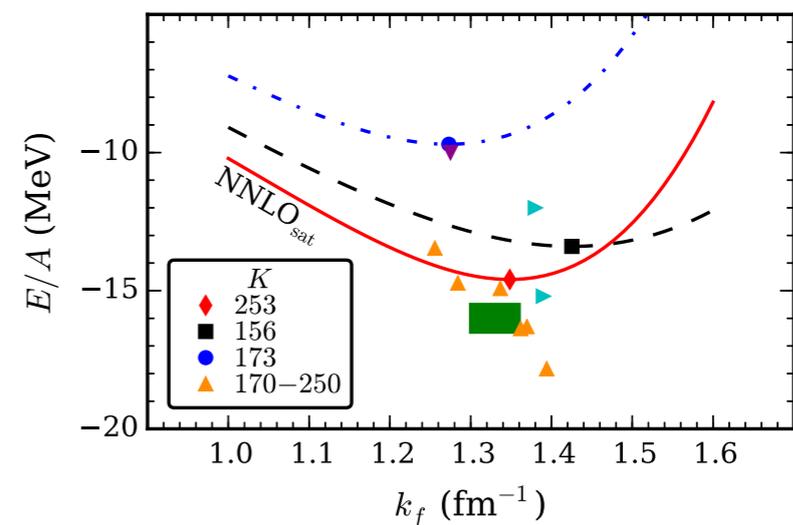
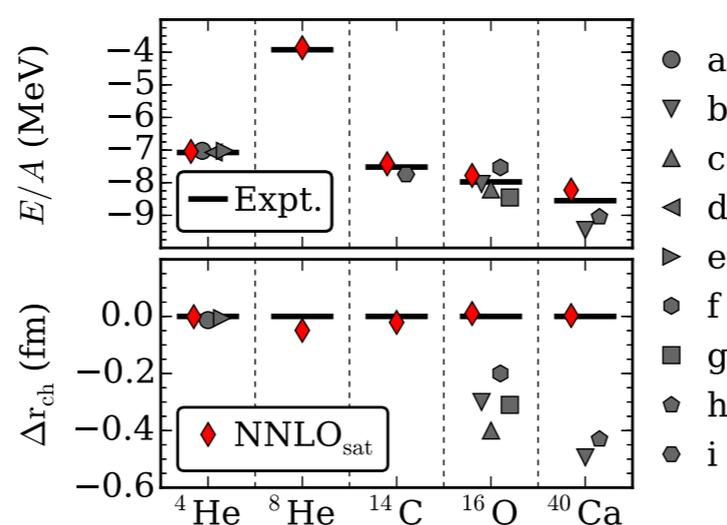
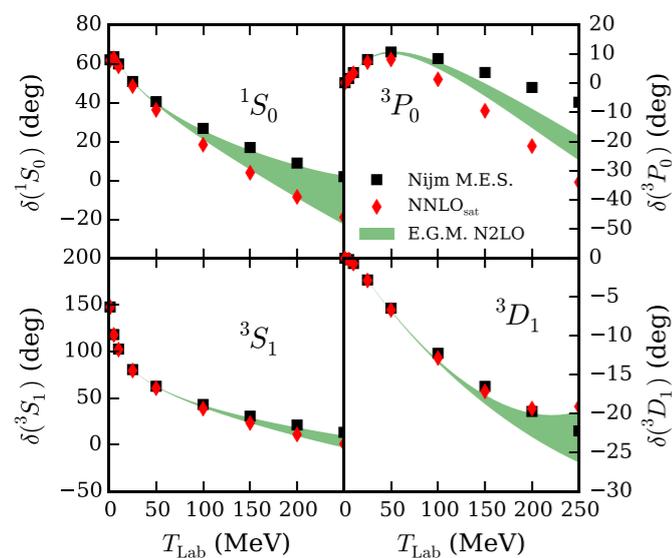


Carlsson et al.,  
PRX 6, 011019 (2016)

# Recent and current developments of novel nuclear interactions

## 3. fits of NN plus 3N forces to two-, few- and many-body observables

**status:** NN plus 3N up to N2LO, NN phase shifts only fitted up to  $T_{\text{lab}} \sim 35$  MeV

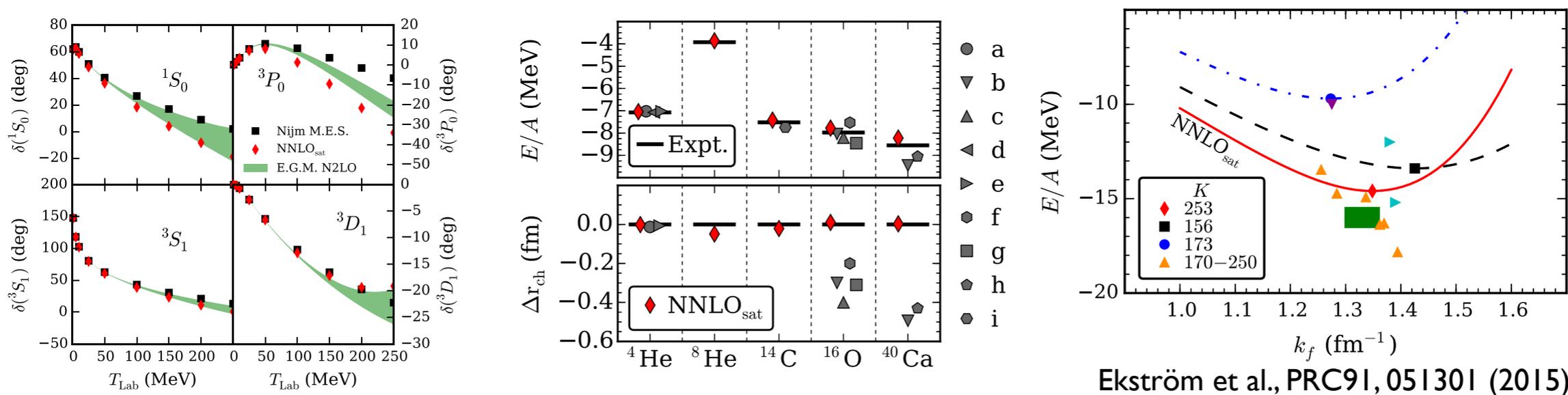


Ekström et al., PRC91, 051301 (2015)

# Recent and current developments of novel nuclear interactions

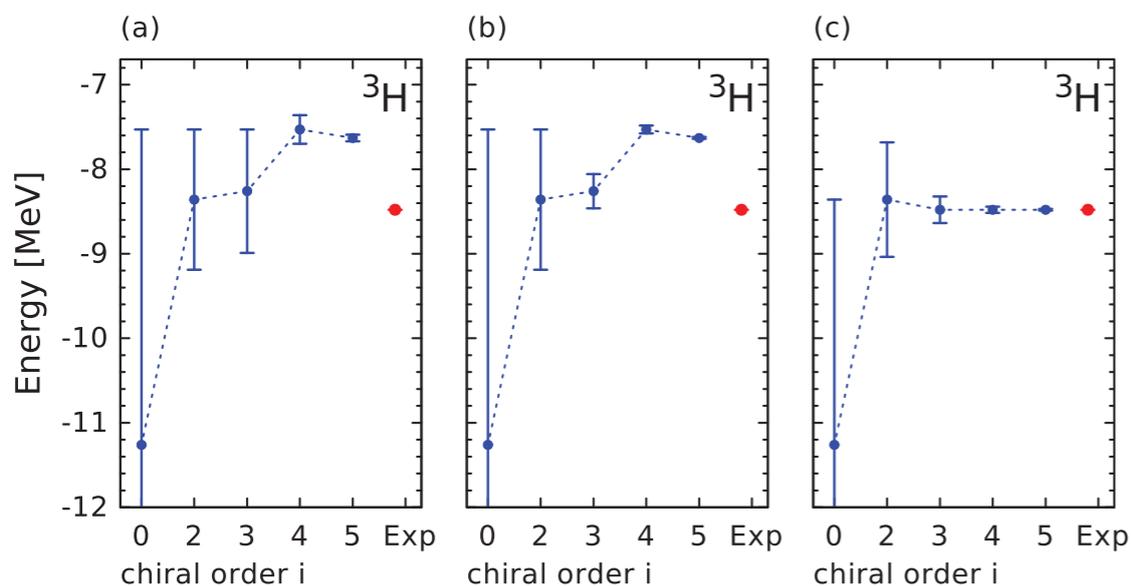
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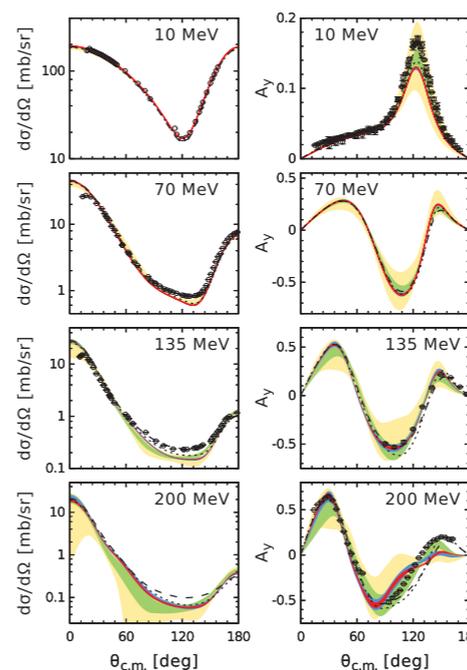
## 4. semilocal NN forces, development of improved method to estimate uncertainties

**status:** NN up to N4LO, 3N interactions in development (almost finished :-))



Epelbaum, Krebs, Meißner,  
PRL 115, 122301 (2015)

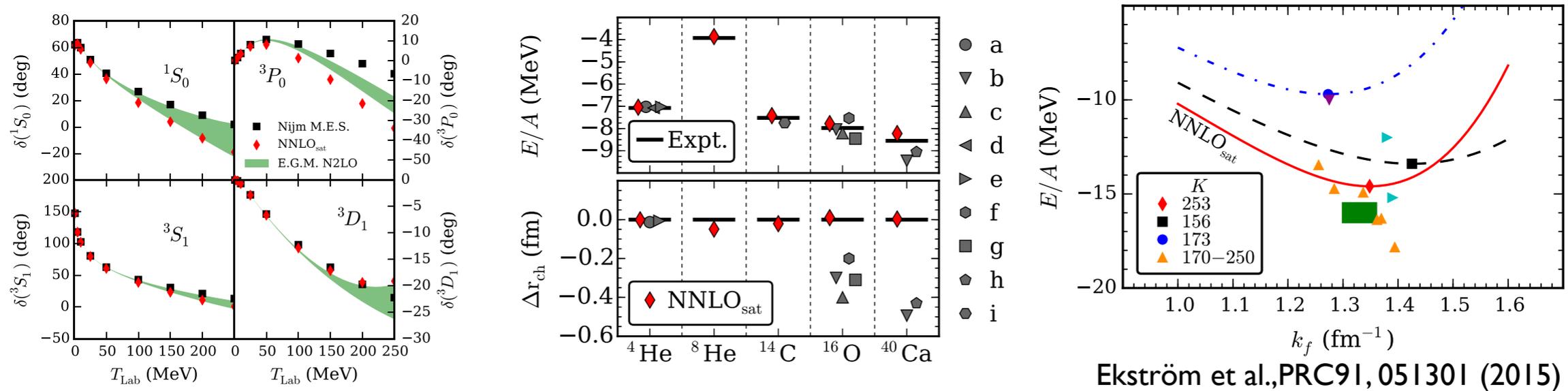
Binder et al.,  
PRC 93, 044002 (2016)



# Recent and current developments of novel nuclear interactions

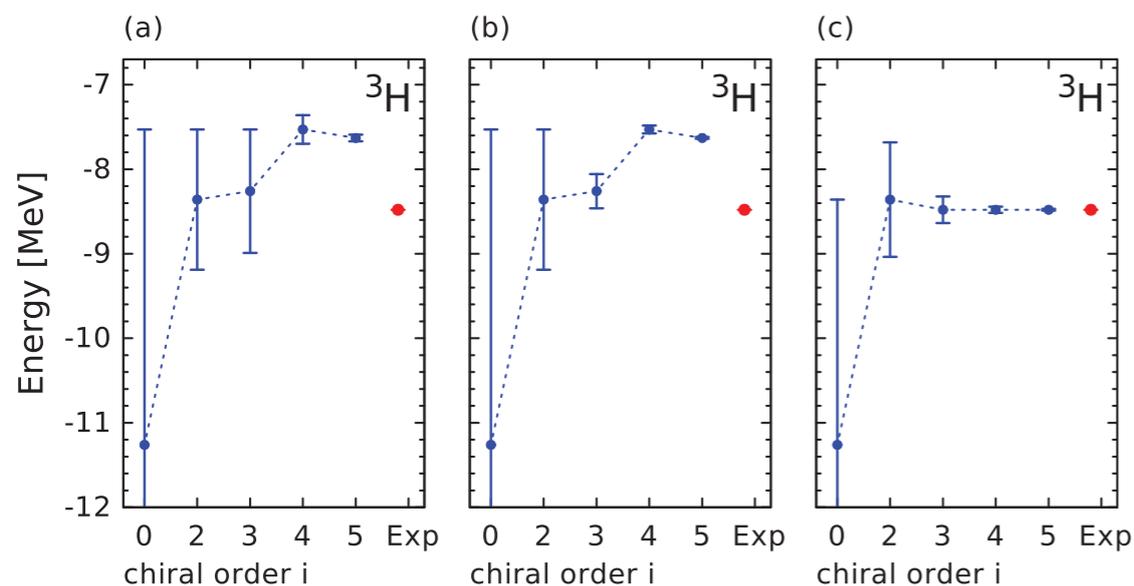
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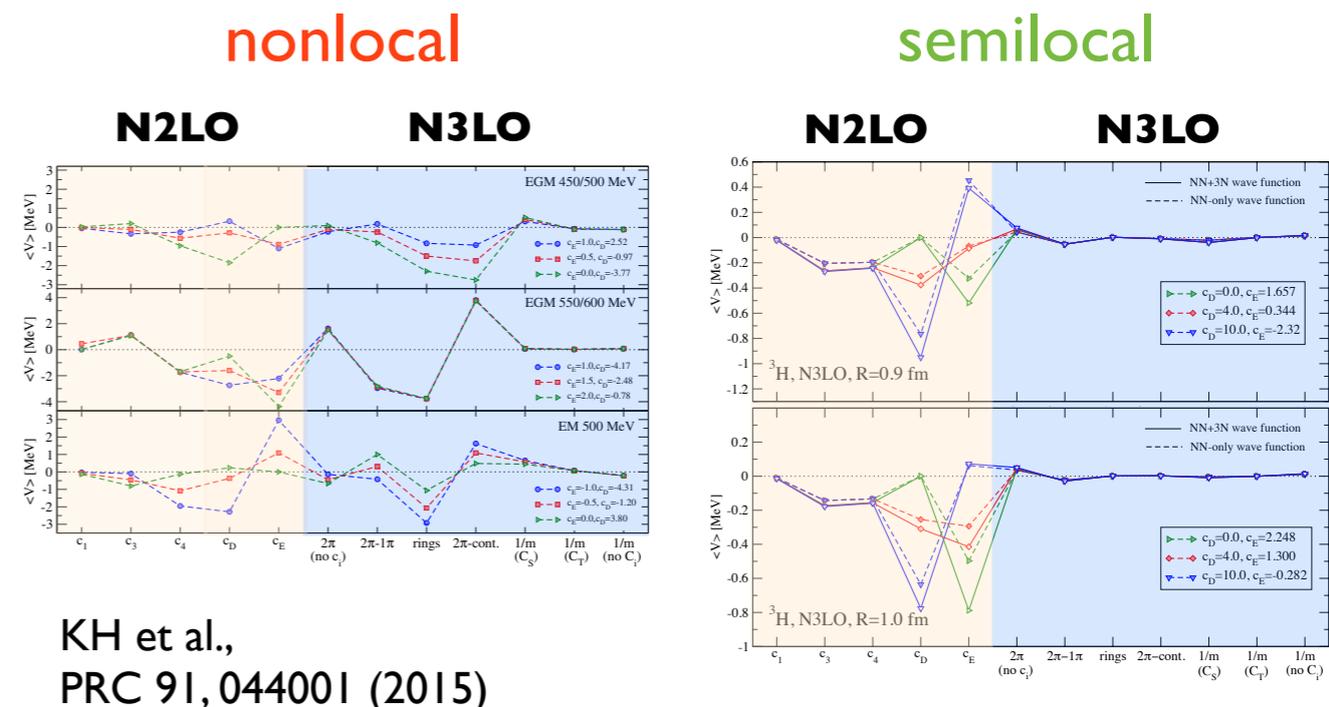
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Epelbaum, Krebs, Meißner,  
PRL 115, 122301 (2015)

Binder et al.,  
PRC 93, 044002 (2016)



## Status and achievements

significant increase in scope of  
ab initio many-body frameworks

remarkable agreement between  
different ab initio many-body methods

discrepancies to experiment dominated by  
deficiencies of present nuclear interactions

## Current developments and open questions

presently active efforts to  
develop improved nucleon interactions  
(fits of LECs, power counting, regularization...)

## Key goals

unified study of atomic nuclei, nuclear matter  
and reactions based on novel interactions

systematic estimates of  
theoretical uncertainties