

# Charmonium production within the statistical hadronisation model

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in collaboration with

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arXiv:1807.01236 [nucl-th]

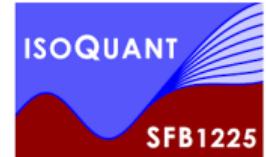
January 16<sup>th</sup>, 2019

## From QCD matter to hadrons

International Workshop XLVII on Gross Properties of Nuclei and Nuclear Excitations  
Hirschgegg, Kleinwalsertal, Austria, January 13-19, 2019



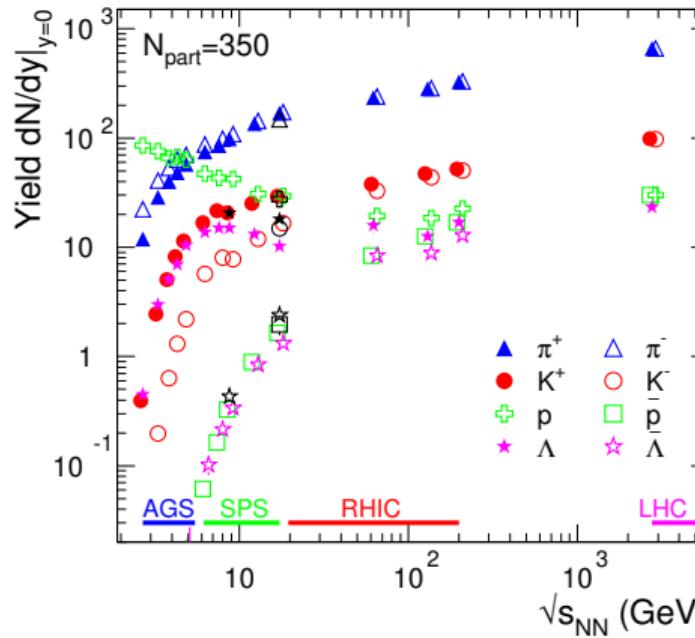
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# Statistical hadronisation in heavy-ion collisions

- ▶ Copious production of newly created particles in relativistic heavy-ion collisions ( $dN_{ch}/dy \sim 10^3$  at LHC energies)

- ▶ Mass hierarchy in particle production
- ▶ Thermal/statistical approach to describe particle production

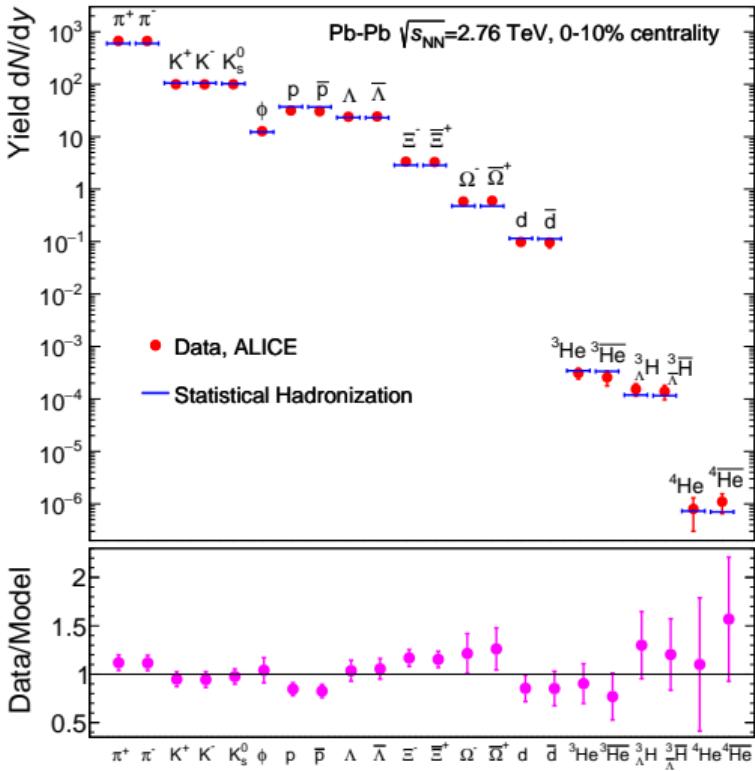


# Statistical hadronisation in heavy-ion collisions

[Andronic *et al.*, Nature 561 (2018) 321]

- ▶ Mass hierarchy in particle production
- ▶ Thermal/statistical approach to describe particle production
- ▶ Grand-canonical partition function
- ▶ Conserve the quantum numbers  $B$ ,  $I_3$ , and  $S$  on average
- ▶ Assume rapid chemical freeze-out at  $T_{\text{CF}}$
- ▶ Outcome:  $T_{\text{CF}}$ ,  $\mu_b$ , and  $V$   
 $T_{\text{CF}} = 156.5 \pm 1.5 \text{ MeV}$ ,  $\mu_b = 0.7 \pm 3.8 \text{ MeV}$

→ see Pok Man Lo's talk for a recent update

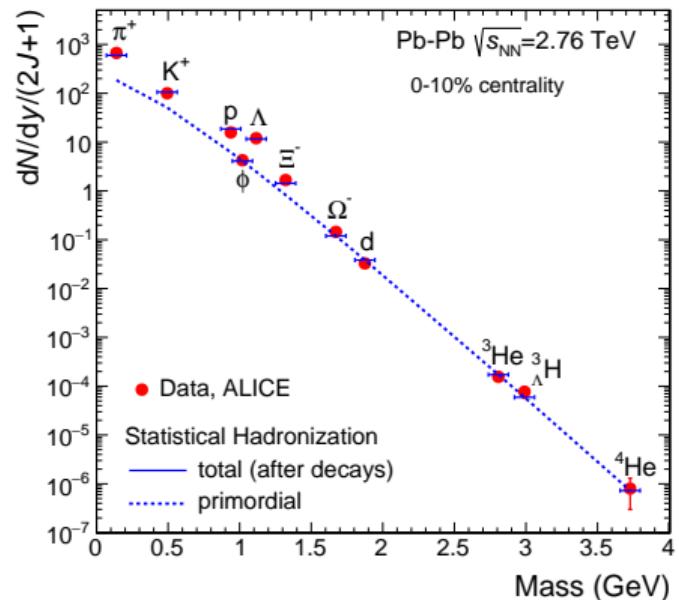


# Statistical hadronisation in heavy-ion collisions

- ▶ Mass hierarchy in particle production
- ▶ For  $m \gg T_{\text{CF}}$ , the yield  $dN/dy$  scales with

$$m^{3/2} \exp(-m/T_{\text{CF}})$$

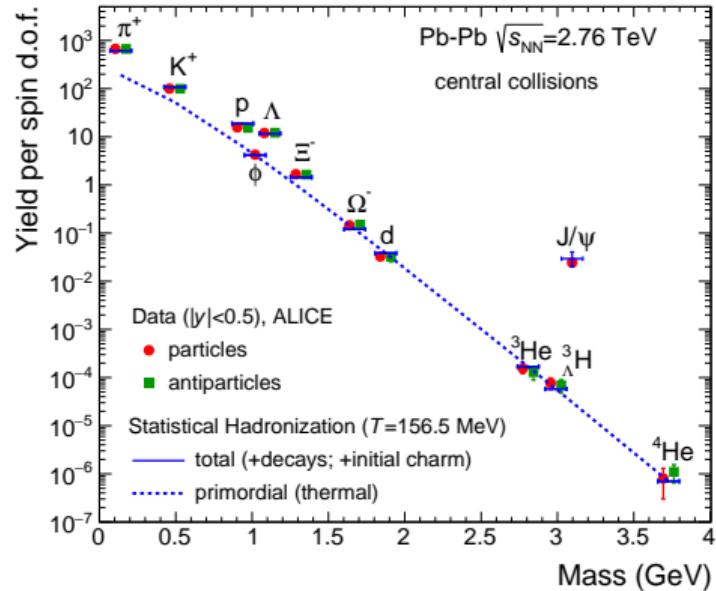
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# Statistical hadronisation in heavy-ion collisions

- ▶ Mass hierarchy in particle production
- ▶ For  $m \gg T_{\text{CF}}$ , the yield  $dN/dy$  scales with
$$m^{3/2} \exp(-m/T_{\text{CF}})$$
- ▶ Significantly different behaviour between charmonium state  $J/\psi$  and hyper-triton which has (approximately) the same mass

[Andronic *et al.*, in preparation]



# Extending the model with charm

[Braun-Munzinger and Stachel, PLB 490 (2000) 196]

[Andronic, Braun-Munzinger and Stachel, NPA 789 (2007) 334]

- ▶ Charm quarks are produced in initial hard scatterings ( $m_{c\bar{c}} \gg T_c$ ) and production can be described by pQCD ( $m_{c\bar{c}} \gg \Lambda_{\text{QCD}}$ )
- ▶ Charm quarks survive and *thermalise* in the QGP
- ▶ Full screening before  $T_{\text{CF}}$
- ▶ Charmonium is formed at phase boundary (together with other hadrons)
- ▶ Thermal model input ( $T_{\text{CF}}, \mu_b \rightarrow n_X^{\text{th}}$ )

$$N_{c\bar{c}}^{\text{dir}} = \underbrace{\frac{1}{2}g_c V \left( \sum_i n_{D_i}^{\text{th}} + n_{\Lambda_i}^{\text{th}} + \dots \right)}_{\text{Open charm}} + \underbrace{g_c^2 V \left( \sum_i n_{\psi_i}^{\text{th}} + n_{\chi_i}^{\text{th}} + \dots \right)}_{\text{Charmonia}}$$

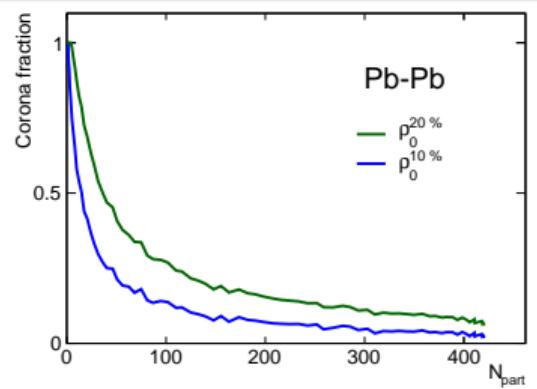
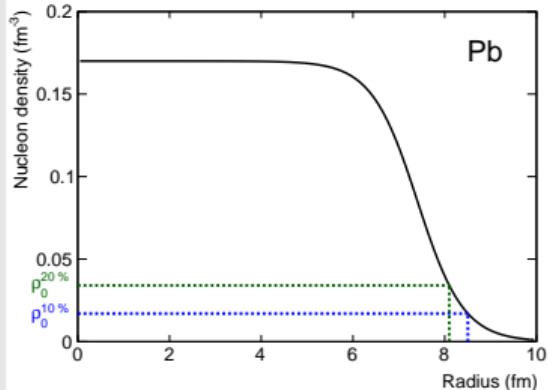
- ▶ Canonical correction  $N_{c\bar{c}}^{\text{dir}} = \frac{1}{2}g_c N_{\text{oc}}^{\text{th}} \frac{l_1}{l_0} (g_c N_{\text{oc}}^{\text{th}}) + g_c^2 N_{c\bar{c}}^{\text{th}} \rightarrow g_c$
- ▶ Outcome  $N_{J/\psi} = g_c^2 n_{J/\psi}^{\text{th}} V, N_D = g_c n_D^{\text{th}} V \frac{l_1}{l_0}, \dots$

# Core and Corona

- ▶ Collision geometry determines which nucleons participate in the fireball
- ▶ Surface nucleons do not contribute to the QGP formation

**Core** Thermal contribution from statistical hadronisation model

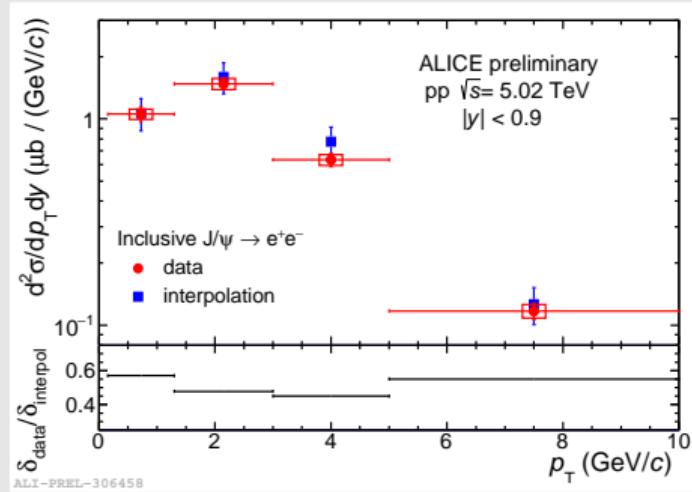
**Corona** pp distributions scaled by  $N_{\text{coll}}$



# New ALICE results at mid-rapidity

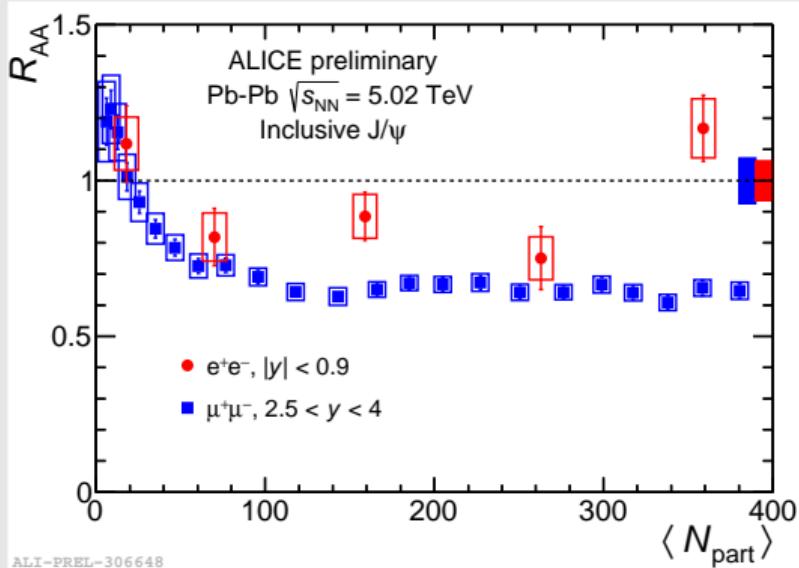
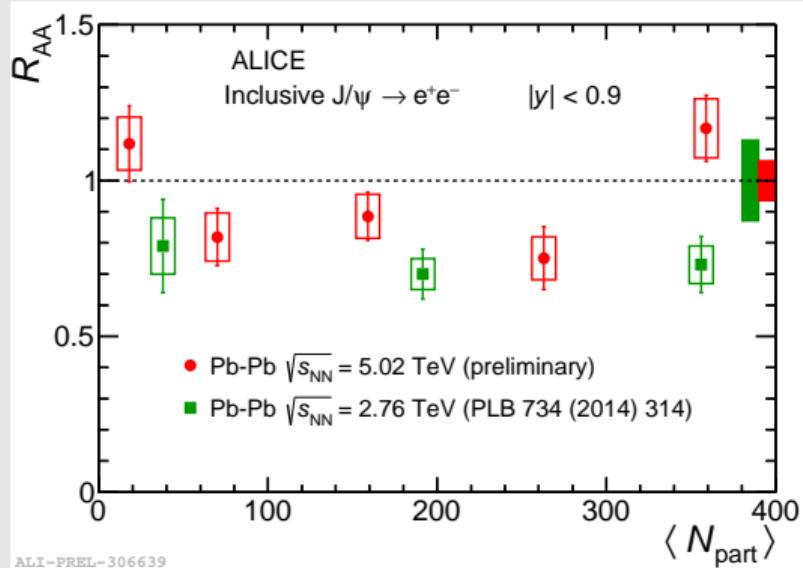
## Cross-section measurement in pp collisions at 5 TeV

- The reference is a crucial ingredient for the precision of the  $R_{AA}$  results
- Previously an interpolated cross section was used
- New measurement with significantly increased statistics from 2017
- Increase precision by factor  $\gtrsim 2$



# New ALICE results at mid-rapidity

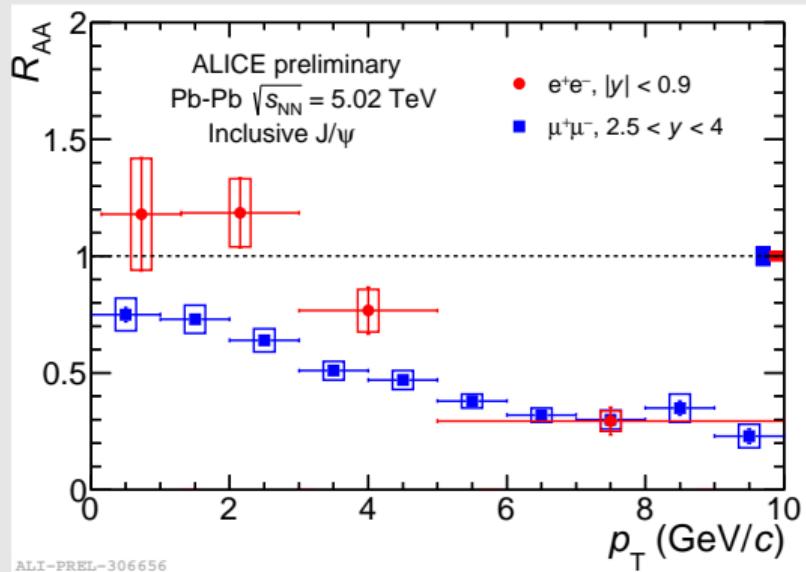
## Comparisons of results in Pb-Pb collisions



- ▶ ‘Enhancement’ at mid-rapidity towards central collisions compared to lower collision energy and forward rapidity

# Transverse momentum dependence

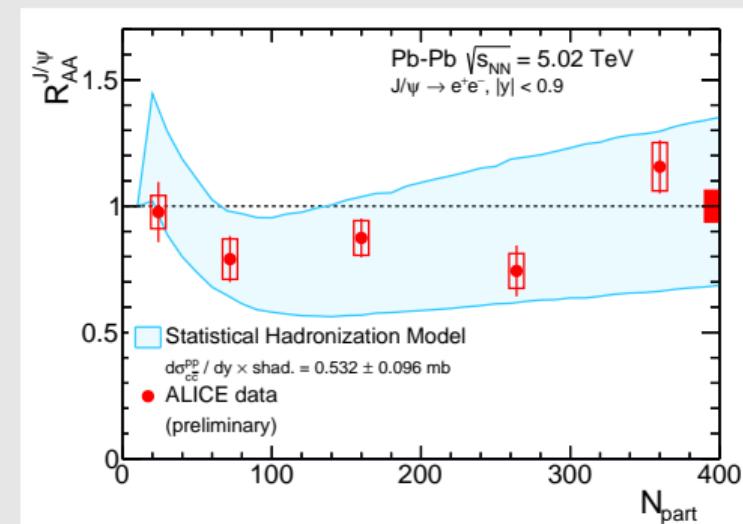
## Finalisation of the analysis of the Pb-Pb data from 2015



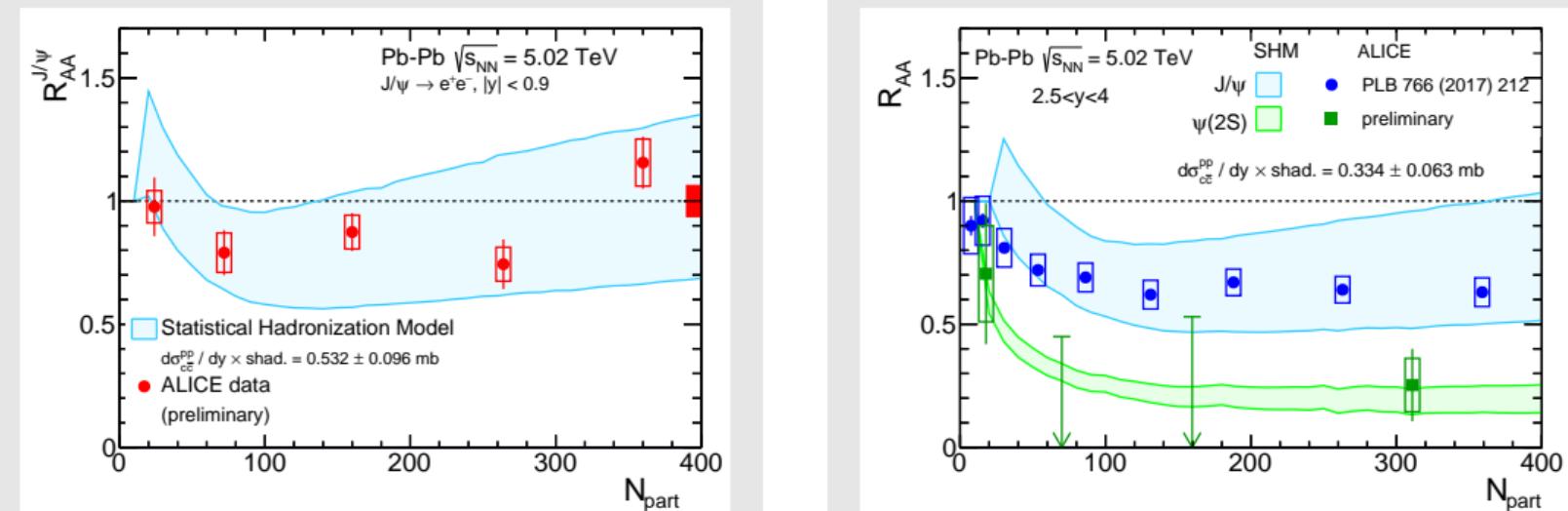
- ▶ ‘Enhancement’ at mid-rapidity concentrated at low  $p_T$
- ▶ Transverse momentum can be used to discriminate between different production mechanisms

# Comparison of the model with data vs centrality at 5.02 TeV

## Mid-rapidity



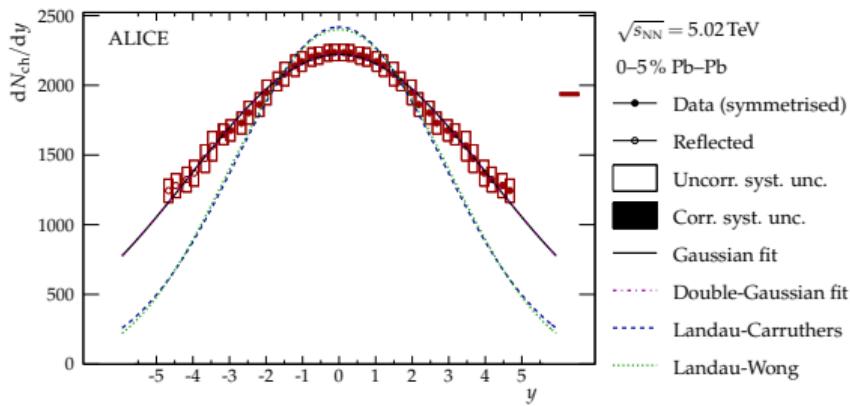
## Forward rapidity



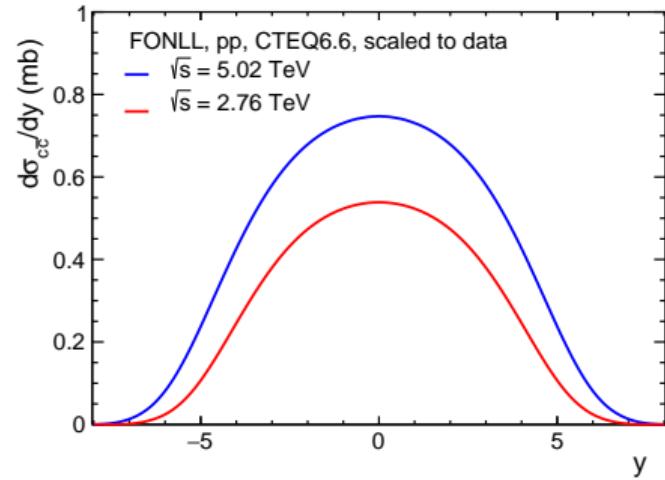
- $d\sigma_{c\bar{c}}/dy$  from measurements in pp collisions in appropriate rapidity region and shadowing coming from open charm and  $J/\psi$  production in p-Pb collisions is applied
- Simultaneous description at mid- and forward rapidity of different charmonium states

# Rapidity dependence of $\text{J}/\psi$ production

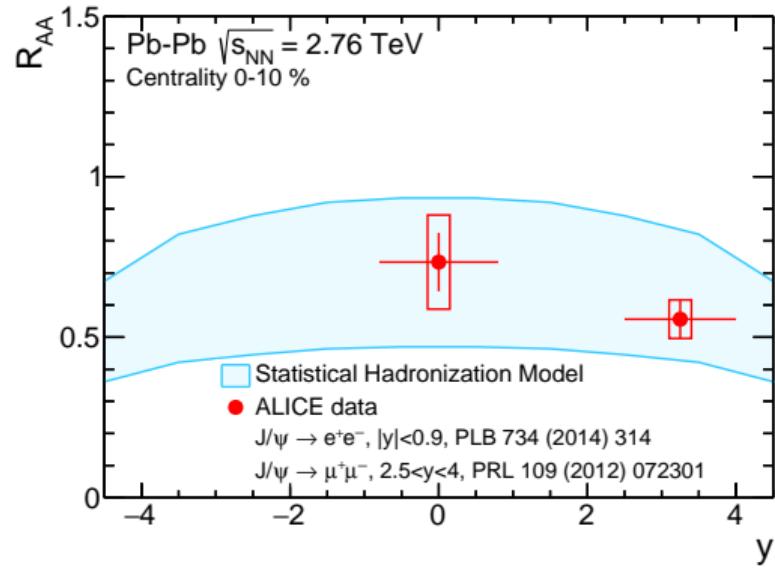
- Rapidity dependence of  $\text{J}/\psi$  production in statistical hadronisation picture is determined by rapidity dependence of charm cross section
- $T_{\text{CF}}, \mu_b$  from thermal fits,  $V(y) = \frac{dN_{\text{ch}}/dy}{n_{\text{ch}}^{\text{SHM}}}$ , where  $\begin{cases} dN_{\text{ch}}/dy & [\text{ALICE, PLB 726 (2013) 610}] \\ n_{\text{ch}}^{\text{SHM}} & [\text{ALICE, PLB 772 (2017) 567}] \\ \hat{\equiv} & \text{particle density from SHM} \end{cases}$
- Rapidity dependence  $d\sigma_{c\bar{c}}/dy$  from FONLL [Cacciari et al., JHEP (2012) 2012:137] anchored to pp measurements from ALICE and LHCb



ALI-PUB-115105



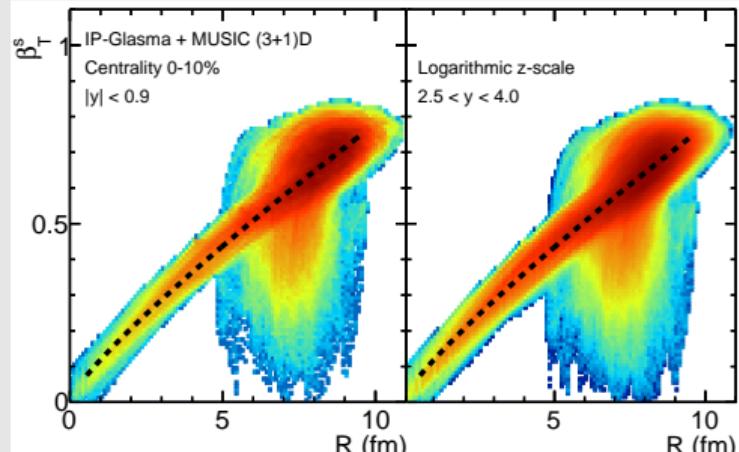
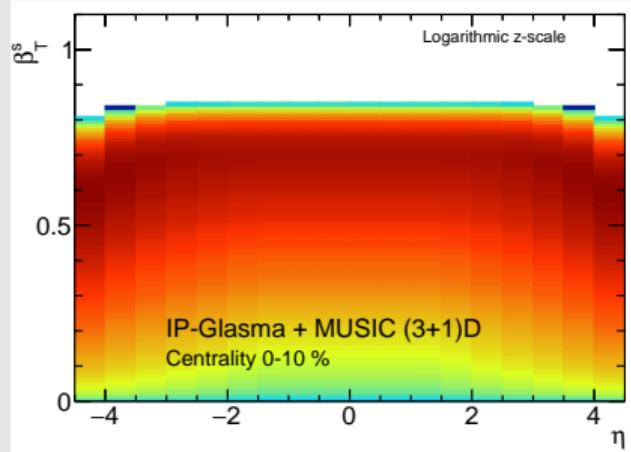
# Comparison with data



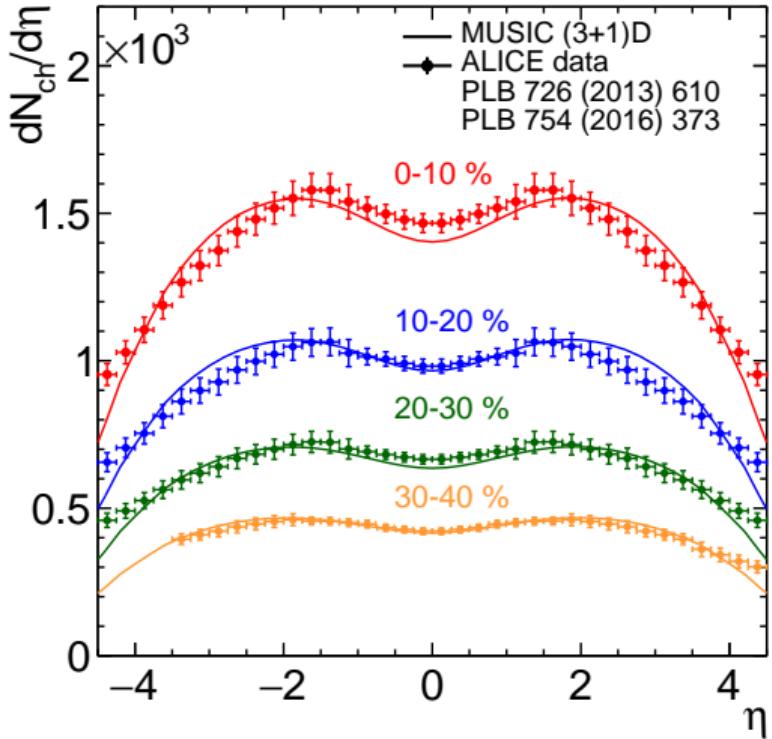
- Good description of data by the model as a function of  $J/\psi$  rapidity
- Fall-off towards large rapidities is significant (and would be in contrast to screening-dominated descriptions)

# Transverse momentum spectra

- The underlying idea of thermalised charm quarks forming charmonia at the hadronisation of the fireball can be extended to compute spectra
- Charm quarks follow collective expansion of the QGP fireball, as modeled well by state of the art viscous hydrodynamics codes used to describe light flavor hadron observables
- Use collective expansion velocity from MUSIC(3+1)D [Schenke, Jeon & Gale, PRC82 (2010) 014903] with QCD inspired parameters [Dubla *et al.*, NPA 979 (2018) 251], and IP-Glasma for initial conditions [Schenke, Tribedy & Venugopalan, PRL 108 (2012) 252301] at  $T = T_{\text{CF}}$



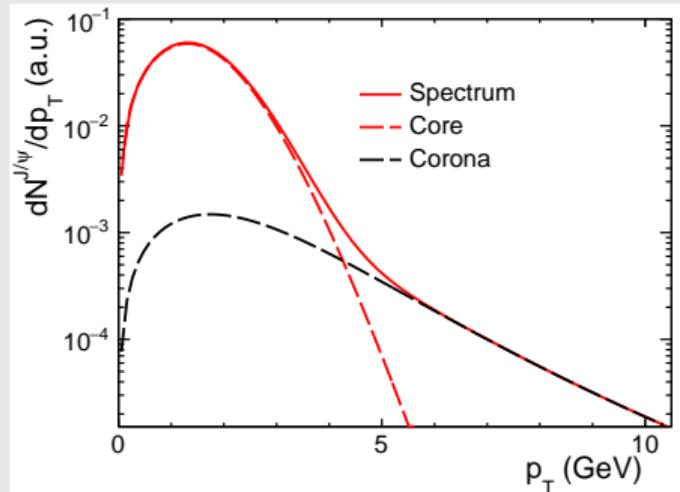
# Comparison of particle distribution



- MUSIC(3+1)D needs input for  $\eta$  dependence  
→ need to compare with data
- For the comparison of the simulation with data, there is also the possibility to run the Cooper-Frye procedure afterwards  
[Cooper & Frye, PRD 10 (1974) 186]  
[Cooper, Frye & Schonberg, PRD 11 (1975) 192]
- Turns 'massless' fluid into massive particles (with subsequent resonance decays)
- Good agreement between hydro simulation and data for  $|\eta| \lesssim 4$

# Transverse momentum parametrisation

- ▶ A rapidity dependent blast wave function for boost-invariant expansion and Hubble flow following the earlier work from Schnedermann, Heinz and Florkowski is used to compute spectral shape using the collective velocity
- ▶ The corona part is added to the thermal part
- ▶ The approach is sensitive to the degree of thermalisation of charm quarks in the fireball
- ▶ If the  $p_T$  distribution of the  $J/\psi$  can be described within this picture for low  $p_T$ , this provides strong support for charm quark thermalisation



# Blast-wave function with Hubble-type expansion

- ▶ Follows [Florkowski, Phenomenology Of Ultra-Relativistic Heavy-Ion Collisions]

$$\frac{d^2N}{p_T dp_T dy} \propto \int_0^R r dr \left\{ m_T \cosh \rho K_1 \left( \frac{m_T \cosh \rho}{T} \right) I_0 \left( \frac{p_T \sinh \rho}{T} \right) - p_T \sinh \rho K_0 \left( \frac{m_T \cosh \rho}{T} \right) I_1 \left( \frac{p_T \sinh \rho}{T} \right) \right\},$$

where  $I_i$  and  $K_i$  with  $i = \{1, 2\}$  are modified Bessel functions,  $T$  is the temperature, and  $\rho$  is given by

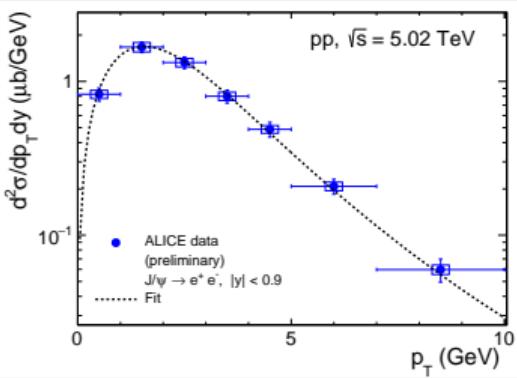
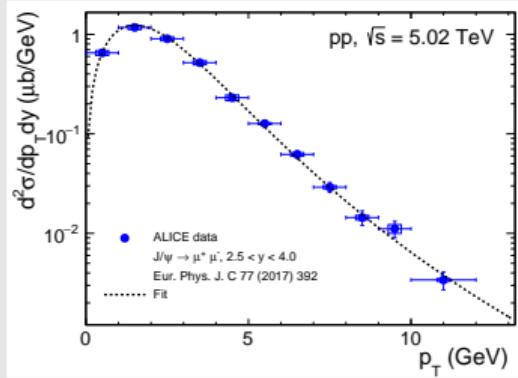
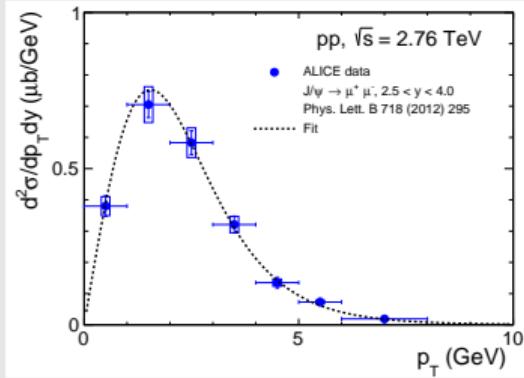
$$\rho = \tanh^{-1} \left\{ \beta_T^s \left( \frac{r}{R} \right)^n \right\},$$

with  $\beta_T^s$  being the transverse surface velocity.

- ▶ For  $J/\psi$  mass, function reliable for  $p_T \lesssim 5$  GeV

# Constraints on corona shape

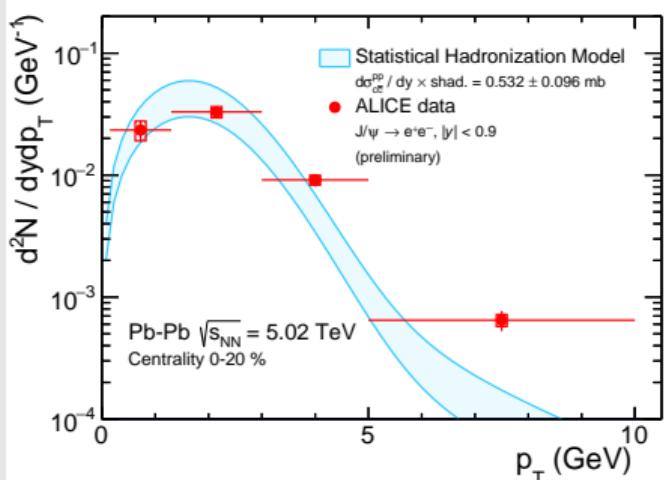
- Corona shape modeled by measured  $p_T$  spectra in pp collisions
- Available data fitted by  $f(p_T) = C \frac{p_T}{\{1 + (p_T/p_0)^2\}^n}$



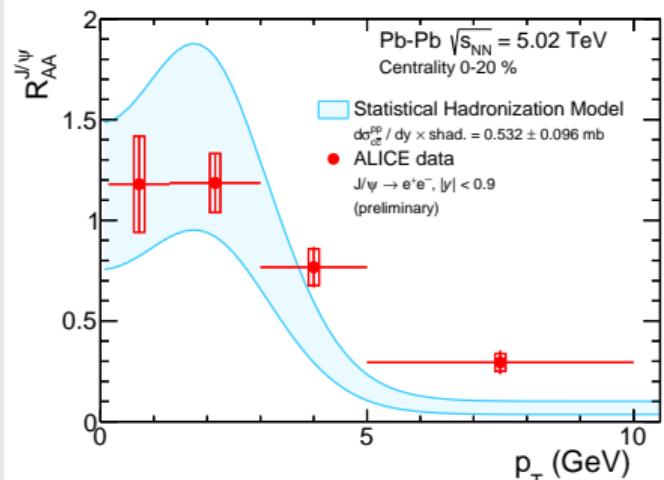
# Comparison of the model with data

$\sqrt{s_{NN}} = 5.02$  TeV, mid-rapidity, 0-20 %

## $p_T$ spectrum



## $R_{AA}$ versus $p_T$

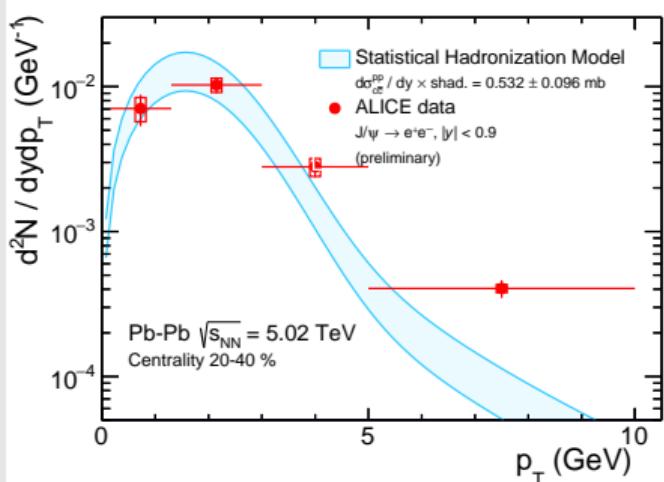


- Very good agreement between data and predictions without free parameters

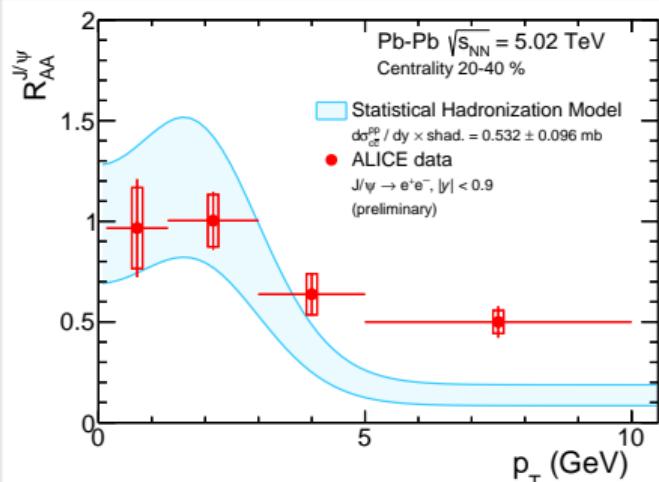
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$\sqrt{s_{\text{NN}}} = 5.02 \text{ TeV}$ , mid-rapidity, 20-40 %

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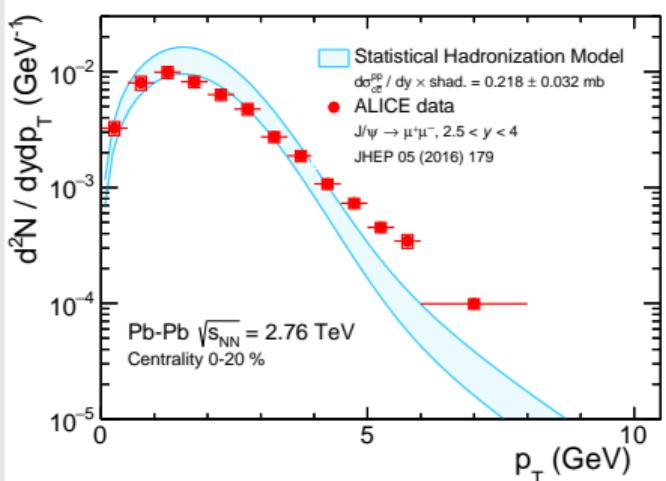


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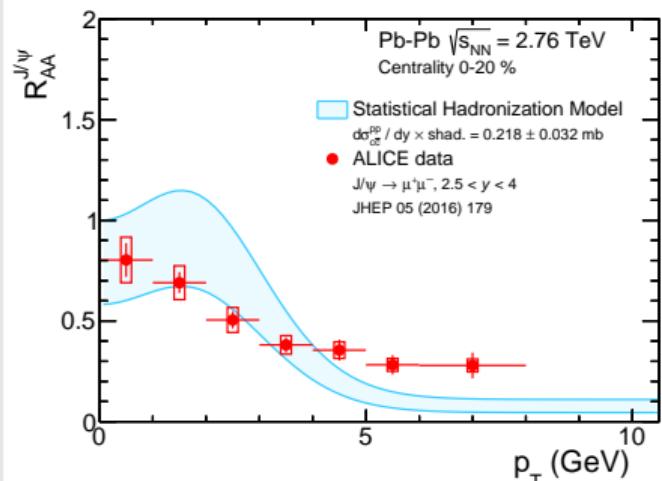
# Comparison of the model with data

$\sqrt{s_{\text{NN}}} = 2.76 \text{ TeV}$ , forward rapidity, 0-20 %

## $p_T$ spectrum



## $R_{\text{AA}}$ versus $p_T$

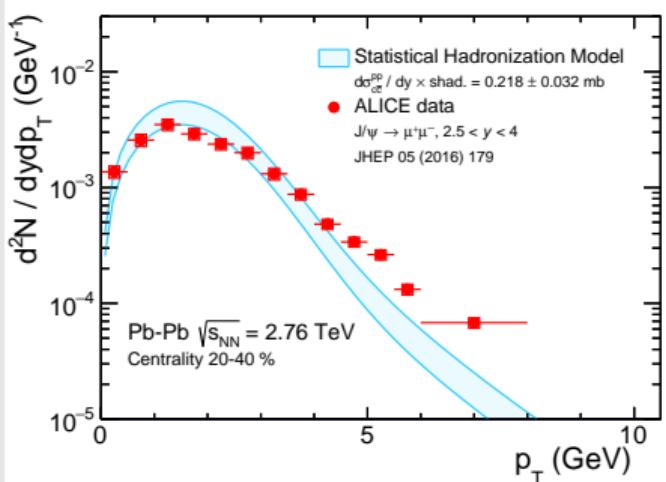


- Very good agreement between data and predictions without free parameters at low  $p_T$

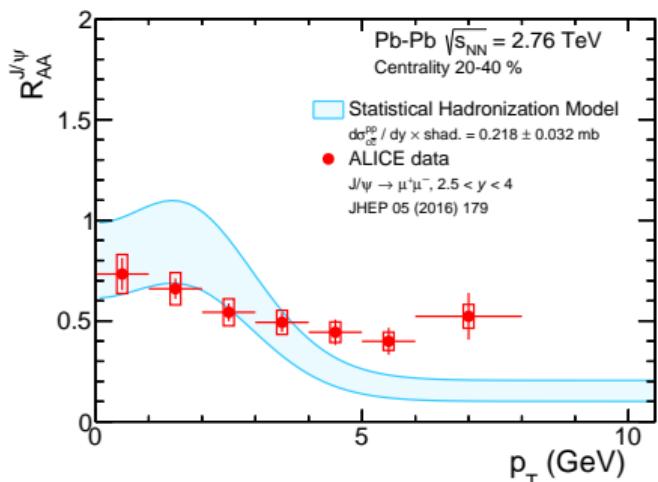
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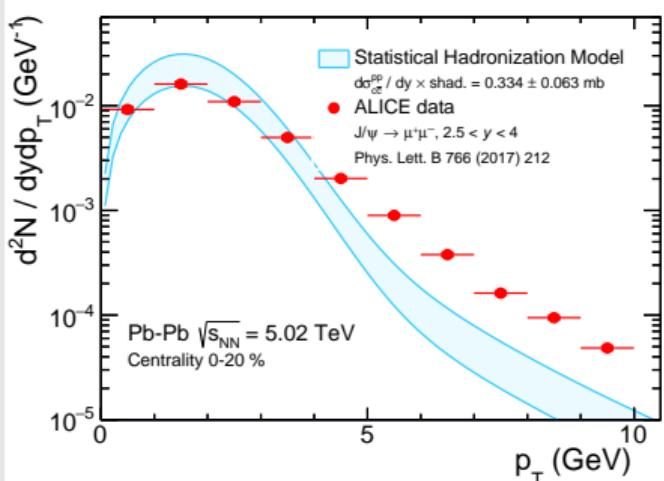


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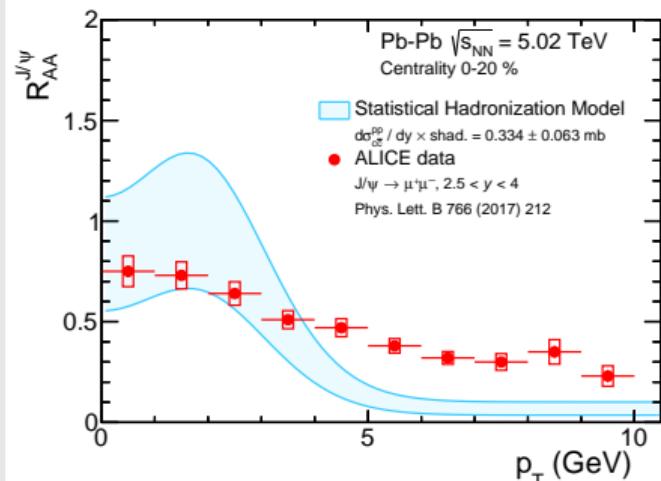
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## $p_T$ spectrum



## $R_{AA}$ versus $p_T$

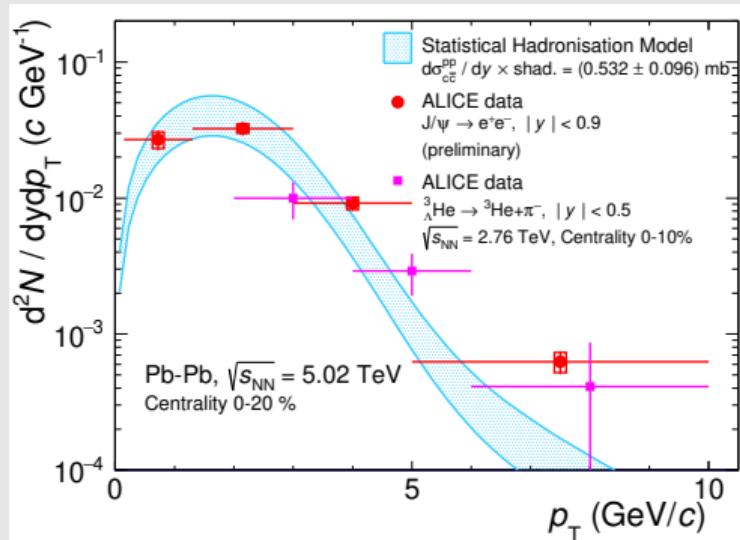


- Very good agreement between data and predictions without free parameters at low  $p_T$

# Comparing hyper-triton with $J/\psi$

[Braun-Munzinger & Dönigus, arXiv:1809.04681 [nucl-ex]]

- ▶ Thermal nature of loosely bound objects like (anti-)(hyper-)nuclei?
- ▶ Surprising flow pattern
- ▶ Consistent with multi-quark states formed at the phase boundary developing later into hadronic wave functions [Andronic *et al.*, Nature 561 (2018) 321]

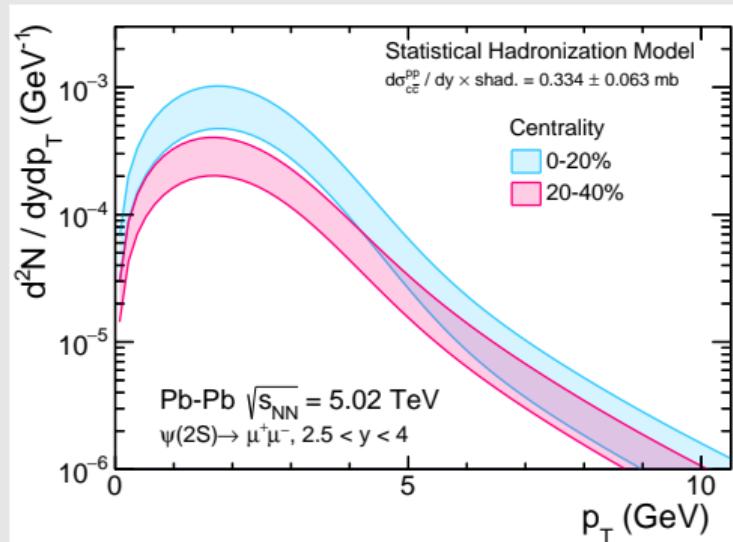
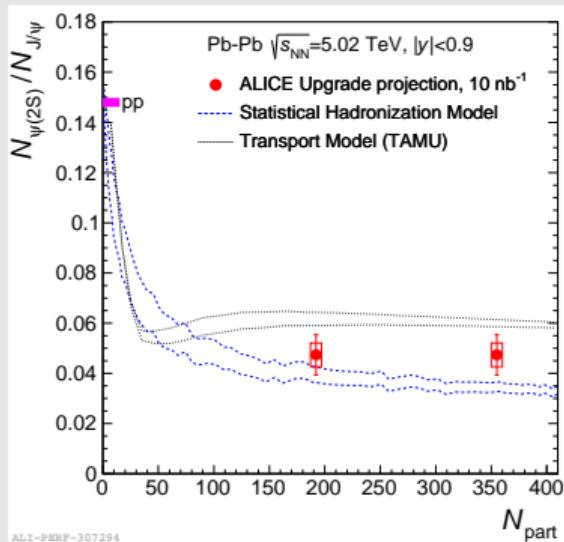


- ▶  $J/\psi$  and (scaled) hyper-triton can be described by the same flow parameters
- ▶ Need the precision on hyper-triton  $p_T$  spectra as will be available in LHC Run3
- ▶ Comparison of loosely bound and compact objects allow for a test of the hypothesis

# Looking towards ALICE high-rate PbPb run

Yellow Report, arXiv:1812.06772 [hep-ph]

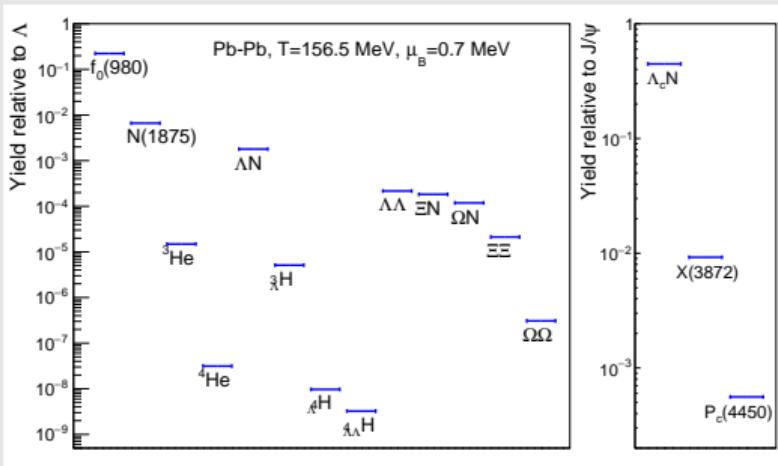
- Charmonium ratio's (e.g.  $\psi(2S)$  or in particular  $\chi_c$ ) are a crucial probe to understand whether colour-less bound state exist above  $T_{CF}$



# Looking towards 2030 and beyond

Yellow Report, arXiv:1812.06772 [hep-ph]

- ▶ Predictions for exotic strange and charmed particles
- ▶ Key particles to understand parton and hadron dynamics

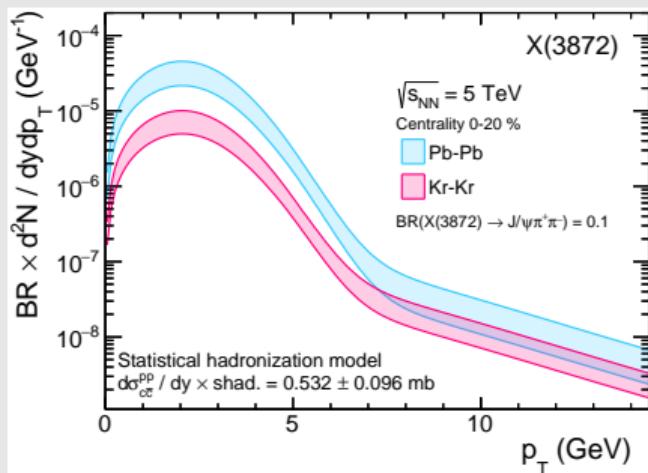


- ▶ Particular interest in  $X(3872)$
- ▶ Invariant mass close to  $D^0 \bar{D}^{*0}$  production threshold
- ▶ Potential tetra-quark state and charmed meson molecule

# X(3872) transverse momentum spectra

Yellow Report, arXiv:1812.06772 [hep-ph]

- ▶ Predictions for exotic strange and charmed particles
- ▶ Key particles to understand parton and hadron dynamics



- ▶ If compact and loosely bound objects are produced at the phase boundary
- ▶ Likely that future colliders will run with smaller nuclei (higher luminosity)  
→  $^{84}\text{Kr}$  would lead to a decrease of the yield on the order of 4 – 5 for low  $p_T$

# What to expect in the near future from the data side

## Pb-Pb data taking in 2018

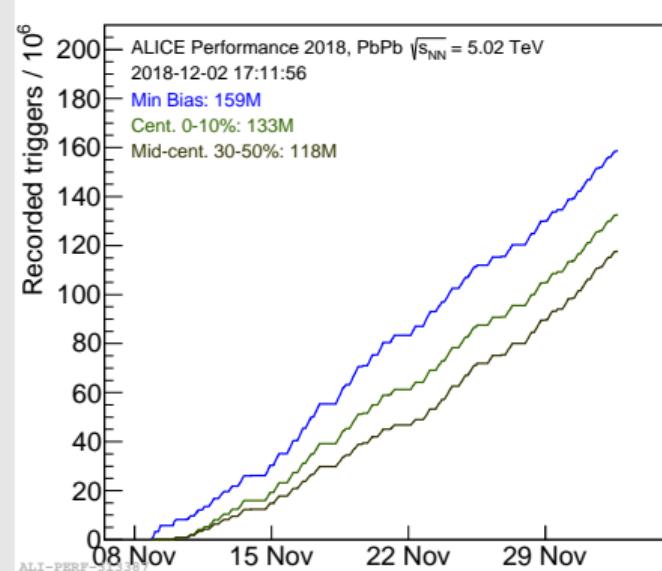
- ▶ Focus on centrality triggers
- ▶ Approximate increase in statistics compared with Pb-Pb statistics from 2015

at mid-rapidity

- 1× minimum bias
- 4× 30 – 50%
- 9× 0 – 10%

at forward rapidity

- 1× di-muon channel



- ▶ Significant increase in precision especially in central collisions

# Summary

- ▶ We presented current developments on charmonium production within the SHM
- ▶ The SHM describes charmonium yields as a function of centrality, rapidity and transverse momentum
- ▶ The agreement at low and moderate  $p_T$  provides strong support for the picture that charmonia are formed from deconfined thermalised charm quarks flowing with the QGP

# Outlook

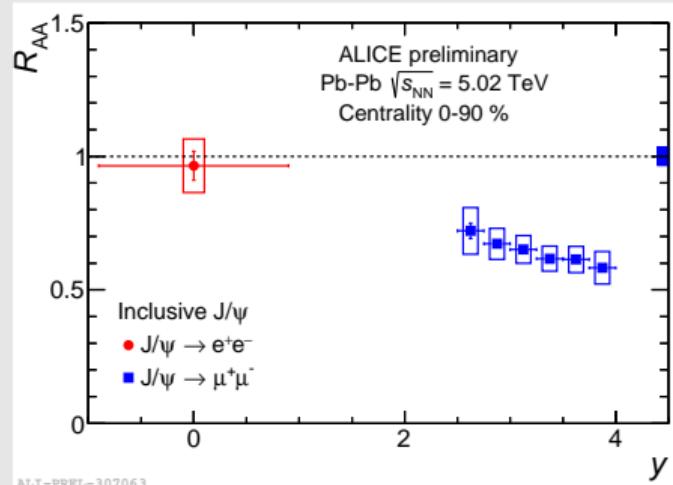
- ▶ With the increase of coming data, the more precise measurement of the charm cross section will help to discriminate between models  
→ crucial to understand whether colour-less bound states exist for  $T > T_{\text{CF}}$
- ▶ In a long term perspective exotic charmonia can help to sharpen our understanding of underlying parton production and dynamics

# Backup

# What to expect in the near future from the data side

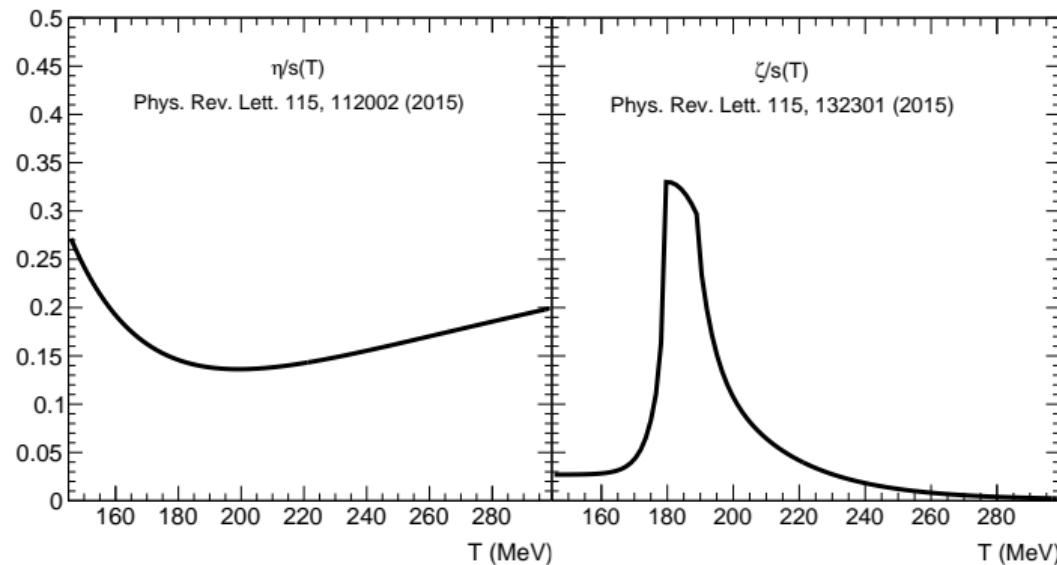
## Finalisation of the analysis of the Pb-Pb data from 2015

- ▶ Including the new reference
- ▶ Significant improvement of the systematic uncertainty on the reference



# QCD inspired parameters as MUSIC input

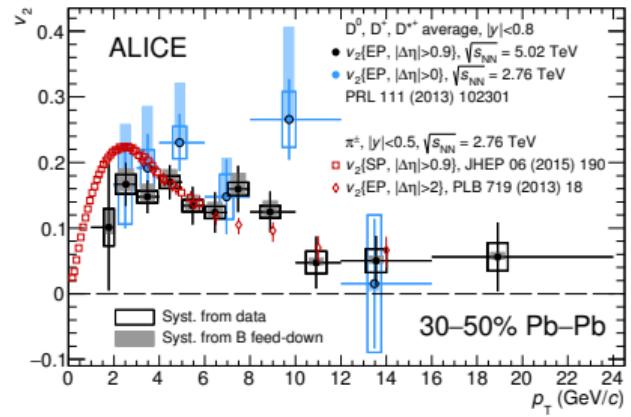
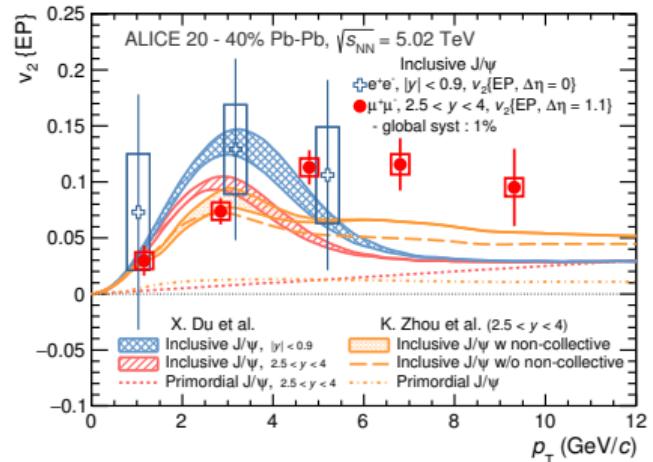
[Dubla *et al.*, NPA 979 (2018) 251]



- $\eta/s(T)$  computed with a QCD based approach used as input parameter for MUSIC simulations

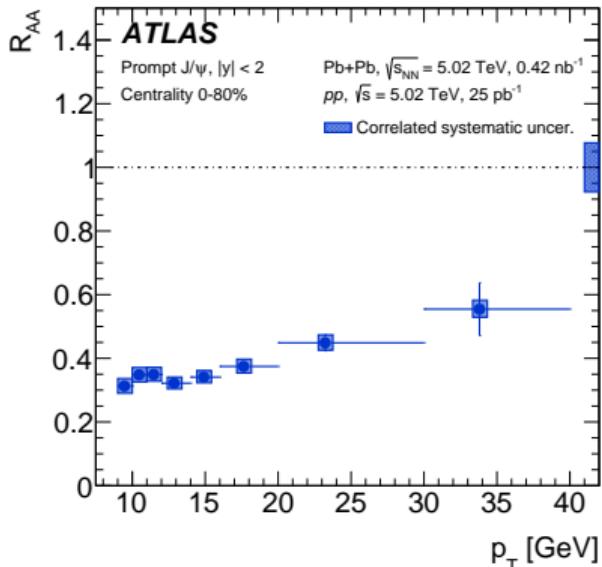
# Thermalisation of charm quarks

- $J/\psi$  [ALICE, PRL 119 (2017) 242301] and  $D$ -mesons [ALICE, PRL 120 (2018) 102301] flow
- Strong support for recombination of thermalised charm quarks at low  $p_T$
- Path-length dependence of suppression towards higher  $p_T$

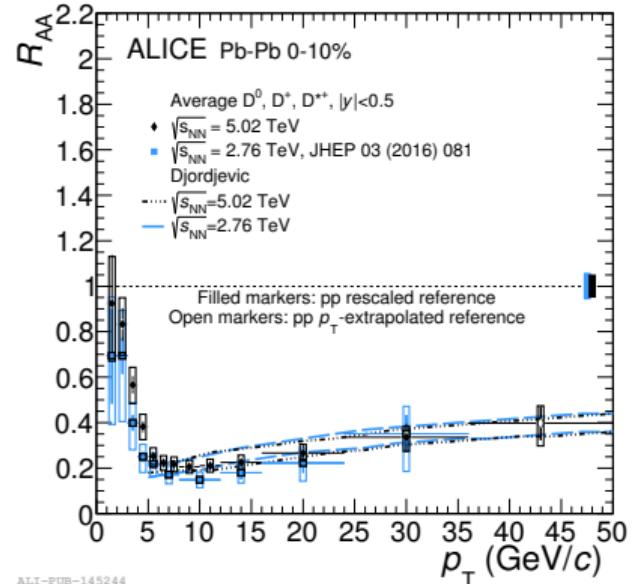


# $R_{AA}$ of charmonia and charmed mesons

[ATLAS Coll., arXiv:1805.04077]



[ALICE Coll., arXiv:1804.09083 [nucl-ex]]



- Data suggests an increase of the  $J/\psi$   $R_{AA}$  with increasing  $p_T$  reminiscent of the behaviour of  $D$  mesons

# Previously used pp interpolation at mid-rapidity

- ▶ No data available for an inclusive  $J/\psi$  cross section in pp collisions at  $\sqrt{s} = 5$  TeV down to zero  $p_T$
- ▶ To estimate the spectrum, an interpolation procedure is used

## Procedure

See also [Bossu *et al.*, arXiv:1103.2394]

- ▶ Available  $p_T$  spectra at mid-rapidity down to zero  $p_T$  is used to estimate the cross section and the  $\langle p_T \rangle$ 
  - 1) PHENIX, PRD85 (2012) 092004
  - 2) CDF, PRD71, (2005) 032001
  - 3) ALICE, PLB718 (2012) 295
  - 4) ALICE, PLB704 (2011) 442
- ▶ Use a one-parameter fit function as a function of  $\langle p_T \rangle / p_T$  to interpolate to the aimed collision energy

